ASSIGNMENT-2 Stack

<u>AIM</u>: Implement stack as an abstract data type using singly linked list and use this ADT for conversion of infix expression to postfix, prefix and evaluation of postfix and prefix expression.

OBJECTIVE:

- 1) To understand the concept of abstract data type.
- 2) How different data structures such as arrays and a stacks are represented as an ADT.

THEORY:

1) What is an abstract data type?

An Abstract Data type is defined as a mathematical model of the data objects that make up a data type as well as the functions that operate on these objects. There are no standard conventions for defining them. A broad division may be drawn between "imperative" and "functional" definition styles. In general terms, an abstract data type is a *specification* of the values and the operations that has two properties:

- It specifies everything you need to know in order to use the data type
- It makes absolutely no reference to the manner in which the data type will be implemented.

When we use abstract data types, our programs divide into two pieces:

- The Application: The part that uses the abstract data type.
- The Implementation: The part that implements the abstract data type.

2) What is stack? Explain stack operations with neat diagrams.

In computer science, a **stack** is a last in, first out (LIFO) abstract data type and data structure. A stack can have any abstract data type as an element, but is characterized by only two fundamental operations: push and pop. The push operation adds an item to the top of the stack, hiding any items already on the stack, or initializing the stack if it is empty. A pop either reveals previously concealed items, or results in an empty stack. A stack is a restricted data structure, because only a small number of operations are performed on it. The nature of the pop and push operations also mean that stack elements have a natural order. Elements are removed from the stack in the reverse order to the order of their addition: therefore, the lower elements are those that have been on the stack the longest. A collection of items in which only the most recently added item may be removed. The

latest added item is at the top. Basic operations are push and pop. Often top and isEmpty are available, too. Also known as "last-in, first-out" or LIFO.

Operations

An abstract data type (ADT) consists of a data structure and a set of **primitive**

• **Push** adds a new element \square **Pop** removes a element

Additional primitives can be defined:

- **IsEmpty** reports whether the stack is empty
- **IsFull** reports whether the stack is full
- **Initialise** creates/initialises the stack
- **Destroy** deletes the contents of the stack (may be implemented by re-initialising
- the stack)

3) Explain how stack can be implemented as an ADT.

User can Add, Delete, Search, and Replace the elements from the stack. It also checks for Overflow/Underflow and returns user friendly errors. You can use this stack implementation to perform many useful functions. In graphical mode, this C program displays a startup message and a nice graphic to welcome the user. The program performs the following functions and operations:

- **Push**: Pushes an element to the stack. It takes an integer element as argument. If the stack is full then error is returned.
- **Pop**: Pop an element from the stack. If the stack is empty then error is returned. The element is deleted from the top of the stack.
- **DisplayTop**: Returns the top element on the stack without deleting. If the stack is empty then error is returned.
- 4) With an example explain how an infix expression can be converted to prefix and postfix form with the stack. (Ans to be written by students)

ALGORITHM:

Abstract Data Type Stack:

Define Structure for stack(Data, Next Pointer) Stack

Empty:

Return True if Stack Empty else
False. Top is a pointer of type
structure stack.

Empty(Top)

Step 1: If Top

= = NULL

```
Step 2: Return
       1;
       Step 3: Return 0;
Push Opertion:
       Top & Node pointer of structure
       Stack. Push(element)
       Step 1: Node>data=element;
       Step
       2; Node->Next =
       Top; Step 3: Top = Node
       Step 3: Stop.
Pop Operation:
       Top & Temp pointer of structure
       Stack. Pop()
       Step 1:If Top
            !=
            NULL
            Then
             i) Temp = Top;
             ii) element=Te
             mp->data; iiI)
             Top
       (Top)>Next;
       delete temp; Step 2:
       Else Stack is Empty.
       Step 3:
       return element:
Infix to Prefix Conversion:
       String is an array of type character which store infix
       expression. This function return Prefix expression.
       InfixToPrefix(S tring) Step 1: I
       = strlen(String);
       Step 2:
       Decrement I;
       Step 3: Do Steps 4 to 9 while I \ge 0
       Step 4: If isalnum(String[I] Then PreExpression[J++] =
       String[I]; Step 5: Else If String[I]=='('
                   Then a) Temp=Pop(&Top);//Pop Operator from stack
                       b) Do Steps while Temp->Operator!=')' and Temp!=NULL
            i) PreExpression[J++] = Temp->Operator;
            ii) Temp = Pop(\&Top);
```

```
Step 6: Else If String[I]==')' Then Push(&Top,Node);//push )' in a stack
       Step 7: Else
                a) Temp = Pop(\&Top);//Pop operator from stack
                b) DO Steps while Temp->Operator != ')' And Temp
                        != NULL And
                       Priority(String[I])<Priority(Temp->Operator)
                                PreExpression[J++] = Temp-
                        >Operator; ii) Temp = Pop(&Top);}
                c) If Temp!=NULL And Temp->Operator==')' Or
                   Priority(String[I])>=Priority(Temp-
              >Operator)) Then Push(&Top,Temp);
       Step 8: Push(&Top,Node);//Push String[I] in a
       stack; Step 9: Decrement I;
       Step 10: Temp = Pop(\&Top);//pop remaining operators from stack
       Step 11: Do Steps while Temp != NULL //Stack is not
       Empty
                   i) PreExpression[J++] = Temp-
                   >Operator; ii)Temp =
                   Pop(&Top);}
       Step 12: PreExpression[J] = NULL;
       Step 13: Reverse PreExpression;
       Step 14:
       Return PreExpression.
Infix to Postfix Conversion:
       String is an array of type character which store infix
       expression. This function return Postfix expression.
       InfixToPost fix(String)
       Step 1: I =
       0;
       Step 2: Do Steps 3 to 8 while String[I] != NULL
       Step 3: If isalnum(String[I] Then PostExpression[J++] =
       String[I]; Step 4: Else If String[I]==')'
                   Then a) Temp=Pop(&Top);//Pop Operator from stack
                      b) Do Steps while Temp->Operator!='(' and Temp!=NULL
                           i) PostExpression[J++] = Temp->Operator;
                        ii) Temp = Pop(\&Top);
       Step 5: Else If String[I]=='(' Then Push(&Top,Node);//push )' in a stack
       Step 6: Else
```

- a) Temp = Pop(&Top);//Pop operator from stack
- b) DO Steps while Temp->Operator != '(' And Temp

!= NULL And Priority(String[I]) >=

Priority(Temp->Operator) iii)

PreExpression[J++] = Temp->Operator; iv)

 $Temp = Pop(\&Top); \}$

c) If Temp!=NULL And Temp->Operator=='('

Or Priority(String[I]) < Priority(Temp-

>Operator)) Then Push(&Top,Temp); Step

7: Push(&Top,Node);//Push String[I] in

a stack; Step 8: Increment I;

Step 9: Temp = Pop(&Top);//pop remaining operators from stack

Step 10: Do Steps while Temp != NULL //Stack is not

Empty

iii)

PostExpres8

8(&Top);} Step 11:

PostExpression[J] = NULL; Step 12:

Return PostExpression.

PostFix Expression Evaluation:

String is an array of type character which store infix

expression. Postfix_Evaluation(String) Step 1: Do

Steps 2 & 3 while String[I]

!= NULL Step 2: If String[I] is operand

Then Push it into Stack Step 3: If it is

an operator Then

Pop two operands from Stack;

Stack Top is 1st Operand & Top-1 is 2nd Operand;

Perform Operation; Step

4: Return Result.

INPUT:

Test Case

O/P

If Stack Empty
Empty | Stack Empty

Display message —Stack Display message —Stack

Full

INPUT:

(A+B) * (C-D) A\$B*C-D+E/F/(G+H) ((A+B)*C-(D-E))\$(F+G) A-B/(C*D\$E) A^B^C

INPUT:

(A+B) * (C-D) A\$B*C-D+E/F/(G+H) ((A+B)*C-(D-E))\$(F+G) A-B/(C*D\$E) A^B^C

POSTFIX OUTPUT:

AB+CD-*
AB\$C*D-EF/GH+/+
AB+C*DE—FG+\$
ABCDE\$*/ABC^^

PREFIX OUTPUT:

+AB-CD +-\$ABCD//EF+GH \$-*+ABC-DE+FG -A/B*C\$DE ^A^BC

NOTE: Here \$ AND ^ are used as raised to operator

Program-

```
#include<iostream>
using namespace std;
typedef struct node
char data;
struct node *next;
                              //n array of structure node
}n;
class stack
n *top;
public:
stack()
                              //constructor of class stack
top=NULL;
int isempty()
                          //check whether stack is empty or not.
if(top==NULL)
return 1;
else
return 0;
void push(char x)
n *p;
p=new node();
p->data=x;
p->next=top;
top=p;
char pop()
```

```
node *p;
char x;
p=top;
x=p->data;
top=top->next;
delete(p);
return x;
char topdata()
return top->data;
};
void infix postfix(char infix[20],char postfix[20]);
int evaluate(int op1,int op2,char op);
void evaluate postfix(char postfix[20]);
int precedence(char x);
void reverse(char a[20],char b[20]);
void infix_prefix(char infix[20],char prefix[20]);
void evaluate prefix(char prefix[20]);
void infix prefix 1(char infix[20],char prefix[20]);
int main()
char infix[20],token,postfix[20],prefix[20];
int ch,result;
do
cout<<"\n1. Infix to Postfix Expression";</pre>
cout<<"\n2. Evaluate Postfix";</pre>
cout<<"\n3. Infix to Prefix Expression";</pre>
cout<<"\n4. Evalute Prefix";</pre>
cout<<"\n5. Exit";</pre>
cout<<"\nEnter your choice: ";</pre>
cin>>ch;
switch(ch)
```

```
case 1:
cout<<"\nEnter Infix expression: ";</pre>
cin>>infix;
infix_postfix(infix,postfix);
cout<<"\n-----";
cout<<"\nPOSTFIX EXPRESSION- "<<postfix<<endl;</pre>
cout<<"----"<<endl;
break;
case 2:
evaluate_postfix(postfix);
break;
case 3:
cout<<"\nEnter Infix expression: ";</pre>
cin>>infix;
infix_prefix(infix,prefix);
cout<<"\n-----
cout<<"\nPREFIX EXPRESSION- "<<pre>refix<<endl;</pre>
cout<<"----"<<endl;
break;
case 4:
evaluate_prefix(prefix);
break;
case 5:
cout<<"\nProgram Exited! ";</pre>
break;
default:
cout<<"WRONG CHOICE! Enter again...";</pre>
}while(ch!=5);
```

```
//infix---> postfix
void infix_postfix(char infix[20],char postfix[20])
stack s;
int i,j=0;
char token,x;
for(i=0;infix[i]!='\0';i++)
token=infix[i];
if(isalnum(token))
                                                       //will check
whether the token is number or an alphabet
postfix[j]=token;
j++;
else
if(token=='(')
                                                      //check whether
token is opening bracket, then push the token.
s.push(token);
else if(token==')')
                                                     //check whether
token is closing bracket.
while((x=s.pop())!='(')
                                                    //pop all
elements until we get opening bracket.
postfix[j]=x;
j++;
else
while(s.isempty()==0 && precedence(token)<=precedence(s.topdata())</pre>
             //first check stack is not empty and then the
precedence.
```

```
postfix[j]=s.pop();
j++;
s.push(token);
while(s.isempty()==0)
postfix[j]=s.pop();
j++;
postfix[j]='\0';
//evaluation of postfix.
void evaluate_postfix(char postfix[20])
stack s;
int i,op1,op2,result;
char token;
int x;
for(i=0;postfix[i]!='\0';i++)
token=postfix[i];
if(isalnum(token))
cout<<"Enter the value "<<token<<" :- ";</pre>
cin>>x;
s.push(char(x));
else
```

```
op2=s.pop(); //first pop
op1=s.pop(); //second pop
result=evaluate(op1,op2,token);
s.push(char(result));
result=s.pop();
cout<<"\n-----";
cout<<"\nPOSTFIX EVALUATION- "<<result<<endl;</pre>
cout<<"----"<<endl;
//to reverse the given infix for prefix
void reverse(char x[20], char y[20]) //x will store infix and
y will store reverse of infix
int i, j=0;
for(i=0;x[i]!='\0';i++);
i--;
                                       //since 'for' loop repeat
once again when the condition is false.
for(j=0;i>=0;j++,i--)
if(x[i]=='(')
y[j]=')';
else if(x[i]==')')
y[j]='(';
else
y[j]=x[i];
y[j]='\0';
//infix---> prefix
```

```
void infix prefix(char infix[20],char prefix[20])
char rev[20],pre1[20];
reverse(infix,rev);
infix_prefix_1(rev,pre1);
reverse(pre1,prefix);
void infix prefix 1(char infix[20],char prefix[20])
stack s;
int i,j=0;
char token,x;
for(i=0;infix[i]!='\0';i++)
token=infix[i];
if(isalnum(token))
                                                       //will check
whether the token is number or an alphabet
prefix[j]=token;
j++;
else
if(token=='(')
                                                      //check whether
token is opening bracket, then push the token.
s.push(token);
else if(token==')')
                                                     //check whether
token is closing bracket.
while((x=s.pop())!='(')
                                                    //pop all
elements until we get opening bracket.
prefix[j]=x;
```

```
else
while(s.isempty()==0 && precedence(token)<precedence(s.topdata())</pre>
             //first check stack is not empty and then the
precedence.
prefix[j]=s.pop();
j++;
s.push(token);
while(s.isempty()==0)
prefix[j]=s.pop();
j++;
prefix[j]='\0';
//evaluation of prefix.
void evaluate prefix(char prefix[20])
stack s;
int i,op1,op2,result;
char token,pre[20];
int x;
reverse(prefix,pre);
for(i=0;pre[i]!='\0';i++)
token=pre[i];
if(isalnum(token))
```

```
cout<<"Enter the value "<<token<<" :- ";</pre>
cin>>x;
s.push(char(x));
else
op1=s.pop();  //first pop
op2=s.pop();  //second pop
result=evaluate(op1,op2,token);
s.push(char(result));
result=s.pop();
cout<<"\n-----";
cout<<"\nPREFIX EVALUATION- "<<result<<endl;</pre>
cout<<"----"<<endl;
int precedence(char x)
if(x=='(')
return 0;
if(x=='+' || x=='-')
return 1;
if(x=='*' || x=='/')
return 2;
return 3;
int evaluate(int op1,int op2,char op)
if(op=='+')
return op1+op2;
if(op=='-')
```

```
return op1-op2;
if(op=='*')
return op1*op2;
if(op=='/')
return op1/op2;
if(op='%')
return op1%op2;
}
```

Output-

- 1. Infix to Postfix Expression
- 2. Evaluate Postfix
- 3. Infix to Prefix Expression
- 4. Evalute Prefix
- 5. Exit

Enter your choice: 1

Enter Infix expression: (5-2)+8/2-1

POSTFIX EXPRESSION- 52-82/+1-

- 1. Infix to Postfix Expression
- 2. Evaluate Postfix
- 3. Infix to Prefix Expression
- 4. Evalute Prefix
- 5. Exit

Enter your choice: 2

Enter the value 5:-5

Enter the value 2:- 2

Enter the value 8:-8

Enter the value 2:- 2

Enter the value 1:-1

POSTFIX EVALUATION- 6

1. Infix to Postfix Expression

- 2. Evaluate Postfix
- 3. Infix to Prefix Expression
- 4. Evalute Prefix
- 5. Exit

Enter your choice: 3

Enter Infix expression: (5-2)+8/2-1

PREFIX EXPRESSION -- +- 52/821

- 1. Infix to Postfix Expression
- 2. Evaluate Postfix
- 3. Infix to Prefix Expression
- 4. Evalute Prefix
- 5. Exit

Enter your choice: 4

Enter the value 1:-1

Enter the value 2:- 2

Enter the value 8:-8

Enter the value 2:- 2

Enter the value 5:-5

PREFIX EVALUATION- 6

- 1. Infix to Postfix Expression
- 2. Evaluate Postfix
- 3. Infix to Prefix Expression
- 4. Evalute Prefix

5. Exit

Enter your choice: 5

Program Exited!

Conclusion: In this experiment we understood how to implement stack as an abstract data type using linked list and use this ADT for conversion of infix expression to postfix, prefix and evaluation of postfix/prefix expression.