

# 1692. Count Ways to Distribute Candies Premium

Hard Topics Companies Hint

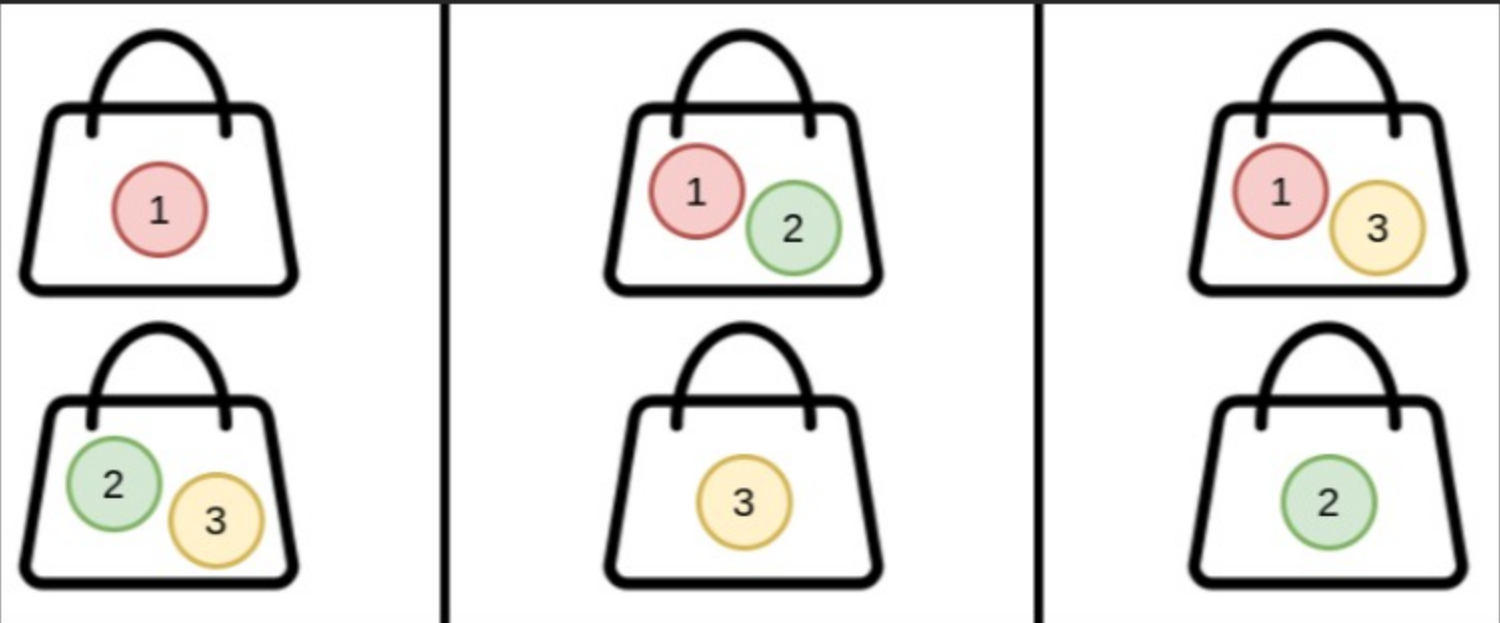
There are  $n$  **unique** candies (labeled  $1$  through  $n$ ) and  $k$  bags. You are asked to distribute **all** the candies into the bags such that every bag has **at least** one candy.

There can be multiple ways to distribute the candies. Two ways are considered **different** if the candies in one bag in the first way are not all in the same bag in the second way. The order of the bags and the order of the candies within each bag do not matter.

For example,  $(1), (2,3)$  and  $(2), (1,3)$  are considered different because candies  $2$  and  $3$  in the bag  $(2,3)$  in the first way are not in the same bag in the second way (they are split between the bags  $(2)$  and  $(1,3)$ ). However,  $(1), (2,3)$  and  $(3,2), (1)$  are considered the same because the candies in each bag are all in the same bags in both ways.

Given two integers,  $n$  and  $k$ , return *the **number** of different ways to distribute the candies*. As the answer may be too large, return it **modulo**  $10^9 + 7$ .

### Example 1:



**Input:**  $n = 3, k = 2$   
**Output:** 3  
**Explanation:** You can distribute 3 candies into 2 bags in 3 ways:  
 $(1), (2,3)$   
 $(1,2), (3)$   
 $(1,3), (2)$

### Example 2:

**Input:**  $n = 4, k = 2$   
**Output:** 7  
**Explanation:** You can distribute 4 candies into 2 bags in 7 ways:  
 $(1), (2,3,4)$   
 $(1,2), (3,4)$   
 $(1,3), (2,4)$   
 $(1,4), (2,3)$   
 $(1,2,3), (4)$   
 $(1,2,4), (3)$   
 $(1,3,4), (2)$

### Example 3:

**Input:**  $n = 20, k = 5$   
**Output:** 206085257  
**Explanation:** You can distribute 20 candies into 5 bags in 1881780996 ways.  $1881780996 \bmod 10^9 + 7 = 206085257$ .

### Constraints:

- $1 \leq k \leq n \leq 1000$

Seen this question in a real interview before? 1/5

Yes No

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Hint 1

Try to define a recursive approach. For the  $i$ th candies, there will be one of the two following cases:

Hint 2

If the  $i - 1$  previous candies are already distributed into  $k$  bags for the  $i$ th candy, you can have  $k * dp[n - 1][k]$  ways to distribute the  $i$ th candy. We need then to solve the state of  $(n - 1, k)$ .

Hint 3

If the  $i - 1$  previous candies are already distributed into  $k - 1$  bags for the  $i$ th candy, you can have  $dp[n - 1][k - 1]$  ways to distribute the  $i$ th candy. We need then to solve the state of  $(n - 1, k - 1)$ .

Hint 4

This approach will be too slow and will traverse some states more than once. We should use memoization to make the algorithm efficient.

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