

Problem Statement

Santa has n candies and he wants to gift them to k kids. He wants to divide as many candies as possible between all k kids. Santa can't divide one candy into parts but he is allowed to not use some candies at all.

Santa will be satisfied if the following conditions are met:

1. The difference between the kid who receives the maximum (b) and the minimum (a) number of candies is at most 1, i.e., $b - a \leq 1$.
2. The number of kids who receive $a + 1$ candies does not exceed $\lfloor k/2 \rfloor$ (where $\lfloor k/2 \rfloor$ is k divided by 2 and rounded down).

Your task is to find the maximum number of candies Santa can distribute while satisfying the conditions.

Input

- The first line contains a single integer t ($1 \leq t \leq 50,000$) — the number of test cases.
- Each of the next t lines contains two integers n and k ($1 \leq n, k \leq 10^9$) — the number of candies and the number of kids.

Problem Analysis

Santa needs to distribute n candies to k kids such that:

1. The difference between the maximum (b) and minimum (a) candies given to any kid is at most 1.
2. The number of kids receiving $a + 1$ candies does not exceed $\lfloor k/2 \rfloor$.

Key Observations

- **Base Distribution:** Each kid can receive $a = n // k$ candies as a baseline.
- **Remainder Handling:** After distributing a candies to all kids, there may be a remainder $r = n \% k$ candies left.
- **Constraint Compliance:** Only $x = \lfloor k/2 \rfloor$ kids can receive the extra $a + 1$ candies.

Algorithm

1. **Compute x :**

$$x = \lfloor k / 2 \rfloor$$

This represents the maximum number of kids allowed to receive $a + 1$ candies.

2. **Calculate Base Distribution:**

$$\text{base} = (n // k) \times k$$

This is the total candies distributed if all kids get a candies.

3. **Compute Remainder:**

$$r = n - \text{\texttt{\text{base}}}$$

This represents the leftover candies after the base distribution.

4. Adjust for Constraints:

- If $r \leq x$: Distribute all r candies to r kids as $a + 1$.
- If $r > x$: Distribute x candies to x kids as $a + 1$, leaving $r - x$ candies unused.

By following this approach, we maximize the number of candies distributed while ensuring Santa's conditions are met.

Example Walkthrough

Test Case

Given:

$$n = 11, k = 3$$

Step-by-Step Calculation

1. Compute x :

$$\begin{aligned} &[\\ &x = \lfloor 3 / 2 \rfloor = 1 \\ &] \end{aligned}$$

This means at most 1 kid can receive $a + 1$ candies.

2. Calculate Base Distribution:

$$\begin{aligned} &[\\ &\text{\texttt{\text{base}}} = (11 // 3) \times 3 = 3 \times 3 = 9 \\ &] \end{aligned}$$

Each kid gets at least $a = 3$ candies.

3. Compute Remainder:

$$\begin{aligned} &[\\ &r = 11 - 9 = 2 \\ &] \end{aligned}$$

2 candies are left to be distributed.

4. Adjust for Constraints:

$$\begin{aligned} &[\\ &\text{\texttt{\text{total}}} = 9 + \min(2, 1) = 9 + 1 = 10 \\ &] \end{aligned}$$

Since $r > x$, only $x = 1$ extra candy can be given.

Distribution

- 2 kids receive 3 candies (a).

- 1 kid receives 4 candies ($a + 1$).

Total Distributed:

```
[  
3 + 3 + 4 = 10  
]
```

which satisfies both constraints.

Code

```
import sys  
  
def solve():  
    n, k = map(int, sys.stdin.readline().split())  
    x = k // 2  
    total = (n // k) * k  
    total += min(n - total, x)  
    print(total)  
  
def main():  
    sys.stdin.readline()  
    for _ in range(int(sys.stdin.readline().strip())):  
        solve()  
  
if __name__ == "__main__":  
    main()
```