1168. Optimize Water Distribution in a Village Premium

Hard ♥ Topics ② Companies ۞ Hint

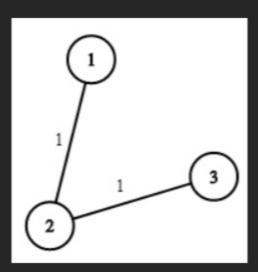
There are n houses in a village. We want to supply water for all the houses by building wells and laying pipes.

For each house i, we can either build a well inside it directly with cost wells [i - 1] (note the -1 due to **0-indexing**), or pipe in water from another well to it. The costs to lay pipes between houses are given by the array pipes where each pipes[j] = [house1j, house2j, costj] represents the cost to connect house1j and house2j together using a pipe. Connections are bidirectional, and there could be multiple valid connections between the same two houses with different costs.

Return the minimum total cost to supply water to all houses.

Input: n = 2, wells = [1,1], pipes = [[1,2,1],[1,2,2]]

Example 1:



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Input: n = 3, wells = [1,2,2], pipes = [[1,2,1],[2,3,1]]
Output: 3
Explanation: The image shows the costs of connecting houses using pipes.
The best strategy is to build a well in the first house with cost 1 and connect the other houses to it with cost 2 so the total cost is 3.
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Example 2:

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Output: 2
Explanation: We can supply water with cost two using one of the three options:
Option 1:

    Build a well inside house 1 with cost 1.

    Build a well inside house 2 with cost 1.

The total cost will be 2.
Option 2:

    Build a well inside house 1 with cost 1.

    Connect house 2 with house 1 with cost 1.

The total cost will be 2.
Option 3:
  - Build a well inside house 2 with cost 1.
  - Connect house 1 with house 2 with cost 1.
The total cost will be 2.
Note that we can connect houses 1 and 2 with cost 1 or with cost 2 but we will always choose the cheapest option.
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Constraints:

- $2 <= n <= 10^4$
- wells.length == n
- 0 <= wells[i] <= 10⁵
- 1 <= pipes.length <= 10⁴

pipes[j].length == 3 • $1 \le house1_j$, $house2_j \le n$ • $0 <= cost_j <= 10^5$ house1_j != house2_j Seen this question in a real interview before? 1/5 Yes No Submissions **78.5K** Acceptance Rate **64.9%** Accepted 51K ♥ Topics Union Find Graph Heap (Priority Queue) Minimum Spanning Tree Companies 0 - 6 months Google 2 O Hint 1 What if we model this problem as a graph problem? A house is a node and a pipe is a weighted edge. O Hint 3

O Hint 5

Discussion (17)

How to represent building wells in the graph model?

The problem is now reduced to a Minimum Spanning Tree problem.

Add a virtual node, connect it to houses with edges weighted by the costs to build wells in these houses.