

## Week 7 answers

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1. Q: Consider the general image inpainting form  $\nabla L \cdot \vec{N} = 0$ , meaning we propagate the information  $L$  in the direction  $\vec{N}$ , as we have discussed in Video 3 this week. Consider  $\vec{N} = (\nabla I)^\perp$ , meaning the perpendicular ( $\perp$ ) to the gradient of the image. What will happen if instead of propagating the Laplacian of  $I$  as in the video, we propagate the image  $I$  itself?

- Any inpainted region will solve the basic equation  $\nabla L \cdot \vec{N} = 0$  for this choice.
- We obtain an inpainted region but the transition between it and its surrounding area is not as smooth.
- The inpainted region will be too smooth.
- The inpainted region will be constant.

A: Since  $L = I$ , we have that  $\nabla L \cdot \vec{N} = 0$  becomes  $\nabla I \cdot \vec{N} = 0$ , and for  $\vec{N} = (\nabla I)^\perp$ , we obtain  $\nabla I \cdot (\nabla I)^\perp = 0$ , which by definition holds for every image. Therefore, any inpainted region holds the equation and we don't obtain the desired result.

2. Q: Consider a region to be inpainted with  $N$  missing pixels, in an image with  $M$  pixels total. In the "smart cut-and-paste" algorithm, how many patch comparisons will need to be performed if a single pixel is inpainted per match? Consider only the order of magnitude, ignoring image boundaries for example.

- $N$ .
- $M/N$ .
- $M$ .
- $N \cdot M$ .

A: For each pixel to be inpainted, we have to compare to all patches centered at each one of the  $M$  image pixels, and therefore we have a total of  $N \cdot M$  searches. Some recent techniques speed-up this by either pre-processing the image or by reducing searchers to pre-specified neighborhoods.

3. Q: For a given image  $I$ ,  $\text{div}(\frac{\nabla I}{|\nabla I|})$  is equal to (div stands for the divergence)

- The Euclidean curvature of the image level lines.
- The tangent to the image level lines.
- The Gaussian curvature of the image when considered as a surface.
- The affine curvature.

A: This is the Euclidean curvature as we discussed in the previous week when describing basic properties of curves represented as level-lines of surfaces (functions). In video 4 this week we further discussed the use of this term as a way to smoothly continue the edges inside the region being inpainted.

4. Q: Consider that you have an image with a single circle, and a small part of it is covered and needs to be inpainted. What would you use for that?

- A Hough transform.

- A combination of smart cut-and-paste and PDEs.
- A variational formulation as then one presented in Video 4.
- A PDE as the one in Video 3.

A: While other techniques might do a decent job, if we know the shape of the occluded object, a circle in this case, the best is to use the Hough transform to detect such object (circle) using the un-occluded regions, and once the estimation has been done, then the shape can be completed.

5. Q: Assume you have a fast moving rigid object in a video, that needs to be removed (inpainted). Which one of the following operations is expected to do a good inpainting job? If you think that more than one option is possible, pick the one that will produce the best result and/or is the simplest one.

- Temporal median filtering: The pixels in the region to be inpainted are replaced by the median of pixels in the same  $(x,y)$  spatial location and at different frames  $t$  (median of  $(x,y,t)$  for  $t$  in some time interval with the current frame at its center).
- Temporal Gaussian/averaging filter: The pixels in the region to be inpainted are replaced by the (weighted) average of pixels in the same  $(x,y)$  spatial location and at different frames  $t$  (median of  $(x,y,t)$  for  $t$  in some time interval with the current frame at its center).
- A cut-and-paste technique.
- A spatial-only inpainting via PDEs.

A: If the object is moving then pixels become un-occluded as the object passes by. If the object is moving fast, only a few frames contain the object for a given pixel location, and therefore a median will work since the majority of the pixels are un-occluded for a given time window (the size of the time window depends on the velocity of the moving object). A Gaussian will mix occluded and un-occluded pixels and then will not perform as well. A cut-and-paste technique might work but is too expensive for this simple scenario.

6. Q: How would you detect scratches in an old movie, knowing they are vertical straight lines?

- With Mumford-Shah segmentation
- With Wiener filtering
- With the Hough transform

A: The Hough transform is ideal for this since we can easily control the orientation.

7. Q: Assume the above scratches are a single pixel wide and appear in relatively uniform areas, how would you inpaint them?

- Simple linear interpolation
- Simple texture synthesis
- PDE-based inpainting

A: For such scenarios linear interpolation is the simplest thing to do and the most efficient.

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