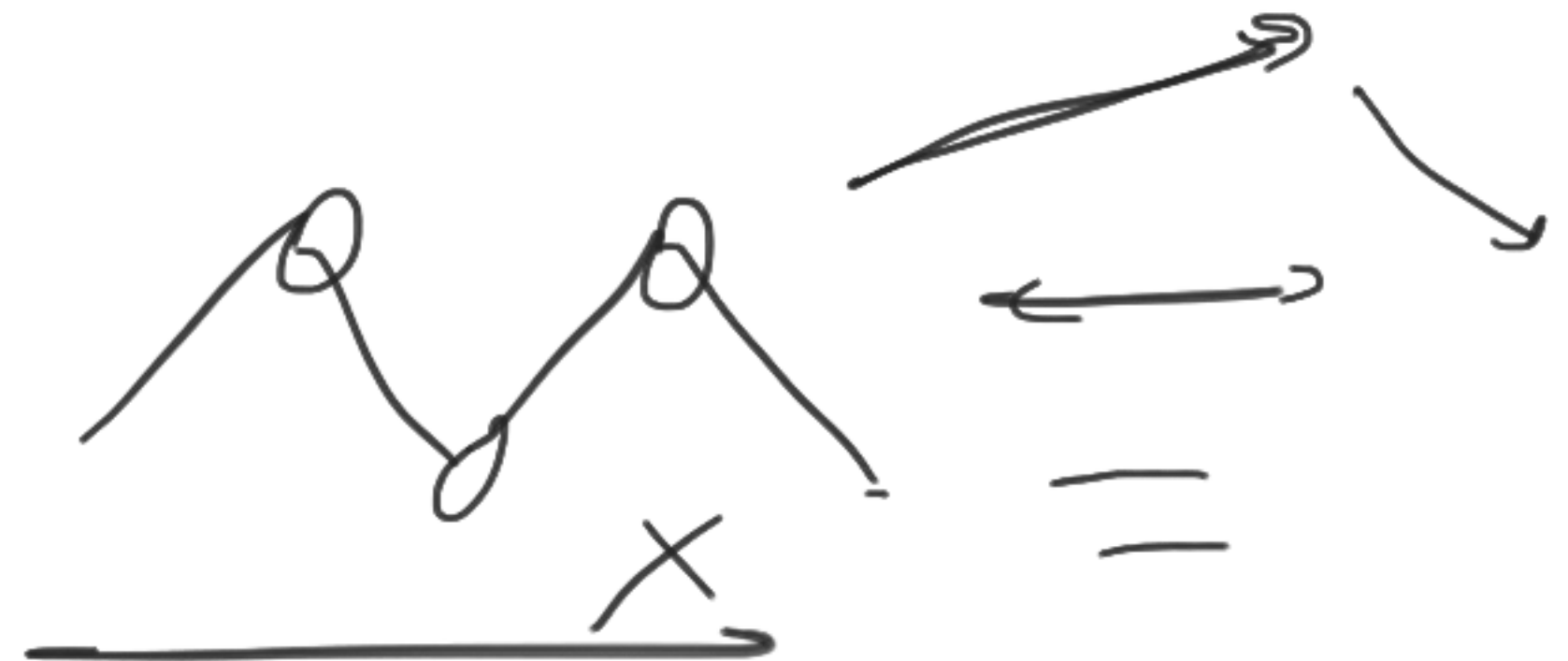
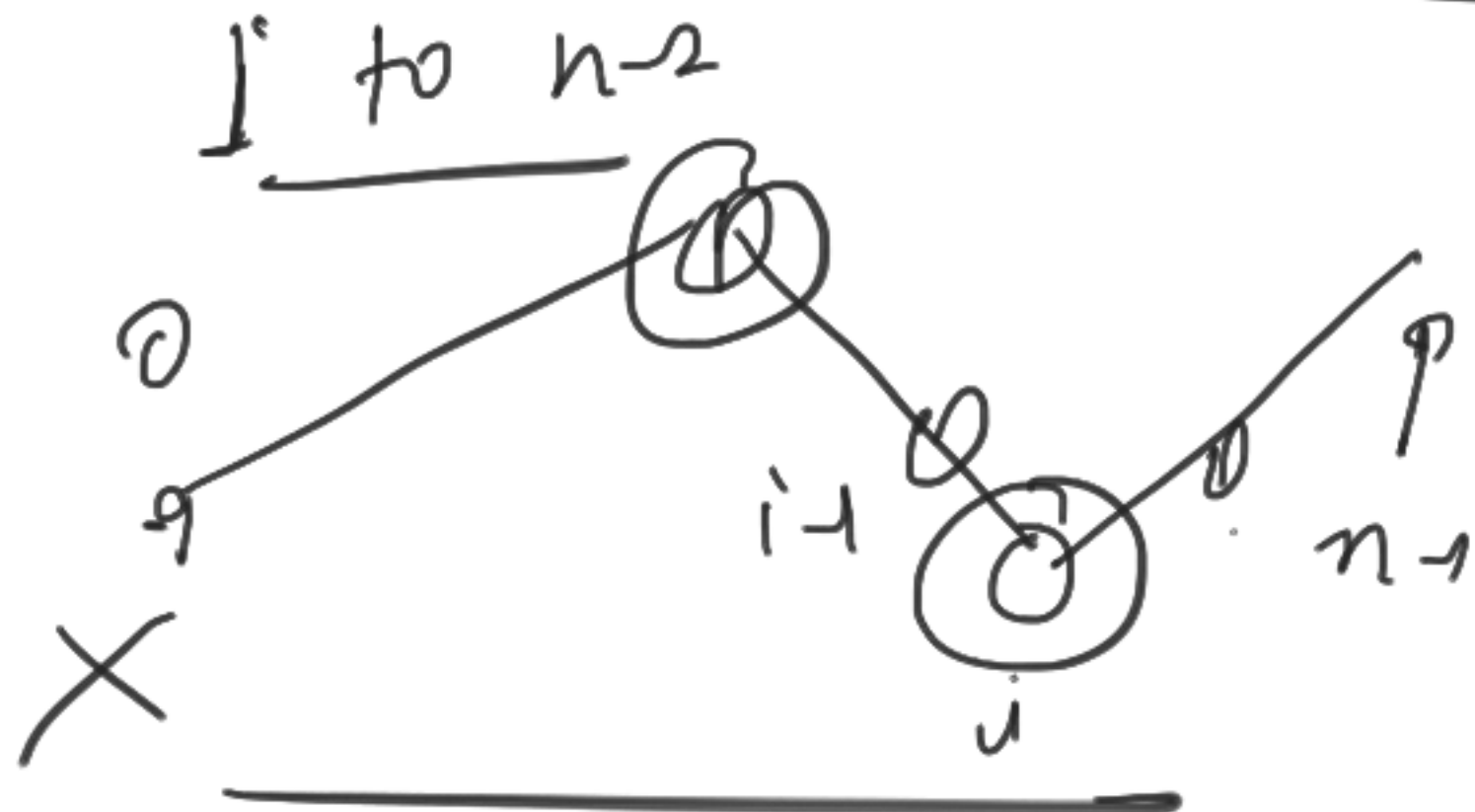


why



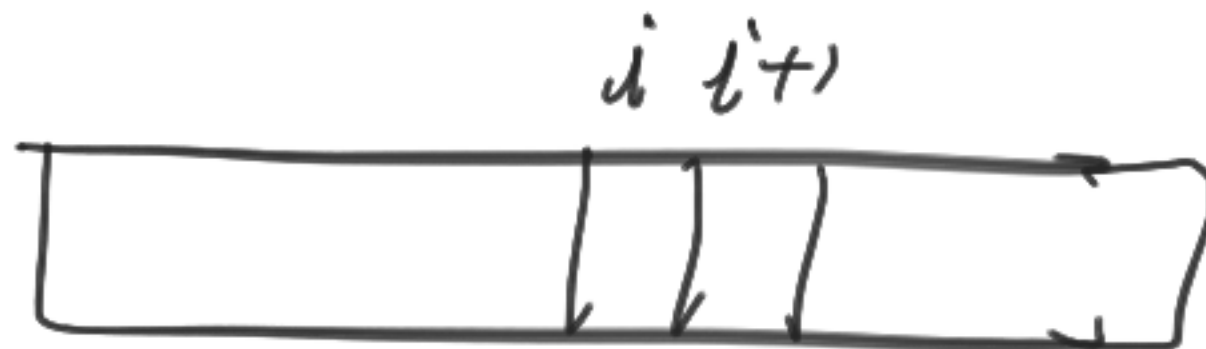
⇒

max and min

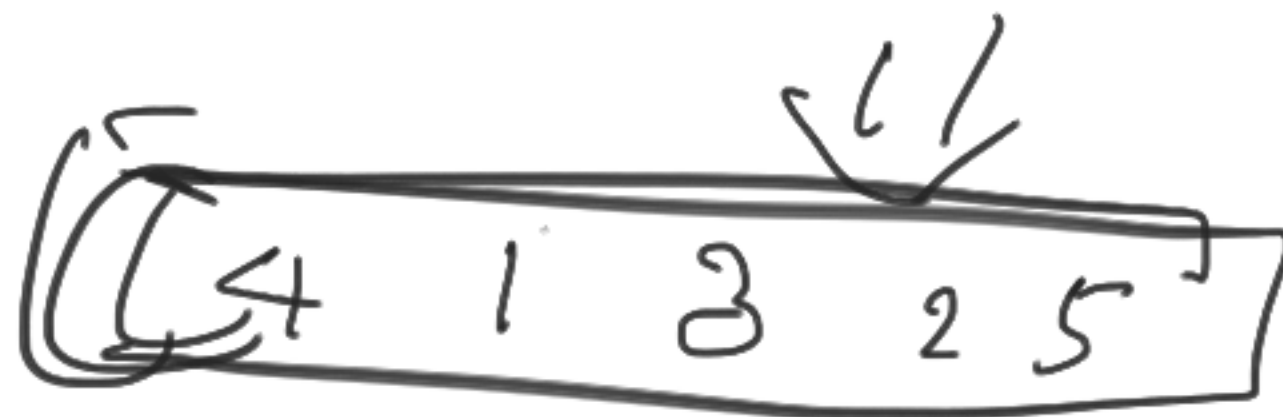
$$l = i + 2$$

⇒

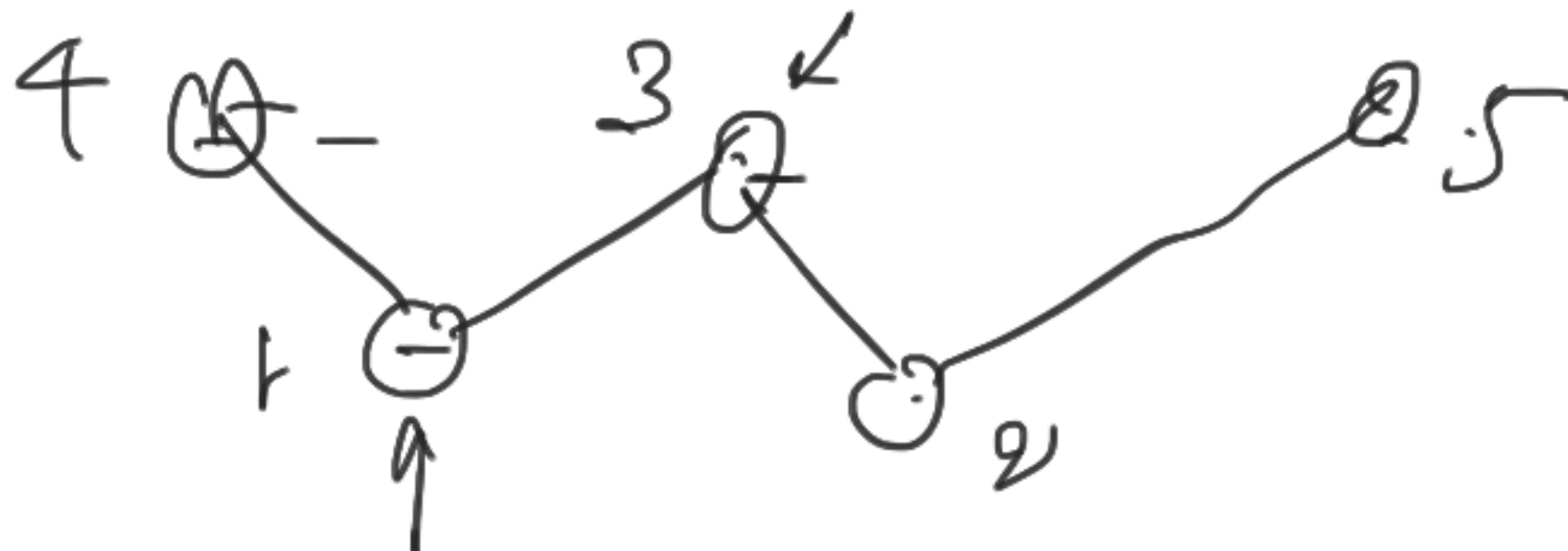
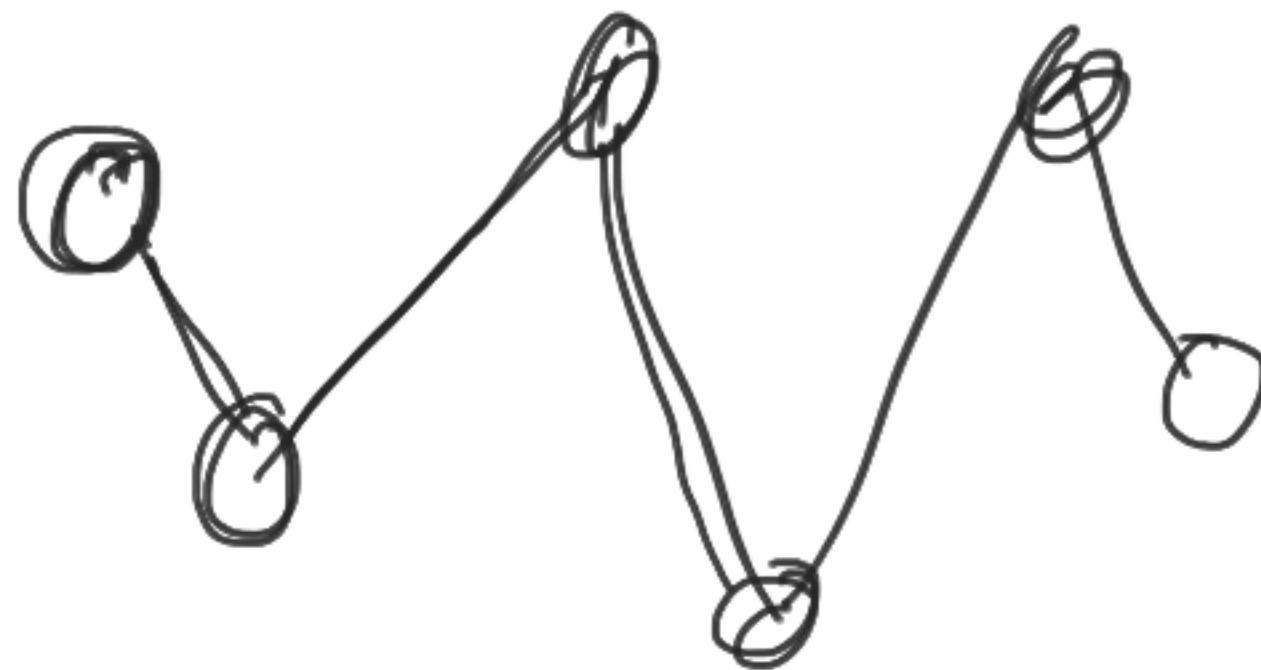
wave array

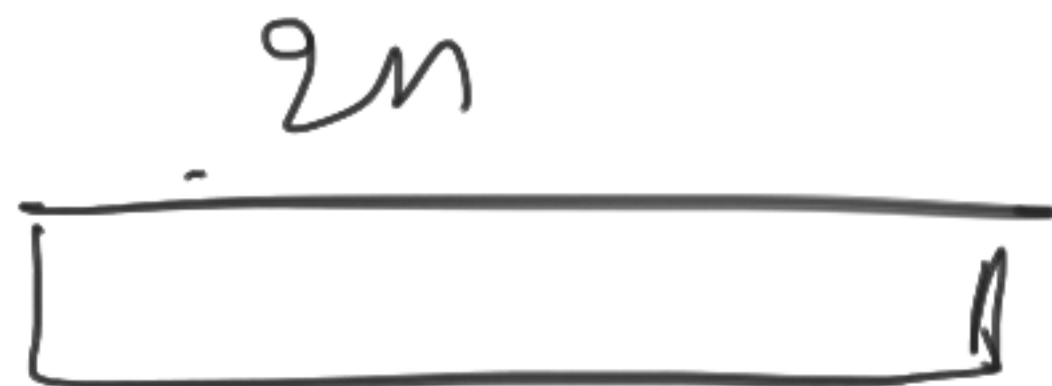
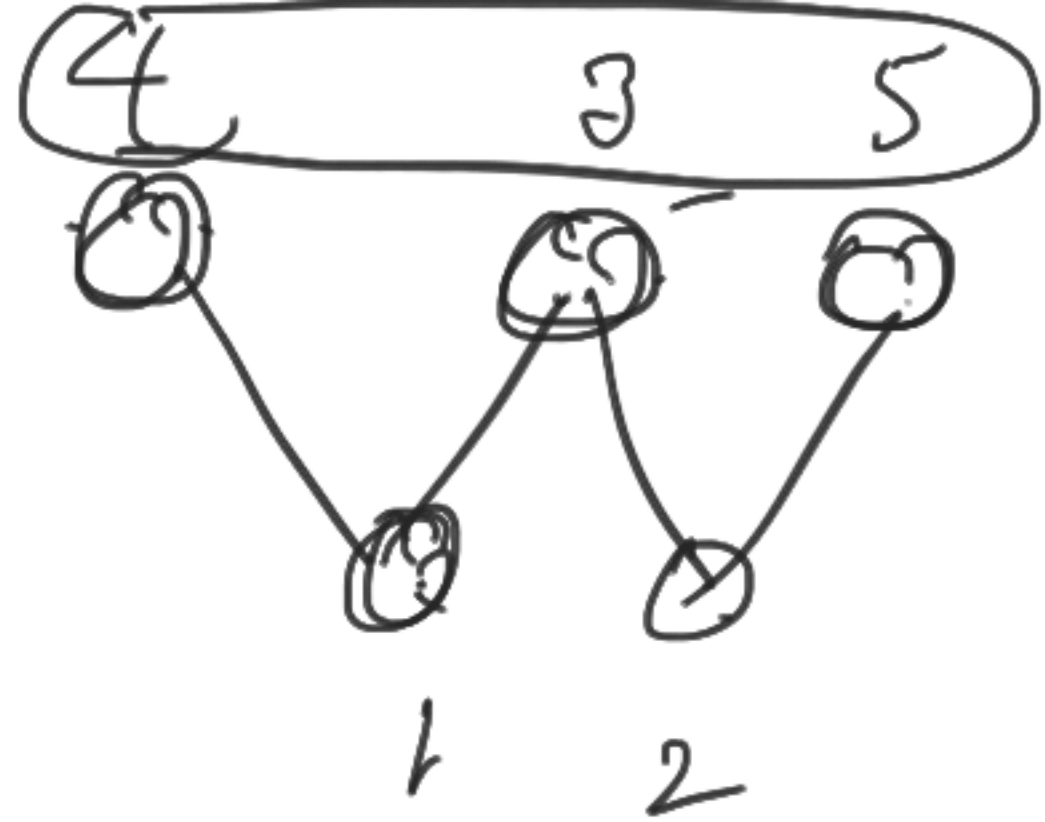


A12



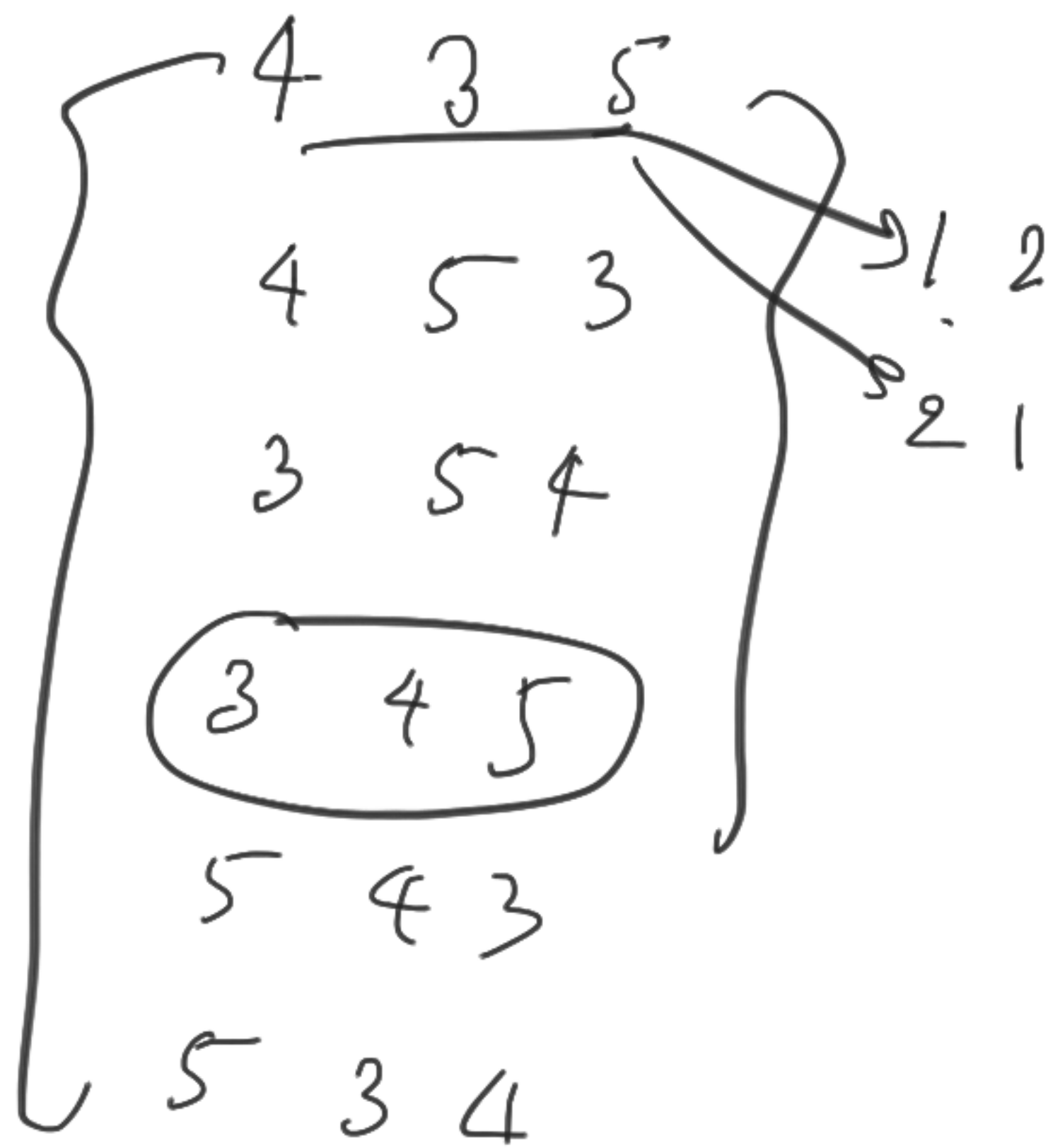
⇒

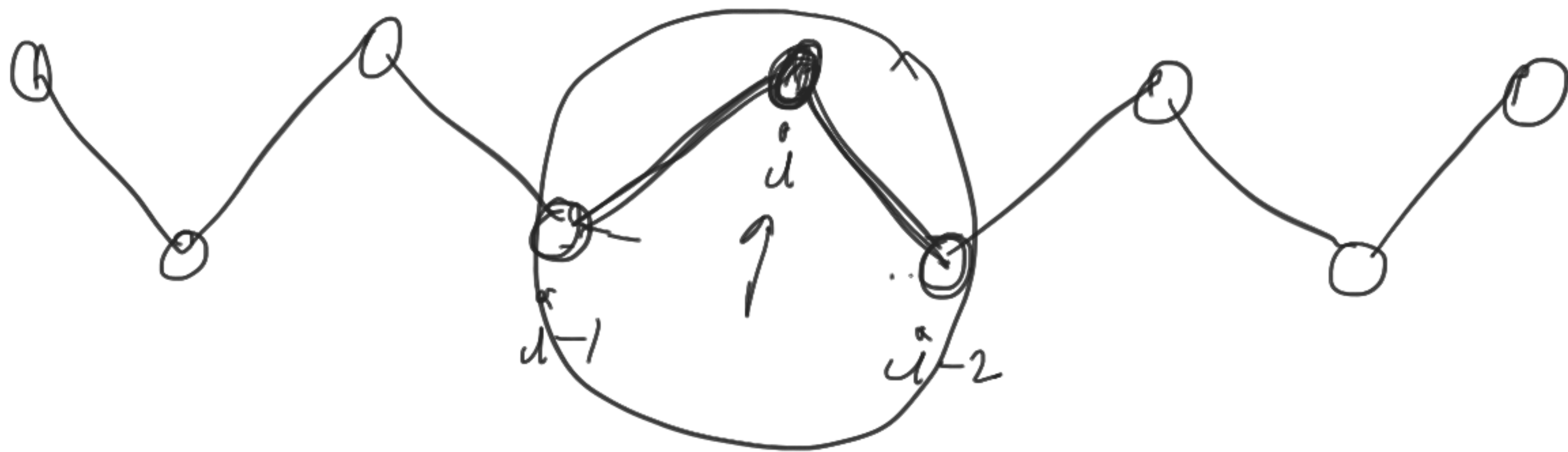
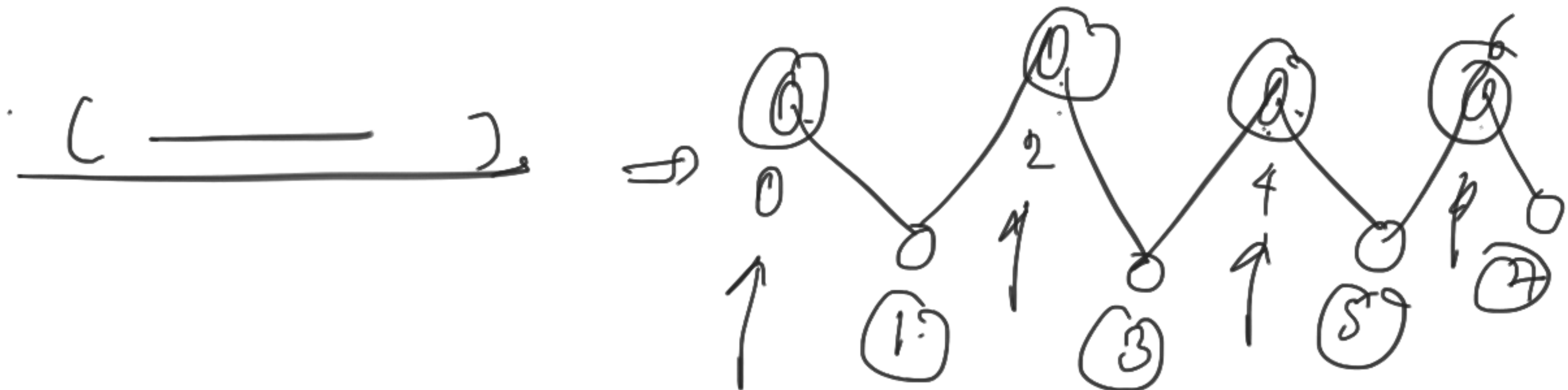


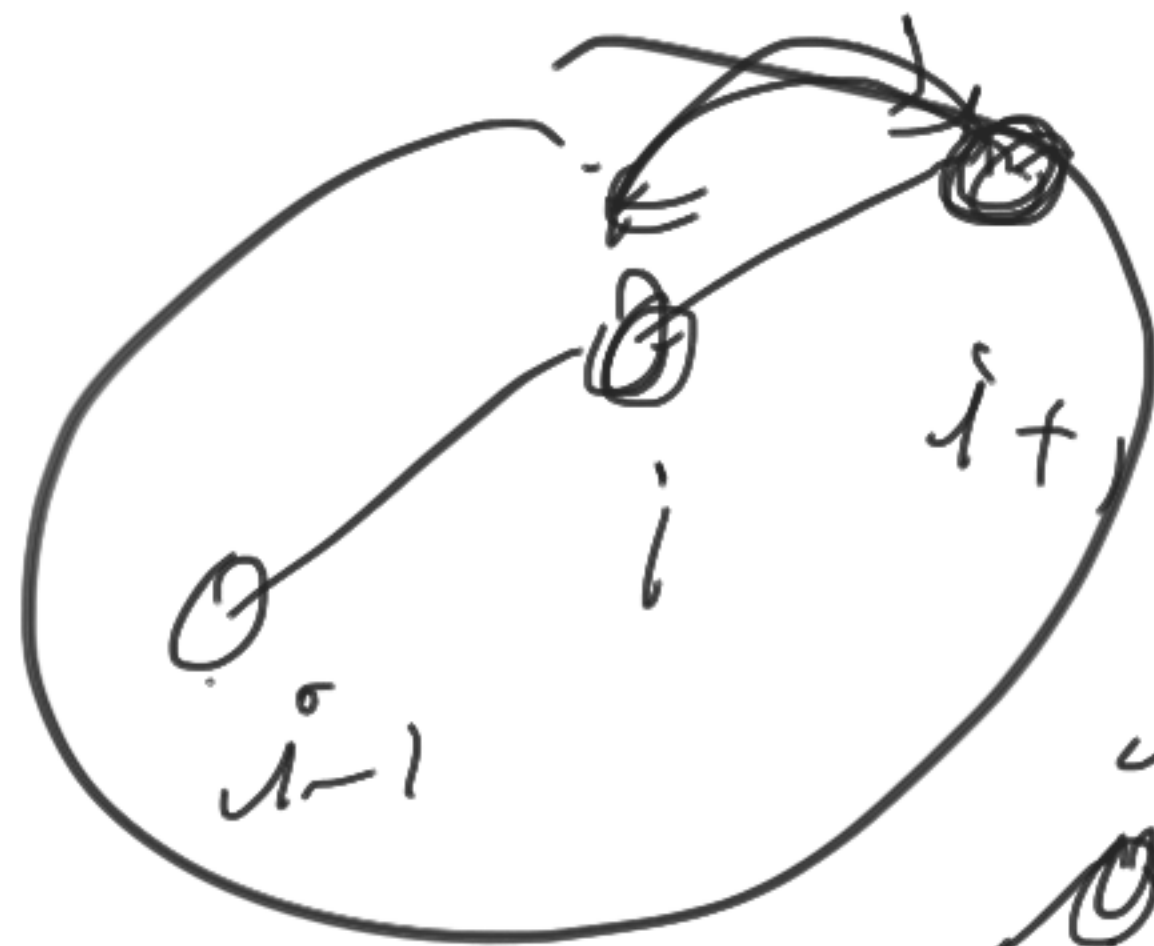
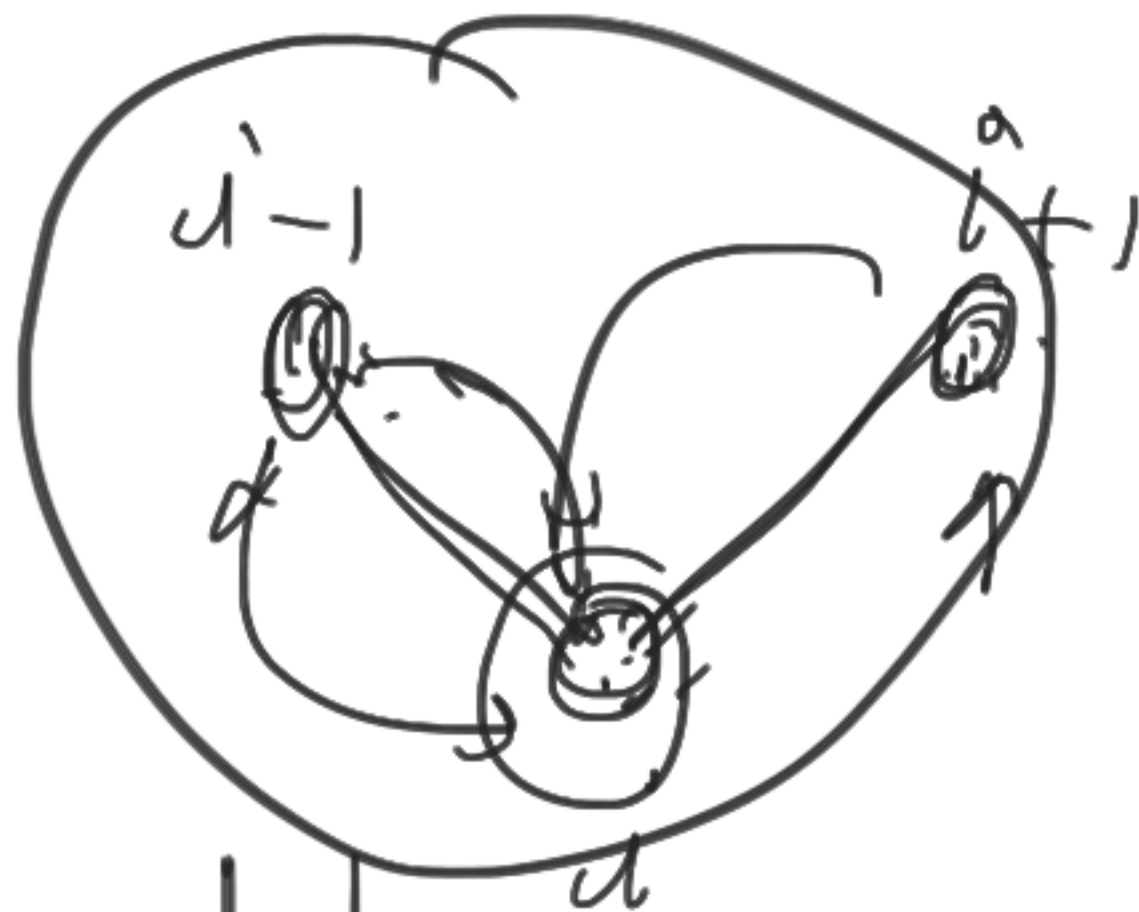
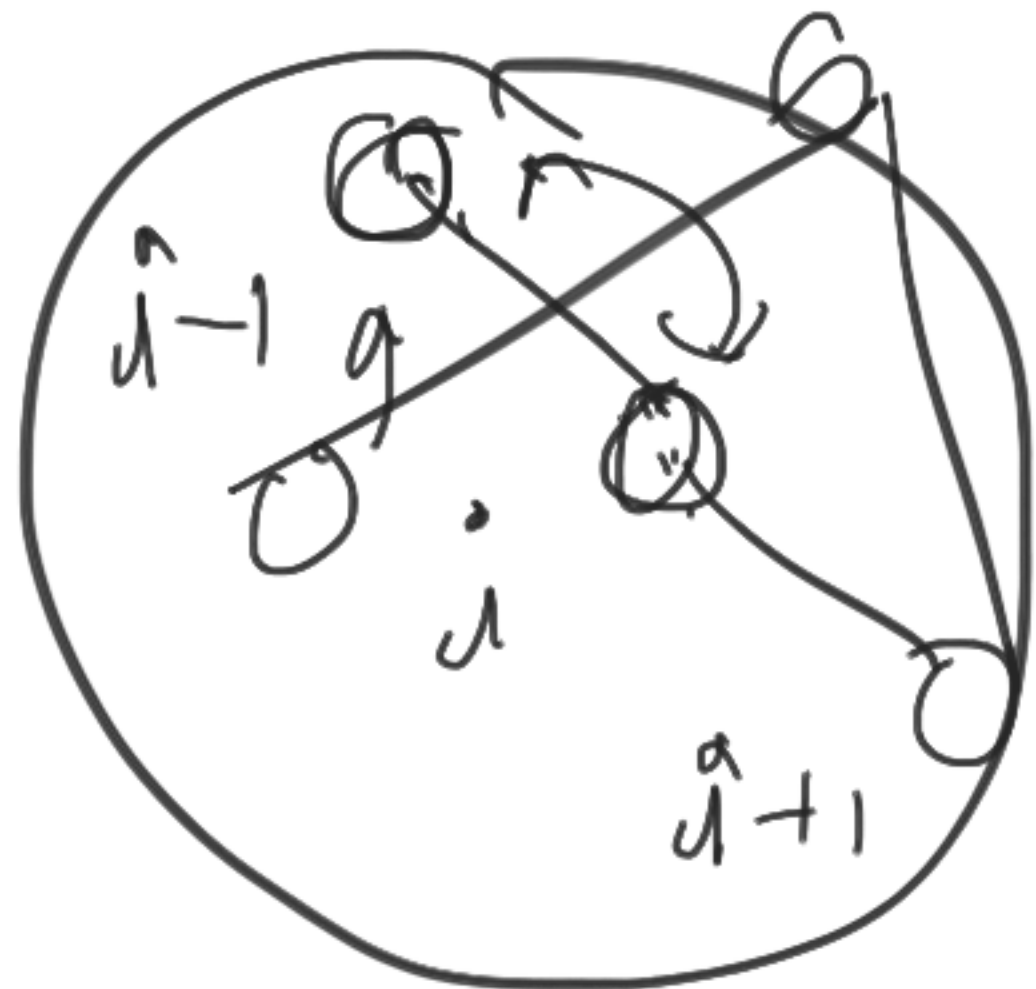


n points $\Rightarrow \lfloor n \rfloor$

n vertices $\Rightarrow \lfloor n \rfloor \Rightarrow (\lfloor n \rfloor)^2$

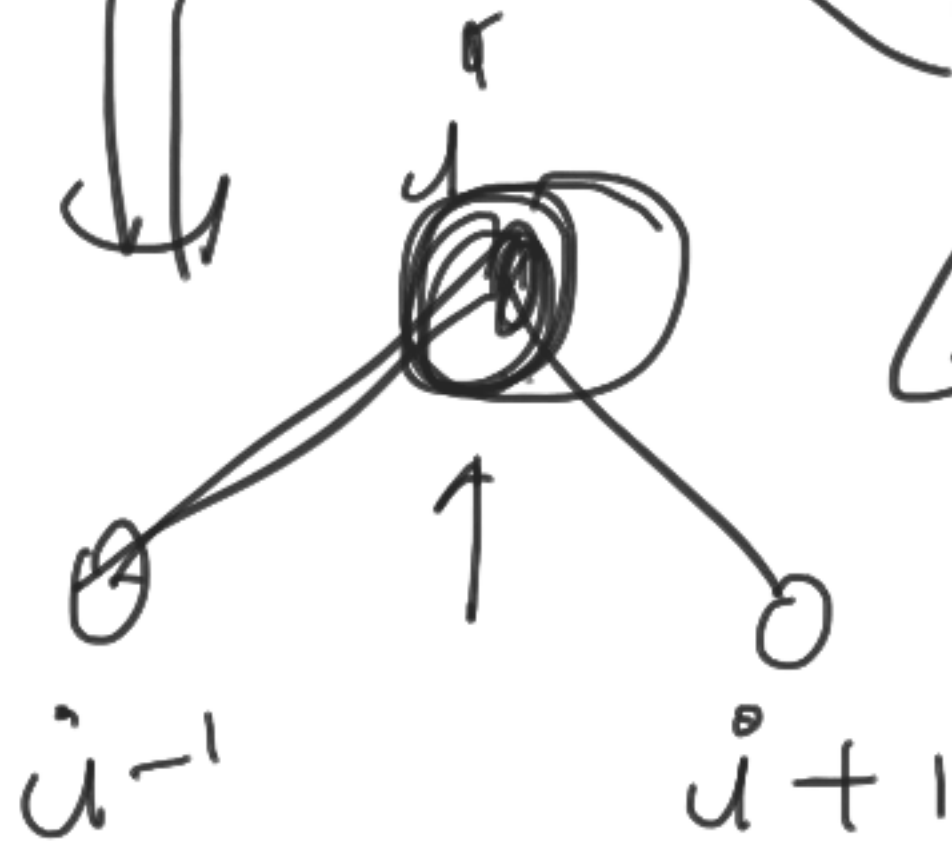






✓

⇔



↓

⇒

0 2 4 $i-1 - i+1$



$$\textcircled{A[i-1]} \leq A[i] \geq A[i+1]$$

↑

↑

↑

$$\textcircled{O(n)}$$

$i-1$ i $i+1$



$$\textcircled{i = 0 \text{ to } n-1}$$

$$i = i + 2$$

$$i = \textcircled{n-1}$$

$$i > 0 \ \& \ i < n-1$$

$$\text{if } (A[i] < A[i-1])$$

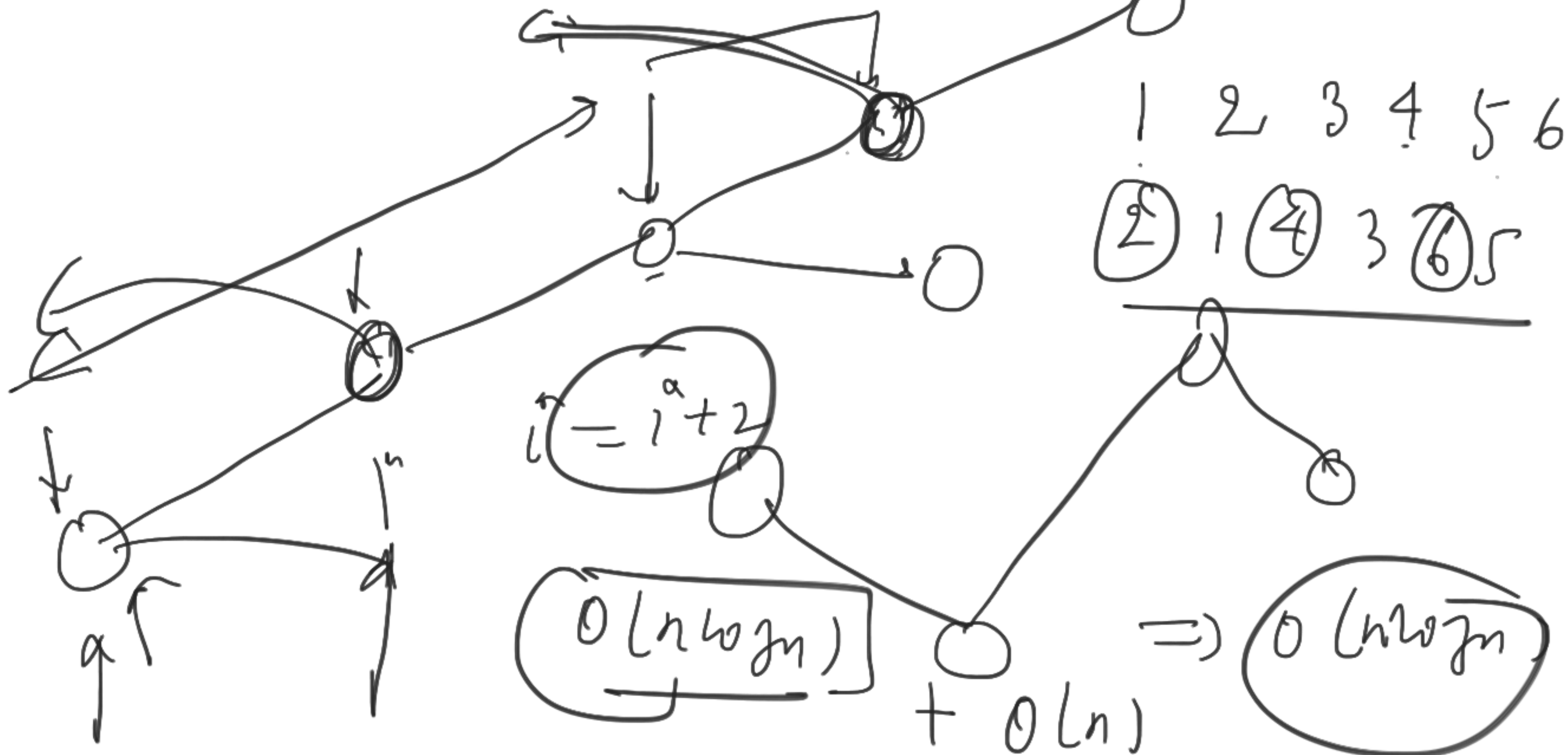
$$\text{Swap}(i, i-1)$$

$$\textcircled{i < n-1}$$

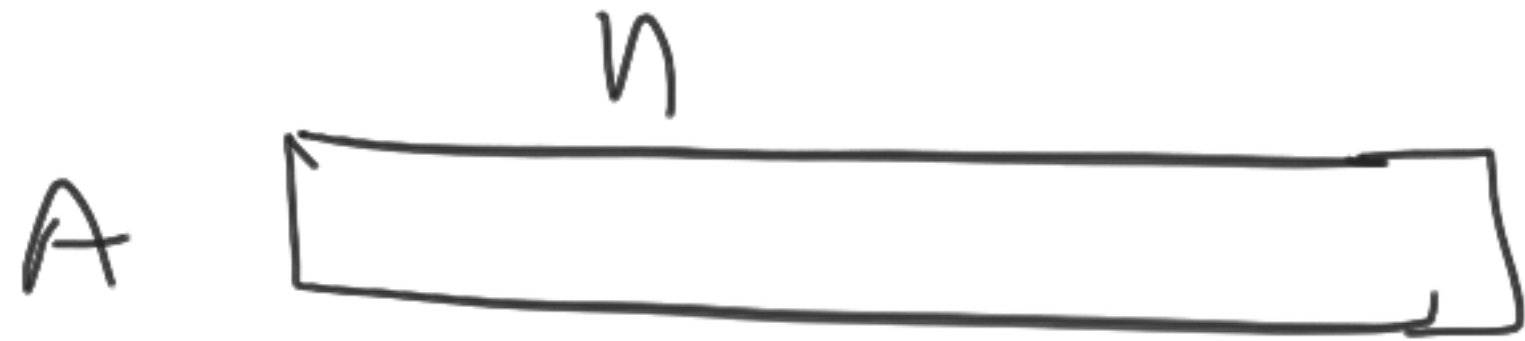
$$\text{if } (A[i] < A[i+1])$$

$$\text{Swap}(i, i+1)$$

Sort the array

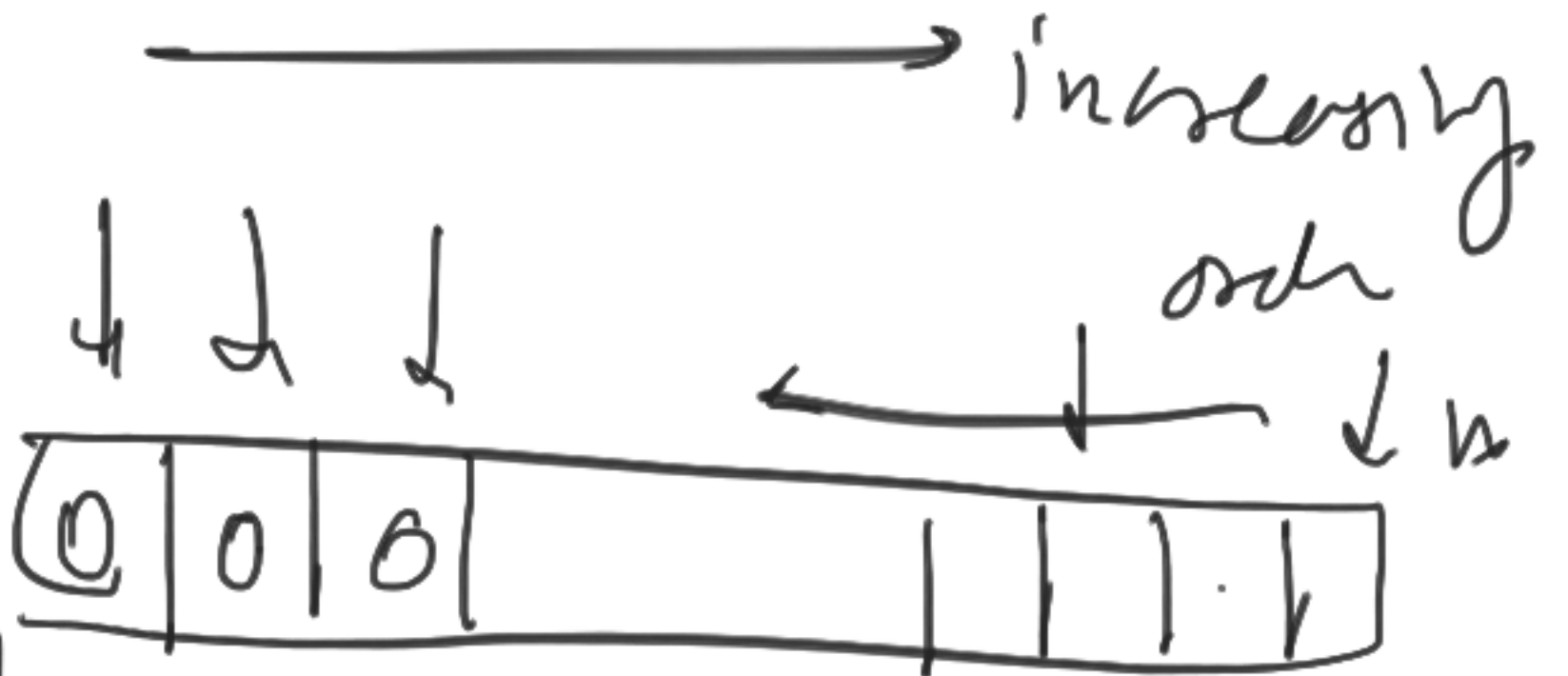


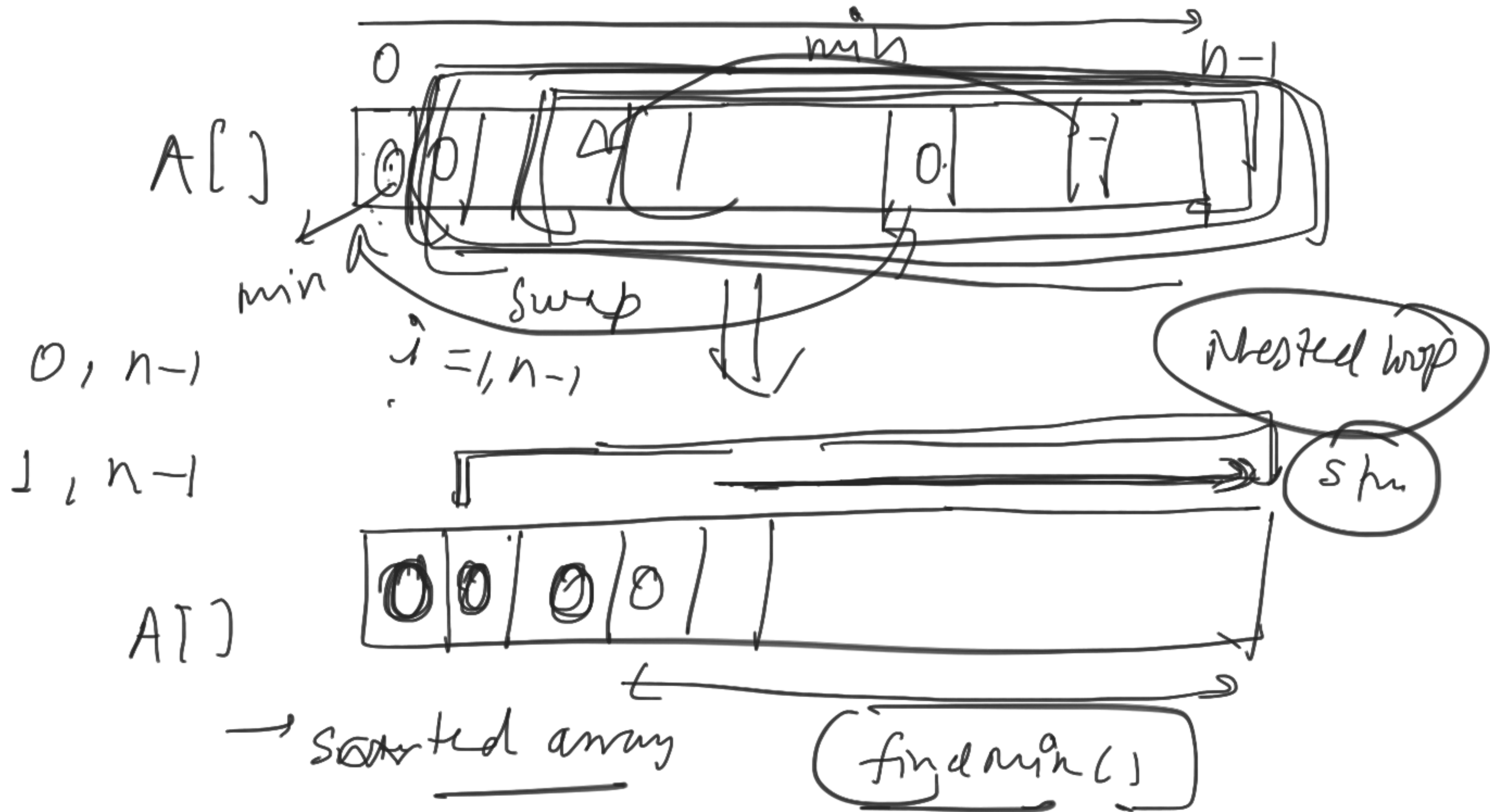
Selection sort
insertion sort



$$A[i-1] \leq A[i] \leq A[i+1]$$

$$A[0] \leq A[1] \leq \dots \leq A[n-1]$$



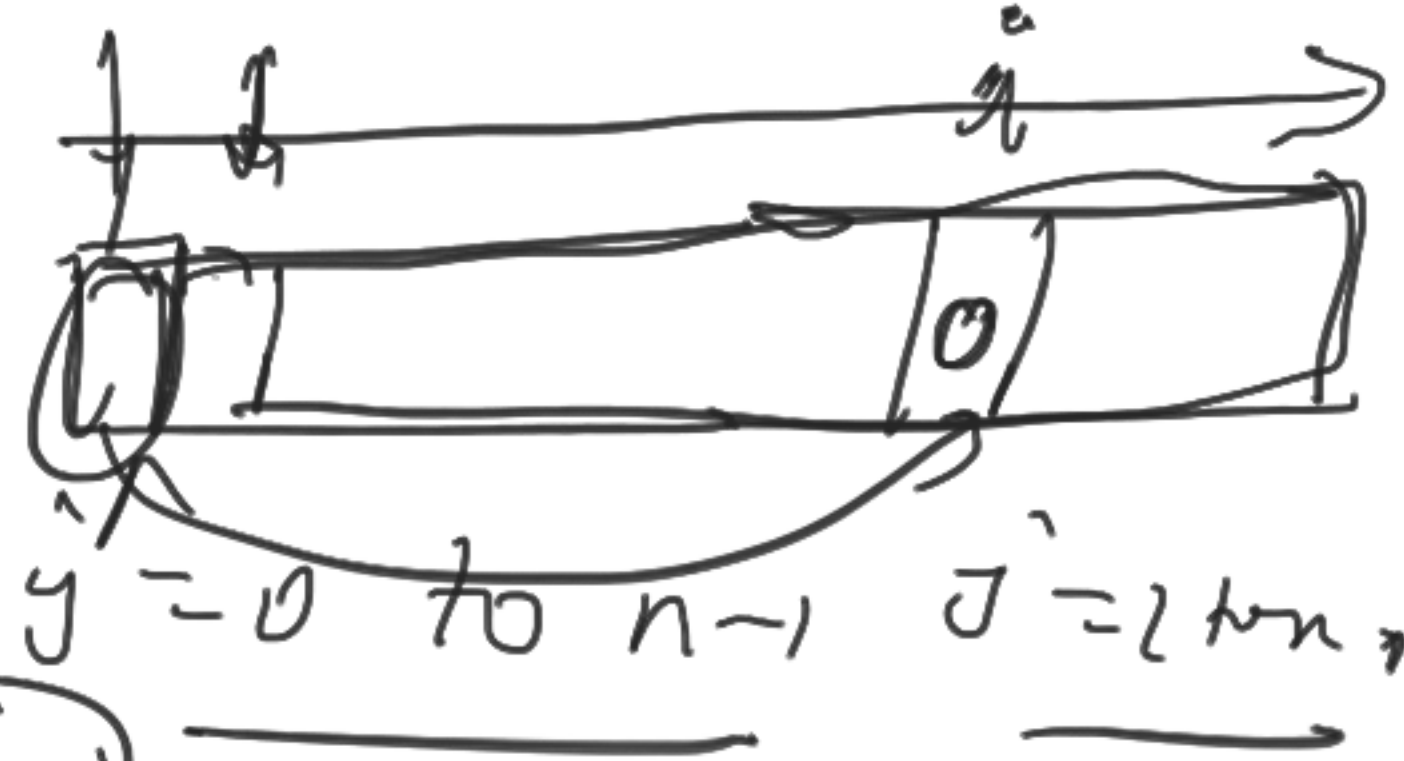


for ($i = 0$ to $n-2$)

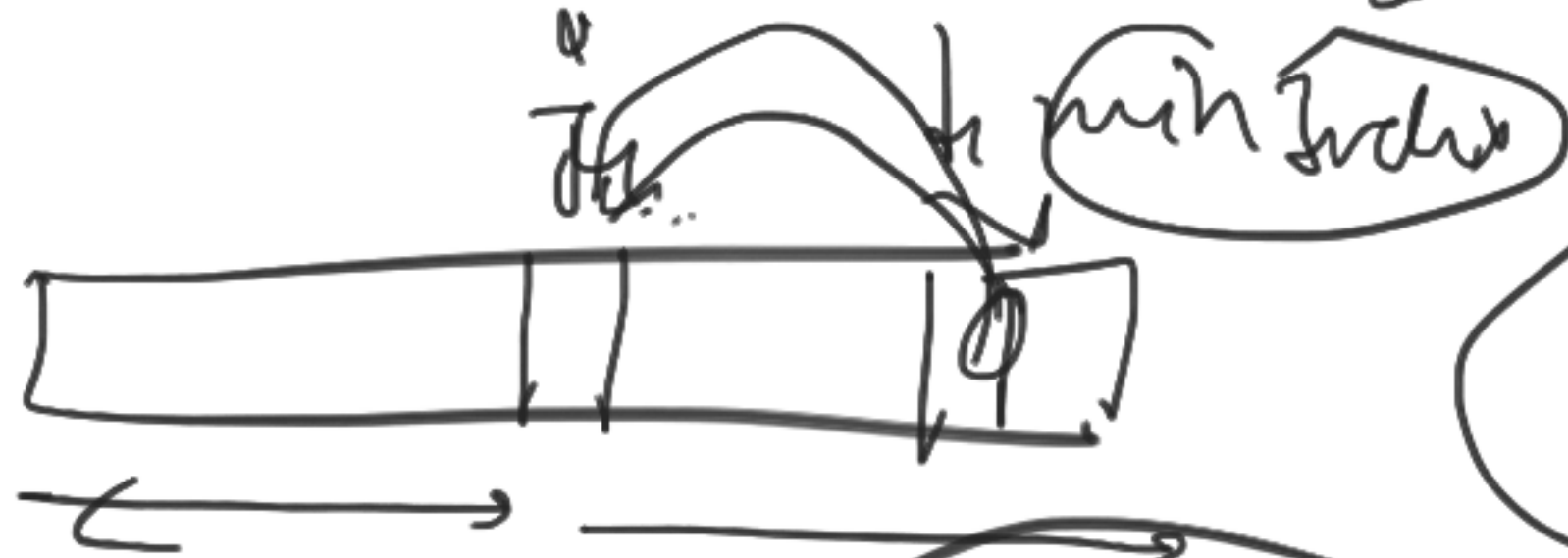
→ n

for ($j = i$ to $n-1$)

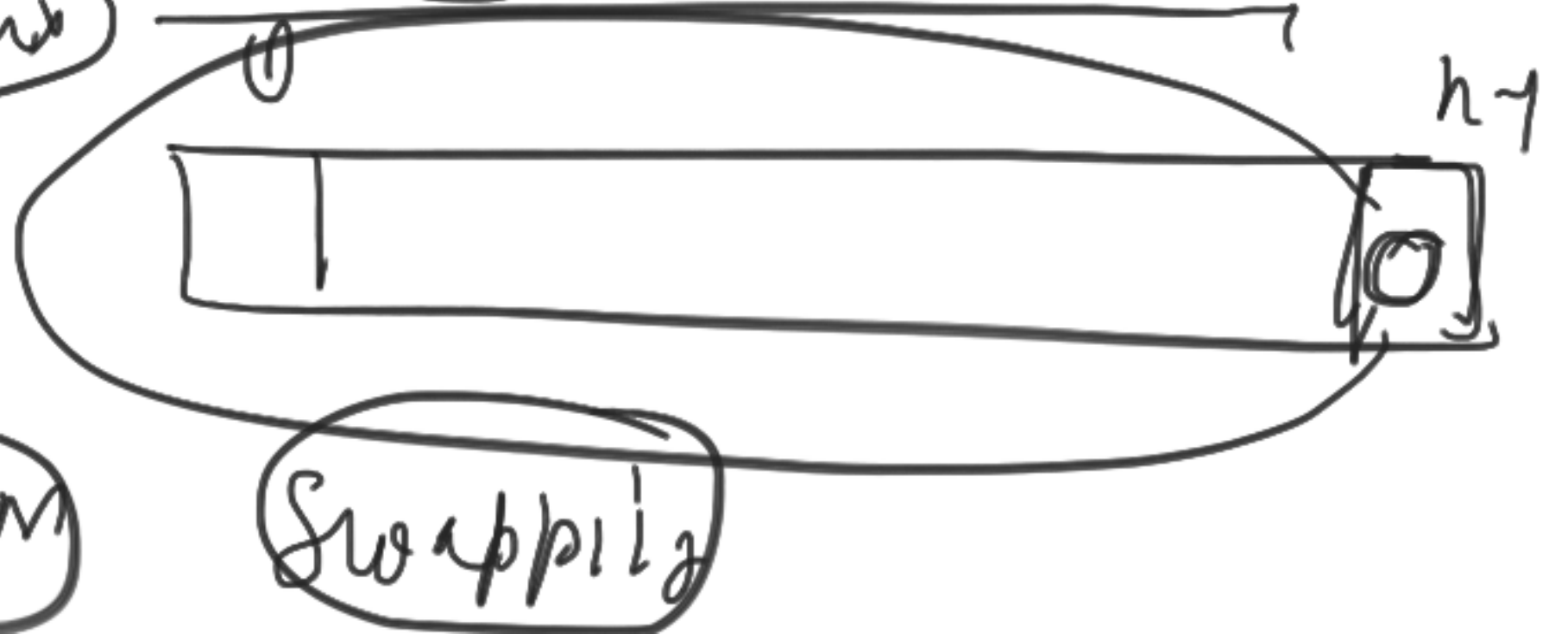
(i to $n-1$)



($n-1$) loop

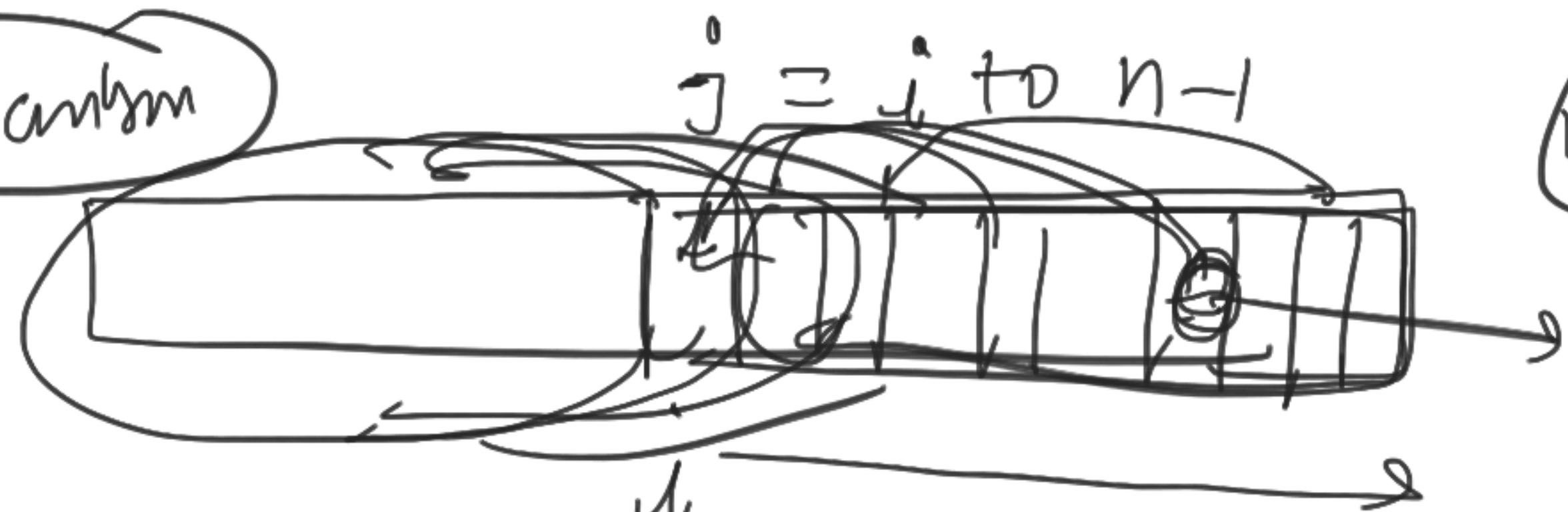


Comparison



Swapping

Comparison



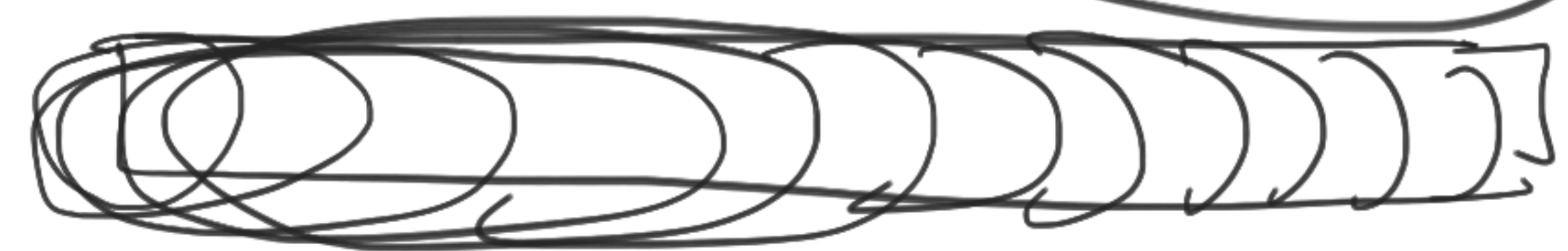
$\text{minIndex} = i$

minIndex

time complexity

n swapping

$n - i$ \rightarrow $O(n^2)$



$$\frac{n(n+1)}{2}$$

$n + n - 1 + n - 2 + \dots + 1$

Why sorting? \Rightarrow in-depth

Sorted \rightarrow binary search

$O(\log n)$

\Rightarrow Recursive

\Rightarrow Iterative

Single loop \swarrow
Two Pointers

Process the data

inserts

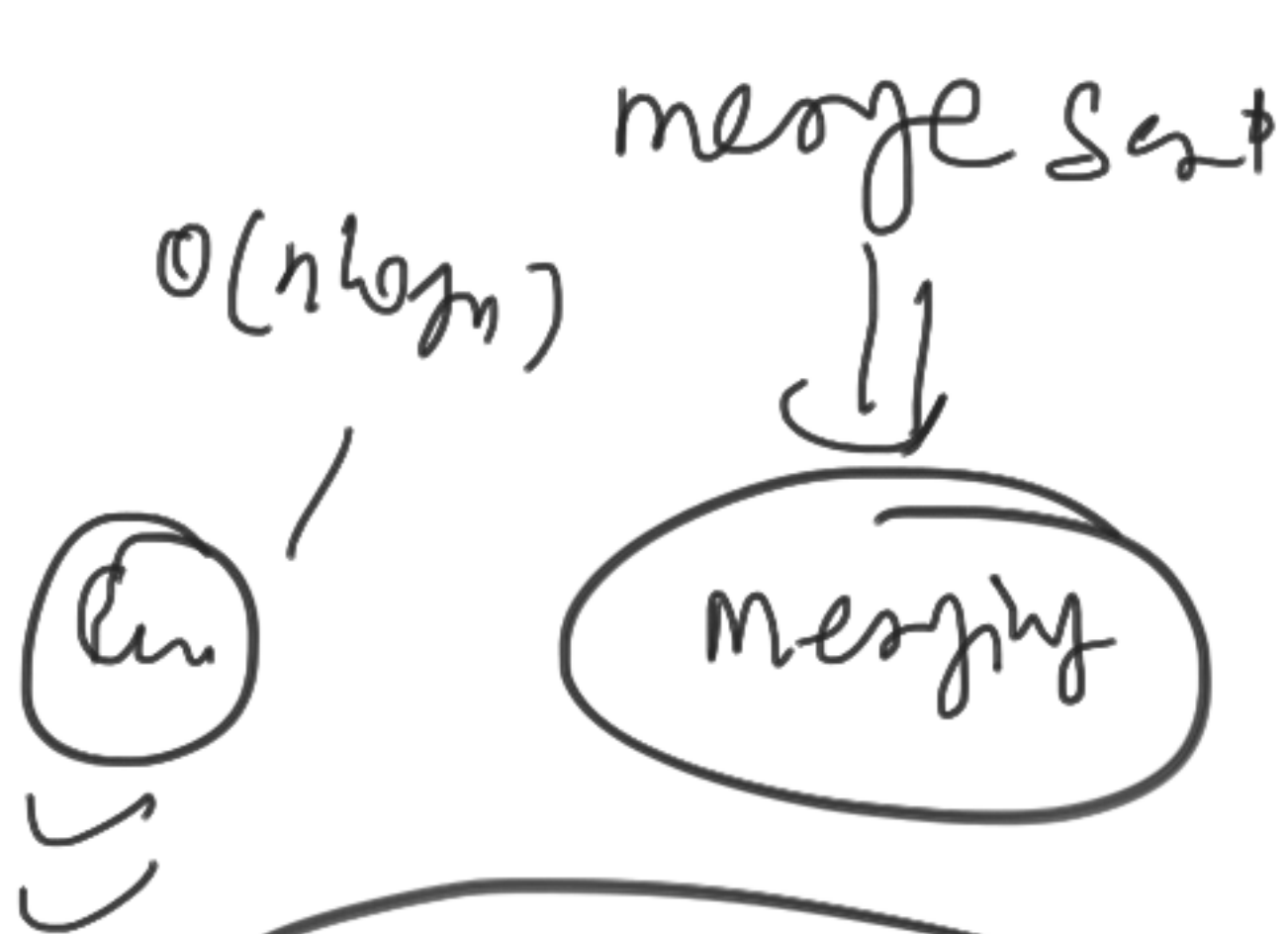


$\Downarrow O(n \log n)$

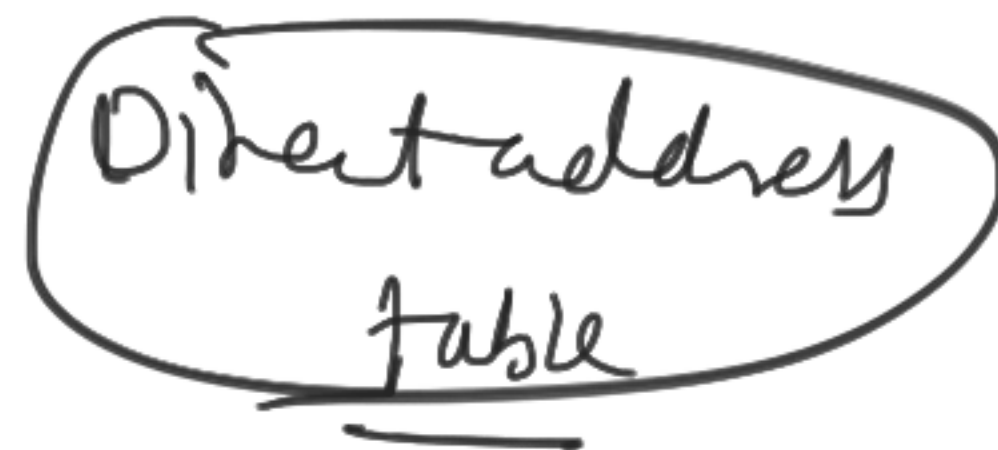


Sorted

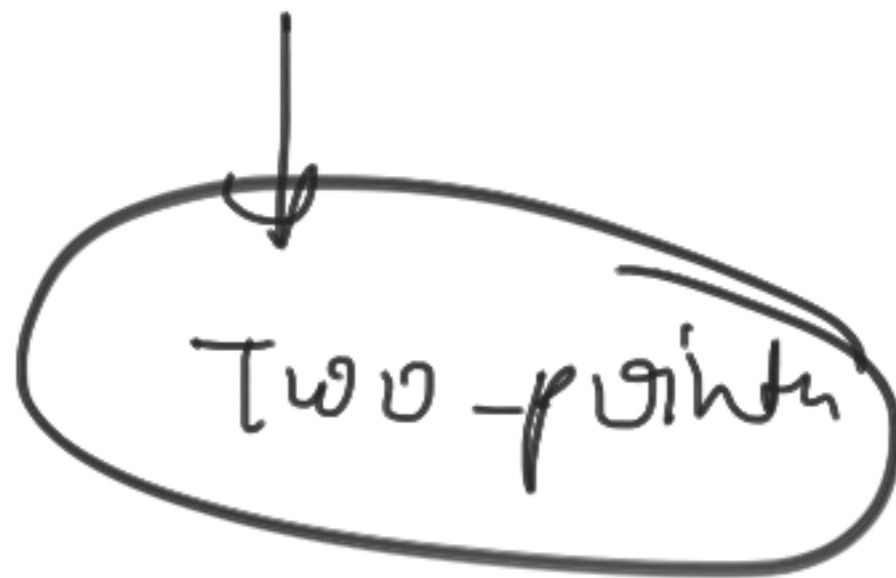
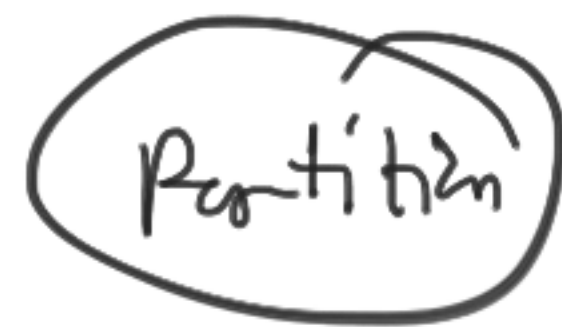




\Rightarrow



\Rightarrow

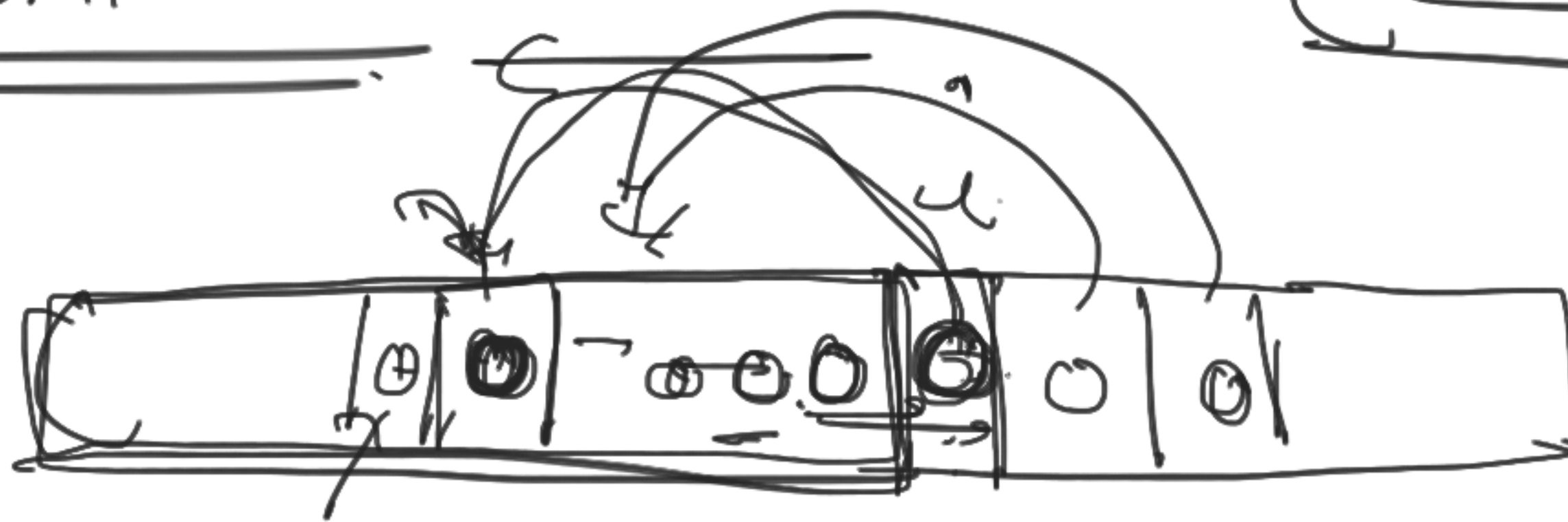


quick sort

A handwritten diagram for quick sort. The words 'quick sort' are written.



Insertion Sort



$O(n)$



Sorted

→

+1

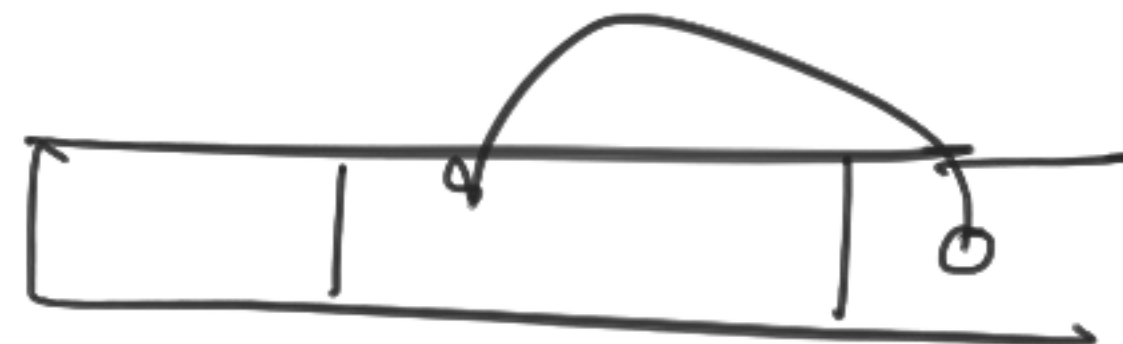
Unsorted part

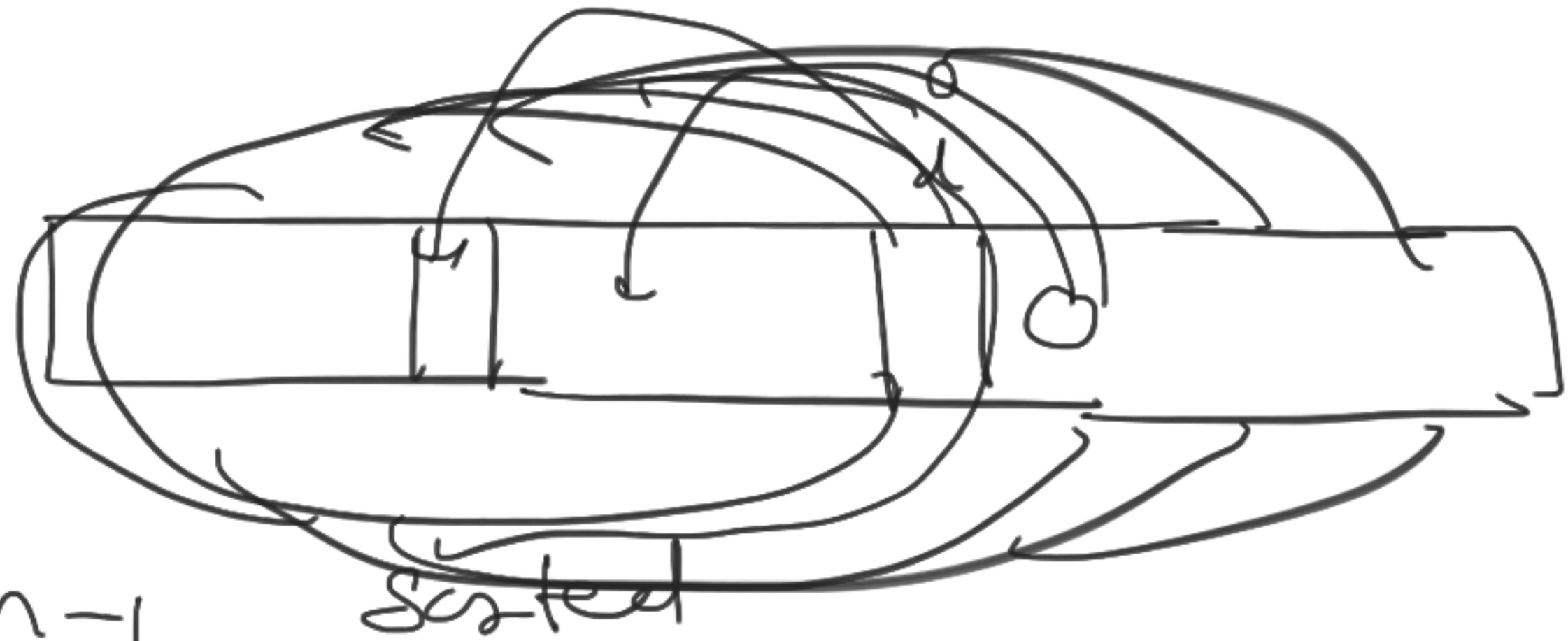
⇒



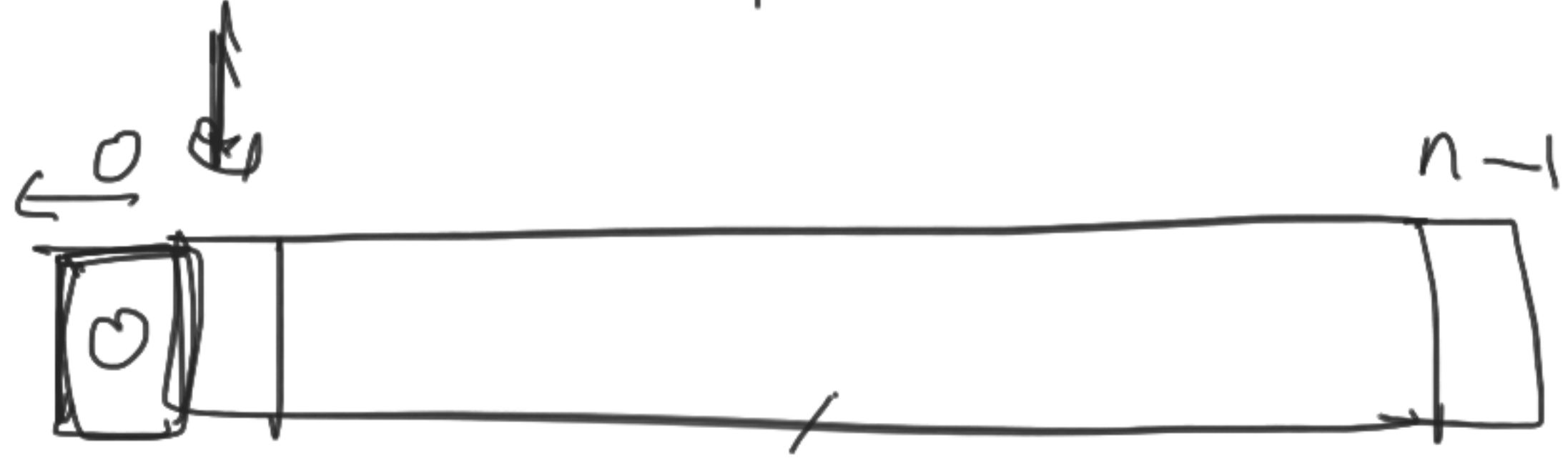
~~at the~~

i

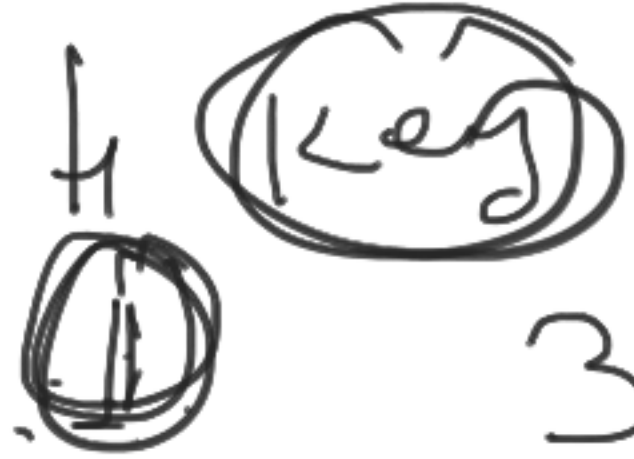




$d = 1 \text{ to } n-1$



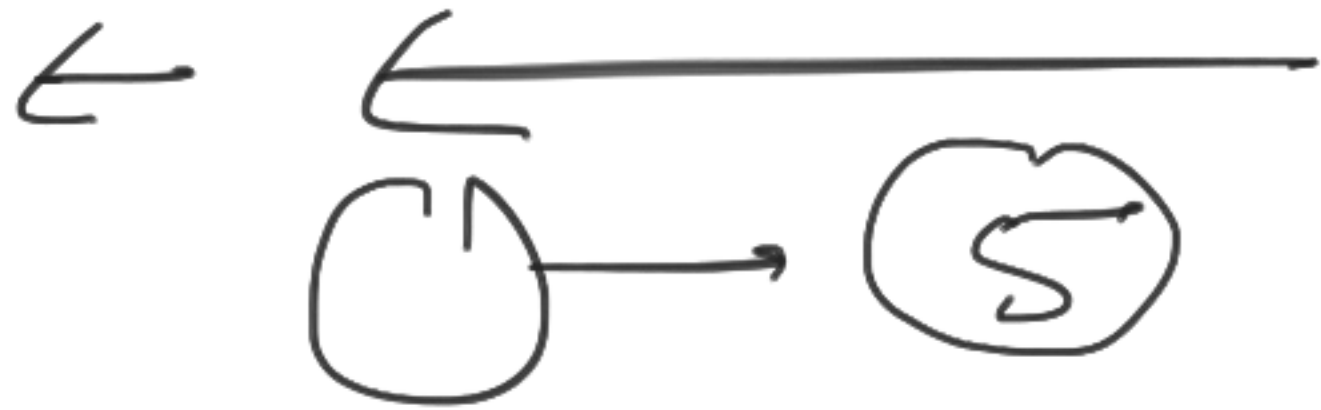
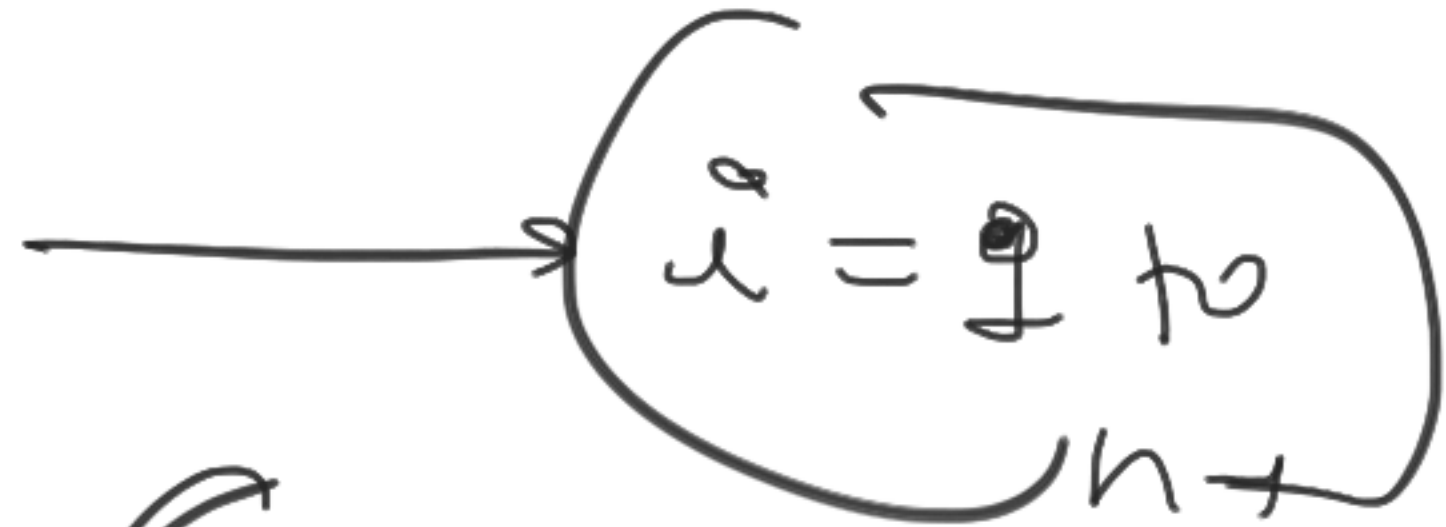
5



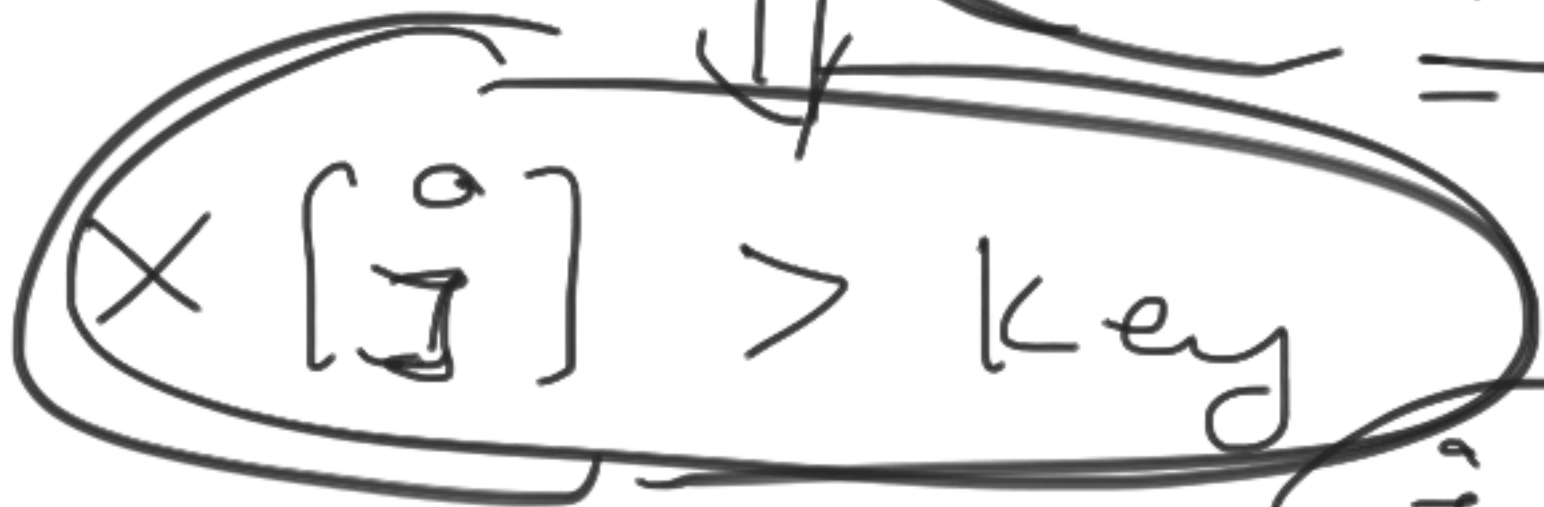
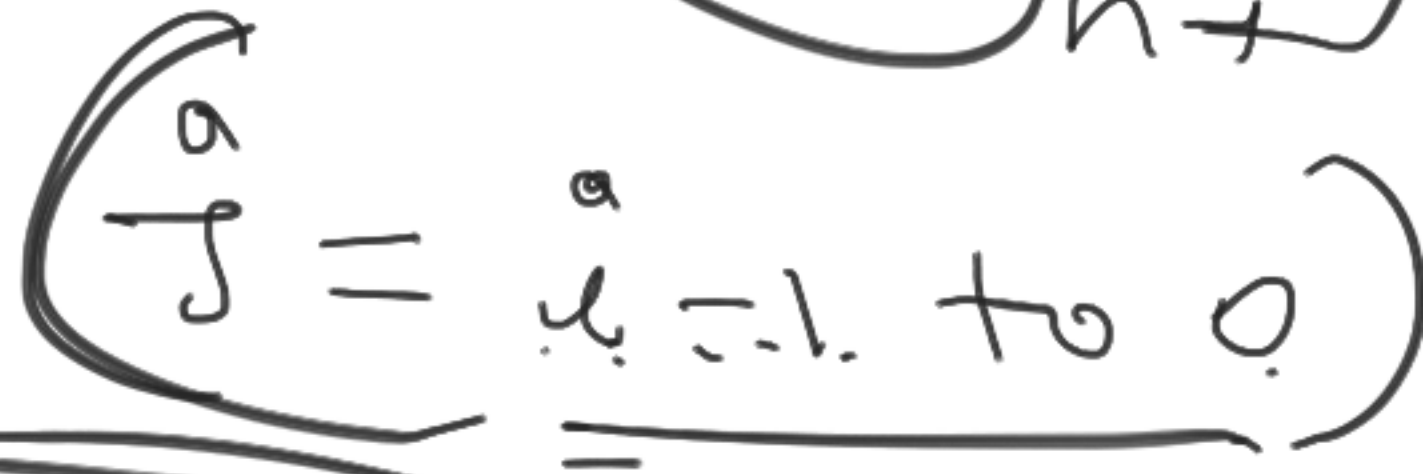
3

10

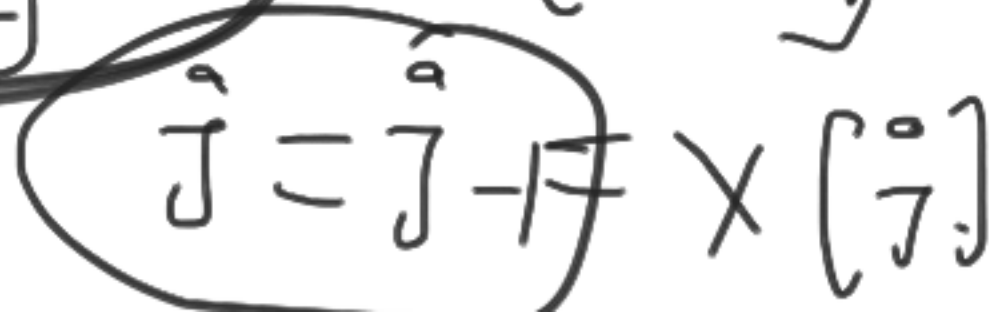
6



20



$X[j+1]$



for ($i = 1$ to $n-1$)

{ $key = x[i]$

$j = i - 1$

while ($j \geq 0$ &&

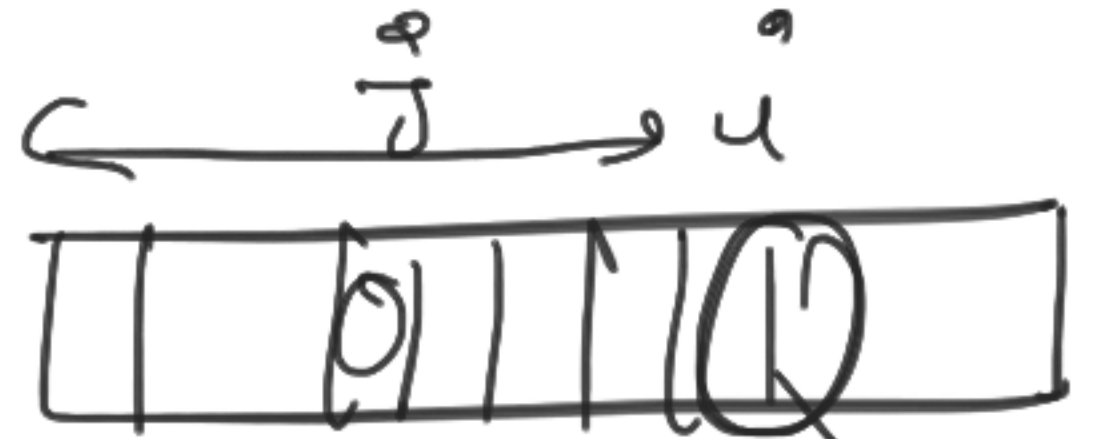
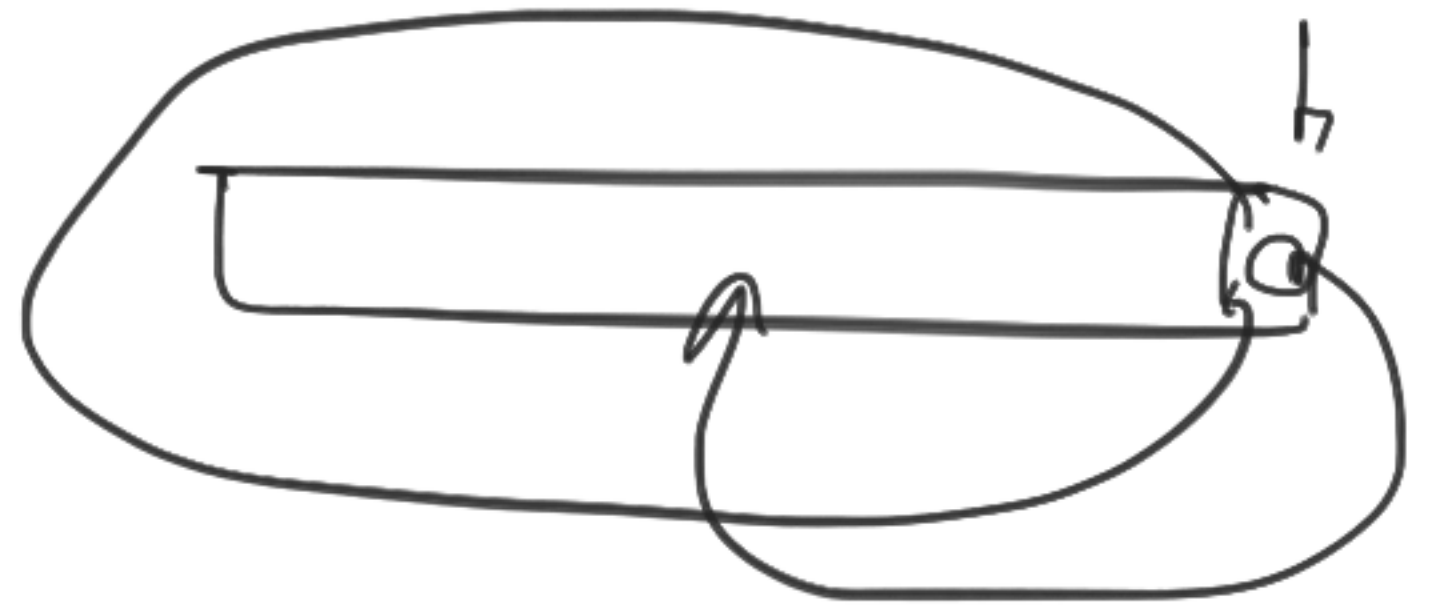
{

$x[j+1] = x[j]$

$j = j - 1$

}

$x[i+1] = key$



$x[j] > key$

$x[j] < key$

key

Data movement

② Worst Case
Best Case

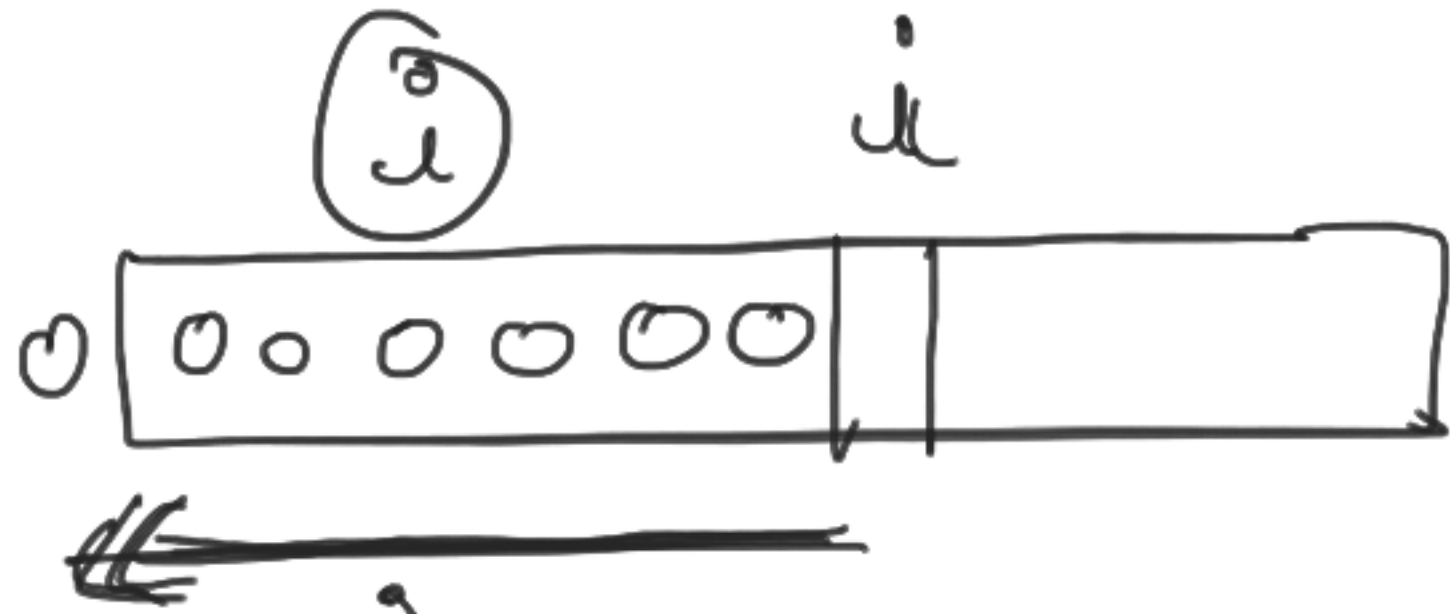
③ When should we use?

④

n inversions.

insertion
sort

Comparative
shifting

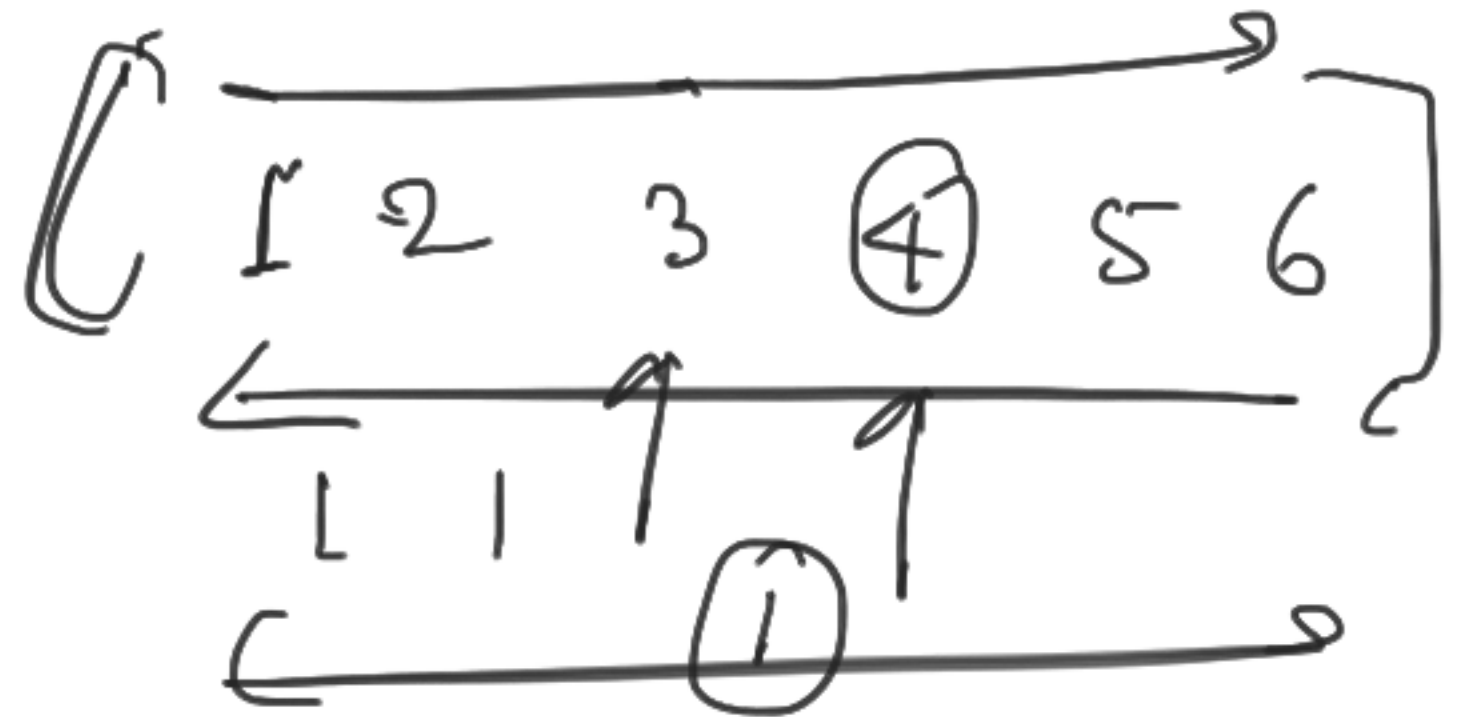
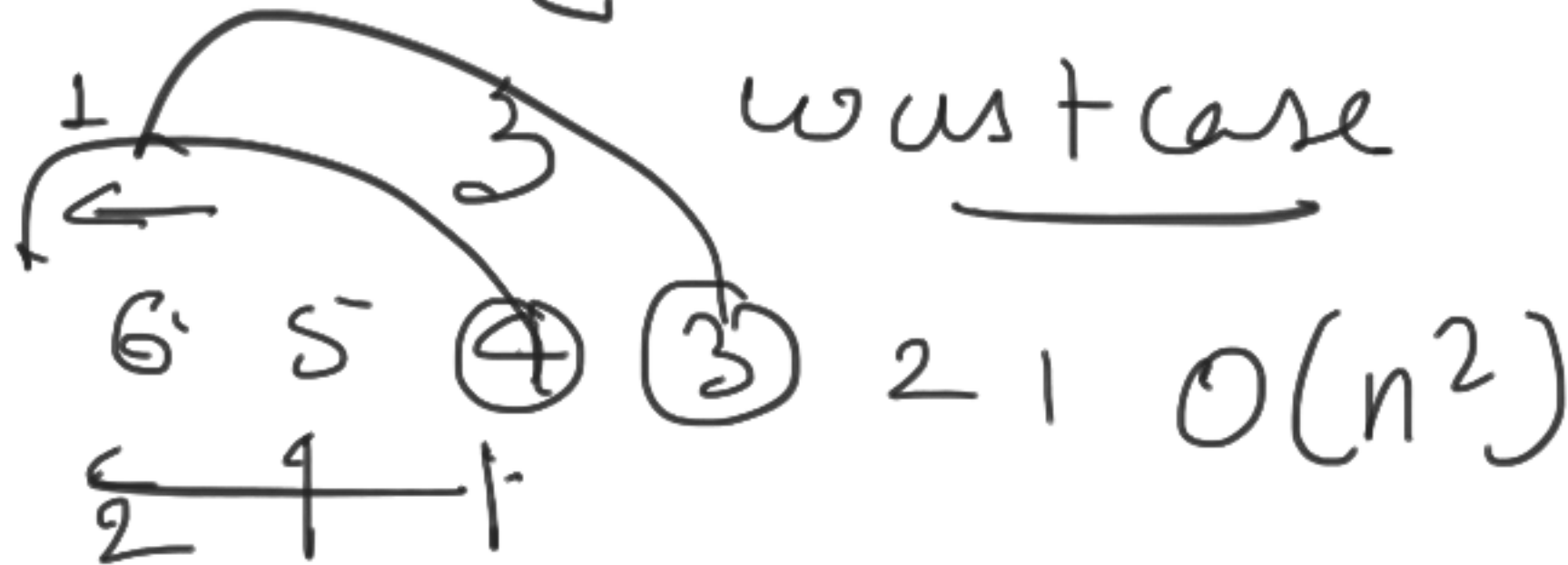


$$\Rightarrow 1 + 2 + \dots + n - 1$$

$$= \frac{n(n-1)}{2} \Rightarrow O(n^2)$$

i comp
 i shifting

worst case

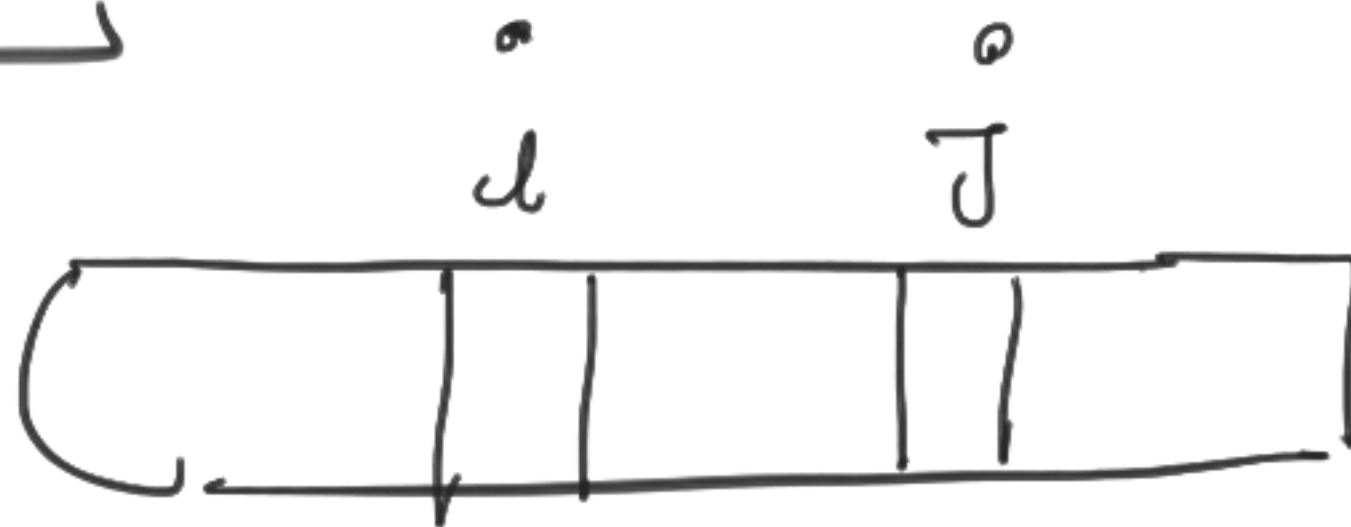


$O(n)$ n comp
 O shift

almost sorted \Rightarrow $O(n)$
 Partially sorted.

inversion

$\begin{pmatrix} 0 & 0 \\ i & j \end{pmatrix}$



if $A[i] > A[j]$

$i < j$

one inversion



(3) (1) (4)

$(3, 2)$ $(3, 1)$
 $(4, 1)$ $(2, 1)$