

# **SOH Prediction of Li-ion Batteries Using Linear Regression and LSTM**

# Project Overview

## Problem Background

- **Lithium-ion batteries** are used in various fields such as **Electric Vehicle (EV)** and **Energy Storage System (ESS)**.
- Therefore, an effective **SOH (State of Health) prediction algorithm** is essential.
- **SOH (State of Health)**: Represents the battery's degradation status, specifically the **capacity to store electricity**.
- SOH generally **decreases as the charge/discharge cycle increases**.
- Batteries are typically used until the **SOH decreases to 60% ~ 70%**.

# 1. Project Overview

## SOH Calculation Method

The State of Health (SOH) is calculated using the battery's current discharge capacity relative to its initial, nominal capacity.

$$SOH = \frac{Q_m}{Q_{nom}}$$

- $Q_{nom}$ : Initial battery discharge capacity (Nominal Capacity)
- Value used: 2 Ah
- $Q_m$ : Battery discharge capacity at the  $m^{th}$  Cycle.

This calculation is performed using the **NASA PCoE Datasets**

## 2. Project Overview

### Data Experiment Conditions

The **NASA PCoE Datasets** used are categorized into three groups based on their experimental conditions:

- Data Group A: **Normal temperature** Charge/Discharge data (B05, B07, B18)
- Data Group B: **Normal temperature High-Power** Charge/Discharge data (B33, B34)
- Data Group C: **Low Temperature** Charge/Discharge data (B46, B47, B48)
- "Our LSTM model performed well because it was trained on a **large and complex dataset** We utilized data from **eight individual batteries** run under different conditions, from normal to low-temperature. For just one cell, the model processed **tens of thousands of high-resolution measurements** recorded over the battery's entire lifespan (up to 200 cycles).

### Project Goals

The objective is to implement an SOH prediction simulation and compare different training scenarios:

1. Implement an **SOH prediction simulation** using **Linear Regression** and **LSTM**.
2. Perform training using **50% of the data**.
3. Perform training using **70% of the data**.
4. **Visualize the prediction results**.
5. **Analyze results using RMSE and MAE**

### 3. Execution Process

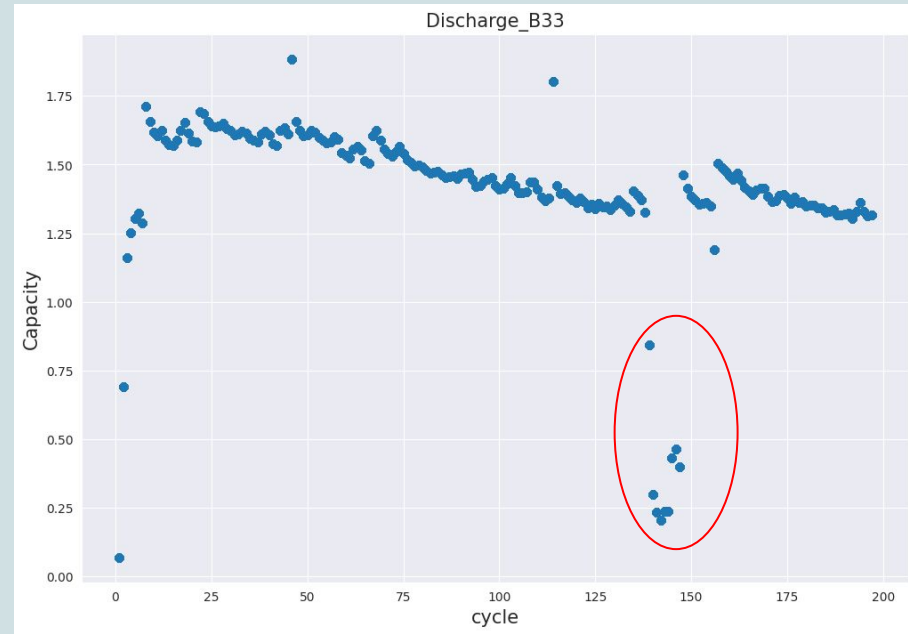
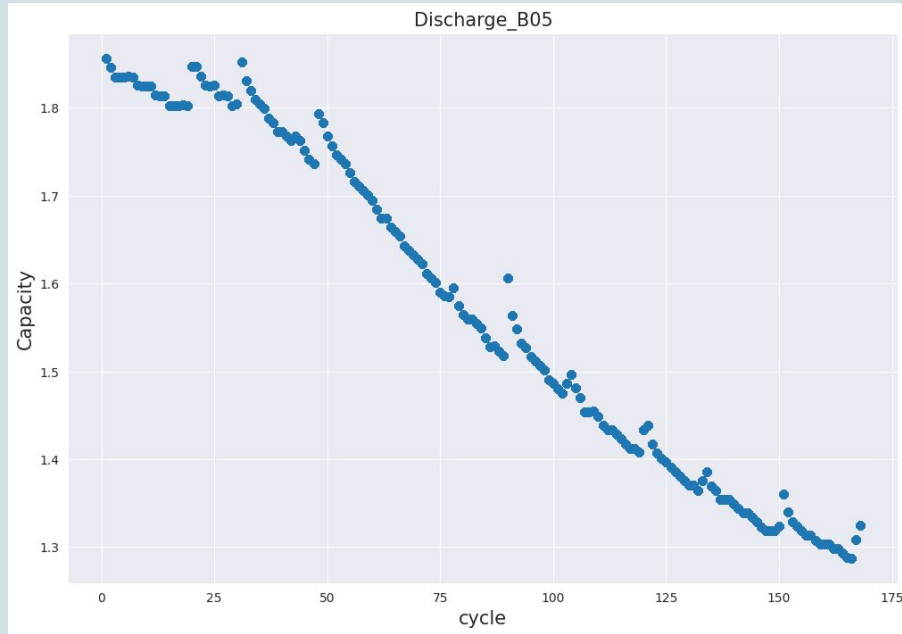
- SOH Calculation Review

The State of Health (SOH) was calculated for each discharge cycle using the **capacity**  $Q_m$  from the NASA PCoE dataset and the **Nominal Capacity** ( $Q_{nom}=2 \text{ Ah}$ ).

	terminal_voltage	terminal_current	temperature	charge_current	charge_voltage	time	capacity	cycle	SOH
0	4.191492	-0.004902	24.330034	-0.0006	0.000	0.000	1.856487	1	0.928244
1	4.190749	-0.001478	24.325993	-0.0006	4.206	16.781	1.856487	1	0.928244
2	3.974871	-2.012528	24.389085	-1.9982	3.062	35.703	1.856487	1	0.928244
3	3.951717	-2.013979	24.544752	-1.9982	3.030	53.781	1.856487	1	0.928244
4	3.934352	-2.011144	24.731385	-1.9982	3.011	71.922	1.856487	1	0.928244
...	...	...	...	...	...	...	...	...	...
50280	3.579262	-0.001569	34.864823	0.0006	0.000	2781.312	1.325079	168	0.662540
50281	3.581964	-0.003067	34.814770	0.0006	0.000	2791.062	1.325079	168	0.662540
50282	3.584484	-0.003079	34.676258	0.0006	0.000	2800.828	1.325079	168	0.662540
50283	3.587336	0.001219	34.565580	0.0006	0.000	2810.640	1.325079	168	0.662540
50284	3.589937	-0.000583	34.405920	0.0006	0.000	2820.390	1.325079	168	0.662540

## 4. SOH Visualization and Outliers

- SOH was plotted against the discharge cycle to observe the **degradation trend**.
- The plots revealed **Outliers** data points significantly deviating from the overall trend, notably in the **Discharge\_B33** graph (Group B).



## 5. Execution Process

### Outlier Removal using Quartiles

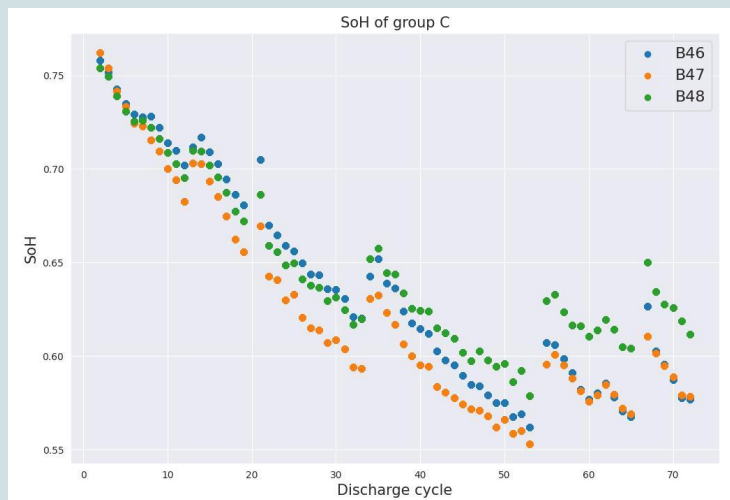
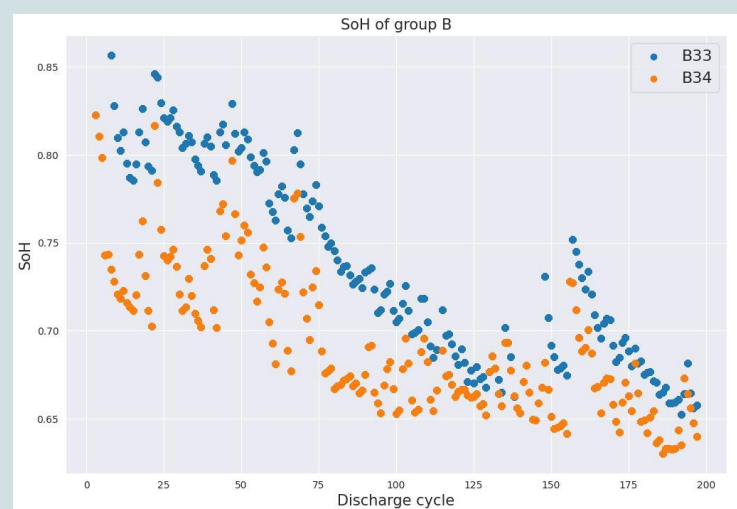
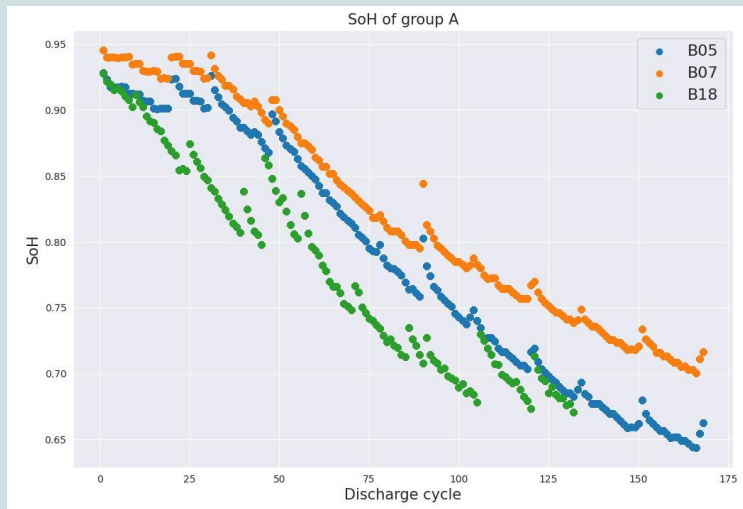
To ensure the models were trained on clean data, outliers that deviated sharply from the degradation trend were removed.

- **Method:** Interquartile Range (IQR) method.
- **IQR Definition:** The difference between the third quartile ( $Q_3$ ) and the first quartile ( $Q_1$ ).

### SOH Degradation Trends by Group

After data cleaning, the SOH versus Discharge Cycle was plotted for all batteries, grouped by their experimental conditions:

- **Group A (Normal Temp: B05, B07, B18):** Exhibits a relatively smooth and continuous SOH degradation trend.
- **Group B (High Power: B33, B34):** Shows a more scattered and complex degradation pattern, suggesting faster aging and more variance under high-power conditions.
- **Group C (Low Temp: B46, B47, B48):** Displays the steepest overall decline and significant fluctuation, characteristic of low-temperature degradation.





## Linear Regression Model

Linear regression was implemented as the **baseline model** to predict SOH based on the relationship between SOH and the discharge cycle.

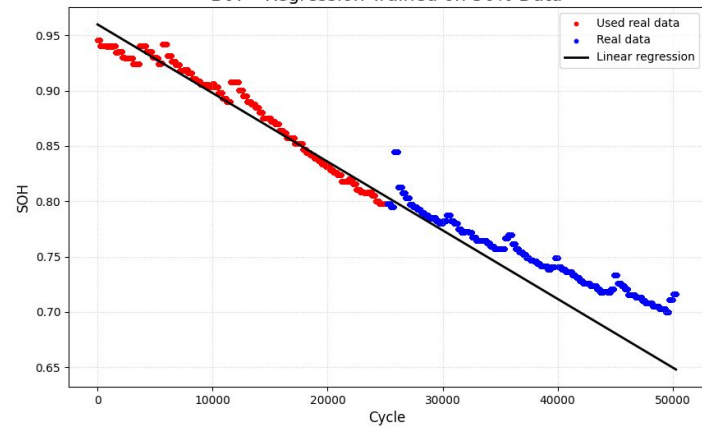
$$\hat{y}_i = a_1 x_i + a_0$$

$$E \equiv E_2(a_0, a_1) = \sum_{i=1}^m [y_i - (a_1 x_i + a_0)]^2$$

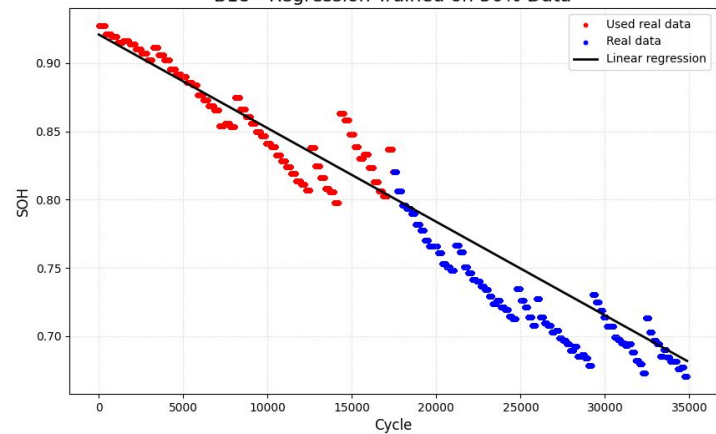
$$a_0 = \frac{\sum_{i=1}^m x_i^2 \sum_{i=1}^m y_i - \sum_{i=1}^m x_i y_i \sum_{i=1}^m x_i}{m \sum_{i=1}^m x_i^2 - \left( \sum_{i=1}^m x_i \right)^2},$$

$$a_1 = \frac{m \sum_{i=1}^m x_i y_i - \sum_{i=1}^m x_i \sum_{i=1}^m y_i}{m \sum_{i=1}^m x_i^2 - \left( \sum_{i=1}^m x_i \right)^2}.$$

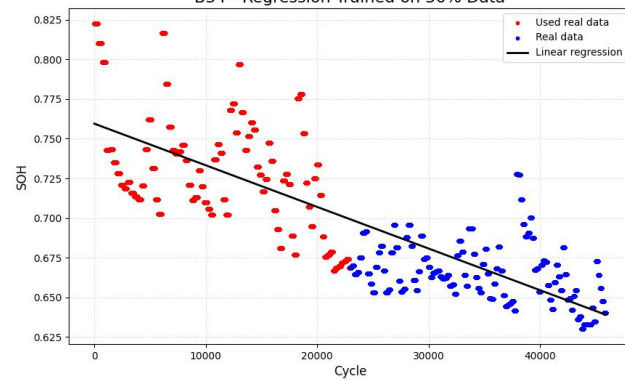
B07 - Regression Trained on 50% Data



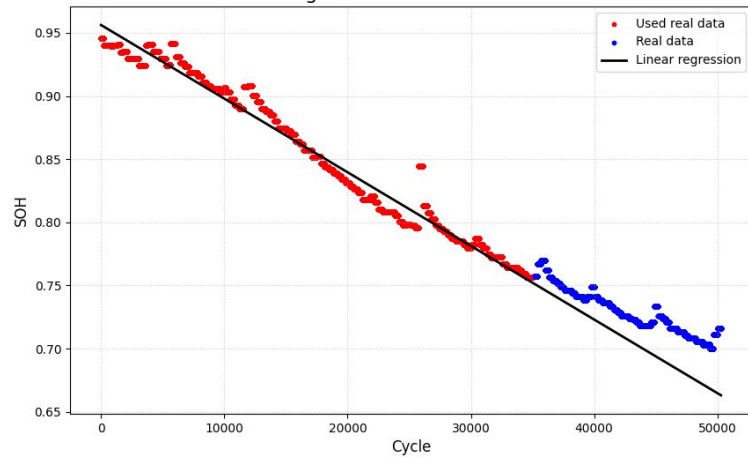
B18 - Regression Trained on 50% Data



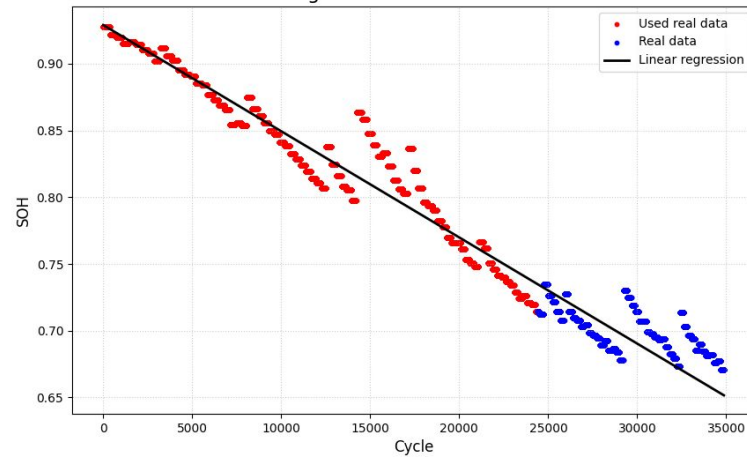
B34 - Regression Trained on 50% Data



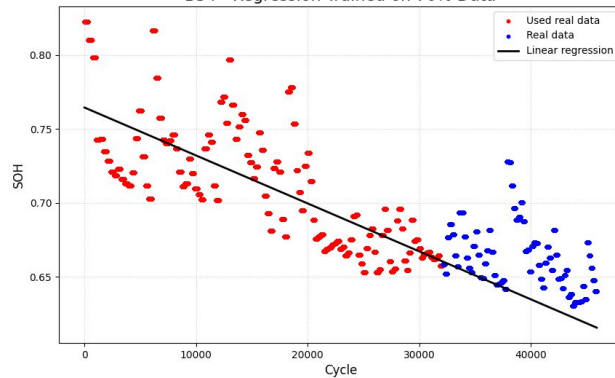
B07 - Regression Trained on 70% Data



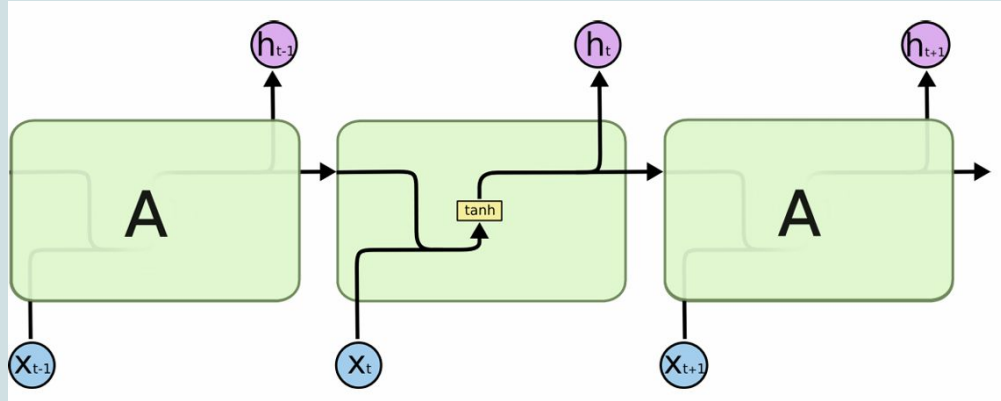
B18 - Regression Trained on 70% Data



B34 - Regression Trained on 70% Data

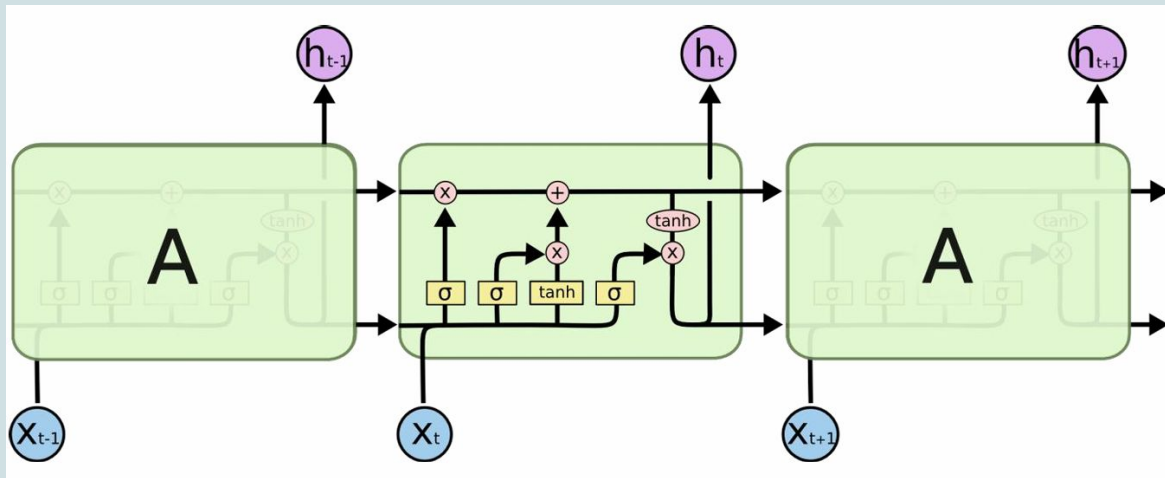


**RNN Concept:** The output at time  $h(t)$  depends on the current input  $x(t)$  and the memory of the previous state  $h(t-1)$



$$\begin{aligned}h_t &= f_w(h_{t-1}, x_t) \\ &= \tanh(w_{hh}h_{t-1} + w_{xh}x_t) \\ y_t &= w_{hy}h_t\end{aligned}$$

**LSTM Advantage:** LSTM solves the **vanishing gradient problem** of standard RNNs, making it highly effective for modeling **long-term dependencies** and time-series data like battery degradation.



$$\begin{aligned}f_t &= \sigma(W_{xh_f}x_t + W_{hh_f}h_{t-1} + b_{h_f}) \\i_t &= \sigma(W_{xh_i}x_t + W_{hh_i}h_{t-1} + b_{h_i}) \\o_t &= \sigma(W_{xh_o}x_t + W_{hh_o}h_{t-1} + b_{h_o}) \\\hat{c}_t &= \tanh(W_{xh_{\hat{c}}}x_t + W_{hh_{\hat{c}}}h_{t-1} + b_{h_{\hat{c}}}) \\c_t &= f_t \odot c_{t-1} + i_t \odot \hat{c}_t \\h_t &= o_t \odot \tanh(c_t)\end{aligned}$$

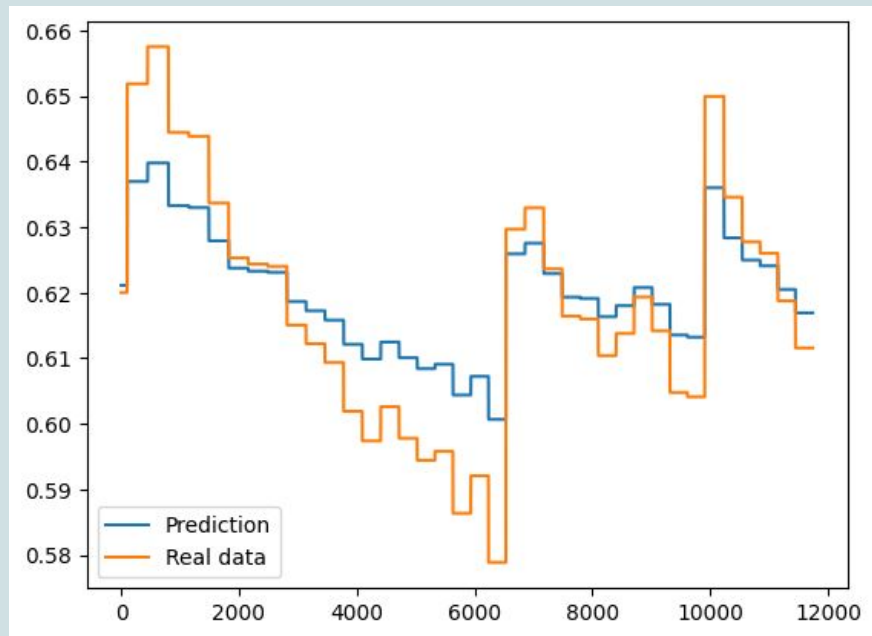
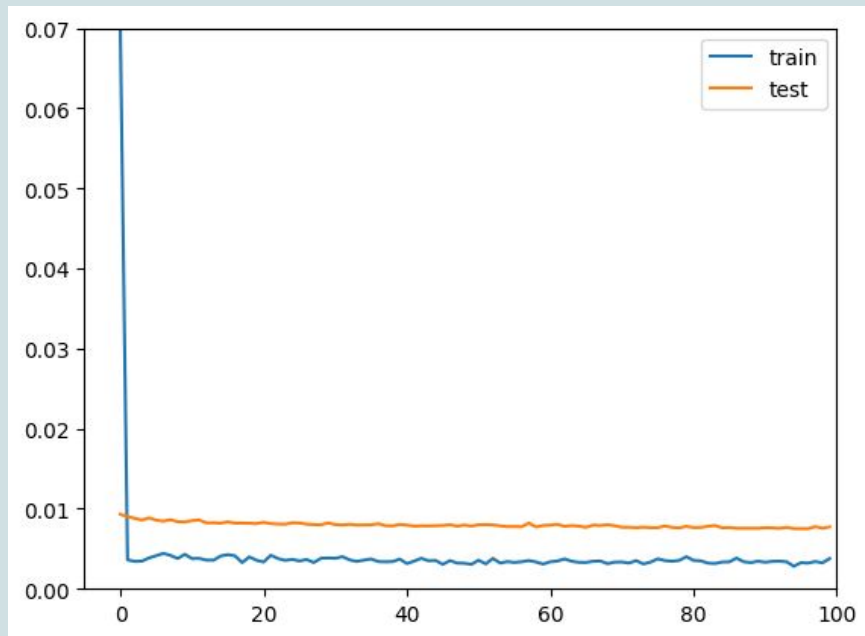
**Gate Mechanism:** LSTM uses three primary gates to regulate the flow of information:

1. **Forget Gate:** Controls what information from the past cell state should be forgotten.
2. **Input Gate:** Controls what new information (current input) should be stored in the cell state.
3. **Output Gate:** Determines the next hidden state based on the new cell state .

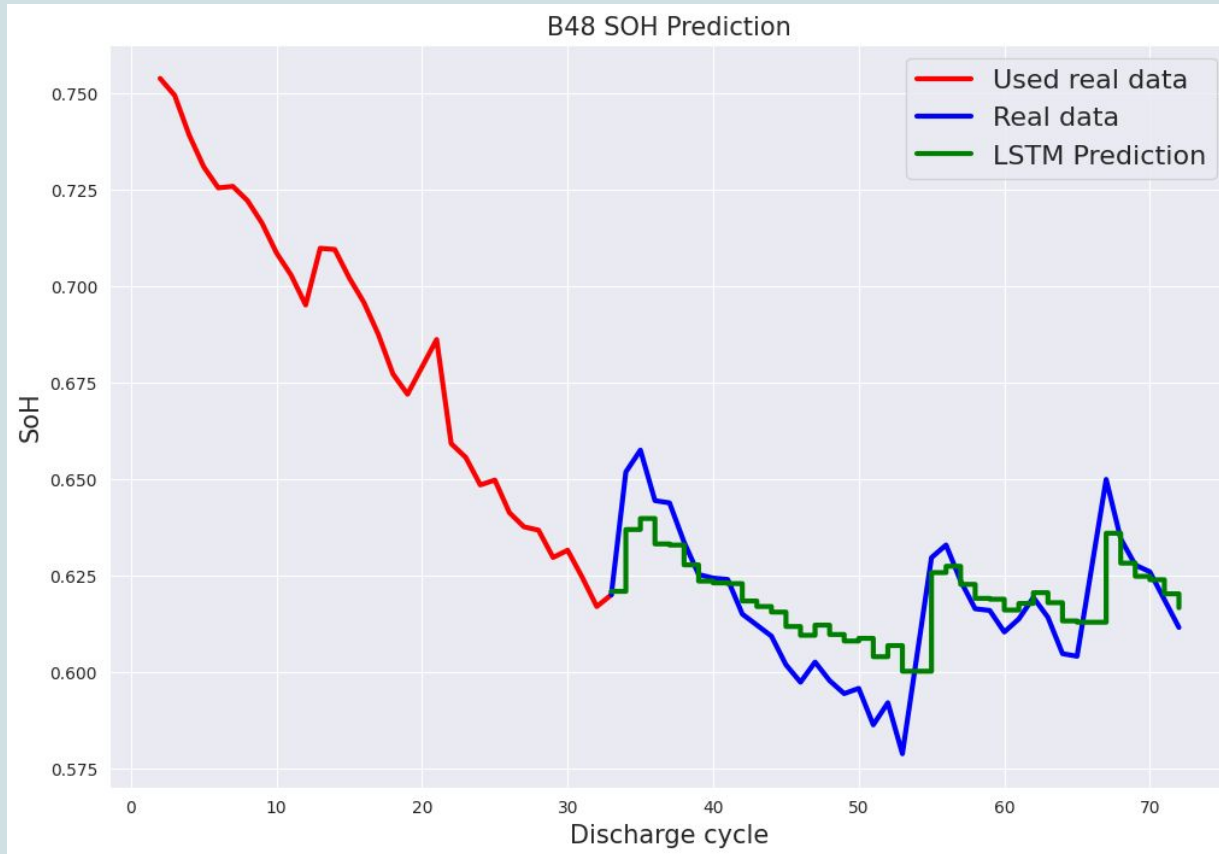
Component	Code	Parameter/Value	Explanation
Model Type	<code>Sequential()</code>	-	A linear stack of layers, used for building a basic deep learning model.
Recurrent Layer	<code>model.add(LSTM(64, ...))</code>	<b>64</b>	Defines a single <b>LSTM layer</b> with <b>64 units (neurons)</b> . These 64 units are the model's internal memory cells that process the sequential SOH data.
Input Shape	<code>input_shape=(trainX.shape[1], trainX.shape[2])</code>	(1, 1)	Specifies the shape of the input data: <b>1 timestep</b> (since <code>look_back=1</code> ) and <b>1 feature</b> (the SOH value).
Output Layer	<code>model.add(Dense(1))</code>	<b>1</b>	A single <b>Dense (fully connected)</b> neuron. This is the output layer responsible for producing the final, single SOH prediction value.
Loss Function	<code>model.compile(loss='mae', ...)</code>	<b>MAE</b> (Mean Absolute Error)	The function the model minimizes during training. MAE measures the average magnitude of the errors, calculating the absolute difference between the predicted and real SOH values.
Optimizer	<code>model.compile(..., optimizer='adam')</code>	<b>Adam</b>	A robust and highly effective optimization algorithm used to update the model weights. It efficiently finds the minimum of the loss function.

# MODEL : TRAINING AND TESTING

Layer	Parameters
LSTM (64)	16,896
Dense (1)	65
<b>Total Parameters</b>	<b>16,961</b>



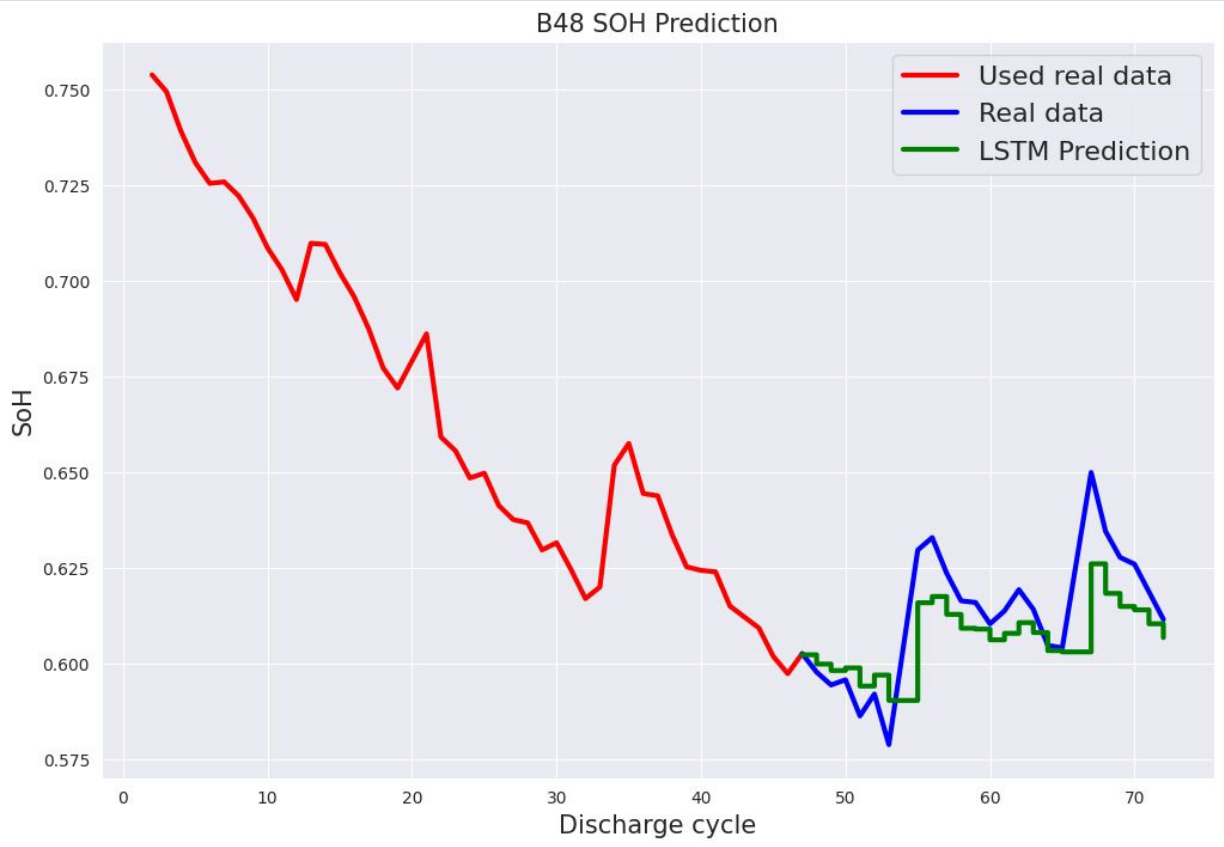
# LSTM Prediction Results (50% Data Training)



Test RMSE: 0.009  
Test MAE: 0.008( difference  
between model's predicted SOH  
and the actual SOH)



# LSTM Prediction Results (70% Data Training)



Test RMSE: 0.010  
Test MAE: 0.008

```
history = model.fit(trainX, trainY, epochs=100, batch_size=20, validation_data=(testX, testY), verbose=1, shuffle = False)
```

✓ 2m 43.2s

```
poch 1/100
22/822 ————— 3s 2ms/step - loss: 0.0471 - val_loss: 0.0109
poch 2/100
22/822 ————— 2s 2ms/step - loss: 0.0037 - val_loss: 0.0093
poch 3/100
22/822 ————— 2s 2ms/step - loss: 0.0037 - val_loss: 0.0107
poch 4/100
22/822 ————— 2s 2ms/step - loss: 0.0039 - val_loss: 0.0098
poch 5/100
22/822 ————— 3s 2ms/step - loss: 0.0037 - val_loss: 0.0129
poch 6/100
22/822 ————— 2s 2ms/step - loss: 0.0037 - val_loss: 0.0104
poch 7/100
22/822 ————— 2s 2ms/step - loss: 0.0037 - val_loss: 0.0095
poch 8/100
22/822 ————— 2s 3ms/step - loss: 0.0039 - val_loss: 0.0107
poch 9/100
22/822 ————— 2s 2ms/step - loss: 0.0037 - val_loss: 0.0091
poch 10/100
22/822 ————— 2s 2ms/step - loss: 0.0037 - val_loss: 0.0092
poch 11/100
22/822 ————— 2s 2ms/step - loss: 0.0039 - val_loss: 0.0087
poch 12/100
22/822 ————— 2s 2ms/step - loss: 0.0031 - val_loss: 0.0090
poch 13/100
22/822 ————— 2s 2ms/step - loss: 0.0035 - val_loss: 0.0088
..
poch 99/100
22/822 ————— 1s 2ms/step - loss: 0.0034 - val_loss: 0.0087
poch 100/100
22/822 ————— 1s 2ms/step - loss: 0.0032 - val_loss: 0.0084
```

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