

UNIT-2

Overview of RDBMS

Outlines...

- Relational Database Concepts
- Integrity
- Normalization

Relational Database Concept

- A database is a structured collection of data related to some real-life phenomena that we are trying to model. A relational database is one where the database structure is in the form of tables. Formally, a relation R defined over n sets $D_1; D_2; \dots; D_n$ (not necessarily distinct) is a set of n -tuples (or simply tuples) $\langle d_1; d_2; \dots; d_n \rangle$ such that $d_1 \in D_1; d_2 \in D_2; \dots; d_n \in D_n$.

Example

- As an example we use a database that models an engineering company. The entities to be modeled are the employees (EMP) and projects (PROJ). For each employee, we would like to keep track of the employee number (ENO), name (ENAME), title in the company (TITLE), salary (SAL), identification number of the project(s) the employee is working on (PNO), responsibility within the project (RESP), and duration of the assignment to the project (DUR) in months. Similarly, for each project we would like to store the project number (PNO), the project name (PNAME), and the project budget (BUDGET).

- EMP

| | | | | | | |
|-----|-------|-------|-----|-----|------|-----|
| ENO | ENAME | TITLE | SAL | PNO | RESP | DUR |
|-----|-------|-------|-----|-----|------|-----|

- PROJ

| | | |
|-----|-------|--------|
| PNO | PNAME | BUDGET |
|-----|-------|--------|

The relation schemas

- EMP(ENO, ENAME, TITLE, SAL, PNO, RESP, DUR)
- PROJ(PNO,PNAME, BUDGET)
- In relation scheme EMP, there are seven attributes: ENO, ENAME, TITLE, SAL, PNO, RESP, DUR. The values of ENO come from the domain of all valid employee numbers, say D1, the values of ENAME come from the domain of all valid names, say D2, and so on. Note that each attribute of each relation does not have to come from a distinct domain. Various attributes within a relation or from a number of relations may be defined over the same domain.

Key Relation schema

- The key of a relation scheme is the minimum non-empty subset of its attributes such that the values of the attributes comprising the key uniquely identify each tuple of the relation.
- The attributes that make up key are called prime attributes.
- The superset of a key is usually called a super key.
- Thus in our example the key of PROJ is PNO, and that of EMP is the set (ENO, PNO). Each relation has at least one key.
- Sometimes, there may be more than one possibility for the key. In such cases, each alternative is considered a candidate key, and one of the candidate keys is chosen as the primary key, which we denote by underlining.
- The number of attributes of a relation defines its degree, whereas the number of tuples of the relation defines its cardinality.

Key Relation schema

- In tabular form, the example database consists of two tables, as shown in Figure. The columns of the tables correspond to the attributes of the relations; **if there were any information entered as the rows, they would correspond to the tuples.**
- The empty table, showing the structure of the table, corresponds to the **relation schema.**
- **when the table is filled with rows, it corresponds to a relation instance.**
- Since the information within a table varies over time, many instances can be generated from one relation scheme.
- Note that from now on, the term relation refers to a relation instance. In Figure we depict instances of the **two relations** that are defined.

Example Relation Instances

EMP

| ENO | ENAME | TITLE | SAL | PNO | RESP | DUR |
|-----|-----------|-------------|-------|-----|------------|-----|
| E1 | J. Doe | Elect. Eng. | 40000 | P1 | Manager | 12 |
| E2 | M. Smith | Analyst | 34000 | P1 | Analyst | 24 |
| E2 | M. Smith | Analyst | 34000 | P2 | Analyst | 6 |
| E3 | A. Lee | Mech. Eng. | 27000 | P3 | Consultant | 10 |
| E3 | A. Lee | Mech. Eng. | 27000 | P4 | Engineer | 48 |
| E4 | J. Miller | Programmer | 24000 | P2 | Programmer | 18 |
| E5 | B. Casey | Syst. Anal. | 34000 | P2 | Manager | 24 |
| E6 | L. Chu | Elect. Eng. | 40000 | P4 | Manager | 48 |
| E7 | R. Davis | Mech. Eng. | 27000 | P3 | Engineer | 36 |
| E8 | J. Jones | Syst. Anal. | 34000 | P3 | Manager | 40 |

PROJ

| PNO | PNAME | BUDGET |
|-----|-------------------|--------|
| P1 | Instrumentation | 150000 |
| P2 | Database Develop. | 135000 |
| P3 | CAD/CAM | 250000 |
| P4 | Maintenance | 310000 |

Repetition Anomaly

- The NAME, TITLE, SAL attribute values are repeated for each project that the employee is involved in.
 - Waste of space
 - Complicates updates

EMP

| <u>ENO</u> | ENAME | TITLE | SAL | <u>PNO</u> | RESP | DUR |
|------------|-----------|-------------|-------|------------|------------|-----|
| E1 | J. Doe | Elect. Eng. | 40000 | P1 | Manager | 12 |
| E2 | M. Smith | Analyst | 34000 | P1 | Analyst | 24 |
| E2 | M. Smith | Analyst | 34000 | P2 | Analyst | 6 |
| E3 | A. Lee | Mech. Eng. | 27000 | P3 | Consultant | 10 |
| E3 | A. Lee | Mech. Eng. | 27000 | P4 | Engineer | 48 |
| E4 | J. Miller | Programmer | 24000 | P2 | Programmer | 18 |
| E5 | B. Casey | Syst. Anal. | 34000 | P2 | Manager | 24 |
| E6 | L. Chu | Elect. Eng. | 40000 | P4 | Manager | 48 |
| E7 | R. Davis | Mech. Eng. | 27000 | P3 | Engineer | 36 |
| E8 | J. Jones | Syst. Anal. | 34000 | P3 | Manager | 40 |

Update Anomaly

- If any attribute of project (say SAL of an employee) is updated, multiple tuples have to be updated to reflect the change.

EMP

| <u>ENO</u> | ENAME | TITLE | SAL | <u>PNQ</u> | RESP | DUR |
|------------|-----------|-------------|-------|------------|------------|-----|
| E1 | J. Doe | Elect. Eng. | 40000 | P1 | Manager | 12 |
| E2 | M. Smith | Analyst | 34000 | P1 | Analyst | 24 |
| E2 | M. Smith | Analyst | 34000 | P2 | Analyst | 6 |
| E3 | A. Lee | Mech. Eng. | 27000 | P3 | Consultant | 10 |
| E3 | A. Lee | Mech. Eng. | 27000 | P4 | Engineer | 48 |
| E4 | J. Miller | Programmer | 24000 | P2 | Programmer | 18 |
| E5 | B. Casey | Syst. Anal. | 34000 | P2 | Manager | 24 |
| E6 | L. Chu | Elect. Eng. | 40000 | P4 | Manager | 48 |
| E7 | R. Davis | Mech. Eng. | 27000 | P3 | Engineer | 36 |
| E8 | J. Jones | Syst. Anal. | 34000 | P3 | Manager | 40 |

Insertion Anomaly

- It may not be possible to store information about a new project until an employee is assigned to it.

EMP

| <u>ENO</u> | ENAME | TITLE | SAL | <u>PNO</u> | RESP | DUR |
|------------|-----------|-------------|-------|------------|------------|-----|
| E1 | J. Doe | Elect. Eng. | 40000 | P1 | Manager | 12 |
| E2 | M. Smith | Analyst | 34000 | P1 | Analyst | 24 |
| E2 | M. Smith | Analyst | 34000 | P2 | Analyst | 6 |
| E3 | A. Lee | Mech. Eng. | 27000 | P3 | Consultant | 10 |
| E3 | A. Lee | Mech. Eng. | 27000 | P4 | Engineer | 48 |
| E4 | J. Miller | Programmer | 24000 | P2 | Programmer | 18 |
| E5 | B. Casey | Syst. Anal. | 34000 | P2 | Manager | 24 |
| E6 | L. Chu | Elect. Eng. | 40000 | P4 | Manager | 48 |
| E7 | R. Davis | Mech. Eng. | 27000 | P3 | Engineer | 36 |
| E8 | J. Jones | Syst. Anal. | 34000 | P3 | Manager | 40 |

Deletion Anomaly

- If an engineer, who is the only employee on a project, leaves the company, his personal information cannot be deleted, or the information about that project is lost.
- May have to delete many tuples.

EMP

| <u>ENO</u> | ENAME | TITLE | SAL | <u>PNO</u> | RESP | DUR |
|------------|-----------|-------------|-------|------------|------------|-----|
| E1 | J. Doe | Elect. Eng. | 40000 | P1 | Manager | 12 |
| E2 | M. Smith | Analyst | 34000 | P1 | Analyst | 24 |
| E2 | M. Smith | Analyst | 34000 | P2 | Analyst | 6 |
| E3 | A. Lee | Mech. Eng. | 27000 | P3 | Consultant | 10 |
| E3 | A. Lee | Mech. Eng. | 27000 | P4 | Engineer | 48 |
| E4 | J. Miller | Programmer | 24000 | P2 | Programmer | 18 |
| E5 | B. Casey | Syst. Anal. | 34000 | P2 | Manager | 24 |
| E6 | L. Chu | Elect. Eng. | 40000 | P4 | Manager | 48 |
| E7 | R. Davis | Mech. Eng. | 27000 | P3 | Engineer | 36 |
| E8 | J. Jones | Syst. Anal. | 34000 | P3 | Manager | 40 |

What to do?

- Take each relation **individually** and “improve” it in terms of the desired characteristics
 - Normal forms
 - Atomic values (1NF)
 - Can be defined according to keys and dependencies.
 - Functional Dependencies (2NF, 3NF, BCNF)
 - Multivalued dependencies (4NF)
 - Normalization
 - Normalization is a process of **concept separation** which applies a top-down methodology for producing a schema by *subsequent refinements and decompositions*.
 - Do not combine unrelated sets of facts in one table; each relation should contain an independent set of facts.
 - Universal relation assumption
 - 1NF to 3NF; 1NF to BCNF

Normalization Issues

- How do we decompose a schema into a desirable normal form?
- What criteria should the decomposed schemas follow in order to preserve the semantics of the original schema?
 - Reconstructability: recover the original relation \Rightarrow no spurious joins
 - Lossless decomposition: no information loss
 - Dependency preservation: the constraints (i.e., dependencies) that hold on the original relation should be enforceable by means of the constraints (i.e., dependencies) defined on the decomposed relations.
- What happens to queries?
 - Processing time may increase due to joins
 - Denormalization

Functional Dependence

- Given relation R defined over $U = \{A_1, A_2, \dots, A_n\}$ where $X \subseteq U, Y \subseteq U$. If, for **all** pairs of tuples t_1 and t_2 in **any** legal instance of relation scheme R ,

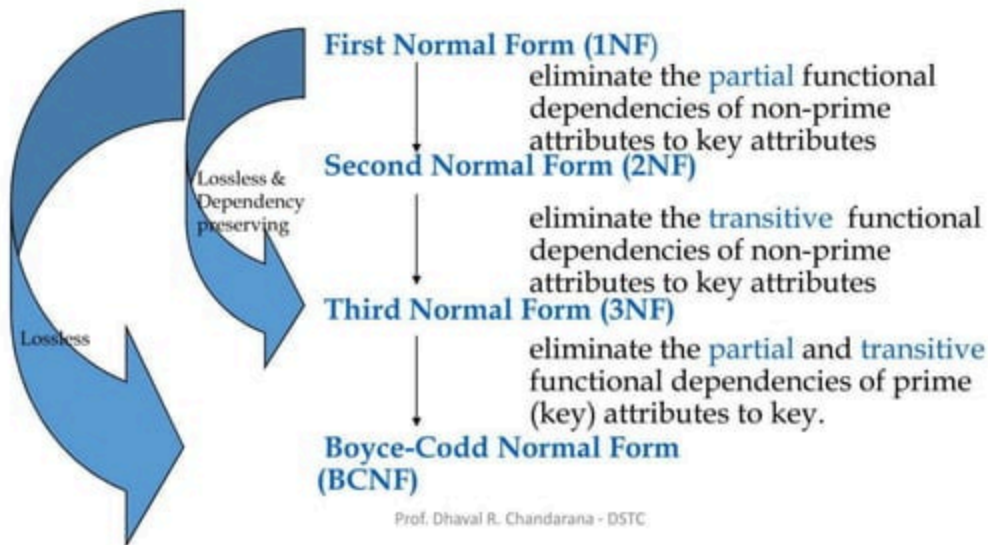
$$t_1[X] = t_2[X] \Rightarrow t_1[Y] = t_2[Y],$$

then the functional dependency $X \rightarrow Y$ holds in R .

- Example
 - In relation EMP
 - $(ENO, PNO) \rightarrow (ENAME, TITLE, SAL, DUR, RESP)$
 - In relation PROJ
 - $PNO \rightarrow (PNAME, BUDGET)$

Normal Forms Based on FDs

1NF eliminates the relations within relations or relations as attributes of tuples.



Normalized Relations – Example

EMP

| ENO | ENAME | TITLE |
|-----|-----------|-------------|
| E1 | J. Doe | Elect. Eng |
| E2 | M. Smith | Syst. Anal. |
| E3 | A. Lee | Mech. Eng. |
| E4 | J. Miller | Programmer |
| E5 | B. Casey | Syst. Anal. |
| E6 | L. Chu | Elect. Eng. |
| E7 | R. Davis | Mech. Eng. |
| E8 | J. Jones | Syst. Anal. |

ASG

| ENO | PNO | RESP | DUR |
|-----|-----|------------|-----|
| E1 | P1 | Manager | 12 |
| E2 | P1 | Analyst | 24 |
| E2 | P2 | Analyst | 6 |
| E3 | P3 | Consultant | 10 |
| E3 | P4 | Engineer | 48 |
| E4 | P2 | Programmer | 18 |
| E5 | P2 | Manager | 24 |
| E6 | P4 | Manager | 48 |
| E7 | P3 | Engineer | 36 |
| E8 | P3 | Manager | 40 |

PROJ

| PNO | PNAME | BUDGET |
|-----|-------------------|--------|
| P1 | Instrumentation | 150000 |
| P2 | Database Develop. | 135000 |
| P3 | CAD/CAM | 250000 |
| P4 | Maintenance | 310000 |

PAY

| TITLE | SAL |
|-------------|-------|
| Elect. Eng. | 40000 |
| Syst. Anal. | 34000 |
| Mech. Eng. | 27000 |
| Programmer | 24000 |

Relational Algebra

Specify how to obtain the result using a set of operators

Form

$$\begin{array}{ccc} \langle \textit{Operator} \rangle_{\langle \textit{parameters} \rangle} \langle \textit{Operands} \rangle & \rightarrow & \langle \textit{Result} \rangle \\ \downarrow & & \downarrow \\ \text{Relation (s)} & & \text{Relation} \end{array}$$

Relational Algebra Operators

- Fundamental
 - Selection
 - Projection
 - Union
 - Set difference
 - Cartesian product
- Additional
 - Intersection
 - θ -join
 - Natural join
 - Semijoin
 - Division
- Union compatibility
 - Same degree
 - Corresponding attributes defined over the same domain

Selection

- Produces a horizontal subset of the operand relation
- General form

$$\sigma_F(R) = \{t \mid t \in R \text{ and } F(t) \text{ is true}\}$$

where

- R is a relation, t is a tuple variable
- F is a formula consisting of
 - operands that are constants or attributes
 - arithmetic comparison operators
 $<, >, =, \neq, \leq, \geq$
 - logical operators
 \wedge, \vee, \neg

Selection Example

EMP

| ENO | ENAME | TITLE |
|-----|-----------|-------------|
| E1 | J. Doe | Elect. Eng. |
| E2 | M. Smith | Syst. Anal. |
| E3 | A. Lee | Mech. Eng. |
| E4 | J. Miller | Programmer |
| E5 | B. Casey | Syst. Anal. |
| E6 | L. Chu | Elect. Eng. |
| E7 | R. Davis | Mech. Eng. |
| E8 | J. Jones | Syst. Anal. |

$\sigma_{\text{TITLE}=\text{'Elect. Eng.'}}(\text{EMP})$

| ENO | ENAME | TITLE |
|-----|--------|-------------|
| E1 | J. Doe | Elect. Eng. |
| E6 | L. Chu | Elect. Eng. |

Projection

- Produces a vertical slice of a relation
- General form

$$\Pi_{A_1, \dots, A_n}(R) = \{t[A_1, \dots, A_n] \mid t \in R\}$$

where

- R is a relation, t is a tuple variable
- $\{A_1, \dots, A_n\}$ is a subset of the attributes of R over which the projection will be performed
- Note: projection can generate duplicate tuples. Commercial systems (and SQL) allow this and provide
 - Projection with duplicate elimination
 - Projection without duplicate elimination

Projection Example

PROJ

| PNO | PNAME | BUDGET |
|-----|-------------------|--------|
| P1 | Instrumentation | 150000 |
| P2 | Database Develop. | 135000 |
| P3 | CAD/CAM | 250000 |
| P4 | Maintenance | 310000 |

$\Pi_{\text{PNO}, \text{BUDGET}}(\text{PROJ})$

| PNO | BUDGET |
|-----|--------|
| P1 | 150000 |
| P2 | 135000 |
| P3 | 250000 |
| P4 | 310000 |

Union

- Similar to set union
- General form

$$R \cup S = \{t \mid t \in R \text{ or } t \in S\}$$

where R, S are relations, t is a tuple variable

- Result contains tuples that are in R or in S , but not both (duplicates removed)
- R, S should be union-compatible

Set Difference

- General Form

$$R - S = \{t \mid t \in R \text{ and } t \notin S\}$$

where R and S are relations, t is a tuple variable

- Result contains all tuples that are in R , but not in S .
- $R - S \neq S - R$
- R, S union-compatible

Cartesian (Cross) Product

- Given relations
 - R of degree k_1 , cardinality n_1
 - S of degree k_2 , cardinality n_2
- Cartesian (cross) product:

$$R \times S = \{t[A_1, \dots, A_{k_1}, A_{k_1+1}, \dots, A_{k_1+k_2}] \mid t[A_1, \dots, A_{k_1}] \in R \text{ and } t[A_{k_1+1}, \dots, A_{k_1+k_2}] \in S\}$$

The result of $R \cdot S$ is a relation of degree $(k_1 + k_2)$ and consists of all $(n_1 \cdot n_2)$ -tuples where each tuple is a concatenation of one tuple of R with one tuple of S .

Cartesian Product Example

EMP

| ENO | ENAME | TITLE |
|-----|-----------|-------------|
| E1 | J. Doe | Elect. Eng. |
| E2 | M. Smith | Syst. Anal. |
| E3 | A. Lee | Mech. Eng. |
| E4 | J. Miller | Programmer |
| E5 | B. Casey | Syst. Anal. |
| E6 | L. Chu | Elect. Eng. |
| E7 | R. Davis | Mech. Eng. |
| E8 | J. Jones | Syst. Anal. |

PAY

| TITLE | SALARY |
|-------------|--------|
| Elect. Eng. | 55000 |
| Syst. Anal. | 70000 |
| Mech. Eng. | 45000 |
| Programmer | 60000 |

EMP × PAY

| ENO | ENAME | EMP.TITLE | PAY.TITLE | SALARY |
|-----|----------|-------------|-------------|--------|
| E1 | J. Doe | Elect. Eng. | Elect. Eng. | 55000 |
| E1 | J. Doe | Elect. Eng. | Syst. Anal. | 70000 |
| E1 | J. Doe | Elect. Eng. | Mech. Eng. | 45000 |
| E1 | J. Doe | Elect. Eng. | Programmer | 60000 |
| E2 | M. Smith | Syst. Anal. | Elect. Eng. | 55000 |
| E2 | M. Smith | Syst. Anal. | Syst. Anal. | 70000 |
| E2 | M. Smith | Syst. Anal. | Mech. Eng. | 45000 |
| E2 | M. Smith | Syst. Anal. | Programmer | 60000 |
| E3 | A. Lee | Mech. Eng. | Elect. Eng. | 55000 |
| E3 | A. Lee | Mech. Eng. | Syst. Anal. | 70000 |
| E3 | A. Lee | Mech. Eng. | Mech. Eng. | 45000 |
| E3 | A. Lee | Mech. Eng. | Programmer | 60000 |
| E8 | J. Jones | Syst. Anal. | Elect. Eng. | 55000 |
| E8 | J. Jones | Syst. Anal. | Syst. Anal. | 70000 |
| E8 | J. Jones | Syst. Anal. | Mech. Eng. | 45000 |
| E8 | J. Jones | Syst. Anal. | Programmer | 60000 |

Intersection

- Typical set intersection

$$\begin{aligned} R \cap S &= \{t \mid t \in R \text{ and } t \in S\} \\ &= R - (R - S) \end{aligned}$$

- R, S union-compatible

θ -Join

- General form

$$R \bowtie_{F(R.A_i, S.B_j)} S = \{t[A_1, \dots, A_n, B_1, \dots, B_m] \mid \\ t[A_1, \dots, A_n] \in R \text{ and } t[B_1, \dots, B_m] \in S \\ \text{and } F(R.A_i, S.B_j) \text{ is true}\}$$

where

- R, S are relations, t is a tuple variable
- $F(R.A_i, S.B_j)$ is a formula defined as that of selection.
- A derivative of Cartesian product
 - $R \bowtie_F S = \sigma_F(R \times S)$

Join Example

EMP

| ENO | ENAME | TITLE |
|-----|-----------|-------------|
| E1 | J. Doe | Elect. Eng. |
| E2 | M. Smith | Syst. Anal. |
| E3 | A. Lee | Mech. Eng. |
| E4 | J. Miller | Programmer |
| E5 | B. Casey | Syst. Anal. |
| E6 | L. Chu | Elect. Eng. |
| E7 | R. Davis | Mech. Eng. |
| E8 | J. Jones | Syst. Anal. |
| E9 | A. Hsu | Programmer |
| E10 | T. Wong | Syst. Anal. |

(a)

EMP ⋈_{EMP.ENO=ASG.ENO} ASG

| ENO | ENAME | TITLE | PNO | RESP | DUR |
|-----|-----------|-------------|-----|------------|-----|
| E1 | J. Doe | Elect. Eng. | P1 | Manager | 12 |
| E2 | M. Smith | Syst. Anal. | P1 | Analyst | 12 |
| E2 | M. Smith | Syst. Anal. | P2 | Analyst | 12 |
| E3 | A. Lee | Mech. Eng. | P3 | Consultant | 12 |
| E3 | A. Lee | Mech. Eng. | P4 | Engineer | 12 |
| E4 | J. Miller | Programmer | P2 | Programmer | 12 |
| E5 | J. Miller | Syst. Anal. | P2 | Manager | 12 |
| E6 | L. Chu | Elect. Eng. | P4 | Manager | 12 |
| E7 | R. Davis | Mech. Eng. | P3 | Engineer | 12 |
| E8 | J. Jones | Syst. Anal. | P3 | Manager | 12 |

(b)

Types of Join

- Equi-join

- The formula F only contains equality
- $R \bowtie_{R.A=S.B} S$

- Natural join

- Equi-join of two relations R and S over an attribute (or attributes) common to both R and S and projecting out one copy of those attributes
- $R \bowtie S = \Pi_{R \cup S} \sigma_F(R \times S)$

Natural Join Example

EMP

| ENO | ENAME | TITLE |
|-----|-----------|-------------|
| E1 | J. Doe | Elect. Eng |
| E2 | M. Smith | Syst. Anal. |
| E3 | A. Lee | Mech. Eng. |
| E4 | J. Miller | Programmer |
| E5 | B. Casey | Syst. Anal. |
| E6 | L. Chu | Elect. Eng. |
| E7 | R. Davis | Mech. Eng. |
| E8 | J. Jones | Syst. Anal. |

PAY

| TITLE | SALARY |
|-------------|--------|
| Elect. Eng. | 55000 |
| Syst. Anal. | 70000 |
| Mech. Eng. | 45000 |
| Programmer | 60000 |

EMP ⋈ PAY

| ENO | ENAME | TITLE | SALARY |
|-----|-----------|-------------|--------|
| E1 | J. Doe | Elect. Eng. | 55000 |
| E2 | M. Smith | Analyst | 70000 |
| E3 | A. Lee | Mech. Eng. | 45000 |
| E4 | J. Miller | Programmer | 60000 |
| E5 | B. Casey | Syst. Anal. | 70000 |
| E6 | L. Chu | Elect. Eng. | 55000 |
| E7 | R. Davis | Mech. Eng. | 45000 |
| E8 | J. Jones | Syst. Anal. | 70000 |

Join is over the common attribute TITLE

Types of Join

- Outer-Join

- Ensures that tuples from one or both relations that do not satisfy the join condition still appear in the final result with other relation's attribute values set to NULL



- Left outer join



- Right outer join



- Full outer join

Outer Join Example

- Left outer join

EMP ⋈_{ENO} ASG

| ENO | ENAME | TITLE | PNO | RESP | DUR |
|-----|-----------|-------------|------|------------|------|
| E1 | J. Doe | Elect. Eng. | P1 | Manager | 12 |
| E2 | M. Smith | Syst. Anal. | P1 | Analyst | 12 |
| E2 | M. Smith | Syst. Anal. | P2 | Analyst | 12 |
| E3 | A. Lee | Mech. Eng. | P3 | Consultant | 12 |
| E3 | A. Lee | Mech. Eng. | P4 | Engineer | 12 |
| E4 | J. Miller | Programmer | P2 | Programmer | 12 |
| E5 | J. Miller | Syst. Anal. | P2 | Manager | 12 |
| E6 | L. Chu | Elect. Eng. | P4 | Manager | 12 |
| E7 | R. Davis | Mech. Eng. | P3 | Engineer | 12 |
| E8 | J. Jones | Syst. Anal. | P3 | Manager | 12 |
| E9 | A. Hsu | Programmer | Null | Null | Null |
| E10 | T. Wong | Syst. Anal. | Null | Null | Null |

Semijoin

- Derivation

$$R \bowtie_F S = \Pi_A(R \bowtie_F S) = \Pi_A(R) \bowtie \Pi_{A \cap B}(S) = R \bowtie_F \Pi_{A \cap B}(S)$$

where

- R, S are relations
- A is a set of attributes

Semijoin Example

EMP ⋈_{EMP.TITLE=PAY.TITLE} PAY

| ENO | ENAME | TITLE |
|-----|-----------|-------------|
| E1 | J. Doe | Elect. Eng. |
| E2 | M. Smith | Analyst |
| E3 | A. Lee | Mech. Eng. |
| E4 | J. Miller | Programmer |
| E5 | B. Casey | Syst. Anal. |
| E6 | L. Chu | Elect. Eng. |
| E7 | R. Davis | Mech. Eng. |
| E8 | J. Jones | Syst. Anal. |

Division (Quotient)

- Given relations

- R of degree k_1 ($R = \{A_1, \dots, A_{k_1}\}$)
- S of degree k_2 ($S = \{B_1, \dots, B_{k_2}\}$)

Let $A = \{A_1, \dots, A_{k_1}\}$ [i.e., $R(A)$] and $B = \{B_1, \dots, B_{k_2}\}$ [i.e., $S(B)$] and $B \subseteq A$.

Then, $T = R \div S$ gives T of degree $k_1 - k_2$ [i.e., $T(Y)$ where $Y = A - B$] such that for a tuple t to appear in T , the values in t must appear in R in combination with *every tuple* in S .

- Derivation

$$R \div S = \Pi_Y(R) - \Pi_Y((\Pi_Y(R) \times S) - R)$$

Division Example

ASG'

| ENO | PNO | PNAME | BUDGET |
|-----|-----|-------------------|--------|
| E1 | P1 | Instrumentation | 150000 |
| E2 | P1 | Instrumentation | 150000 |
| E2 | P2 | Database Develop. | 135000 |
| E3 | P3 | CAD/CAM | 250000 |
| E3 | P4 | Maintenance | 310000 |
| E4 | P2 | Database Develop. | 135000 |
| E5 | P2 | Database Develop. | 135000 |
| E6 | P4 | Maintenance | 310000 |
| E7 | P3 | CAD/CAM | 250000 |
| E8 | P3 | CAD/CAM | 250000 |

PROJ'

| PNO | PNAME | BUDGET |
|-----|-------------|--------|
| P3 | CAD/CAM | 250000 |
| P4 | Maintenance | 310000 |

(ASG' \div PROJ')

| |
|-----|
| ENO |
| E3 |

Relational Calculus

- Specify the properties that the result should hold
- Tuple relational calculus
- Domain relational calculus

Tuple Relational Calculus

- Query of the form $\{t \mid F\{t\}\}$ where
 - t is a tuple variable
 - F is a well-formed formula
- Atomic formula
 - Tuple-variable membership expressions
 - $R.t$ or $R(t)$: tuple t belongs to relation R
 - Conditions
 - $s[A] \theta t[B]$; s and t are tuple variables, A and B are components of s and t , respectively, $\theta \in \{<, >, =, \neq, \leq, \geq\}$; e.g., $s[\text{SAL}] > t[\text{SAL}]$
 - $s[A] \theta c$; s , A , and θ as defined above, c is a constant; e.g., $s[\text{ENAME}] = \text{'Smith'}$
- SQL is an example of tuple relational calculus (at least in its simple form)

Domain Relational Calculus

- Query of the form $x_1, x_2, \dots, x_n \mid F(x_1, x_2, \dots, x_n)$ where
 - F is a well-formed formula in which x_1, x_2, \dots, x_n are the free variables
- QBE is an example

| EMP | ENO | ENAME | TITLE |
|-----|-----------|-------|-------|
| | <u>E2</u> | P. | |

| ASG | ENO | PNO | RESP | DUR |
|-----|-----------|-----------|------|-----|
| | <u>E2</u> | <u>P3</u> | | |

| PROJ | PNO | PNAME | BUDGET |
|------|-----------|---------|--------|
| | <u>P3</u> | CAD/CAM | |

INTEGRITY RULES

- Integrity rules are constraints that define consistent state of the database. They are usually expressed as assertions. Integrity constraints can be structural or behavioral.
- Structural constraints are inherent to the data model in the sense that they captured information on data relationships that cannot be modeled directly.
- Behavioral constraints permit the capturing of the semantics of the applications.
- The dependencies discussed in the preceding section are behavioral constraints.
- According to the two minimal structural constraints of the relational model are the **entity rule** and **referential integrity rules**.

INTEGRITY RULES

- By definition, any relation has a primary key. The entity rule dictates that each attribute of the key is no null. In Example attribute PNO of relation PROJ and attributes ENO,PNO of relation EMP cannot have null values. This constraint is necessary to enforce the fact that keys are unique.
- **Referential integrity is useful for capturing relationships between objects that the relational model cannot represent.**
- Referential integrity involves two relation is the key of another relation.
- In example there can be referential integrity constraint between relation PROJ and EMP on attribute PNO.
- This rules prescribe that each employee belong to at least one existing project.