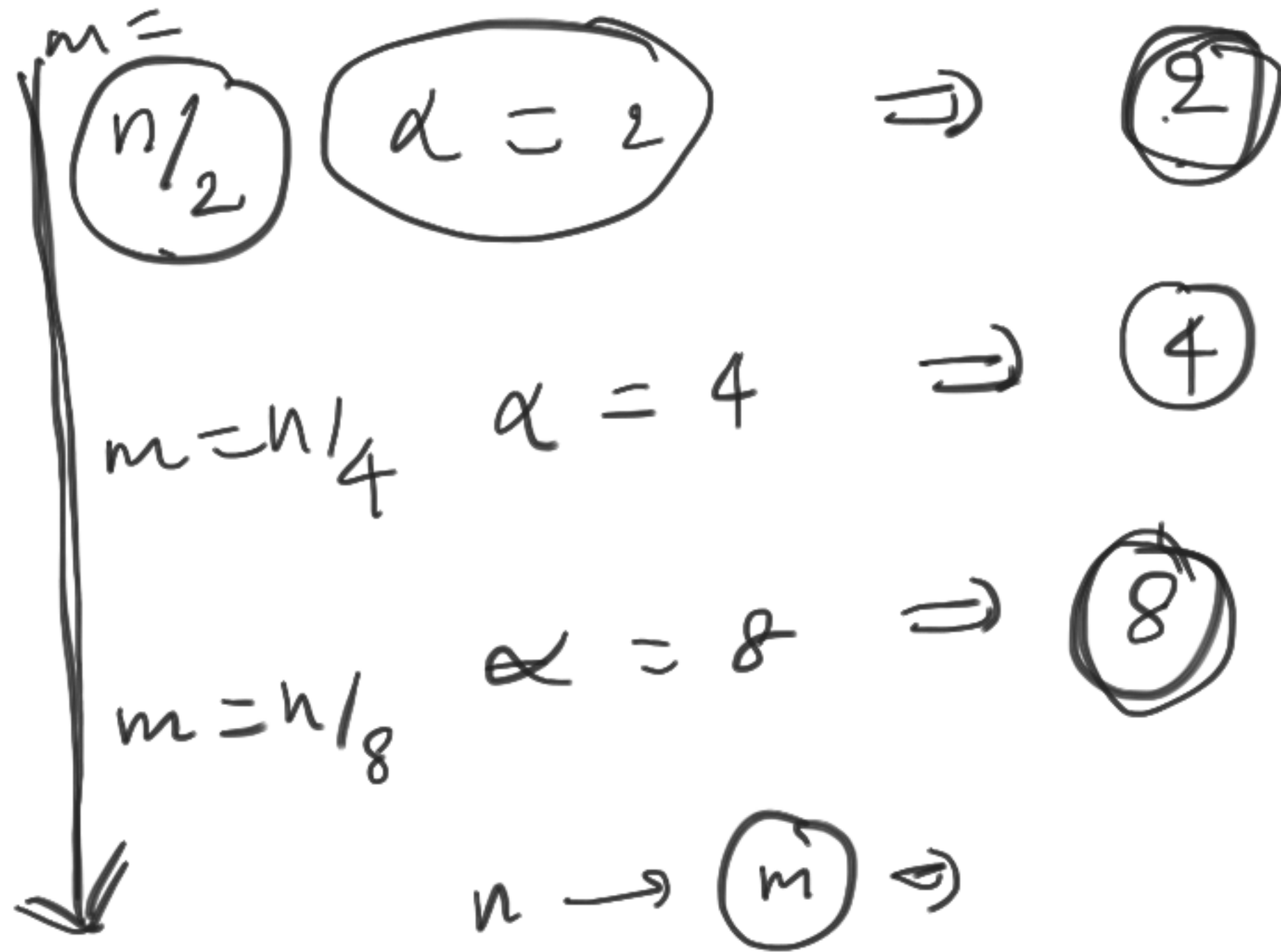


$$d = n/m \Rightarrow O(\alpha) \Rightarrow \xrightarrow{\alpha}$$



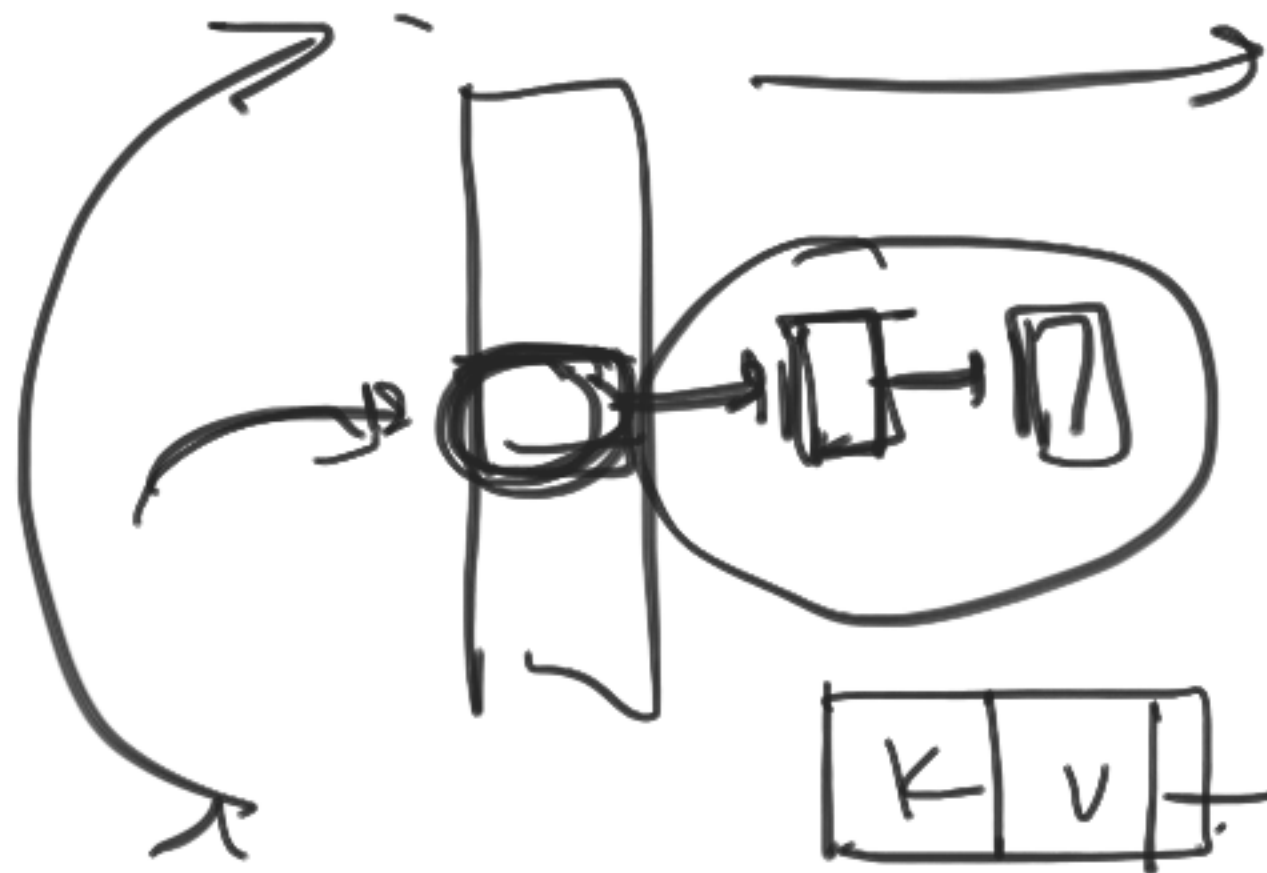
Time memory tradeoff

$m \geq n$

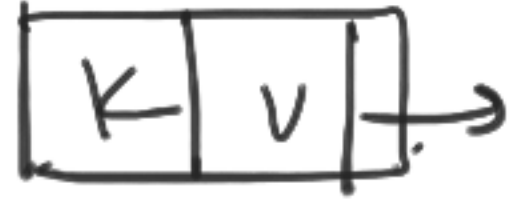
List

Array

Open addressing



n Keys



$m \geq n$

$O(\log n)$

BST

AVL
red-black

$n = 10^{10}$

$m = 10^5$

insert
deletion

$O(\log \alpha)$

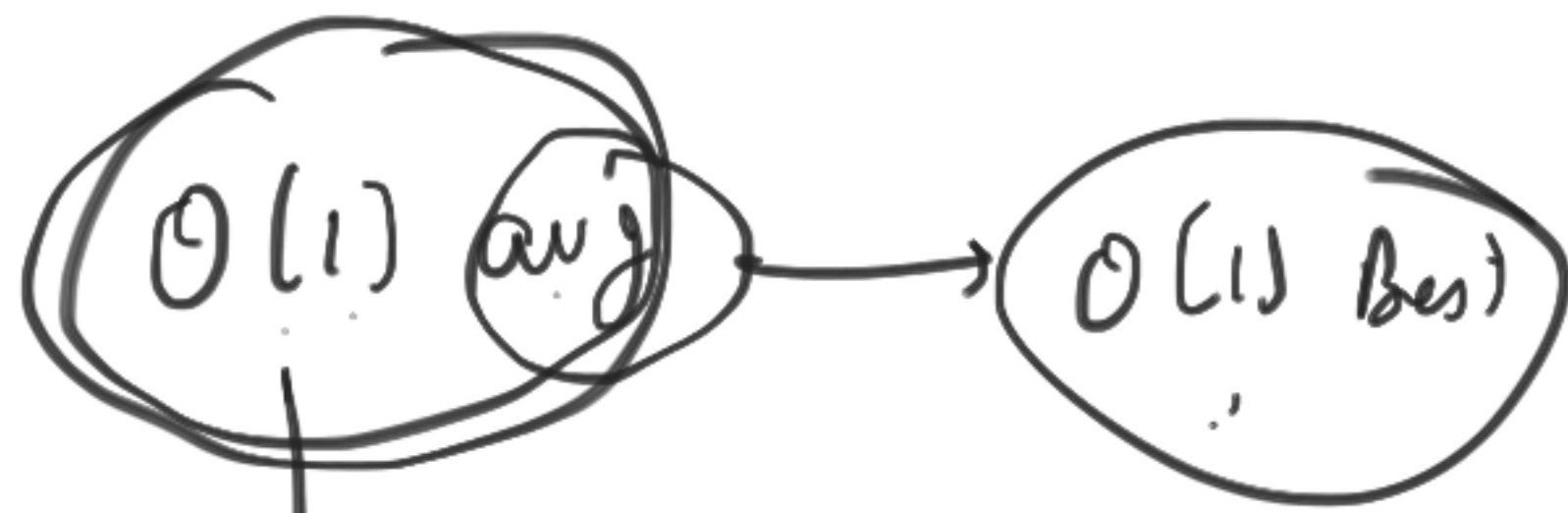
$$\alpha = \frac{10^{10}}{10^5} = 10^5$$

$O(\alpha)$

$O(m)$

Ans

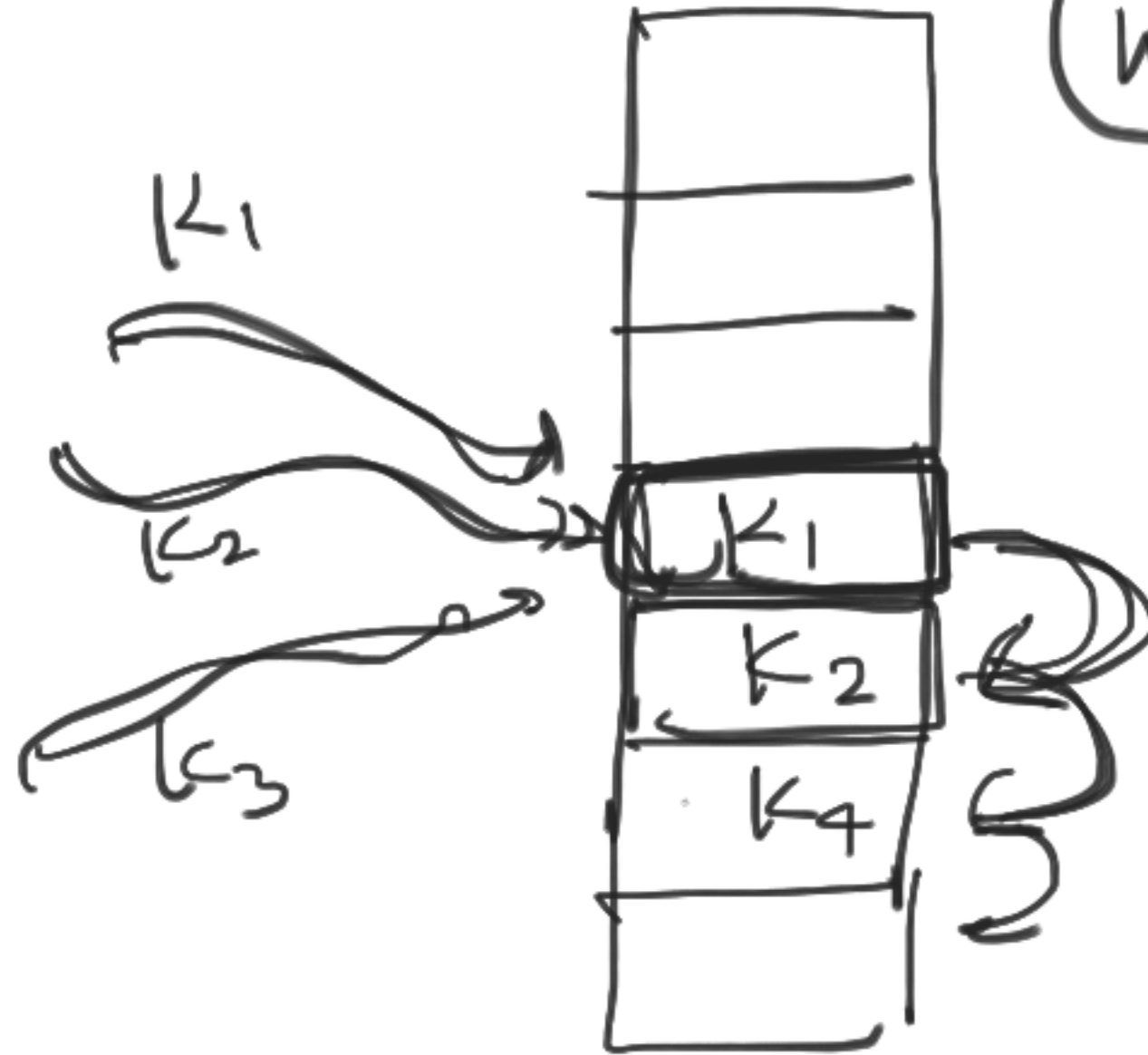




k/m

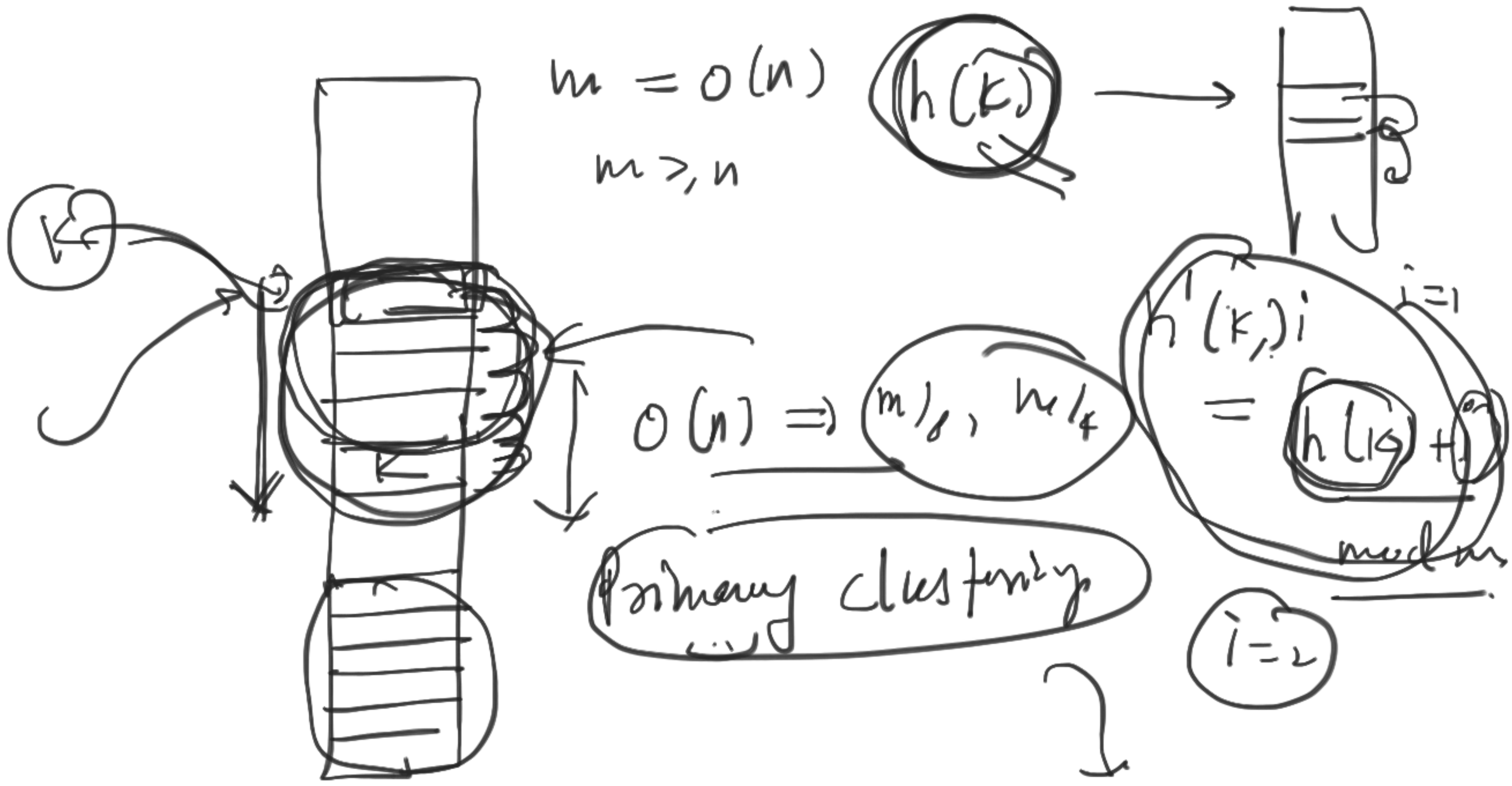
$O(n)$ worst

n keys



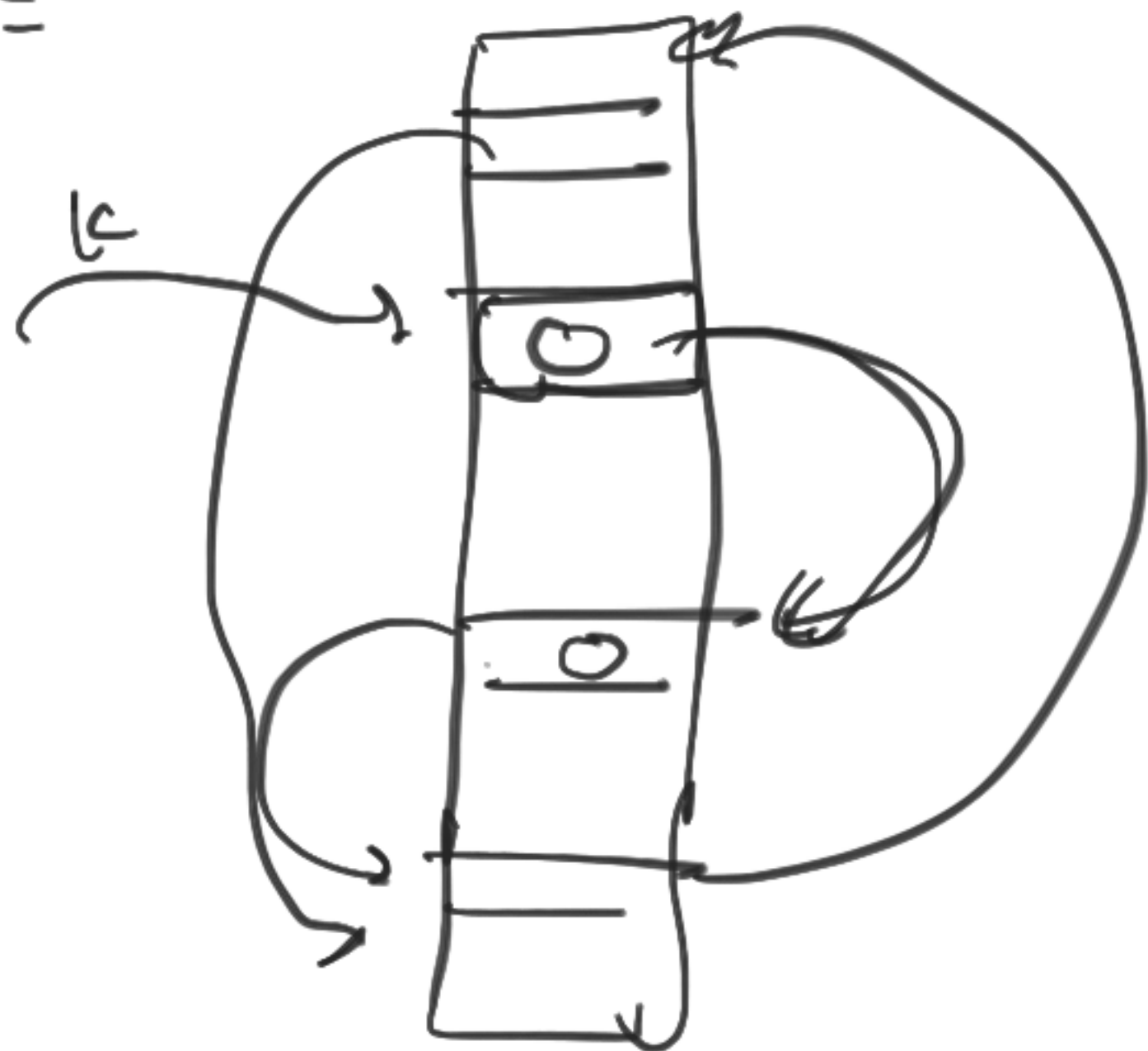
$m' \geq n$

Linear Probing



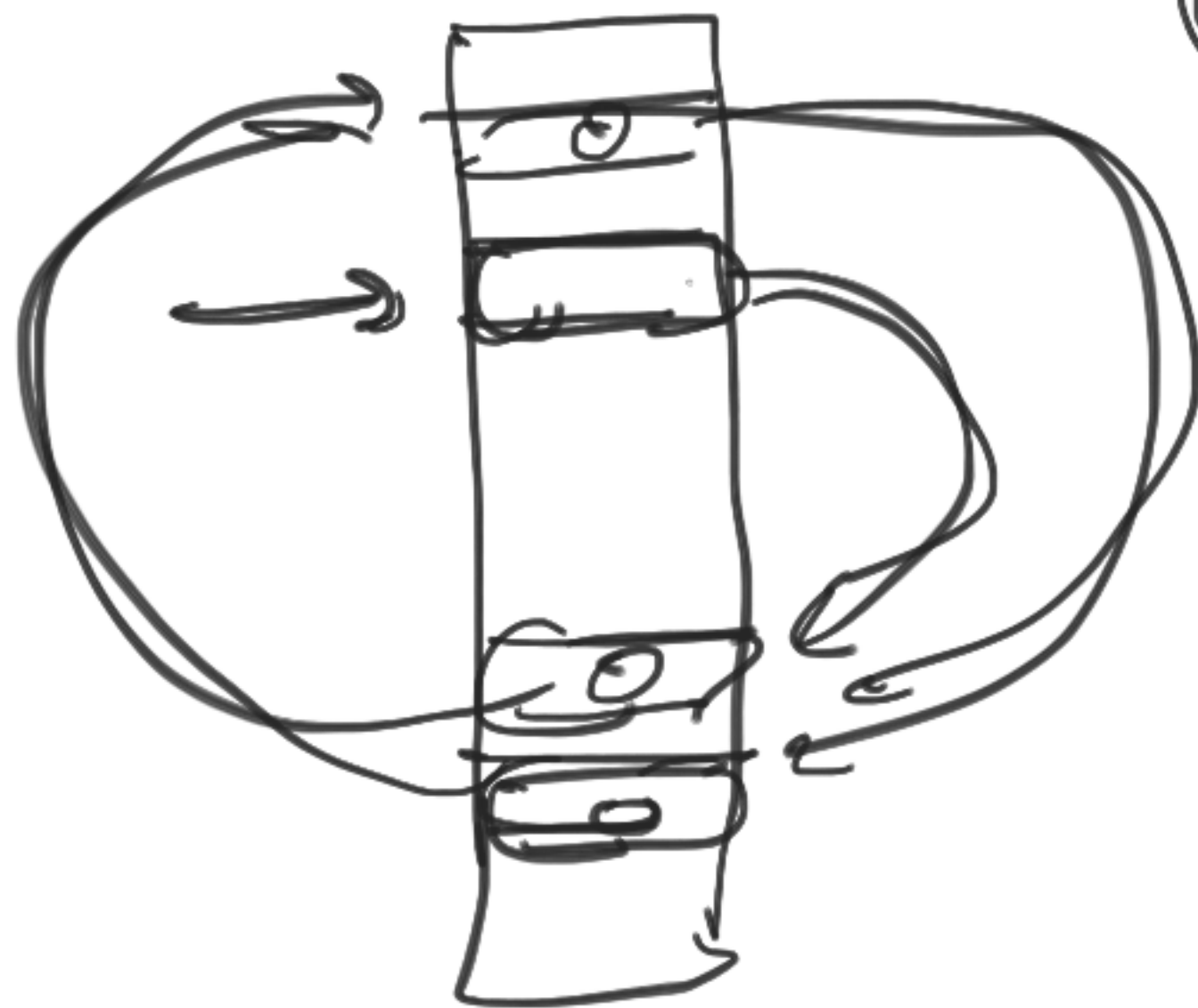
$$h^l(k, i) = (h(k) + i^2) \bmod m$$

$i =$



double hashing

$$h^l(k, i) = (h(k) + h_0(k, i)) \bmod m$$

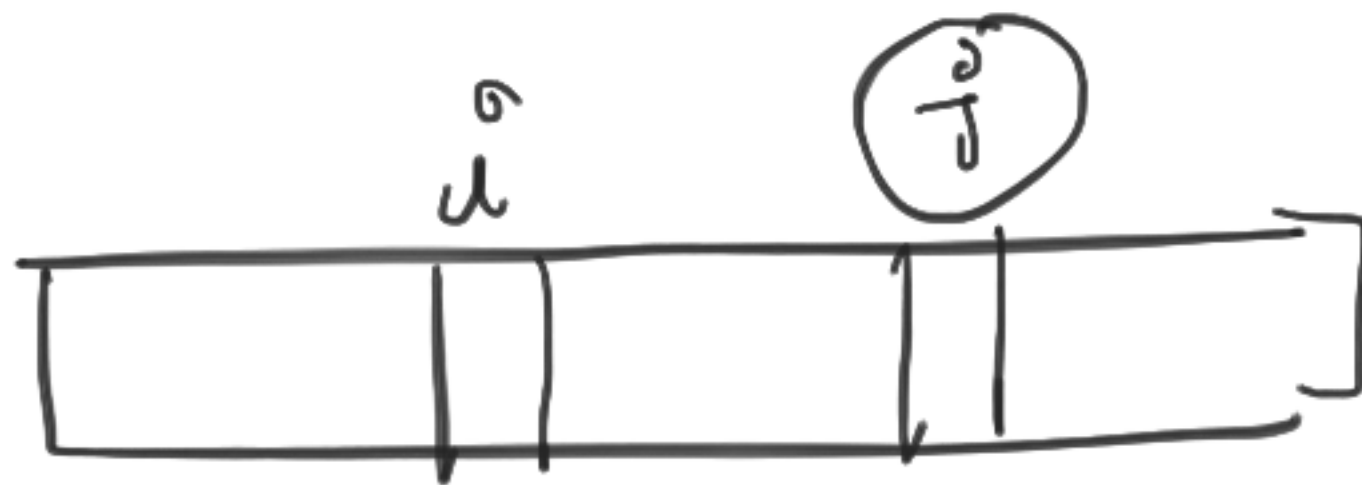


mid
 ← max

$O(1)$ avg

5 4 3 2 1 (1)

max difference array



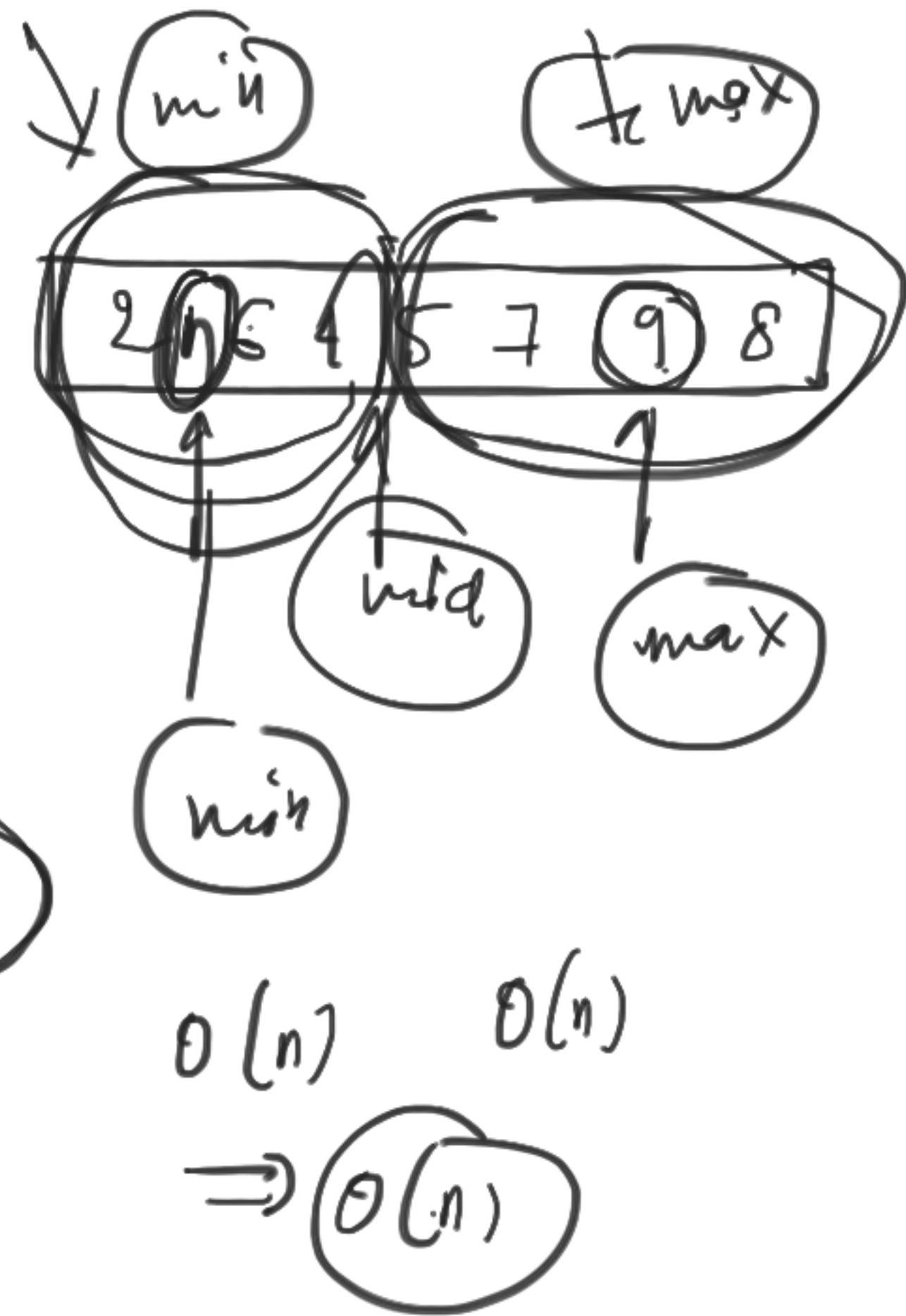
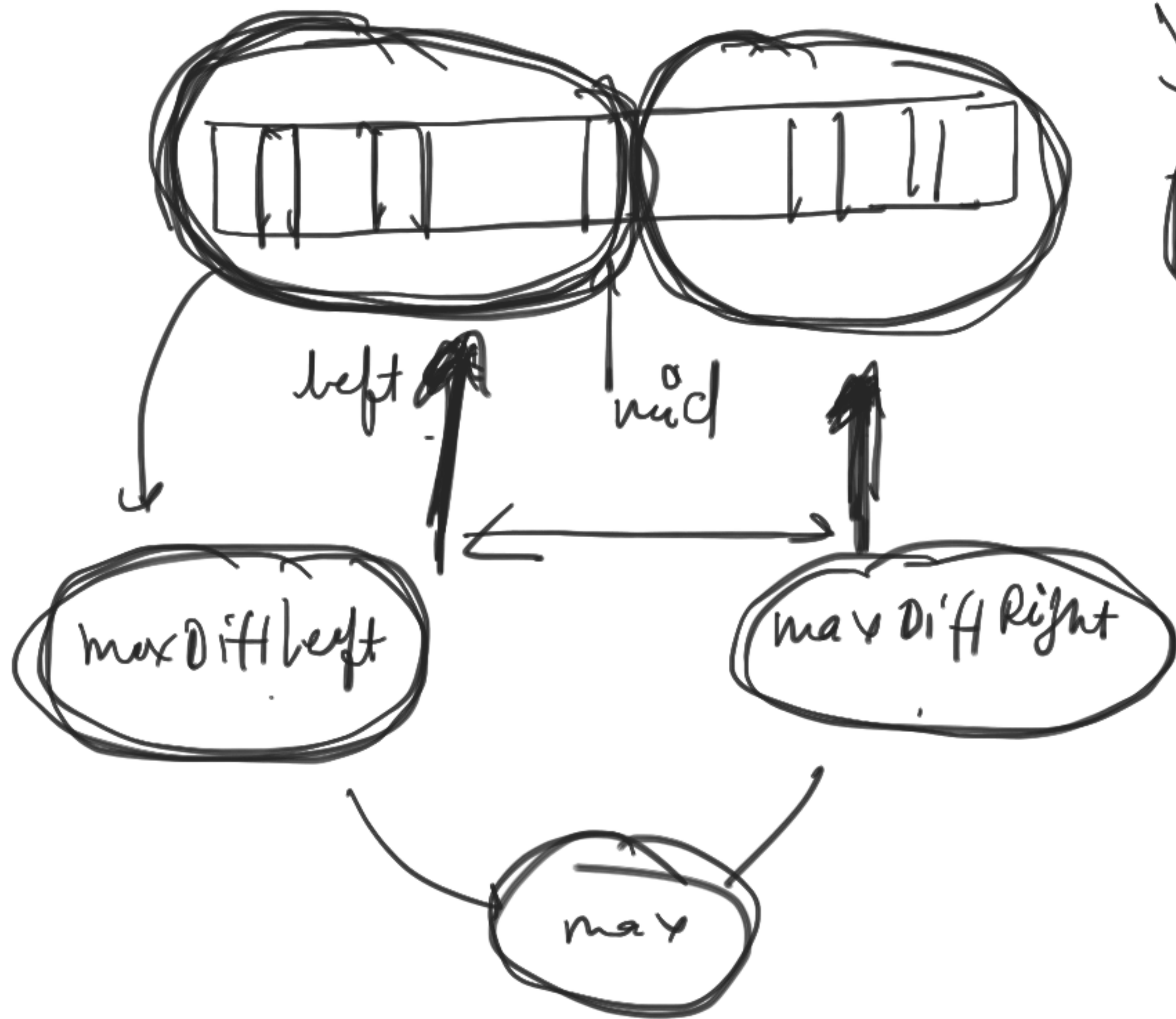
$j > i$

$A[j] - A[i]$

max

recursion

$A[j] > A[i]$

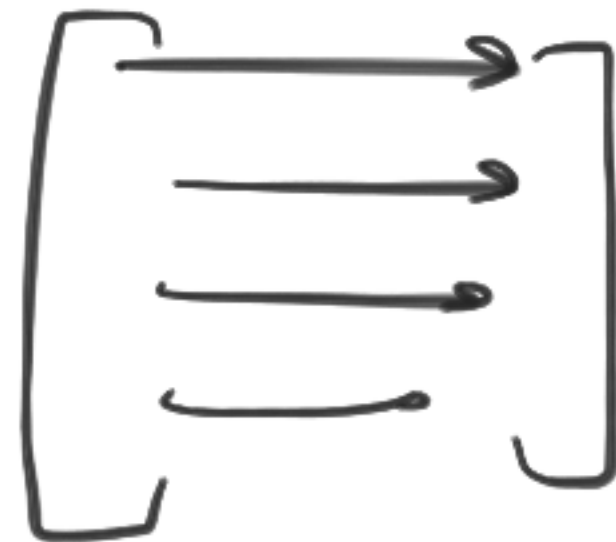


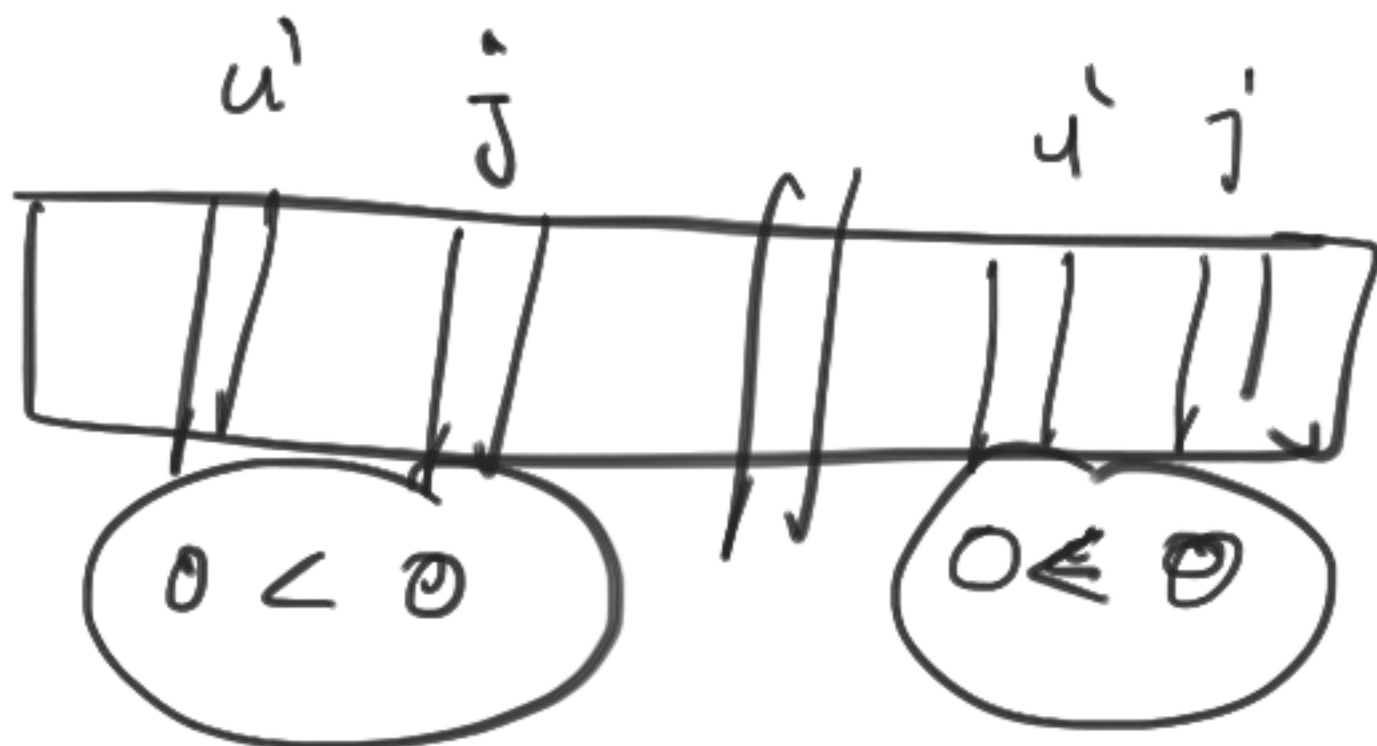
$$n \longrightarrow 2 \left(\frac{n}{2} \right) + o(n) + o(1)$$

$$T(n) = 2T\left(\frac{n}{2}\right) + o(n) \quad \checkmark$$

$$T(n) = \Theta(n \log n)$$

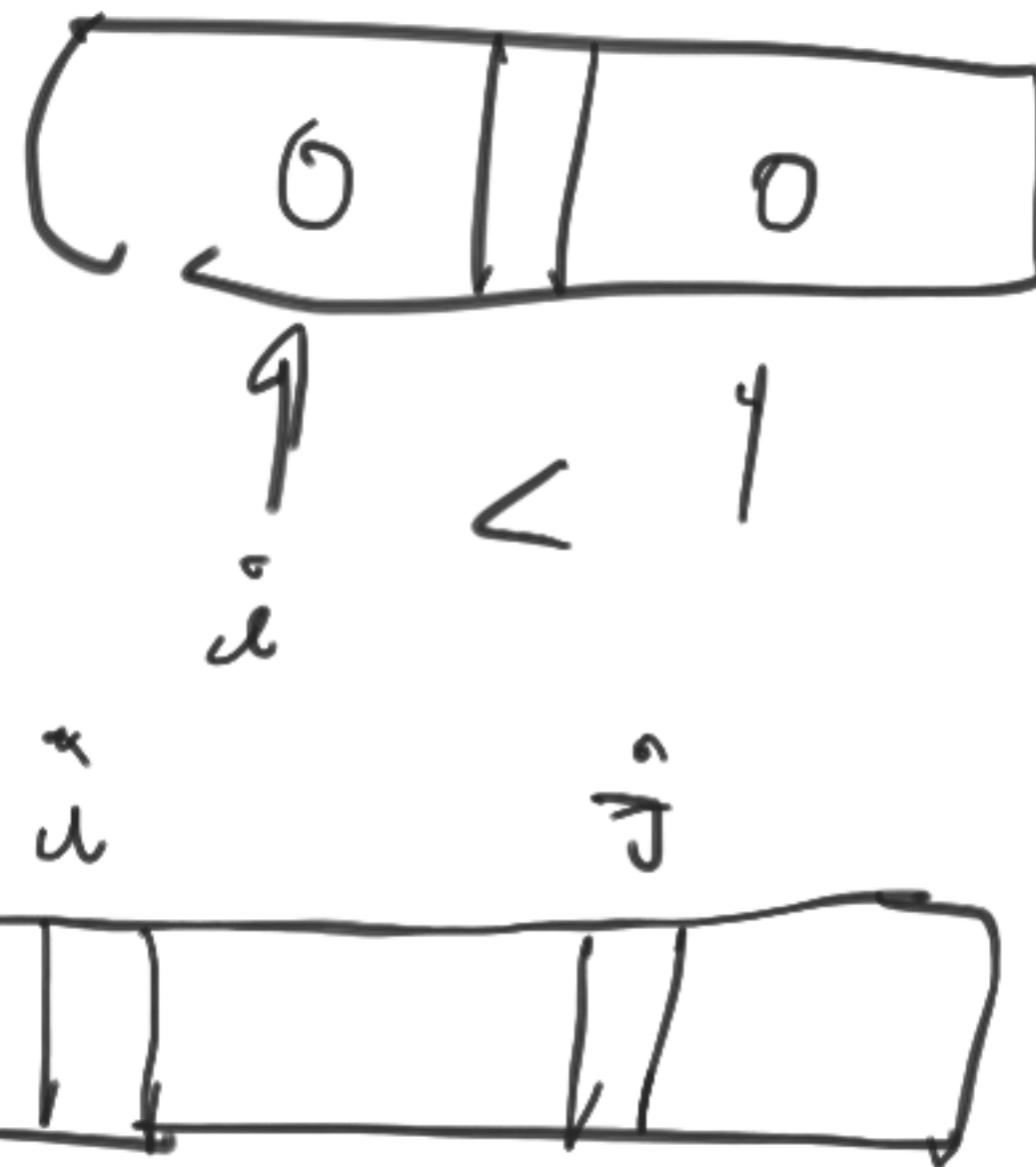
merge sort





$i < j$
 $A[i] < A[j]$

$A[j] - A[i] =$



$$\text{max} \quad A[i] - A[i]$$

$$= (A[i] - A[i-1]) + A[i-1] - A[i-2] + A[i-2] - A[i-3]$$

$$+ \dots + A[i+1] - A[i]$$

$$+ (i-2, i-3) - (i+1, i)$$

max

$A[]$



\Downarrow

$O(n)$

$O(n)$

$n-1$

m

$diff$



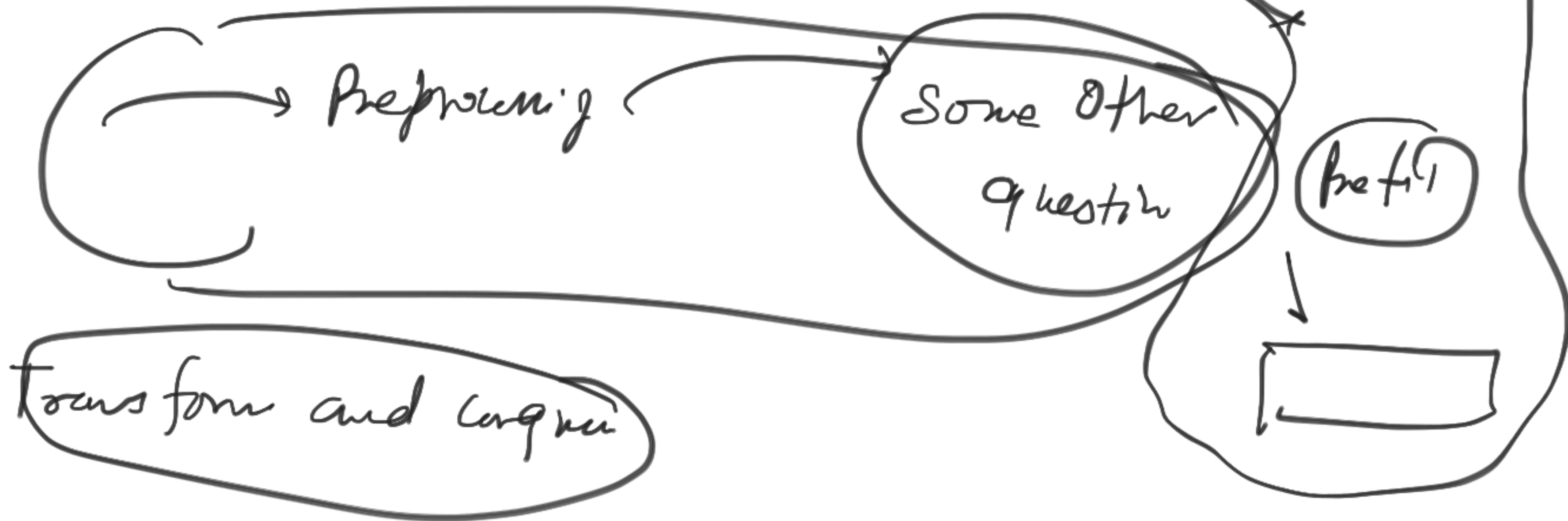
$A[i] - A[i-1]$

max Subarray sum

Kadane algorithm

$\Rightarrow O(n) \quad O(1) \text{ space}$

$O(n) + O(n) \Rightarrow \{O(n) \text{ time}\}$
 $O(n) + O(1) \Rightarrow \{O(n) \text{ space}\}$



Next week

(1) (2) merge

⇒ break

off

Doubts

Pattern sheet

to man

Cover your gaps

4-8

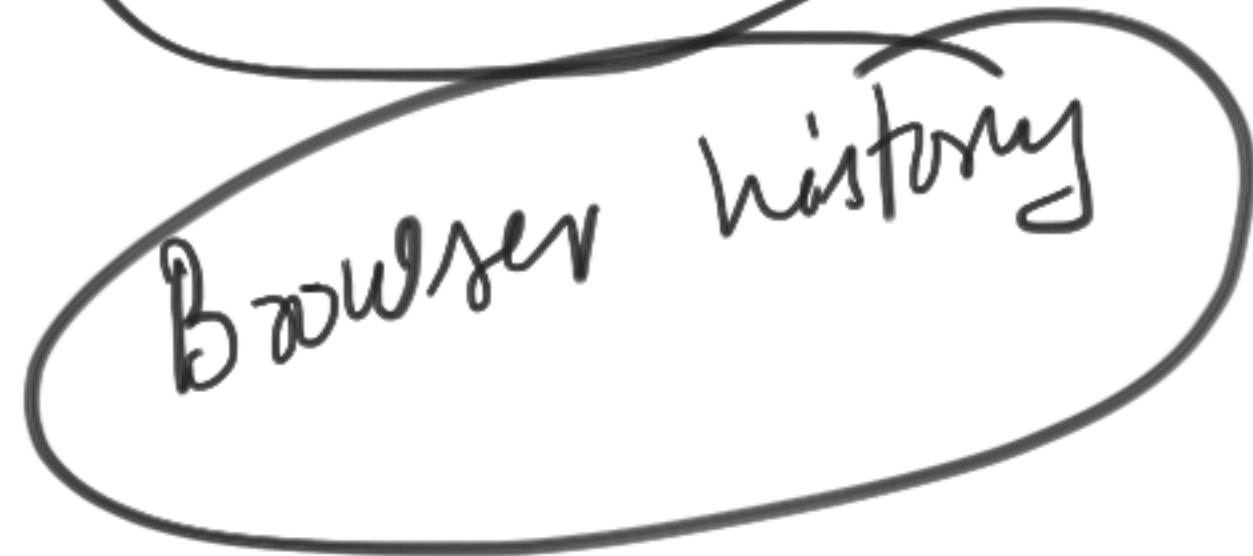
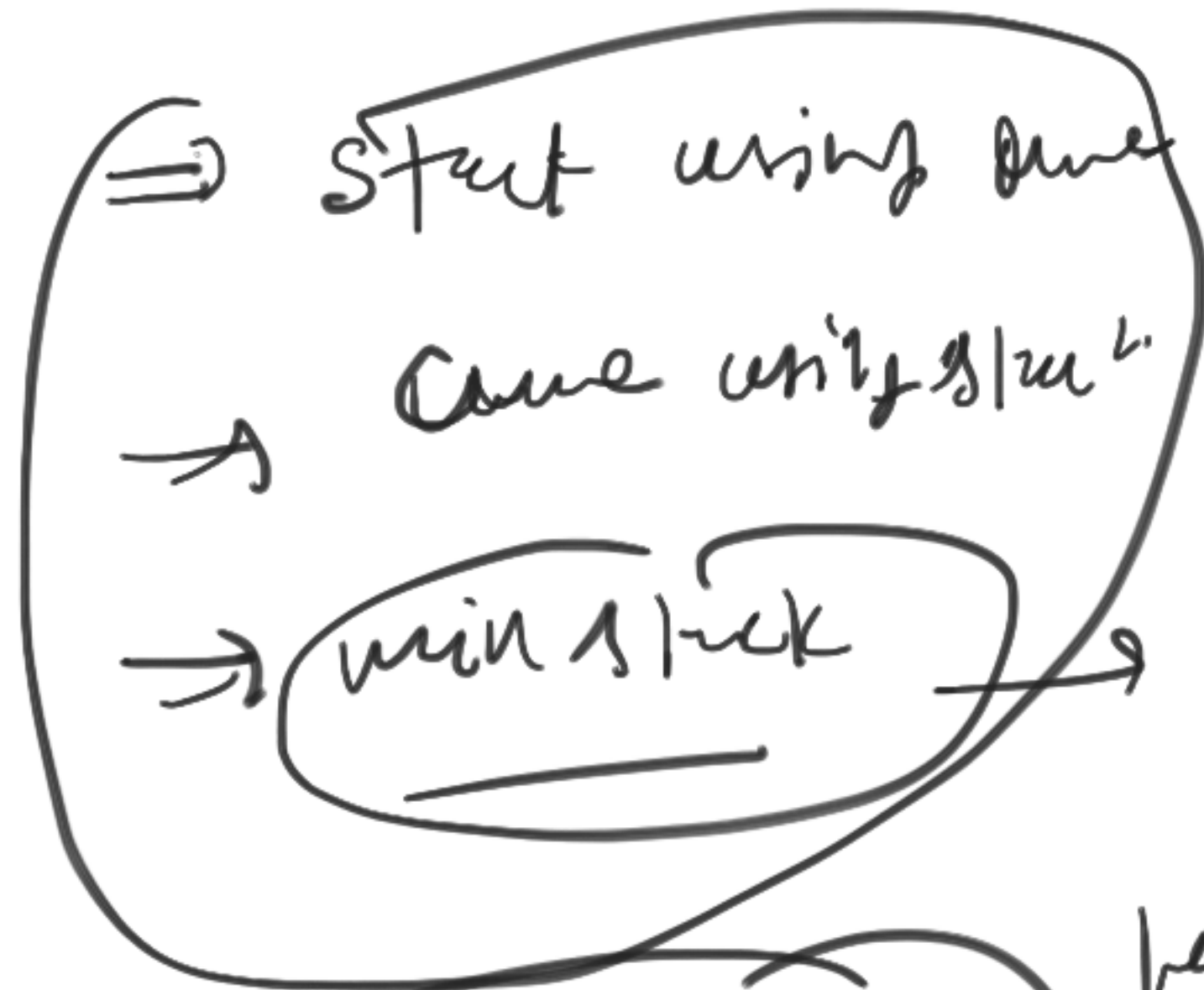
⇒



7



71



back to do

