

Q2) a) long  $5000 \times 5.20 = 26,000$

$$5000 \times 5.80 = 29,000$$

$$\text{profit} = 3000$$

b) short  $37500 \times 1.60 = 60,000$

$$37500 \times 1.40 = 52,500$$

$$\text{profit} = 7500$$

c) short  $40 \times 7500 = 300,000$

$$40 \times 7800 = 312,000$$

$$\text{loss} = 12,000$$

d) long  $5 \times 3 \times 15000 = 225,000$

$$5 \times 3 \times 13500 = 202,500$$

$$\text{loss} = 22,500$$

- $K = F_0$  the strike of the European Put
- $S_T$  the spot price at maturity

Portfolio:

- Long one forward (payoff  $S_T - F_0$ )
- Long one European put with strike  $K = F_0$  (payoff  $\max\{K - S_T, 0\}$ )

So, at T

$$\pi_T = S_T - F_0 + \max\{F_0 - S_T, 0\}$$

So,

$$\pi_T = (S_T - F_0) + (F_0 - S_T) \text{ if } S_T < F_0$$

$$= 0$$

and

$$\pi_T = (S_T - F_0) + 0 \text{ if } S_T > F_0$$

$$= S_T - F_0$$

that is exactly payoff of European Call with strike  $K = F_0$ .

$$\pi_T = \max\{S_T - F_0, 0\}$$

At maturity the two-instrument portfolio have same payoff as the European call with that strike and maturity.



1. Short Forward Contract

$$\text{Profit or loss} = (\text{Forward Price} - \text{Spot Price}) \times 1,000$$

Forward Price = \$2050 per ounce

Spot Price (\$)	Profit or loss (\$)
1400	6,50,000
1500	5,50,000
1560	4,90,000
1600	4,50,000
1800	2,50,000
2050	0
2200	-1,50,000
2300	-2,50,000
2400	-3,50,000

## Put-Call Parity: Risk-Free Rate

→ Using the European put-call parity for a non-dividend stock:

$$C - P = S - Ke^{-rT}$$

$T = 12$  months, Strike Price ( $K$ ) = 120

$C = \$20$        $P = \$5$

Current Stock Price ( $S$ ) = \$130

Plugging in the values,

$$\Rightarrow 20 - 5 = 130 - 120 \times e^{-r \cdot 1}$$

$$\Rightarrow 15 = 130 - 120 \times e^{-r}$$

$$\Rightarrow e^{-r} = \frac{115}{120} = 0.9583$$

Taking log on both sides,

$$\Rightarrow -r = \ln(0.9583)$$

$$\Rightarrow -r = -0.0429$$

$$\Rightarrow r = 0.043$$

## 5. Portfolio of Forward + Put Option

Let  $T$  be the time of maturity

→  $F_0$  be the forward price agreed at time 0. (so the forward payoff at  $T$  is  $S_T - F_0$ ),



### Q3 (A) FUTURE CONTRACT

PAGE NO.       
SPOT CONTRACT.

① Agreement to sell/buy at a future date

② Price: agreed today, settled in future

③ Settlement: on contract's maturity date

④ Standardized terms (quantity, quality)

Agreement for immediate purchase/sale.

Based on current market price.

Immediate (usually T+2 days)

Customised b/w buyer & seller.

(B) How does a futures contract work on commodity exchange?

① Consider a buyer & seller agree to a standardised contract via commodity exchange (wheat futures contract)

② The contract specifies

1) Quantity

2) Quality grade.

3) Delivery date (say after 3 months)

4) Futures price (₹ x quintal)

③ Both parties deposit margin with the exchange to reduce default risk.

④ The position is marked to market daily & margin is adjusted accordingly.

⑤ On maturity, either physical delivery takes place. Parties square off their positions & settle profit/loss.

(C) ROLE OF COMMODITY EXCHANGE :-

① contracts are pre-defined in terms of quality, quantity & expiry.

② Handling by the clearing house which acts as the counterparty to both buyer & seller.



- 3) Collects initial & maintenance margin to ensure both parties honor the contract
- ④ Adjusts profit/loss daily to avoid accumulation of large risk.
- ⑤ Ensures delivery of commodity (if opted) as per contract terms / enable cash settlement.

(Q4) OPTION TYPE  $\Rightarrow$  European Put.

$$P = \$3$$

$$K = \$40$$

$$S_0 = \$42$$

$$\text{Payoff} = \max(K - S_T, 0)$$

$$\text{Profit} = \text{Payoff} - \text{Premium}$$

(i) To make a profit :-

$$\text{Profit} = \max(K - S_T, 0) - 3 > 0$$

$$\Rightarrow (K - S_T) > 3$$

$$S_T < K - 3 = 37$$

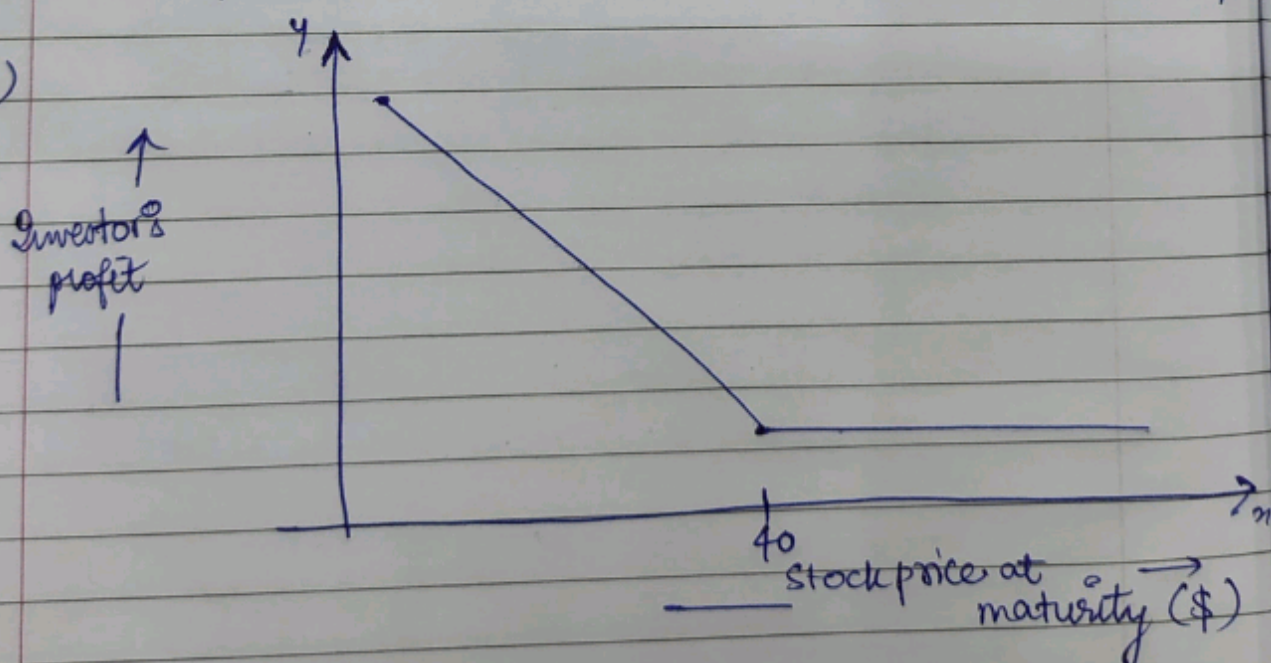
Ans = if stock price at maturity is less than \$37.

(ii) When Strike price > Stock Price at maturity

$$K > S_T \Rightarrow \text{Put is exercised when } S_T < 40$$

so the option is exercised if the stock price falls below \$40

iii)



Assn 2.1

Sonali : Q 1, 5

Harshita : Q 3, 4

Himanshi : Q 2, 6

Assn 2.2

Q 1, 5, 6

Q 3, 4

Q 2