

## Hashmap

27 August 2023 13:05

Stores key value pair.

frequency	
key	value
1 - 2	
2 - 2	
3 - 1	
5 - 1	

key	value
food item	price
maggi	50
coke	40
pizza	100
(string)	(int)

Time  $O(1)$

$\langle \text{int}, \text{int} \rangle$

## First unique char in a string

27 August 2023 13:11

$str = \underline{\text{leet}}$   $\underline{\text{t}}$   $\underline{\text{C}}$   $\underline{\text{o}}$   $\underline{\text{d}}$   $\underline{\text{e}}$   $\underline{\text{l}}$   $\underline{\text{t}}$

2 for loops

$ans = 4$  'c'

$str = \underline{\text{g}}$   $\underline{\text{a}}$   $\underline{\text{c}}$   $\underline{\text{e}}$   $\underline{\text{c}}$   $\underline{\text{a}}$   $\underline{\text{g}}$  e

$ans = -1$  'x'

~~love leet code~~  $ans = 'v'$  2  
Time:  ~~$O(N^2)$~~ , Space:  $O(1)$   
 $O(N)$

~~love~~  $leet$   $code$

freq.

l - 2

o - 2

v - 1

e - 3

t - 1

c - 1

Time:  $O(N)$

Time  $\tau O(N)$   
Space  $O(N) \cancel{O(1)}$

$c = 1$   
 $d = 1$

$b' \rightarrow z'$

26

## Two sum

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$$\text{arr} = \{ 3, 1, 5, 8, 10, 7 \}$$

index ?  
target = 17

10, 7

index = [4, 5]

① Two loops.  $O(N^2)$

② ~~sorting + 2 pointer~~  $O(N \log N)$

③ Hashmap  $O(N)$

$$\text{arr} = \{ 3, 1, 5, 8, 7, 10 \}$$

target = 17

[i, map[diff]]

diff =  
target - curval

$$17 - 3 = 14$$

$$17 - 1 = 16$$

$$17 - 10 = 7$$

Map	values, arr	index
3	0	0
1	1	1
5	2	2
8	3	3
7	4	4

Time  $\leftarrow O(N)$

Time  $\leftarrow O(L^N)$   
Space  $\leftarrow O(N) \rightarrow \underline{\text{map}}$

## Group anagrams

27 August 2023 13:49

State - taste

cat - act

eat - ate / tea

input = [ "eat", "tea", "tan", "ate", "nat", "bat" ]

ans = [ eat, tea, ate ], [ tan, nat ], [ bat ] M

$$M = \underline{N \times m} \stackrel{\textcircled{1}}{=} O(N^3)$$

Hashmap < String, list<String> >

key will be sorted string .

$$\textcircled{2} \quad O(N \log N)$$

$$O(M \times N \log N)$$

↑  
sorting 1 word

"leetcode" N

$$O(N \log N)$$

$$\begin{aligned} bb &= 196 \\ ac &= 196 \end{aligned}$$

③  
act, ate, tea  
eat

act → [ act ]

length

freq. of each char.

1 0 0 0 0 | 0 0 0 1 0 0 0  
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25

[ #1#0#0#0#0#1#0#0#1# ] -

[eat, tea, tan, ate, net, bat]

hashmap <string, list<string>>

- {  $\#1\#\#0\#0\#1-$  }  $\rightarrow$  { eat, tea, ate } ↗
- {  $\#1\#\#1\#\#0$  }  $\rightarrow$  { tan, rat } ↗
- {  $\#\#0\#\#1\#\#0$  }  $\rightarrow$  { bat } ↗

Time  $\leftarrow O(M \times N)$

"a b a z"

$\mathcal{O}(N)$

$$\begin{array}{r} \cancel{2} \\ \cancel{X} \quad \underline{1 \ 0 \ 0 \ 0 \ 0 \ 0} \quad \text{(zeroes)} \\ \hline 0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 2 \quad \underline{\hspace{2cm}} \end{array}$$

9-0  
6-1  
C-2  
2 } 3

#?#)##0 \_\_\_\_\_ # =

## Subarray sum equals k

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π = 7

$$\begin{bmatrix} 3 & 4 & 7 & 2 & -3 & 1 & 4 & 2 & 1 \end{bmatrix}$$

$$\text{ans} = \underline{\underline{6}}$$

[3,4]

[7]

[4,2,1]

[1,4,2]

$$[7, 2, -3, 1]$$

$$[2, -3, 1, 4, 2, 1]$$

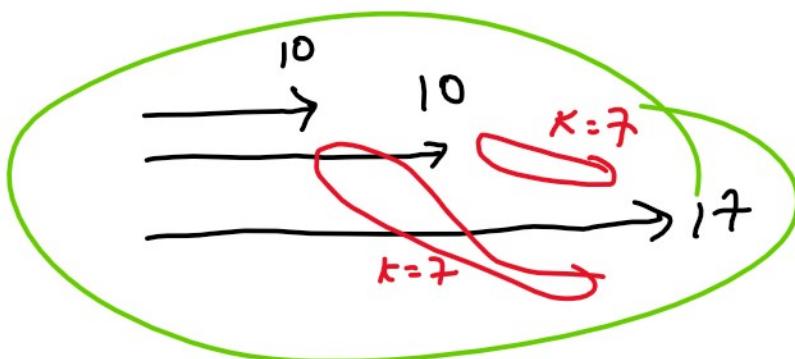
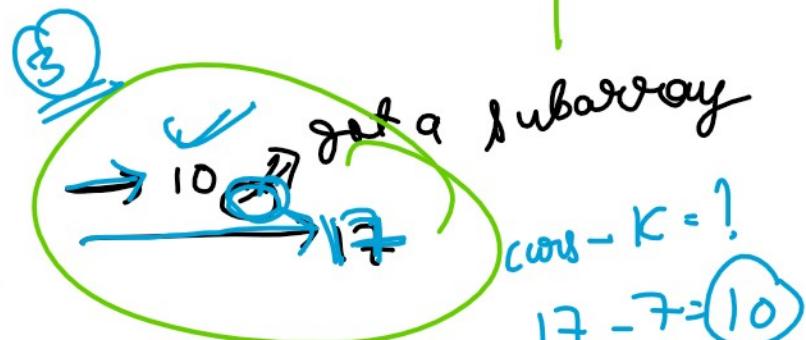
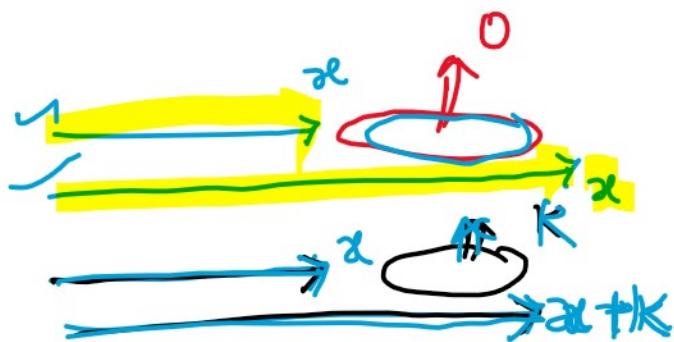
$O(N)$ )

~~- 5(N<sup>4</sup>)~~

generating all  
subarrays.

map

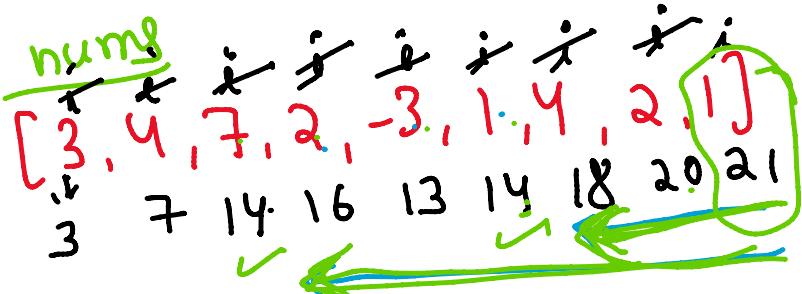
Count



2 subarrays.

$$S_1 S_0 + 0 - S + 1 + 7$$

*subangif*



$$\text{prefixSum} - k$$

$$3 - 7 = -4$$

$$7 - 7 = 0$$

$$14 - 7 = 7$$

$$16 - 7 = 9$$

$$\text{count} = 0$$

$$13 - 7 = 6$$

$$14 - 7 = 7$$

$$18 - 7 = 11$$

$$20 - 7 = 13$$

$k = 7$

HashMap

prefixSum - count

prefixSum = k

0 - 1	3 - 1
7 - 1	14 - 12
16 - 1	13 - 1
18 - 1	20 - 1

$[3, 4], [7], [7, 2, -3, 1], [1, 4, 2]$   
 $[4, 2, 1], [2, -3, 1, 4, 2, 1]$

Time  $\in O(N)$   
 Space  $\in O(N)$



Algorithms

Time

Space

$$f(n) = 7n^2 + 5n \\ = O(N^2)$$

$$f(n) = \frac{n}{5} + \log N \\ = O(N)$$

$$f(n) = 5n^4 + 2n^3 + n^2 \\ = O(N^4)$$

$$f(n) = 2n + 100 \log N \\ = O(N)$$

→ Bubble sort

$O(N^2)$

→ Binary search

$O(\log N)$

→ Revision

$O(N \log N)$

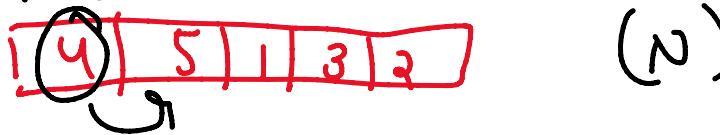
→ Merge sort

## Bubble sort

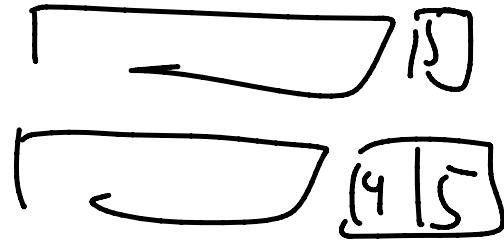
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Time  $\in O(N^2)$   
Space  $\in O(1)$

pairwise comparison  
and move the largest element to the end



$N-1$   
 $N-2$   
 $N-3$   
|  
 $\vdots$   
 $j$ .  
 $k$ .



$$\begin{aligned}
 &= ((1+2+3+\dots+(N-2)+(N-1))k \\
 &= \left( \frac{N(N-1)}{2} \right) k \\
 &= \frac{N^2 k}{2} - \frac{N}{2} k \\
 &\in O(N^2)
 \end{aligned}$$

Recurrence relation

$$\begin{aligned}
 T(n) &= k \cdot (n-1) + T(n-1) \\
 \cancel{T(n-1)} &= k \cdot (n-2) + \cancel{T(n-2)} \\
 \cancel{\cancel{T(n-2)}} &= k \cdot (n-3) + \cancel{\cancel{T(n-3)}} \\
 &\vdots
 \end{aligned}$$

$$\begin{aligned} \cancel{T(1)} &= k_1 + 0 \\ T(n) &= k((n-1) + (n-2) + \dots + 2 + 1) \\ &= \frac{n(n-1)}{2} \times k \\ &= \frac{n^2 k}{2} - \frac{n}{2} k \\ &= O(N^2) \end{aligned}$$

## Binary Search

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Time  $\leftarrow O(\log N)$

Space  $\leftarrow O(1)$



$(n)$

$$\frac{N}{2^0}$$

$(n/2)$

$$\frac{N}{2^1}$$

$(n/4)$

$$\frac{N}{2^2}$$

$(n/8)$

$$\frac{N}{2^3}$$

$$l = \frac{N}{2^K}$$

$$2^K = N$$

$\frac{n}{2^0}$

$$\frac{N}{2^0}$$

$\frac{n}{2^1}$

$$\frac{N}{2^1}$$

$\frac{n}{2^2}$

$$\frac{N}{2^2}$$

$\frac{n}{2^3}$

$$\frac{N}{2^3}$$

$$\log_2 2^K = \log_2 N$$

$$K = \log N$$

Time  $\leftarrow O(\log N)$

Recurser

$$T(n) = K + T(n/2)$$

$$T(n/2) = K + T(n/4)$$

$$T(n/4) = K + T(n/8)$$

$$\cancel{T(n/4)} = k + \cancel{T(1)/8}$$

" "

⋮

$$\cancel{T(1)} = k + 0$$

$$T(n) = \sum_{j=0}^{\log n} k \Rightarrow k \log N$$

$$T(n) = \log N$$

~~$O(\log N)$~~

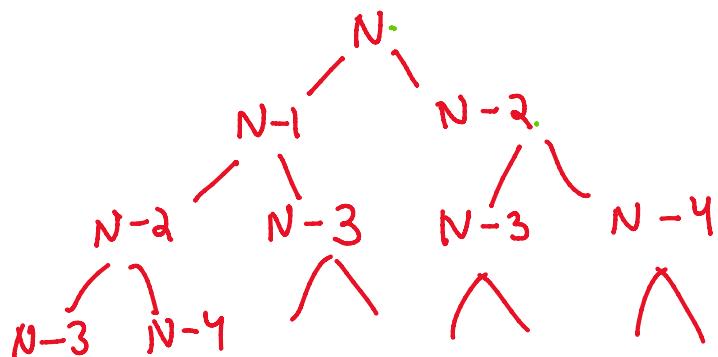
## Fibonacci series

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$$\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$$

0 1 1 2 3 5 8 13 ...

1  $2^0$   
2  $2^1$   
 $4$   $2^2$   
 $8$   $2^3$   
 $16$   $2^4$   
 $\vdots$   $2^{N-1}$



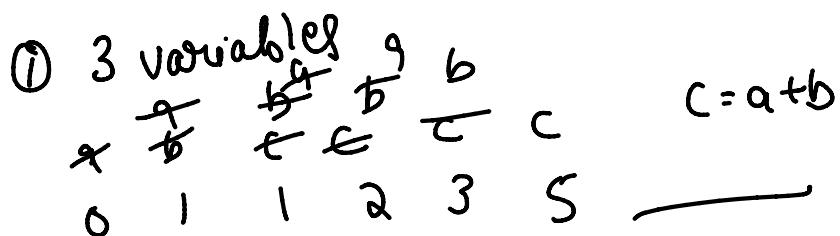
$$= K (1+2+4+8+\dots+2^{N-1})$$

$$= K \frac{2^N - 1}{2 - 1}$$

$$= K(2^N)$$

=  $O(2^N)$  DP / 3 variables.

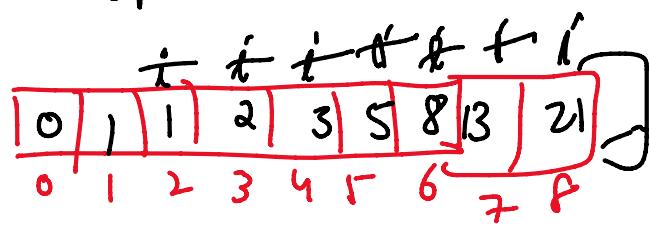
$O(N) \rightarrow \text{space}$



Time  $\rightarrow O(N)$

Space  $\rightarrow O(1)$

$$\text{dp}[i] = \text{dp}[i-1] + \text{dp}[i-2]$$



Time  $\rightarrow O(N)$   
Space  $\rightarrow O(N)$

③ using recursion.

$$\text{Time} \in O(2^N)$$

$$\text{Space} \in O(N)$$

Recurrence

$$T(N) = T(N-1) + T(N-2) + K$$

$$T(N) = 2T(N-1) + K$$

$$2T(N-1) = 4T(N-2) + 2K$$

$$4T(N-2) = 8T(N-3) + 4K$$

⋮

$$T(1) = \dots + 2^{N-1}K$$

$$T(N) = K + 2K + 4K + 8K + \dots + 2^{N-1}K$$

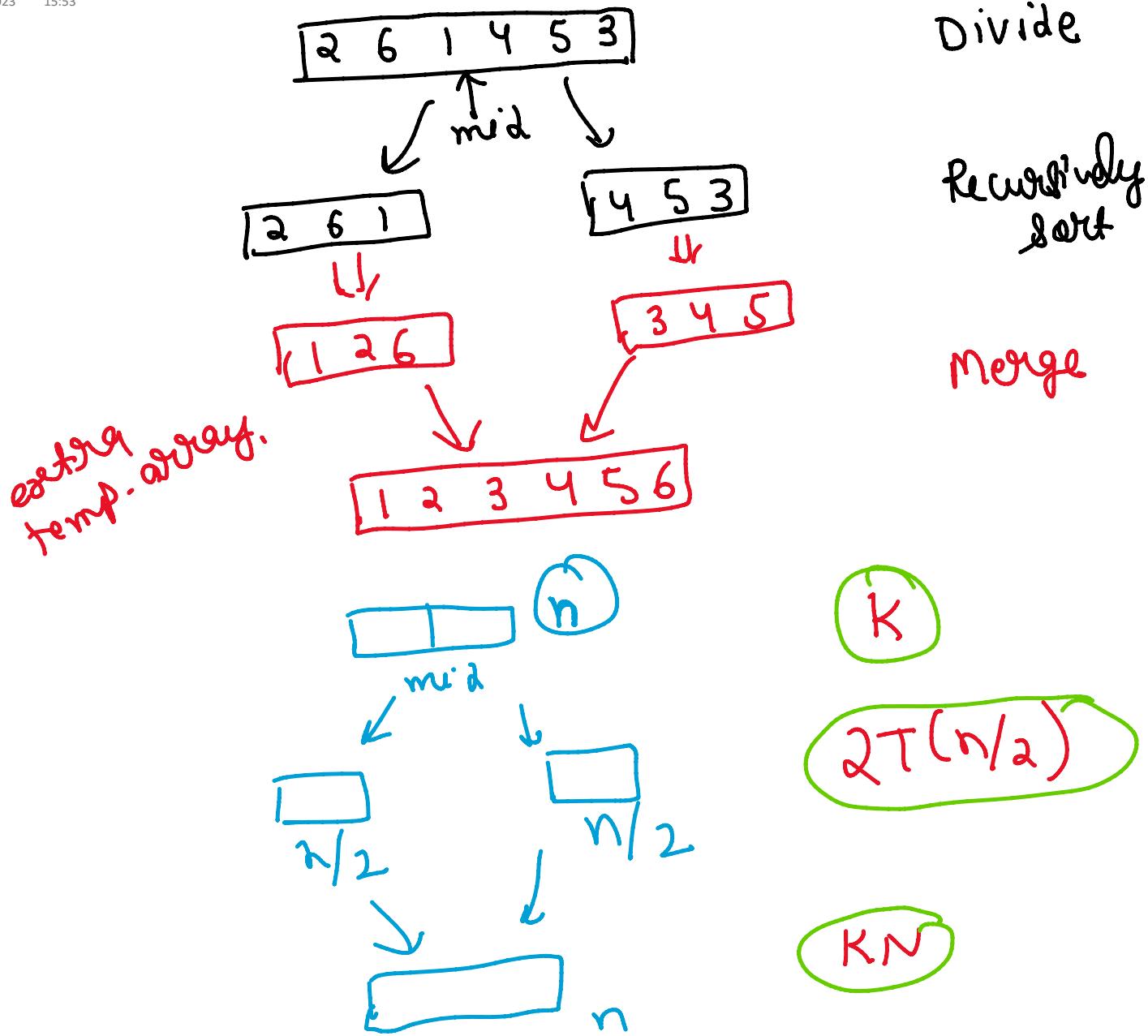
$$= K(1+2+4+8+\dots+2^{N-1})$$

$$= K \frac{(2^N - 1)}{2 - 1}$$

$$= O(2^N)$$

## Merge sort

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$$T(n) = K + 2T(n/2) + KN$$

$$T(n) = K'N + \cancel{2T(n/2)} \rightarrow n^2$$

$$\cancel{2T(n/2)} = \cancel{2K'} \frac{N}{2} + \cancel{4T(n/4)} \rightarrow n^3$$

$$\cancel{4T(n/4)} = \cancel{4K'} \frac{N}{4} + \cancel{8T(n/8)} \rightarrow n^4$$

$$\begin{aligned}
 & 4T(n/4) = 4k' \frac{N}{4} + 8T(n/8) \\
 & \vdots \quad | \quad | \\
 & T(i) = k' n + O(1) \\
 & T(n) = \sum_{i=0}^{\log n} k' n \\
 & = k' n \log n \\
 & = O(N \log N)
 \end{aligned}$$

$O(N)$

