



LISTS

Introduction

- Array

successive items located at fixed distance apart

- disadvantage

- data movements during insertion and deletion
- waste space in storing n ordered lists of varying size

- possible solution

- linked list

Pointer Review (1)

Pointer Can Be Dangerous

```
int i, *pi;
```

i 1000
 ?

 2000
pi ?

```
pi = &i;
```

i 1000
*pi ?

 2000
pi 1000

```
i = 10 or *pi = 10
```

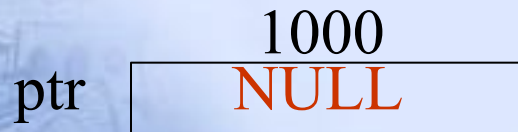
i 1000
*pi 10

 2000
pi 1000

- Set to NULL
- Explicit typecasts

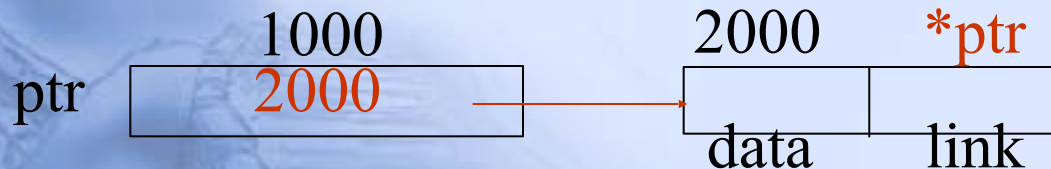
Pointer Review (2)

```
typedef struct list_node *list_pointer;  
typedef struct list_node {  
    int data;  
    list_pointer link;  
}  
list_pointer ptr = NULL;
```

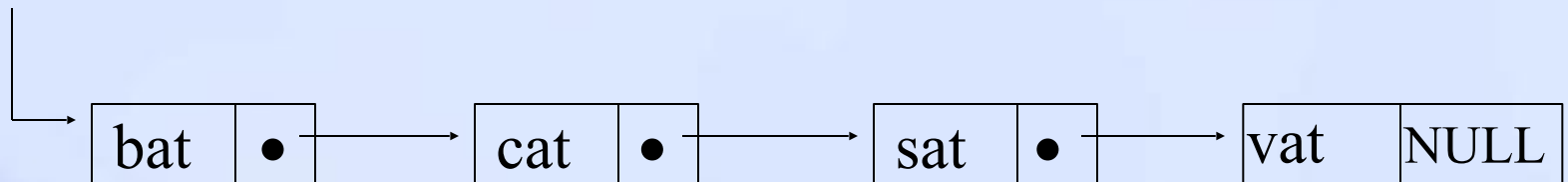


ptr->data or (*ptr).data

```
ptr = malloc(sizeof(list_node));
```

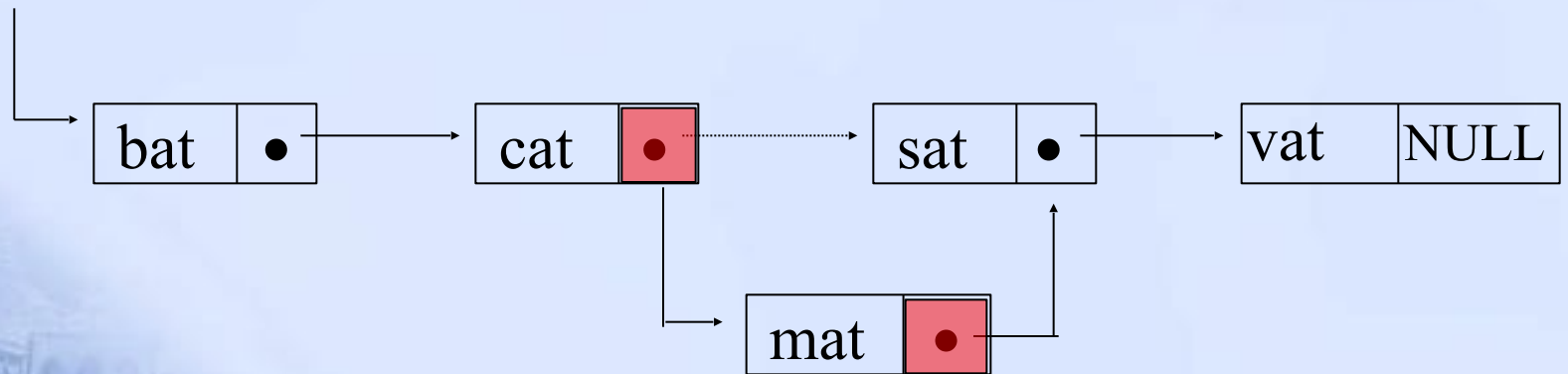


4.2 SINGLY LINKED LISTS

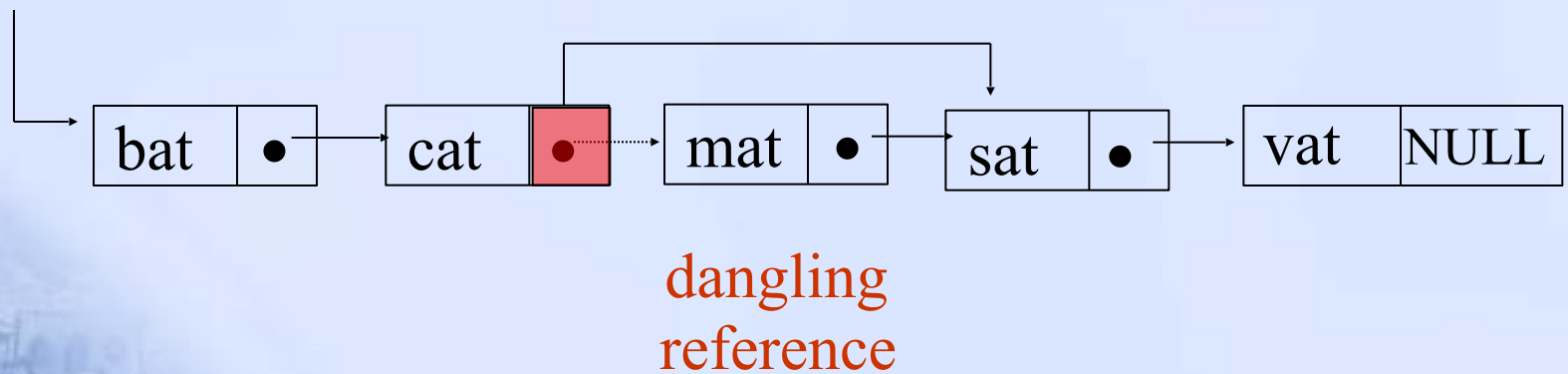


***Figure 4.1: Usual way to draw a linked list**

Insertion



***Figure 4.2: Insert mat after cat**



***Figure 4.3: Delete *mat* from list**

Example 4.1: create a linked list of words

Declaration

```
typedef struct list_node *list_pointer;  
typedef struct list_node {  
    char data [4];  
    list_pointer link;  
};
```

Creation

```
list_pointer ptr =NULL;
```

Testing

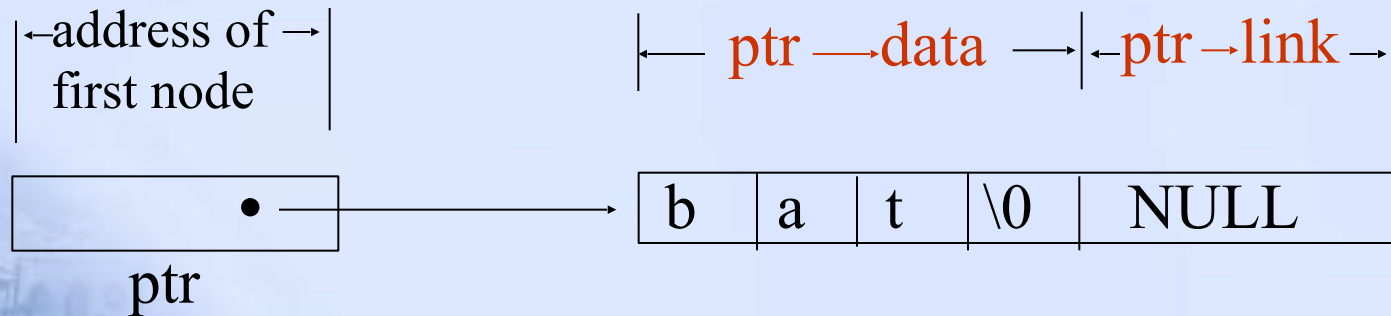
```
#define IS_EMPTY(ptr) (!(ptr))
```

Allocation

```
ptr=(list_pointer) malloc (sizeof(list_node));
```

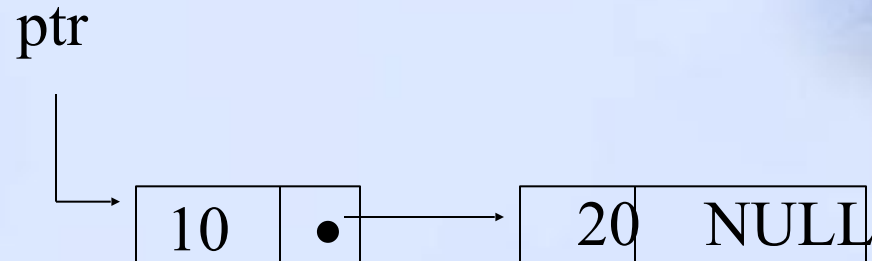


```
strcpy(ptr -> data, "bat");  
ptr -> link = NULL;
```



***Figure 4.4: Referencing the fields of a node(p.142)**

Example: create a two-node list

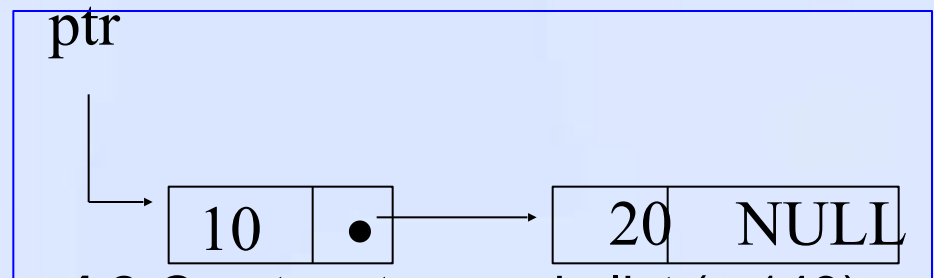


```
typedef struct list_node *list_pointer;  
struct list_node {  
    int data;  
    list_pointer link;  
};  
list_pointer ptr = NULL
```

Example 4.2: (p.142)

```
list_pointer create2( )
{
/* create a linked list with two nodes */
list_pointer first, second;

first = (list_pointer) malloc(sizeof(list_node)); // new list_node;
second = ( list_pointer) malloc(sizeof(list_node)); //new list_node
second -> link = NULL;
second -> data = 20;
first -> data = 10;
first ->link = second;
return first;
}
```



***Program 4.2: Create a two-node list (p.143)**

List Insertion:

Insert a node after a specific node

```
void insert(list_pointer *ptr, list_pointer node)
{
    /* insert a new node with data = 50 into the list ptr after node */
    list_pointer temp;

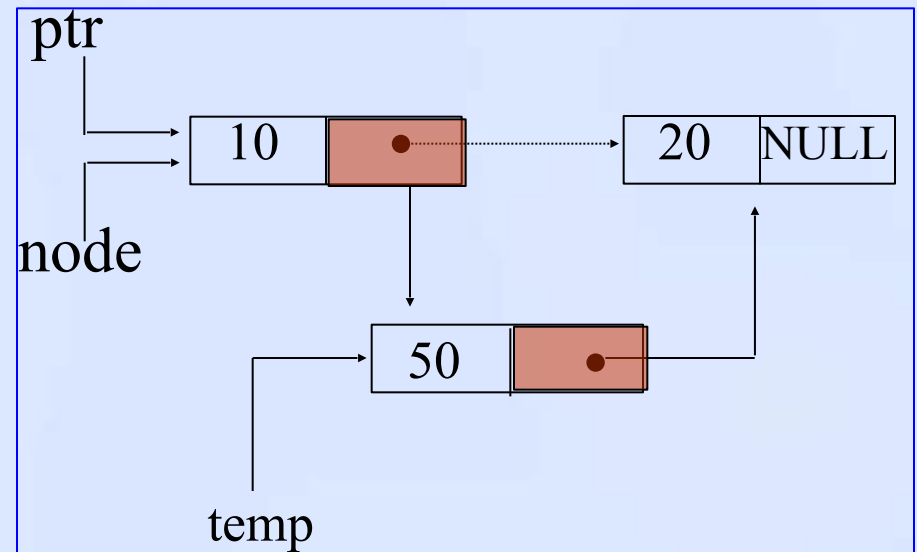
    temp = (list_pointer) malloc(sizeof(list_node));

    if (IS_FULL(temp)){
        cout<<"The memory is full\n";
        exit (1);
    }
```

```

temp->data = 50;
if (*ptr) { noempty list
    temp->link = node ->link;
    node->link = temp;
}
else { empty list
    temp->link = NULL;
    *ptr = temp;
}
}

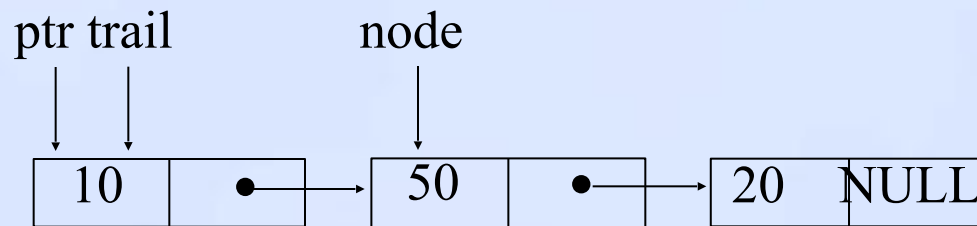
```



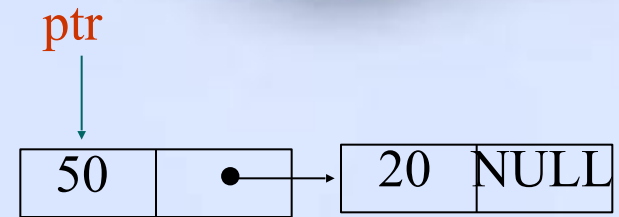
***Program 4.3: Simple insert into front of list (p.144)**

List Deletion

Delete the first node.

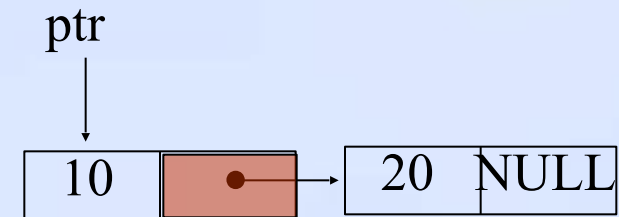
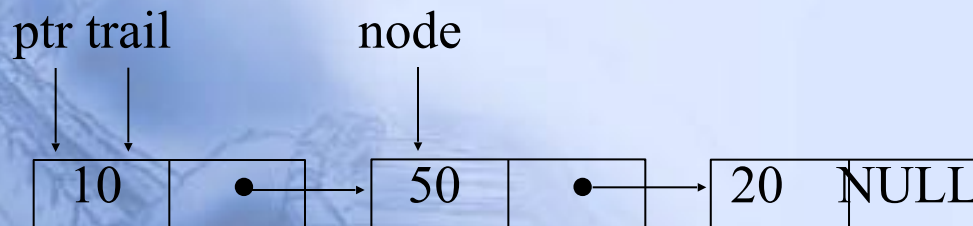


(a) before deletion



(b) after deletion

Delete node other than the first node.




```
void delete(list_pointer *ptr, list_pointer trail, list_pointer node)
```

```
{
```

```
/* delete node from the list, trail is the preceding node  
ptr is the head of the list */
```

```
if (trail)
```

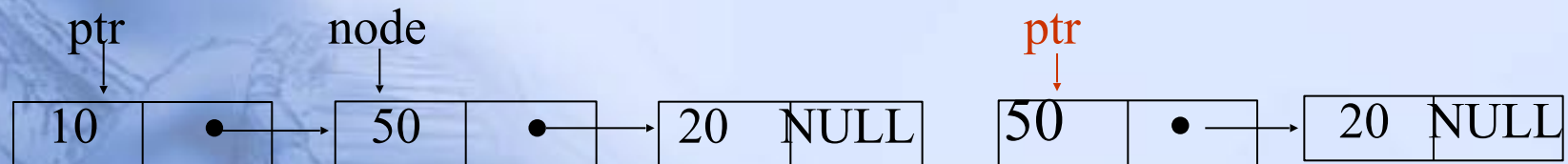
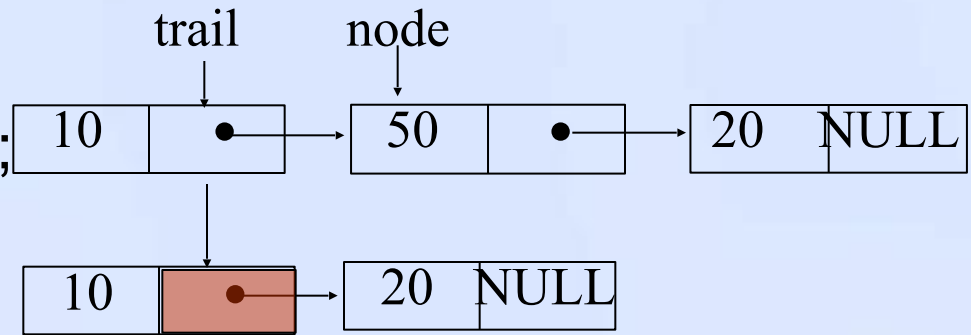
```
    trail->link = node->link;
```

```
else
```

```
    *ptr = (*ptr) ->link;
```

```
    free(node);
```

```
}
```

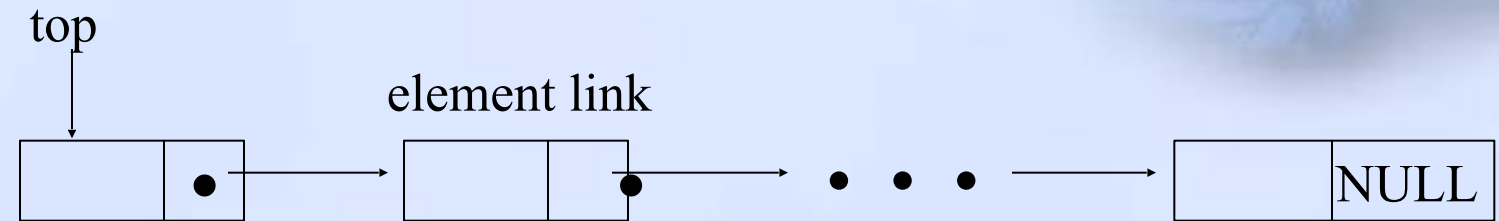


Print out a list (traverse a list)

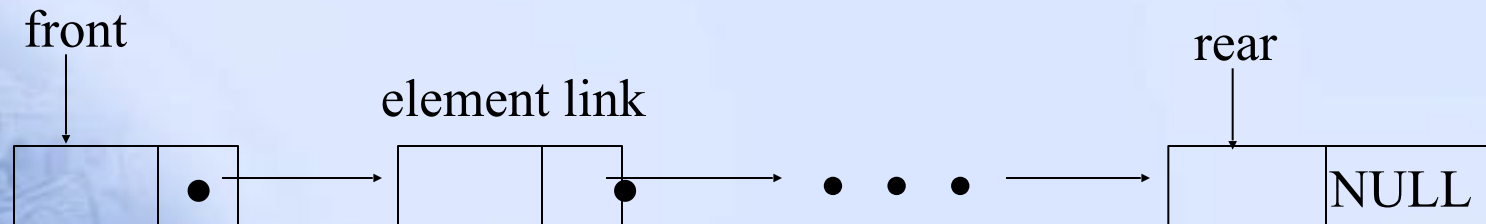
```
void print_list(list_pointer ptr)
{
    printf("The list contains: ");
    for ( ; ptr; ptr = ptr->link)
        printf("%4d", ptr->data);
    printf("\n");
}
```

***Program 4.5: Printing a list (p.146)**

4.3 DYNAMICALLY LINKED STACKS AND QUEUES



(a) Linked Stack



(b) Linked queue

***Figure 4.10: Linked Stack and queue (p.147)**

Push in the linked stack

```
void add(stack_pointer *top, element item)
{
    /* add an element to the top of the stack */
    stack_pointer temp =
        (stack_pointer) malloc (sizeof (stack));
    if (IS_FULL(temp)) {
        fprintf(stderr, " The memory is full\n");
        exit(1);
    }
    temp->item = item;
    temp->link = *top;
    *top= temp;
}
```

***Program 4.6: Add to a linked stack (p.149)**

pop from the linked stack

```
element delete(stack_pointer *top) {  
    /* delete an element from the stack */  
    stack_pointer temp = *top;  
    element item;  
    if (IS_EMPTY(temp)) {  
        fprintf(stderr, "The stack is empty\n");  
        exit(1);  
    }  
    item = temp->item;  
    *top = temp->link;  
    free(temp);  
    return item;  
}
```

***Program 4.7: Delete from a linked stack (p.149)**

enqueue in the linked queue

```
void addq(queue_pointer *front, queue_pointer *rear, element item)
{ /* add an element to the rear of the queue */
    queue_pointer temp =
        (queue_pointer) malloc(sizeof (queue));
    if (IS_FULL(temp)) {
        fprintf(stderr, " The memory is full\n");
        exit(1);
    }
    temp->item = item;
    temp->link = NULL;
    if (*front) (*rear) -> link = temp;
    else *front = temp;
    *rear = temp; }
```


dequeue from the linked queue (similar to push)

```
element deleteq(queue_pointer *front) {  
    /* delete an element from the queue */  
    queue_pointer temp = *front;  
    element item;  
    if (IS_EMPTY(*front)) {  
        fprintf(stderr, "The queue is empty\n");  
        exit(1);  
    }  
    item = temp->item;  
    *front = temp->link;  
    free(temp);  
    return item;  
}
```

Polynomials

$$A(x) = a_{m-1}x^{e_{m-1}} + a_{m-2}x^{e_{m-2}} + \dots + a_0x^{e_0}$$

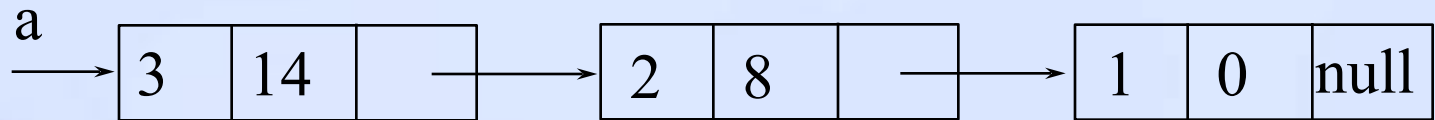
Representation

```
typedef struct poly_node *poly_pointer;  
typedef struct poly_node {  
    int coef;  
    int expon;  
    poly_pointer link;  
};  
poly_pointer a, b, c;
```

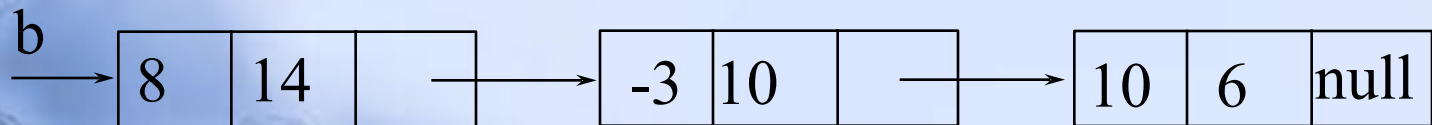
coef	expon	link
------	-------	------

Examples

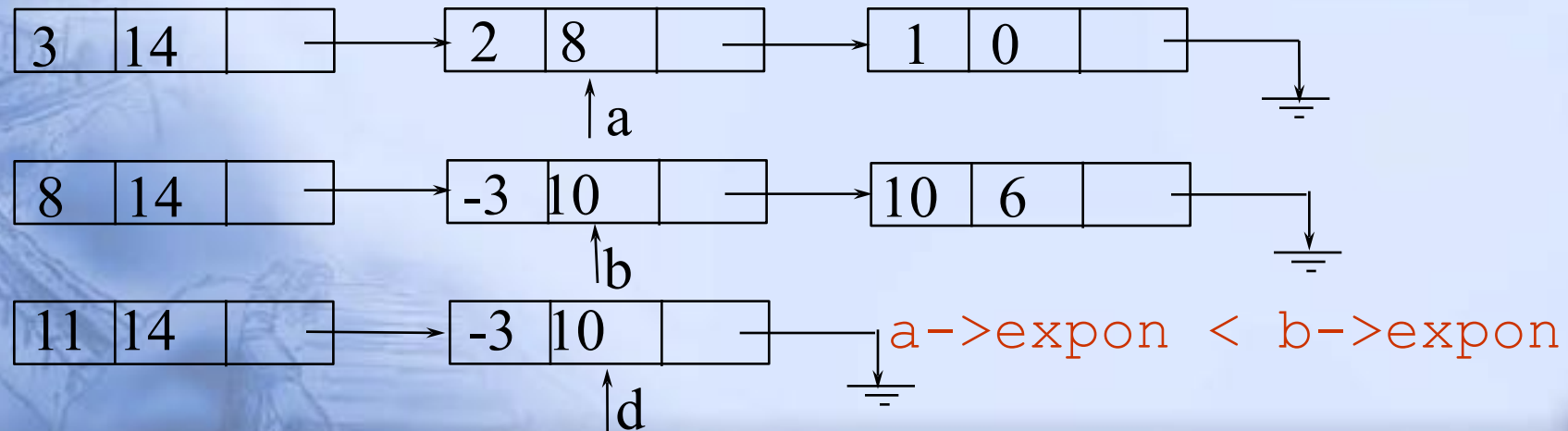
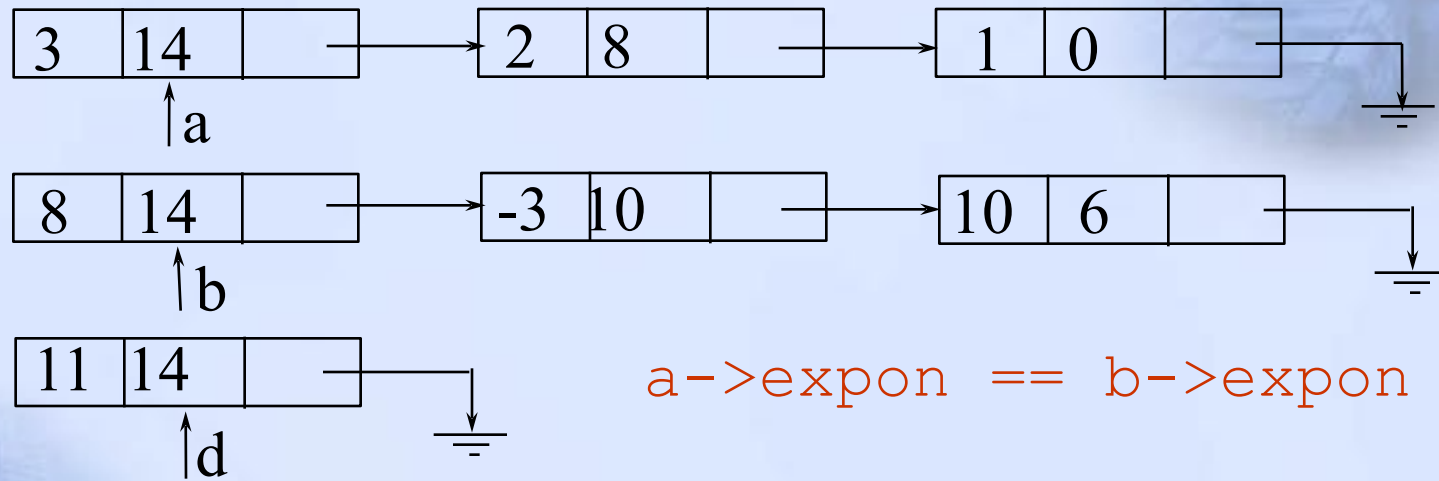
$$a = 3x^{14} + 2x^8 + 1$$



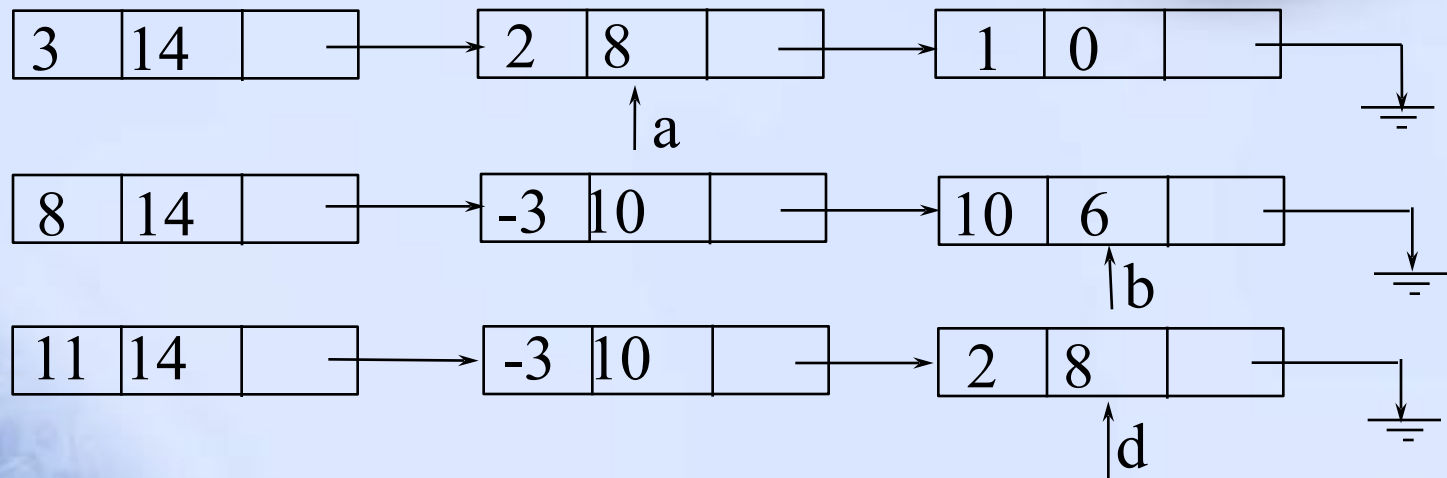
$$b = 8x^{14} - 3x^{10} + 10x^6$$



Adding Polynomials



Adding Polynomials (Continued)



$a \rightarrow \text{expon} > b \rightarrow \text{expon}$

Alogrithm for Adding Polynomials

```
poly_pointer padd(poly_pointer a, poly_pointer b)
{
    poly_pointer front, rear, temp;
    int sum;

    //create a dummy node
    rear = (poly_pointer)malloc(sizeof(poly_node));
    if (IS_FULL(rear)) {
        fprintf(stderr, "The memory is full\n");
        exit(1);
    }
    front = rear;
    while (a && b) {
        switch (COMPARE(a->expon, b->expon)) {
```



```

        case -1: /* a->expon < b->expon */
            attach(b->coef, b->expon, &rear);
            b = b->link;
            break;
        case 0: /* a->expon == b->expon */
            sum = a->coef + b->coef;
            if (sum) attach(sum, a->expon, &rear);
            a = a->link;      b = b->link;
            break;
        case 1: /* a->expon > b->expon */
            attach(a->coef, a->expon, &rear);
            a = a->link;
    }
}
for (; a; a = a->link)
    attach(a->coef, a->expon, &rear);
for (; b; b = b->link)
    attach(b->coef, b->expon, &rear);
rear->link = NULL;

//delete dummy node;
temp = front; front = front->link; free(temp);
return front;
}

```

Delete extra initial node.

Attach a Term

```
void attach(float coefficient, int exponent,
            poly_pointer *ptr)
{
    /* create a new node attaching to the node pointed to
       by ptr.
       ptr is updated to point to this new node. */
    poly_pointer temp;
    temp = (poly_pointer) malloc(sizeof(poly_node));
    if (IS_FULL(temp)) {
        fprintf(stderr, "The memory is full\n");
        exit(1);
    }
    temp->coef = coefficient;
    temp->expon = exponent;
    (*ptr)->link = temp;
    *ptr = temp;
}
```

Analysis

(1) coefficient additions

$$0 \leq \text{additions} \leq \min \{m, n\}$$

where m (n) denotes the number of terms in A (B).

(2) exponent comparisons

extreme case

$$e_{m-1} > f_{m-1} > e_{m-2} > f_{m-2} > \dots > e_0 > f_0$$

$m+n-1$ comparisons

(3) creation of new nodes

extreme case

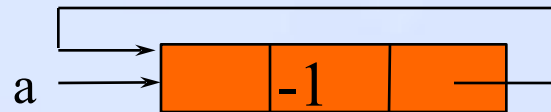
$m + n$ new nodes

summary $O(m+n)$

Head Node

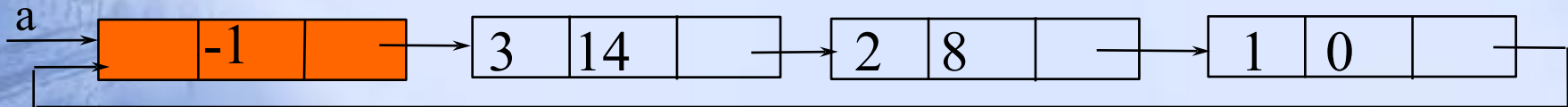
Represent **polynomial** as **circular list**.

(1) zero



Zero polynomial

(2) others



$$a = 3x^{14} + 2x^8 + 1$$

Another Padd

```
poly_pointer cpadd(poly_pointer a, poly_pointer b)
{
    poly_pointer starta, d, lastd;
    int sum, done = FALSE;
    starta = a;
    a = a->link;
    b = b->link;
    d = get_node();
    d->expon = -1;    lastd = d;
    do {
        switch (COMPARE(a->expon, b->expon)) {
            case -1: attach(b->coef, b->expon, &lastd);
                    b = b->link;
                    break;
```

Set expon field of head node to -1.

Another Padd (*Continued*)

```
case 0: if (starta == a) done = TRUE;
        else {
            sum = a->coef + b->coef;
            if (sum) attach(sum, a->expon, &lastd);
            a = a->link;    b = b->link;
        }
        break;
case 1: attach(a->coef, a->expon, &lastd);
        a = a->link;
    }
} while (!done);
lastd->link = d;
return d;
}
```

Link last node to first

Additional List Operations

```
typedef struct list_node *list_pointer;  
typedef struct list_node {  
    char data;  
    list_pointer link;  
};
```

Invert single linked lists

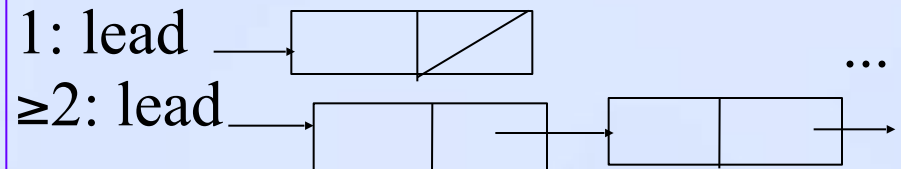
Concatenate two linked lists

Invert Single Linked Lists

Use two extra pointers: middle and trail.

```
list_pointer invert(list_pointer lead)
{
    list_pointer middle, trail;
    middle = NULL;
    while (lead) {
        trail = middle;
        middle = lead;
        lead = lead->link;
        middle->link = trail;
    }
    return middle;
}
```

0: null



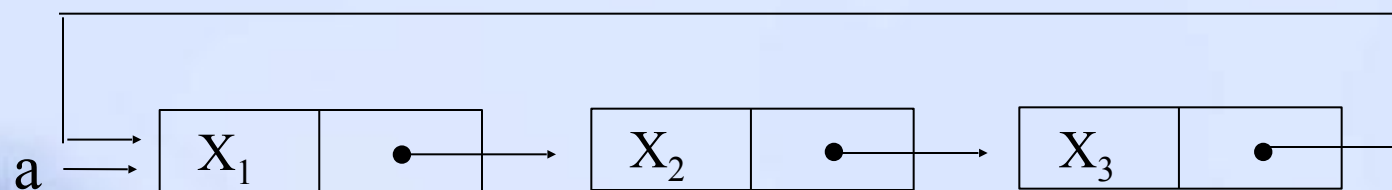
Concatenate Two Lists

```
list_pointer concatenate(list_pointer
                        ptr1, list_pointer ptr2)
{
    list_pointer temp;
    if (IS_EMPTY(ptr1)) return ptr2;
    else {
        if (!IS_EMPTY(ptr2)) {
            for (temp=ptr1; temp->link; temp=temp->link);
            temp->link = ptr2;
        }
        return ptr1;
    }
}
```

$O(m)$ where m is # of elements in the first list

4.5.2 Operations For Circularly Linked List

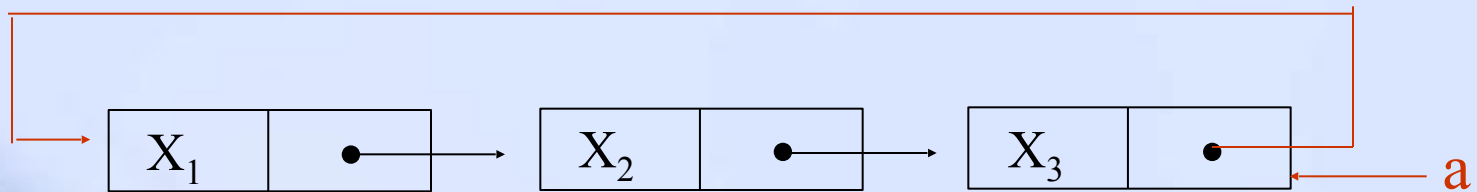
What happens when we insert a node to the front of a circular linked list?



Problem: move down the whole list.

***Figure 4.16: Example circular list (p.165)**

A possible solution:

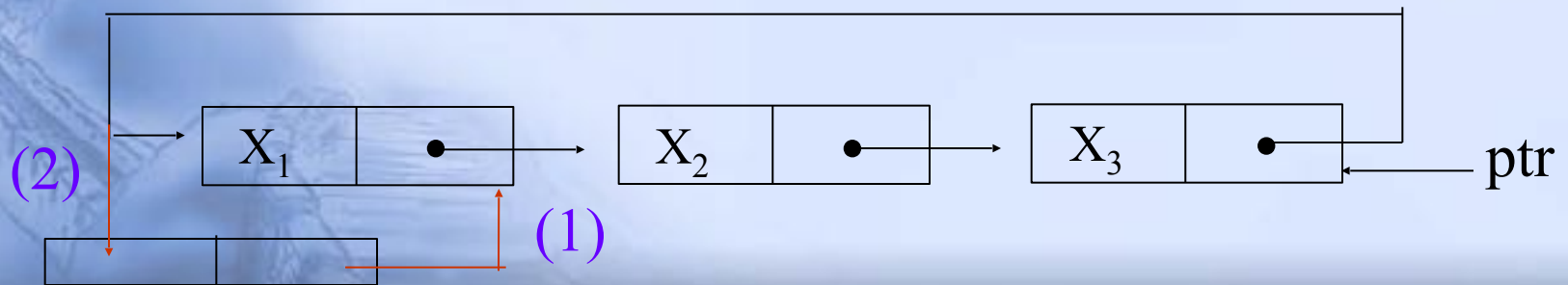


Note a pointer points to the last node.

***Figure 4.17: Pointing to the last node of a circular list (p.165)**

Operations for Circular Linked Lists

```
void insert_front (list_pointer *ptr, list_pointer
node)
{
    if (IS_EMPTY(*ptr)) {
        *ptr= node;
        node->link = node;
    }
    else {
        node->link = (*ptr)->link;    (1)
        (*ptr)->link = node;          (2)
    }
}
```



Length of Linked List

```
int length(list_pointer ptr)
{
    list_pointer temp;
    int count = 0;
    if (ptr) {
        temp = ptr;
        do {
            count++;
            temp = temp->link;
        } while (temp!=ptr);
    }
    return count;
}
```

4.8 Doubly Linked List

Move in forward and backward direction.

Singly linked list (*in one direction only*)

How to get the preceding node during deletion or insertion?

Using 2 pointers

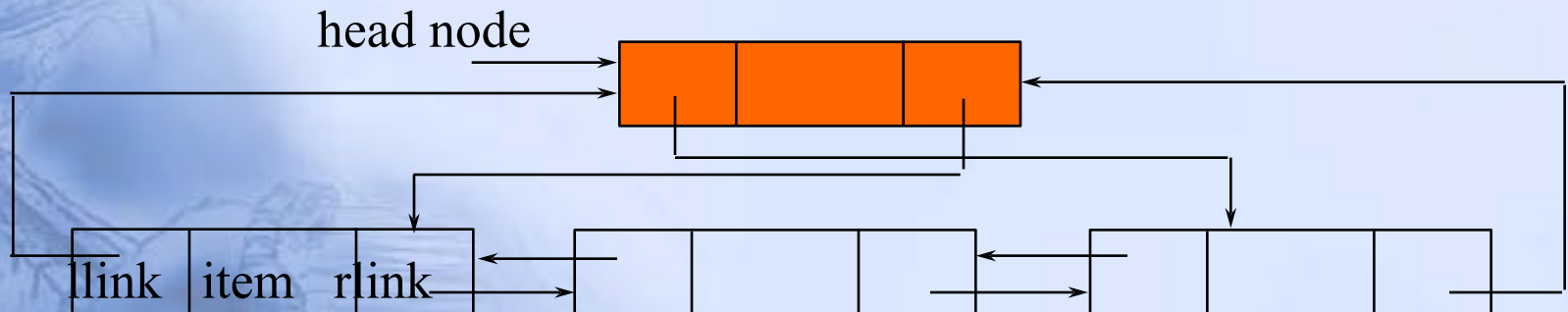
Node in doubly linked list consists of:

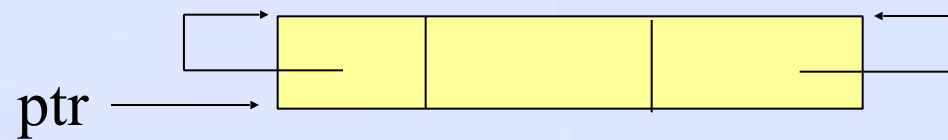
1. *left link field* (llink)
2. *data field* (item)
3. *right link field* (rlink)

Doubly Linked Lists

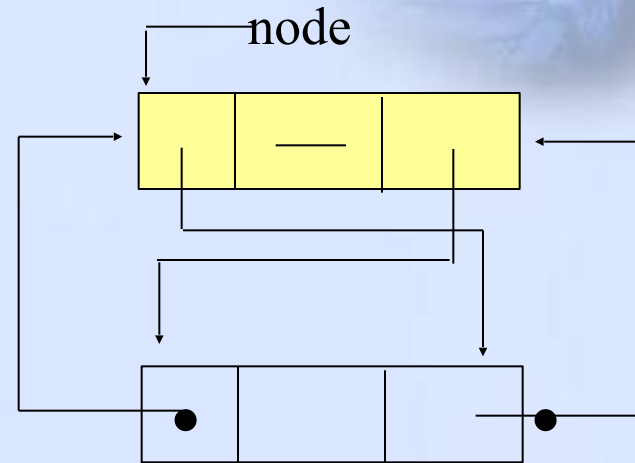
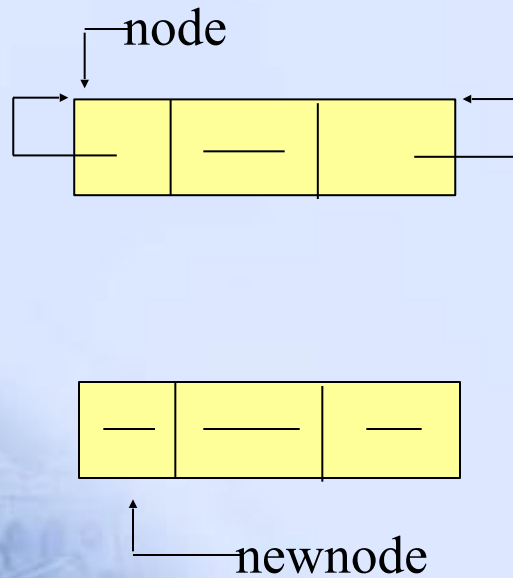
```
typedef struct node *node_pointer;  
typedef struct node {  
    node_pointer llink;  
    element item;  
    node_pointer rlink;  
}
```

ptr
 $= \text{ptr} \rightarrow \text{rlink} \rightarrow \text{llink}$
 $= \text{ptr} \rightarrow \text{llink} \rightarrow \text{rlink}$





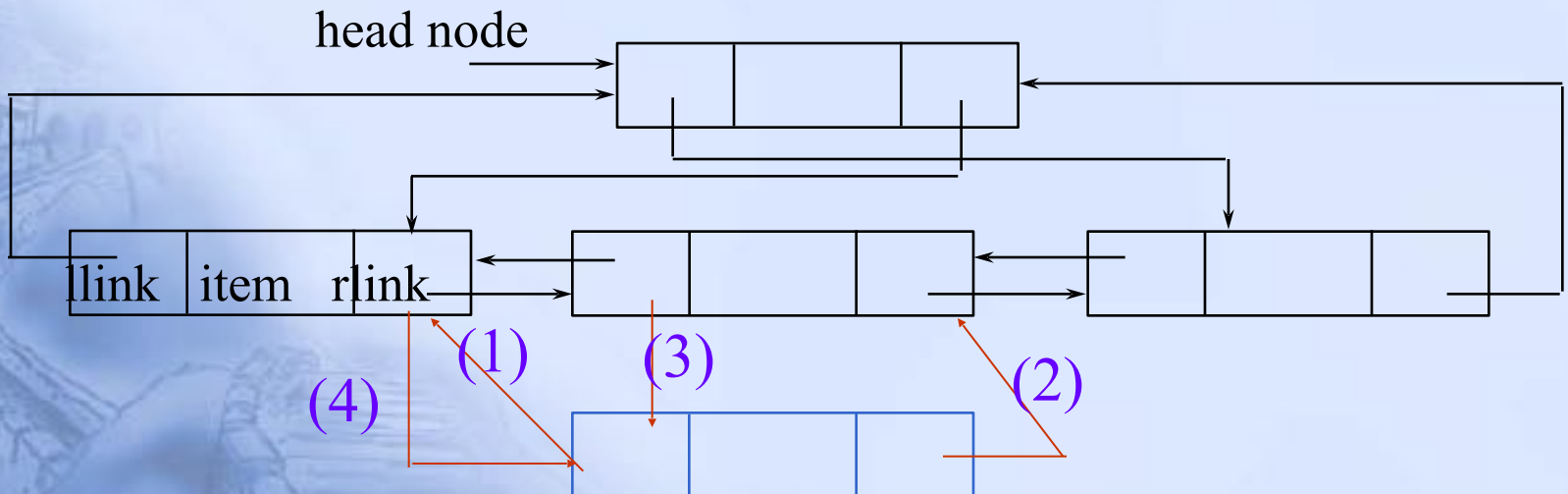
***Figure 4.24: Empty doubly linked circular list with head node (p.180)**



***Figure 4.25: Insertion into an empty doubly linked circular list (p.181)**

Insert

```
void dininsert(node_pointer node, node_pointer newnode)
{
    (1) newnode->llink = node;
    (2) newnode->rlink = node->rlink;
    (3) node->rlink->llink = newnode;
    (4) node->rlink = newnode;
}
```



Delete

```
void ddelete(node_pointer node, node_pointer
deleted)
{
    if (node==deleted) printf("Deletion of head node
                           not permitted.\n");
    else {
        (1) deleted->llink->rlink= deleted->rlink;
        (2) deleted->rlink->llink= deleted->llink;
        free(deleted);
    }
}
```

