

Rendering algorithms

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Rasterization vs Ray tracing

For each primitive

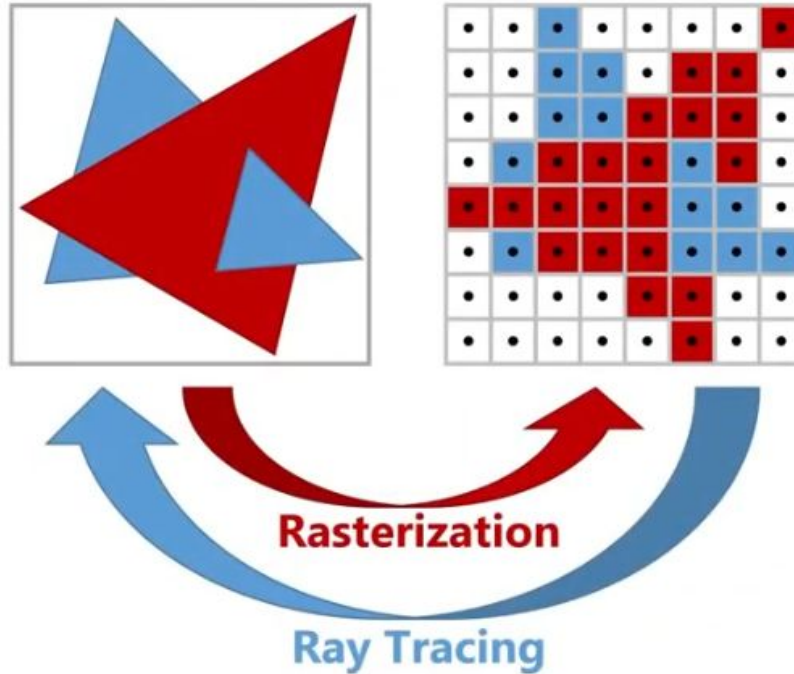
Find the pixel which it maps to

For each pixel

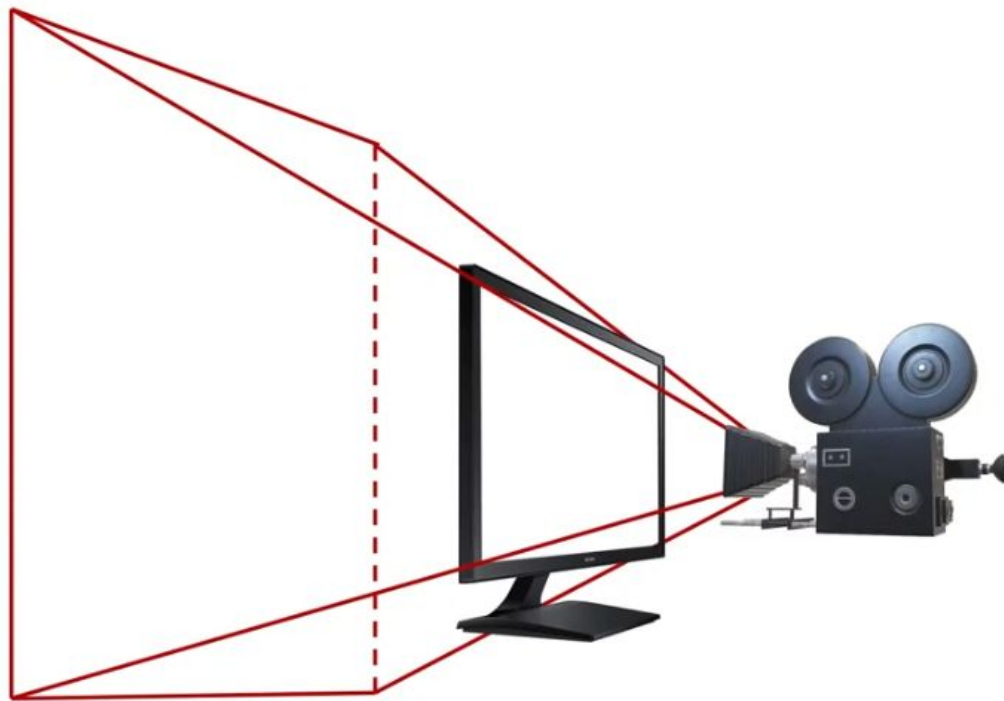
Find all the primitive which contributes to that pixel

If objects are opaque, find the closest primitive

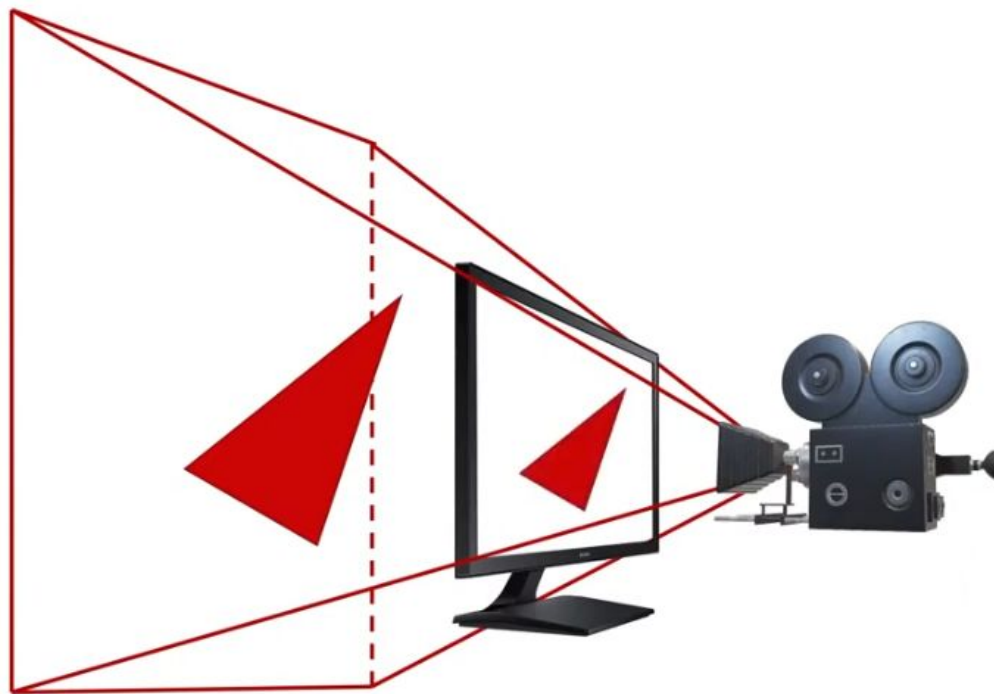
Rasterization vs Ray tracing



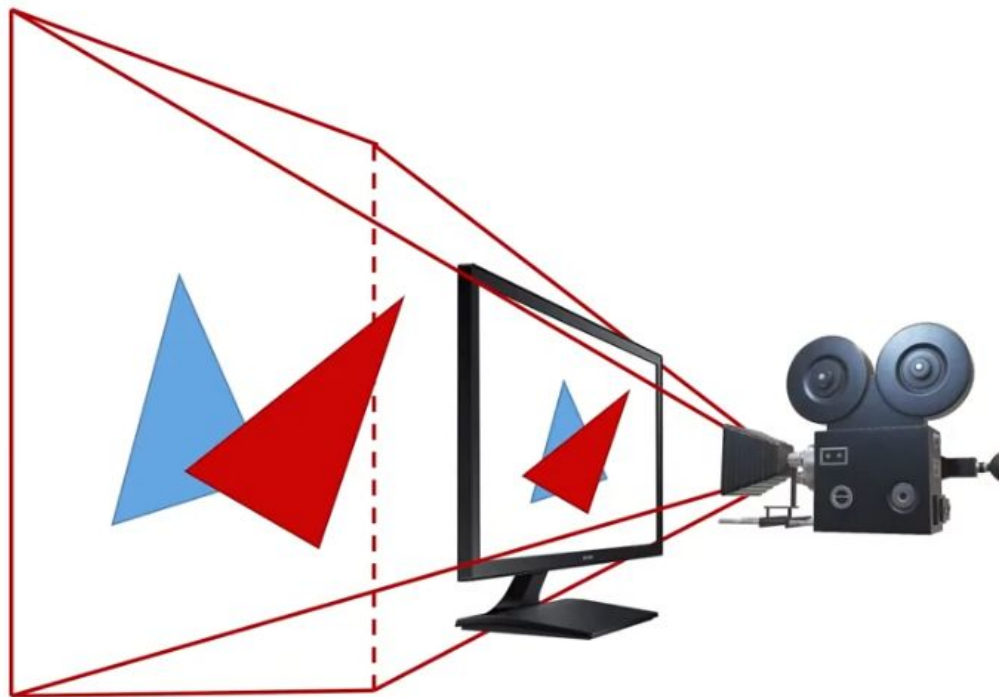
Ray tracing



Ray tracing



Ray tracing



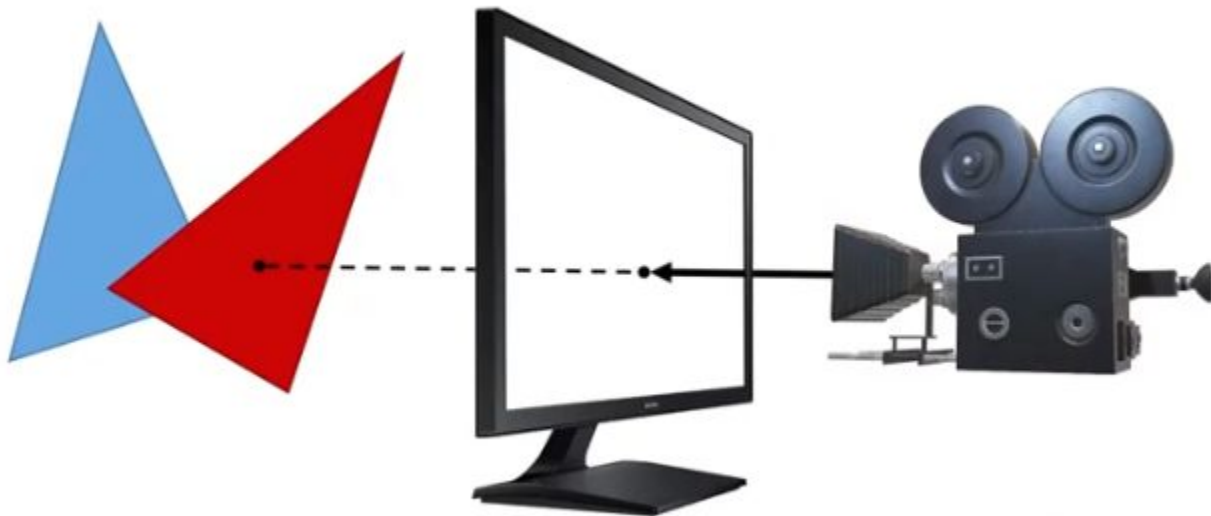
Ray tracing



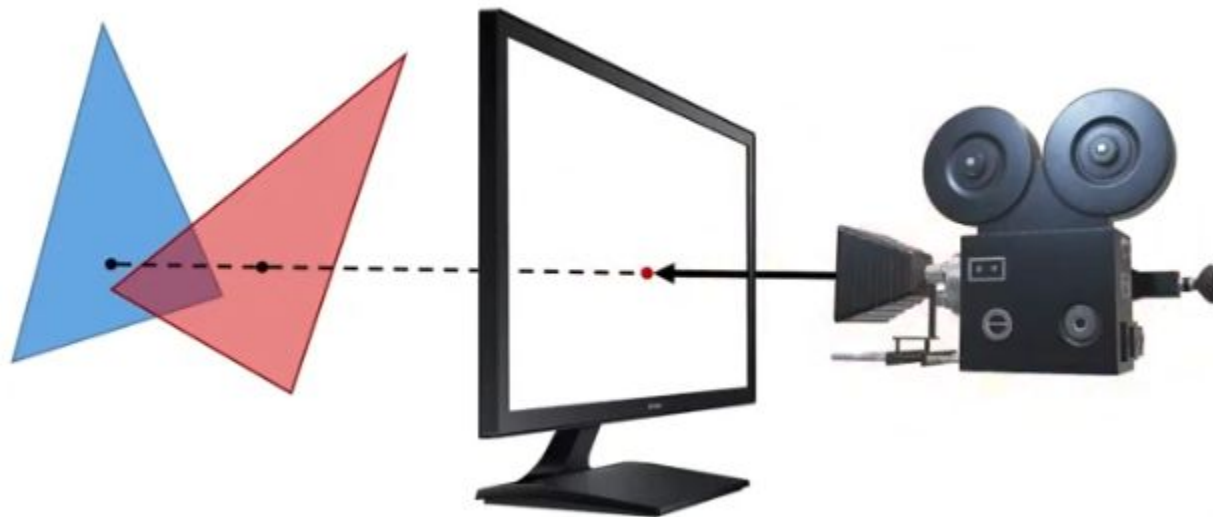
Ray tracing



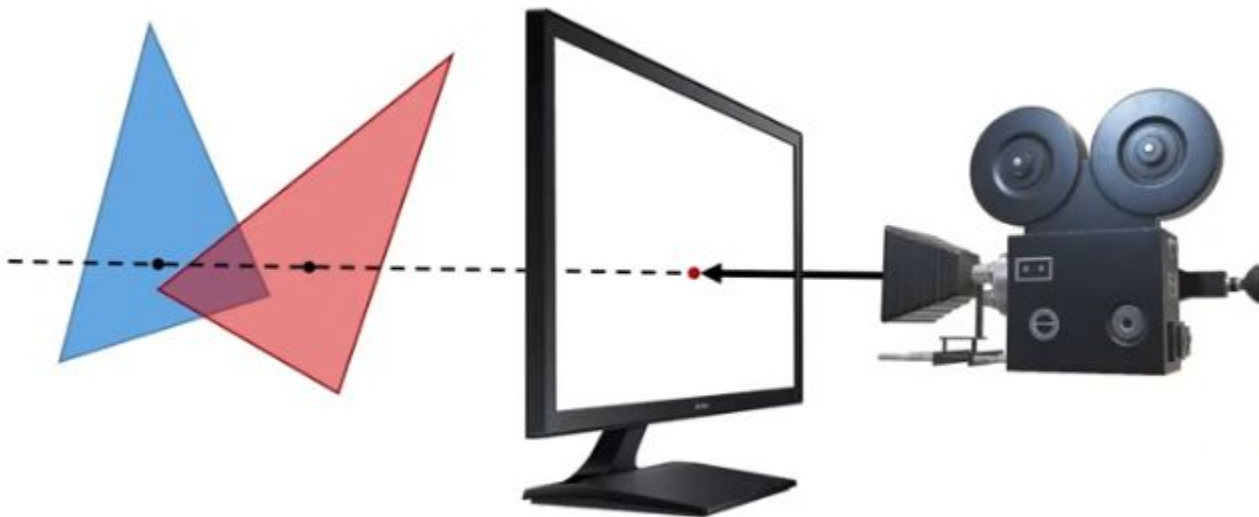
Ray tracing



Ray tracing



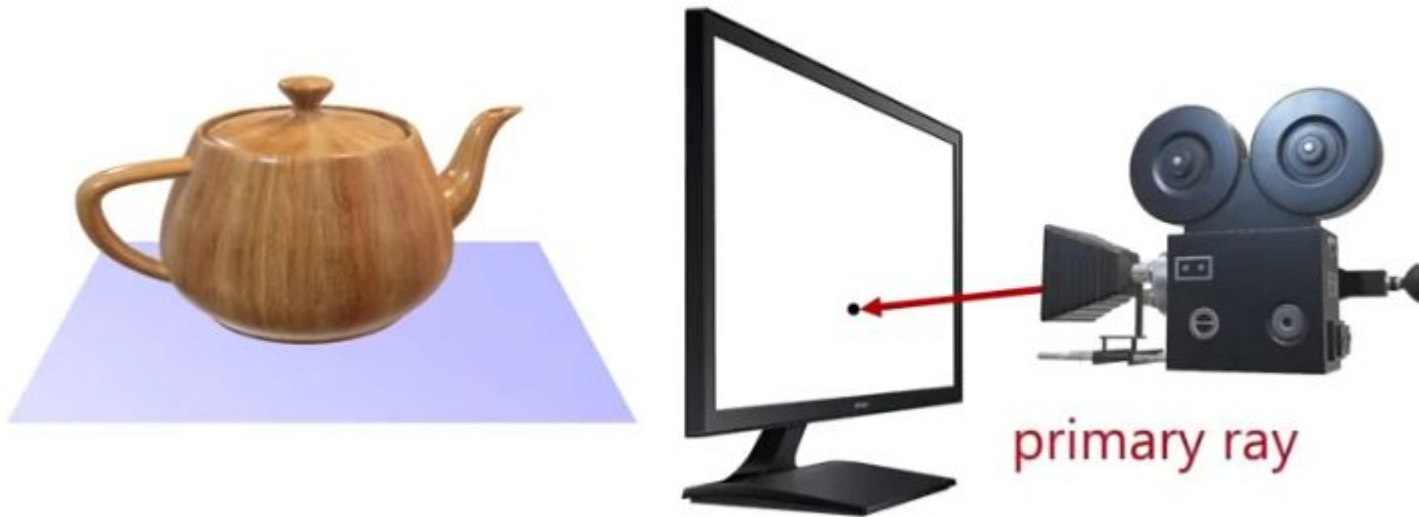
Ray tracing



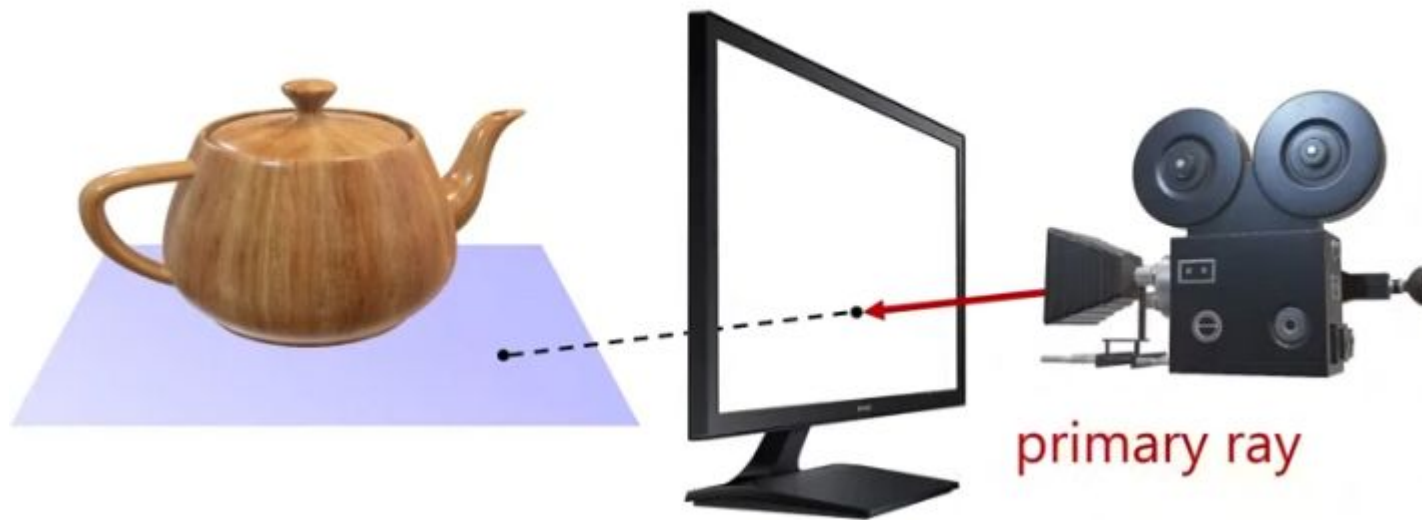
Ray tracing



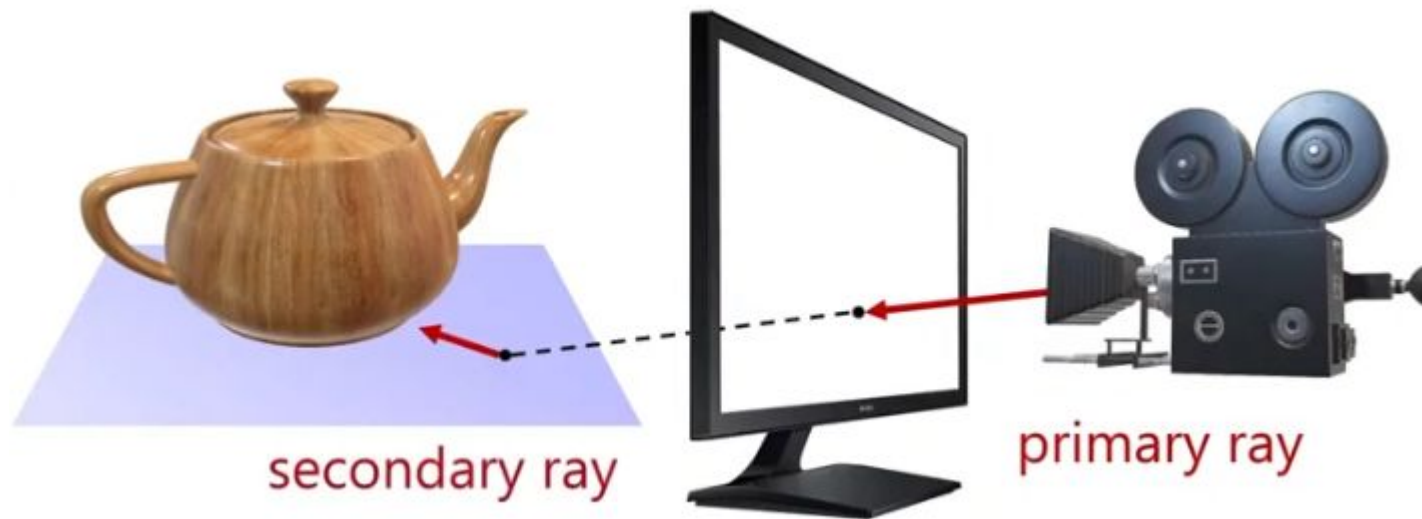
Ray tracing



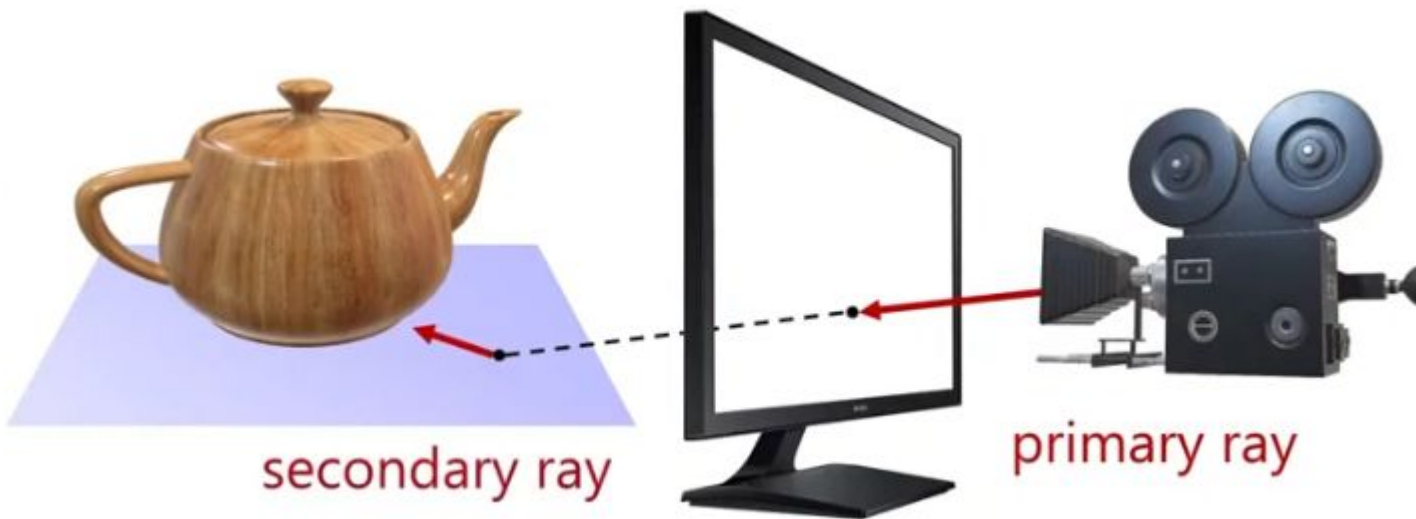
Ray tracing



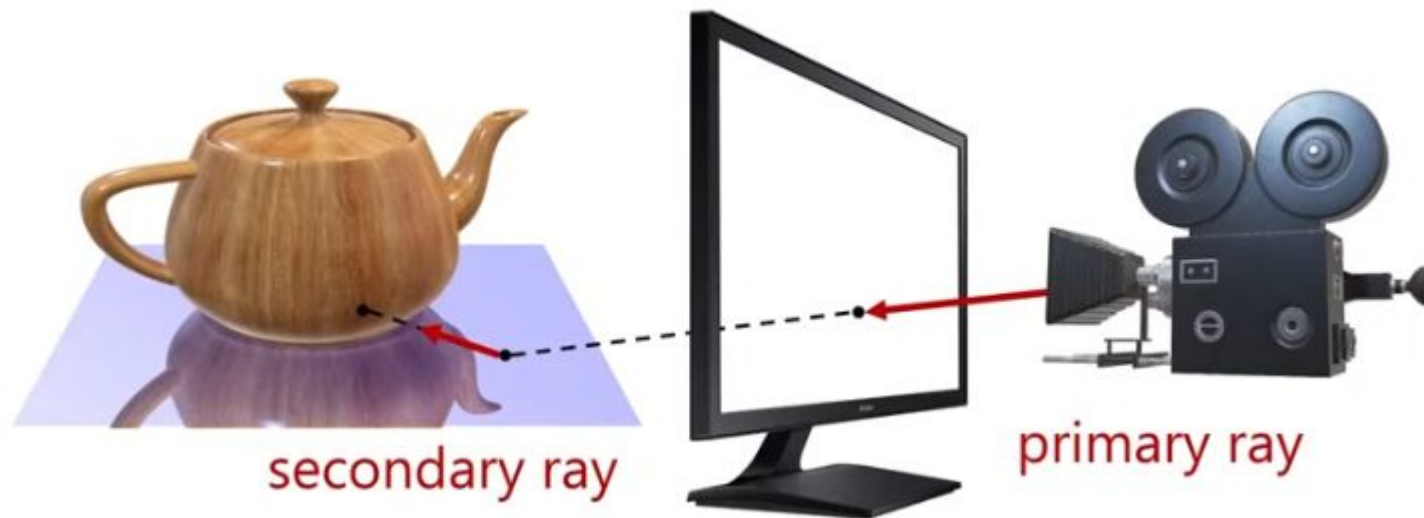
Ray tracing



Ray tracing



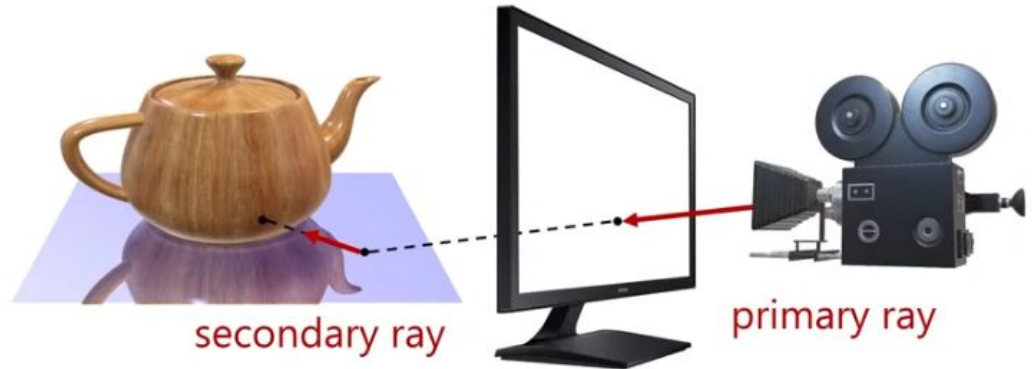
Ray tracing



Ray tracing

Secondary rays handle

1. Shadows
2. Reflection
3. Refraction
4. Realistic illumination
5. ...



Rasterization vs Ray tracing

For each primitive

Find the pixel which it maps to

Fast

Linear memory access

Linear complexity

For each pixel

Find all the primitive which contributes to that pixel

If objects are opaque, find the closest primitive

Slow

Random memory access

Logarithmic complexity

Rasterization vs Ray tracing

Combining the two

Rasterization

Visibility (Primary function of a rendering algorithm)

Ray tracing

Secondary functions like

Shadows etc

Ray tracing

Software

On CPU

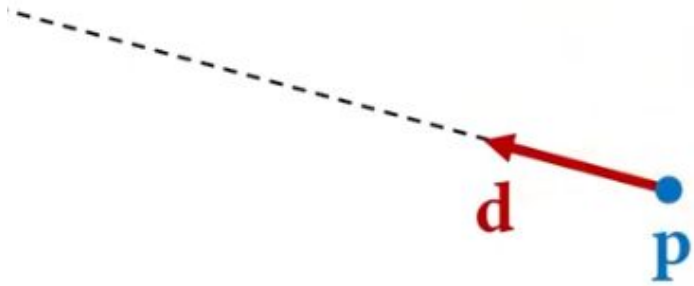
On GPU

On hardware

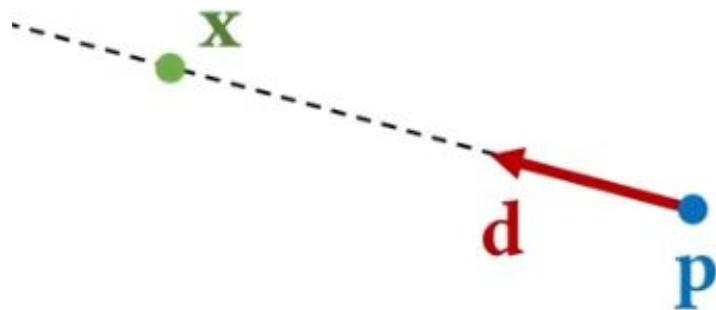
On GPU

On special hardware

How

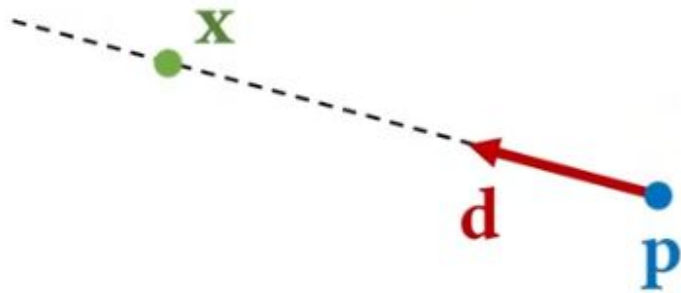


How



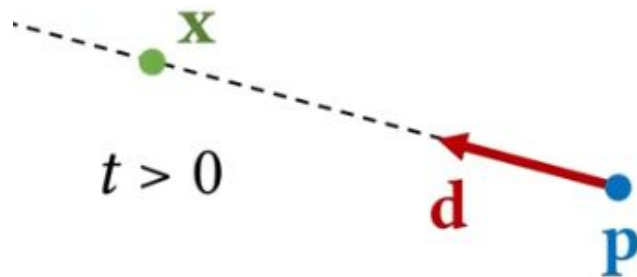
How

$$\mathbf{x} = \mathbf{p} + t \mathbf{d}$$



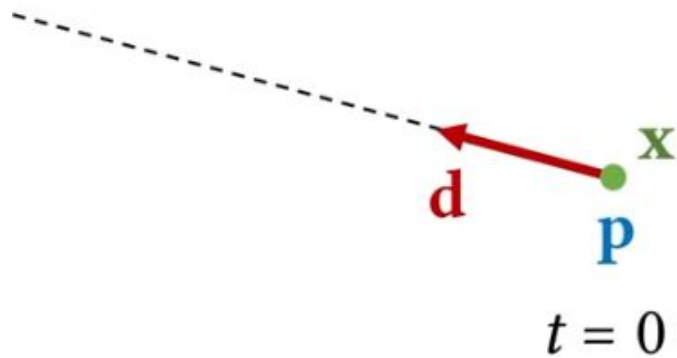
How

$$\mathbf{x} = \mathbf{p} + t \mathbf{d}$$



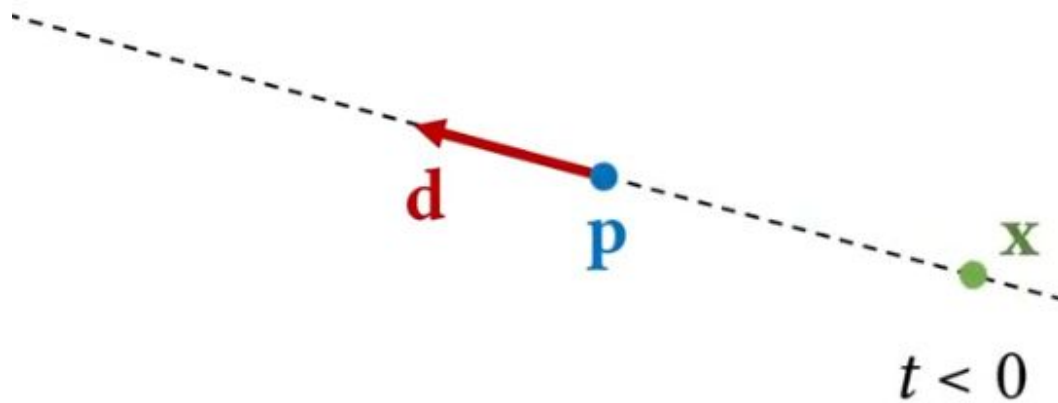
How

$$\mathbf{x} = \mathbf{p} + t \mathbf{d}$$



How

$$\mathbf{x} = \mathbf{p} + t \mathbf{d}$$



How

Implicit Surface:

$$f(\mathbf{x}) = 0$$

$$\mathbf{x} = \mathbf{p} + t \mathbf{d}$$

How

Implicit Surface:

$$f(\mathbf{p} + t \mathbf{d}) = 0$$

How

Implicit Surface:

$$f(\mathbf{p} + t \mathbf{d}) = 0$$

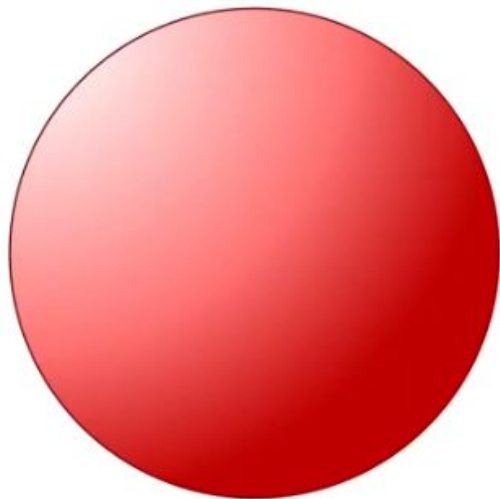
$\exists t$  **Hit!**

$$f(\mathbf{p} + t \mathbf{d}) \neq 0$$

$\forall t$  **No Hit!**

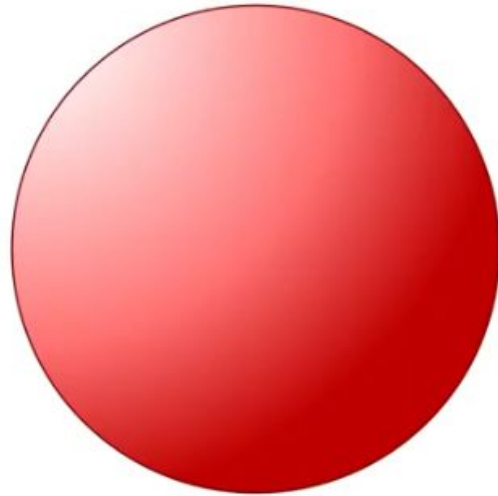
How

$$f(\mathbf{x}) = 0$$



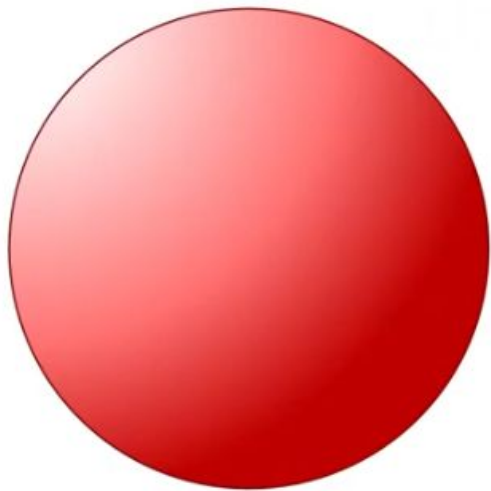
How

$$f(\mathbf{x}) = x^2 + y^2 + z^2 - r^2 = 0$$



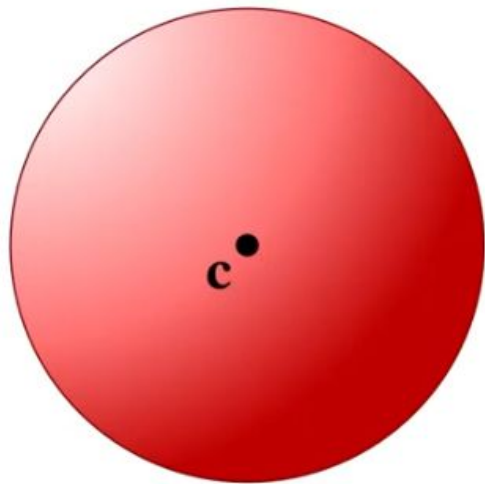
How

$$f(\mathbf{x}) = \mathbf{x} \cdot \mathbf{x} - r^2 = 0$$



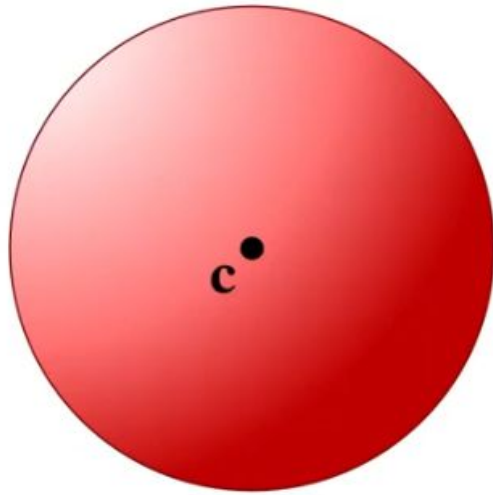
How

$$f(\mathbf{x}) = \mathbf{x} \cdot \mathbf{x} - r^2 = 0$$



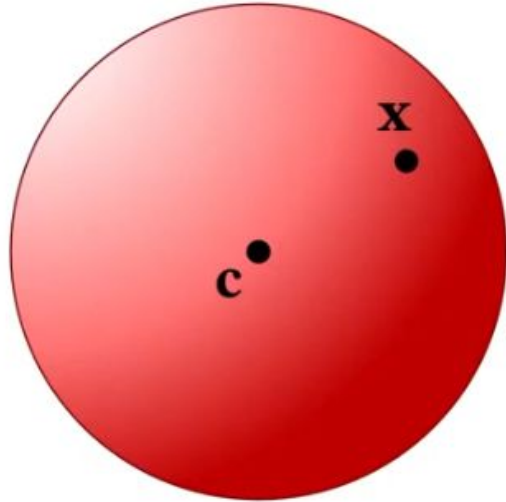
How

$$f(\mathbf{x}) = (\mathbf{x} - \mathbf{c}) \cdot (\mathbf{x} - \mathbf{c}) - r^2 = 0$$



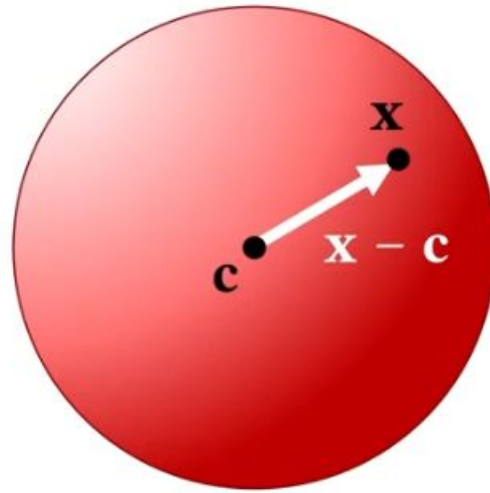
How

$$f(\mathbf{x}) = (\mathbf{x} - \mathbf{c}) \cdot (\mathbf{x} - \mathbf{c}) - r^2 = 0$$



How

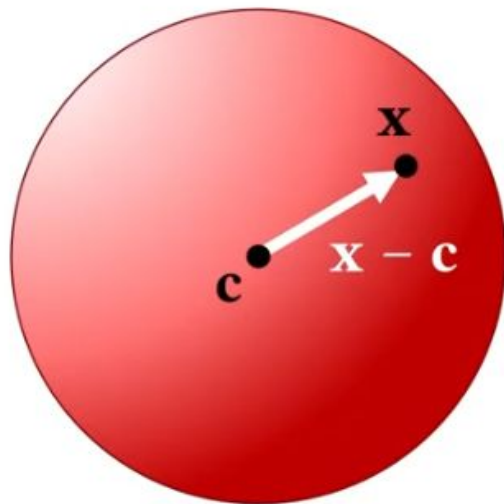
$$f(\mathbf{x}) = (\mathbf{x} - \mathbf{c}) \cdot (\mathbf{x} - \mathbf{c}) - r^2 = 0$$



$$|\mathbf{x} - \mathbf{c}| = r$$

How

$$f(\mathbf{x}) = (\mathbf{x} - \mathbf{c}) \cdot (\mathbf{x} - \mathbf{c}) - r^2 = 0$$



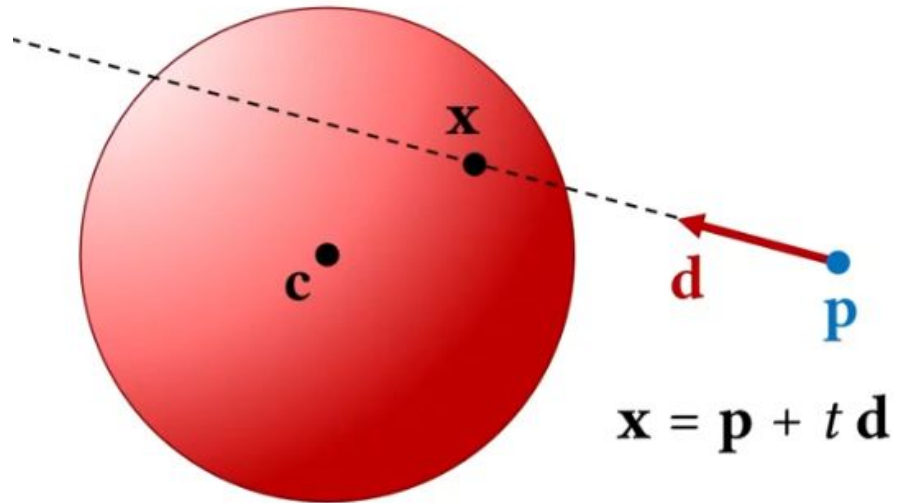
$$|\mathbf{x} - \mathbf{c}| = r$$

$$\sqrt{(\mathbf{x} - \mathbf{c}) \cdot (\mathbf{x} - \mathbf{c})} = r$$

$$(\mathbf{x} - \mathbf{c}) \cdot (\mathbf{x} - \mathbf{c}) = r^2$$

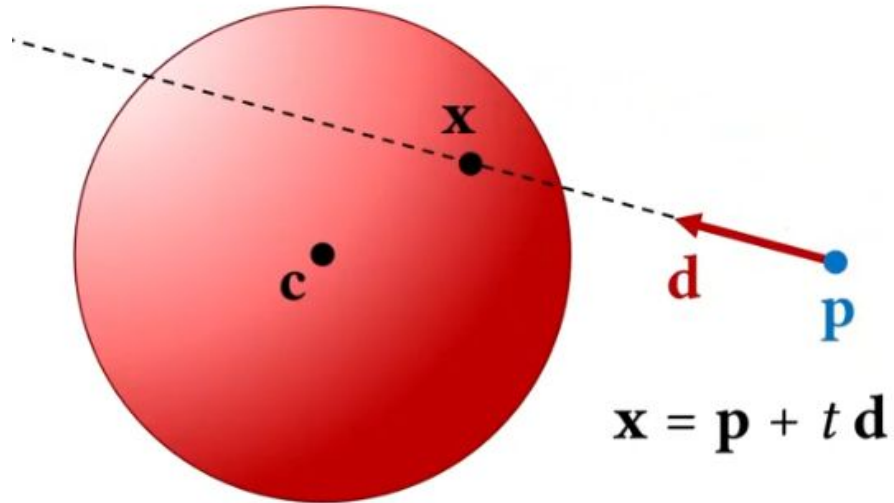
How

$$f(\mathbf{x}) = (\mathbf{x} - \mathbf{c}) \cdot (\mathbf{x} - \mathbf{c}) - r^2 = 0$$



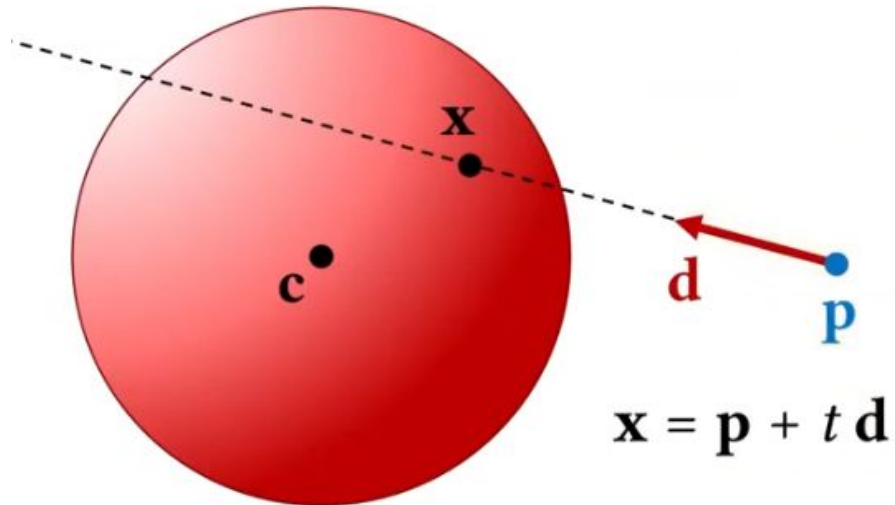
How

$$(\mathbf{p} + t \mathbf{d} - \mathbf{c}) \cdot (\mathbf{p} + t \mathbf{d} - \mathbf{c}) - r^2 = 0$$



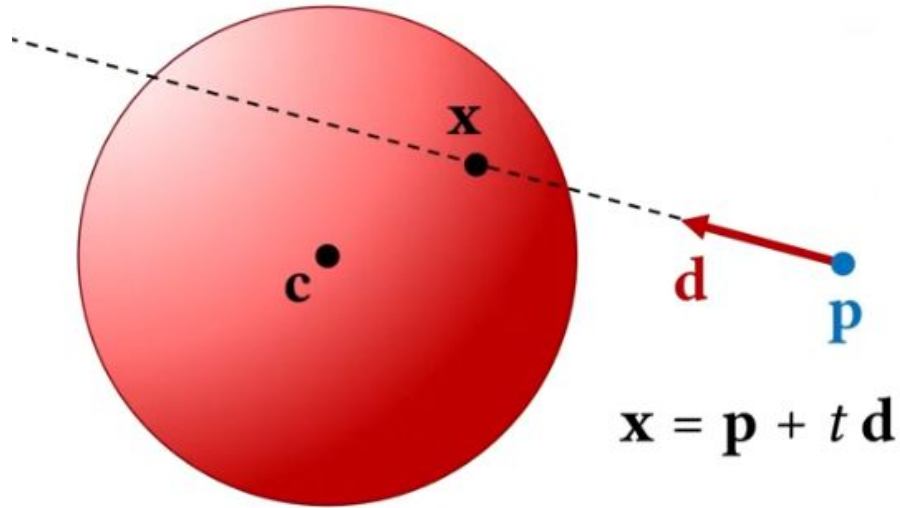
How

$$(\mathbf{p} - \mathbf{c} + t \mathbf{d}) \cdot (\mathbf{p} - \mathbf{c} + t \mathbf{d}) - r^2 = 0$$



How

$$(\mathbf{d} \cdot \mathbf{d})t^2 + 2\mathbf{d} \cdot (\mathbf{p} - \mathbf{c})t + (\mathbf{p} - \mathbf{c}) \cdot (\mathbf{p} - \mathbf{c}) - r^2 = 0$$



How

$$\underbrace{(\mathbf{d} \cdot \mathbf{d})}_{a} t^2 + \underbrace{2\mathbf{d} \cdot (\mathbf{p} - \mathbf{c})}_{b} t + \underbrace{(\mathbf{p} - \mathbf{c}) \cdot (\mathbf{p} - \mathbf{c}) - r^2}_{c} = 0$$

$$at^2 + bt + c = 0$$

$$t_{1,2} = \frac{-b \pm \sqrt{\Delta}}{2a}$$

$$\Delta = b^2 - 4ac$$

How

$$\underbrace{(\mathbf{d} \cdot \mathbf{d})}_{a} t^2 + \underbrace{2\mathbf{d} \cdot (\mathbf{p} - \mathbf{c})}_{b} t + \underbrace{(\mathbf{p} - \mathbf{c}) \cdot (\mathbf{p} - \mathbf{c}) - r^2}_{c} = 0$$

$$at^2 + bt + c = 0$$

$$t_{1,2} = \frac{-b \pm \sqrt{\Delta}}{2a}$$

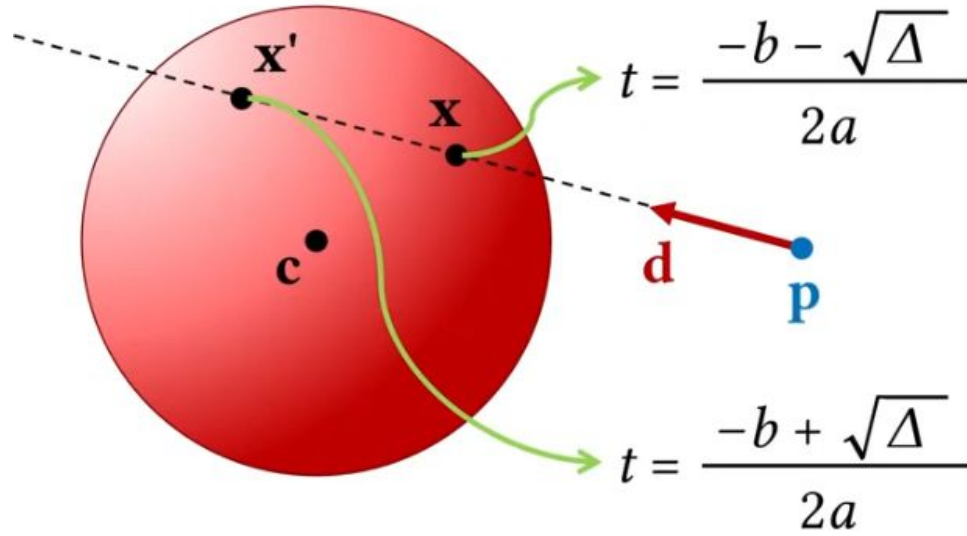
$$\Delta = b^2 - 4ac$$

$\Delta < 0$  **No Hit!**

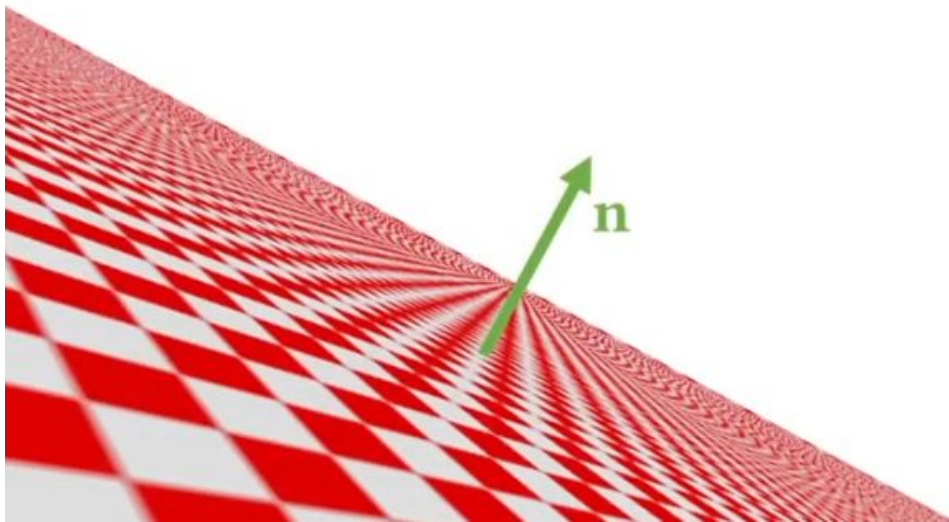
$\Delta \geq 0$  **Hit!**

How

$$(\mathbf{d} \cdot \mathbf{d})t^2 + 2\mathbf{d} \cdot (\mathbf{p} - \mathbf{c})t + (\mathbf{p} - \mathbf{c}) \cdot (\mathbf{p} - \mathbf{c}) - r^2 = 0$$

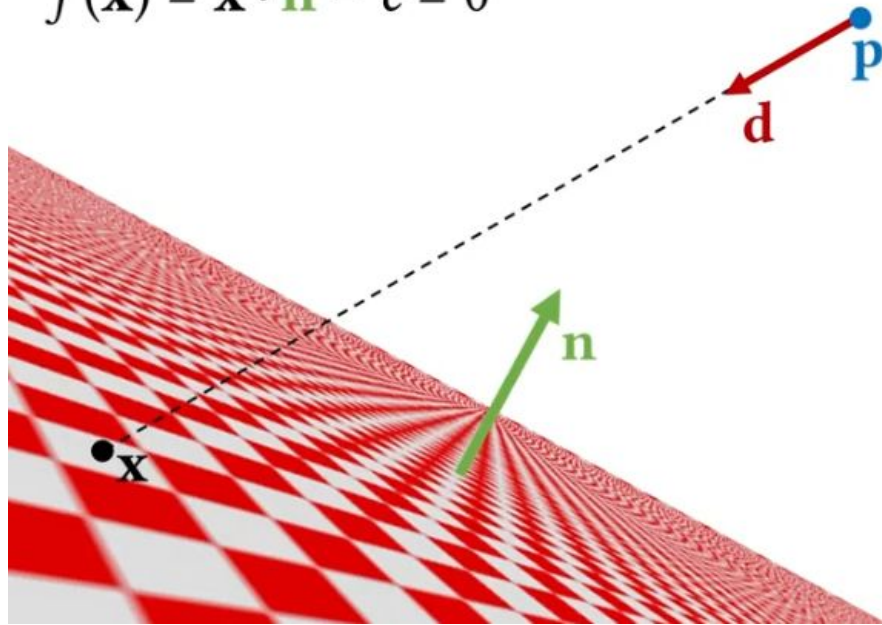


How



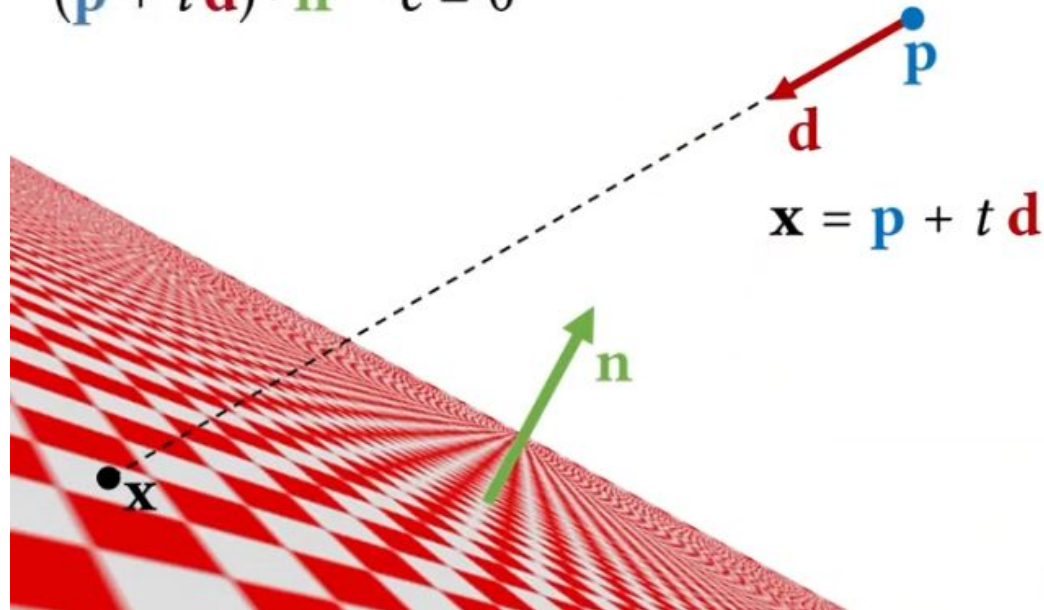
How

$$f(\mathbf{x}) = \mathbf{x} \cdot \mathbf{n} - c = 0$$



How

$$(\mathbf{p} + t\mathbf{d}) \cdot \mathbf{n} - c = 0$$

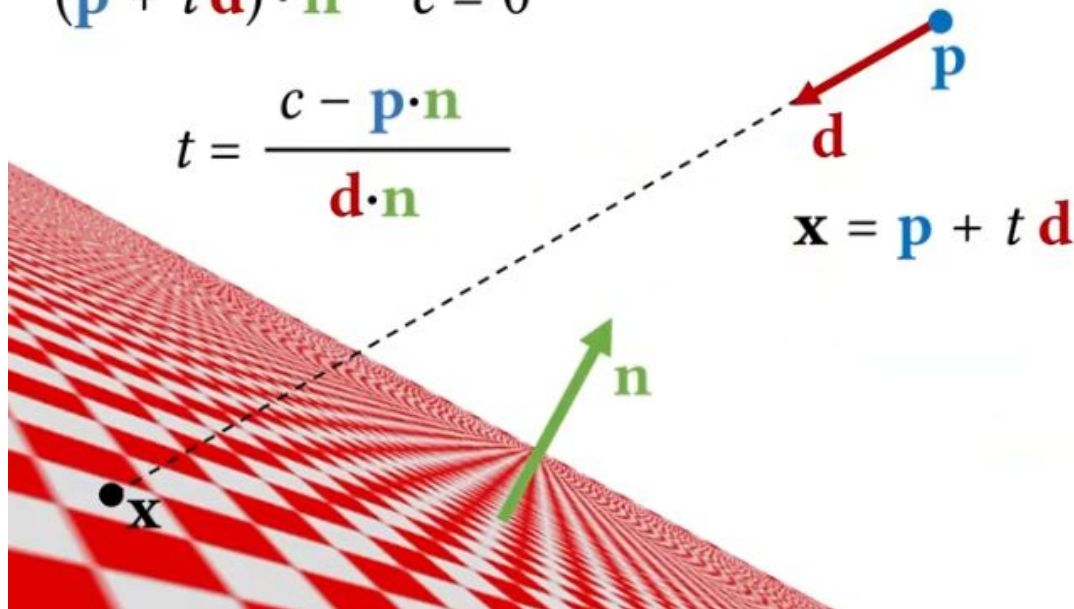


How

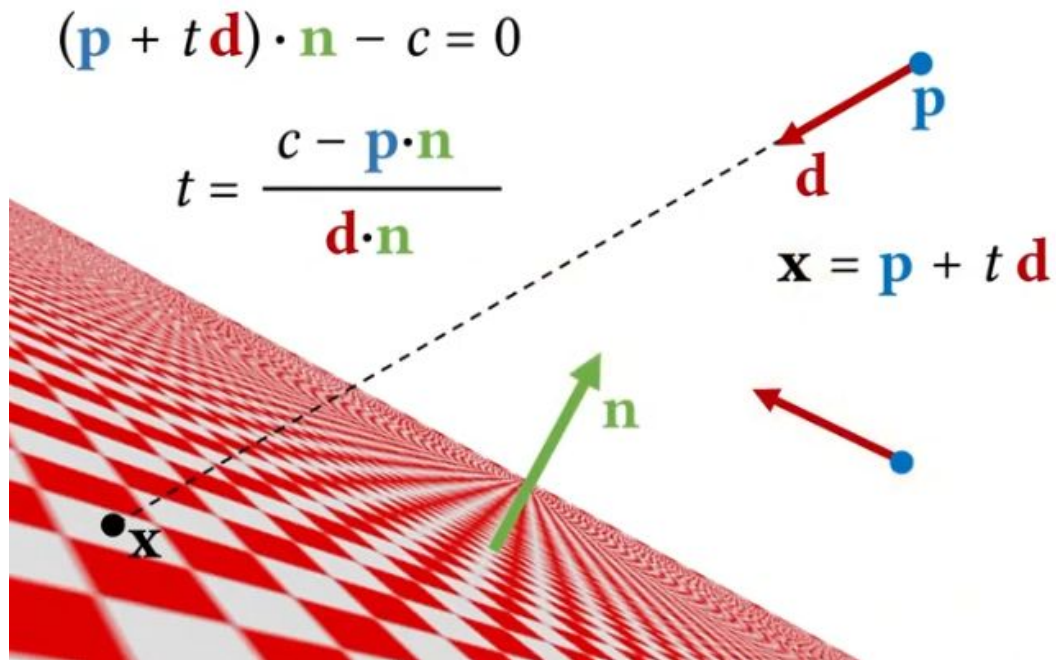
$$(\mathbf{p} + t\mathbf{d}) \cdot \mathbf{n} - c = 0$$

$$t = \frac{c - \mathbf{p} \cdot \mathbf{n}}{\mathbf{d} \cdot \mathbf{n}}$$

$$\mathbf{x} = \mathbf{p} + t\mathbf{d}$$



How

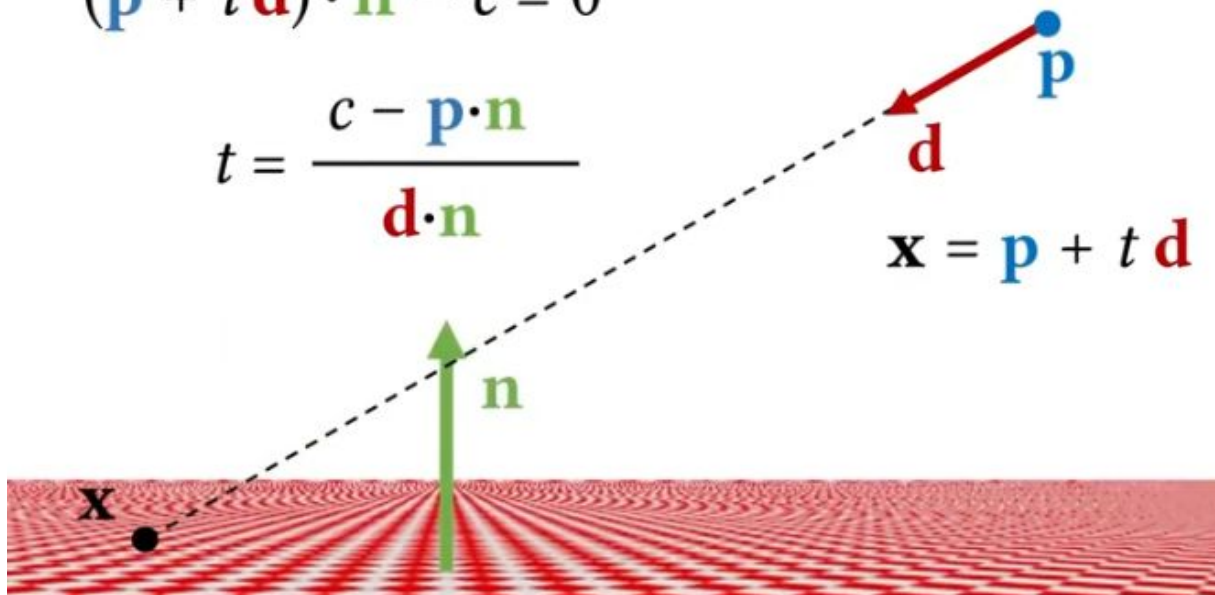


How

$$(\mathbf{p} + t\mathbf{d}) \cdot \mathbf{n} - c = 0$$

$$t = \frac{c - \mathbf{p} \cdot \mathbf{n}}{\mathbf{d} \cdot \mathbf{n}}$$

$$\mathbf{x} = \mathbf{p} + t\mathbf{d}$$



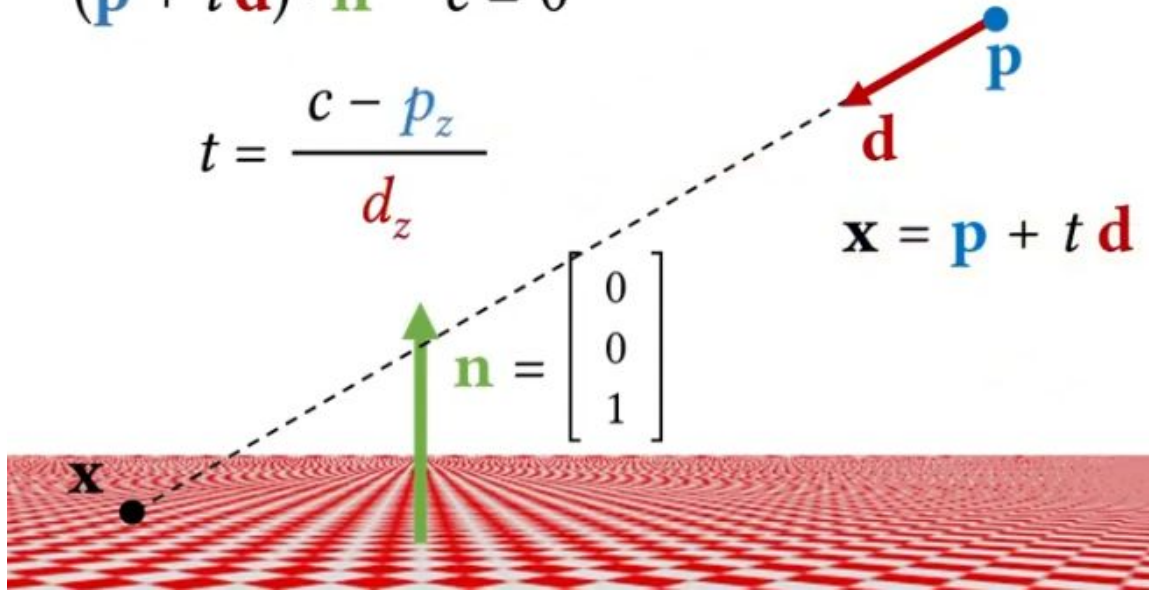
How

$$(\mathbf{p} + t\mathbf{d}) \cdot \mathbf{n} - c = 0$$

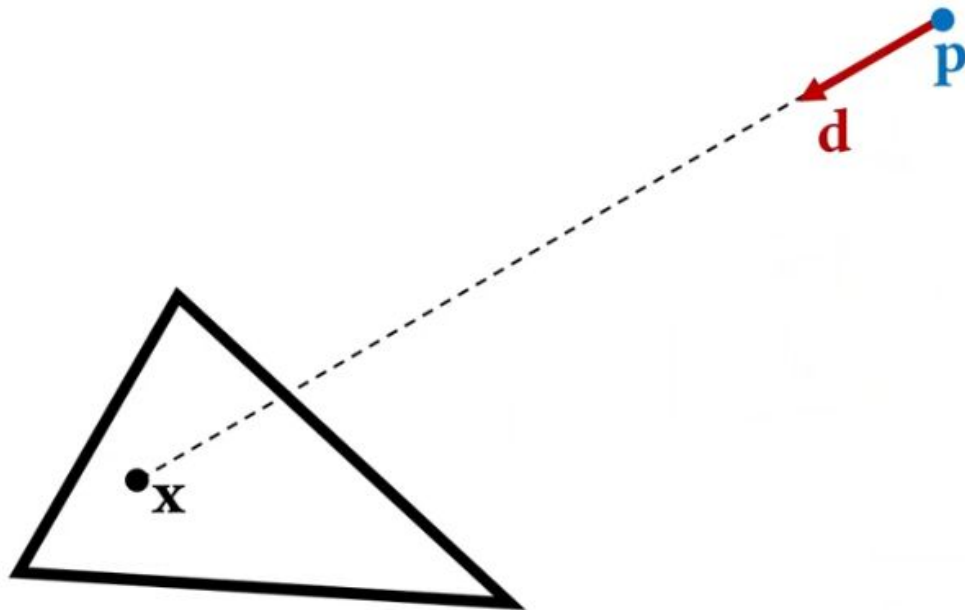
$$t = \frac{c - p_z}{d_z}$$

$$\mathbf{x} = \mathbf{p} + t\mathbf{d}$$

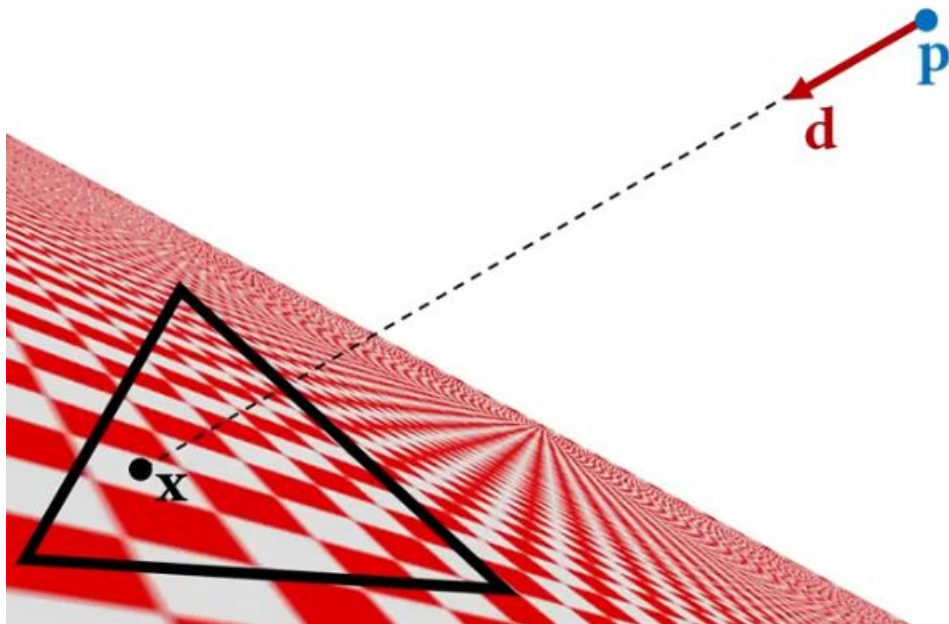
$$\mathbf{n} = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$



How

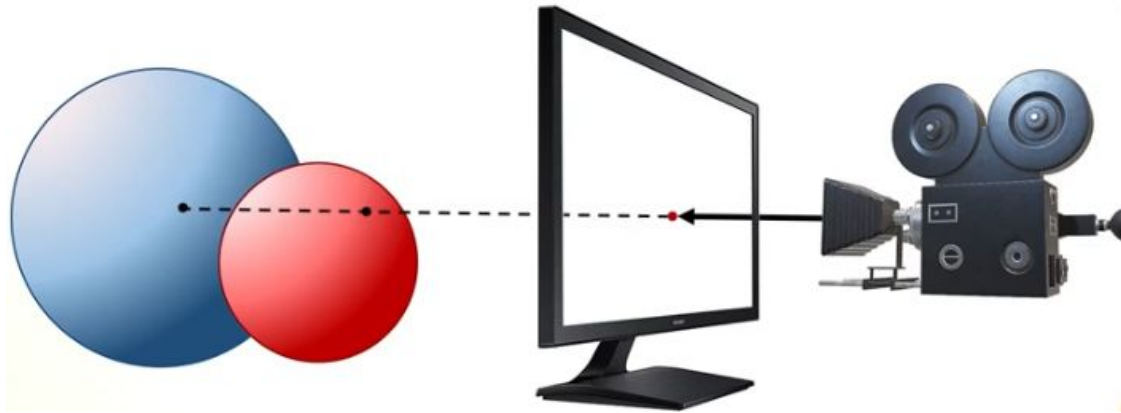


How



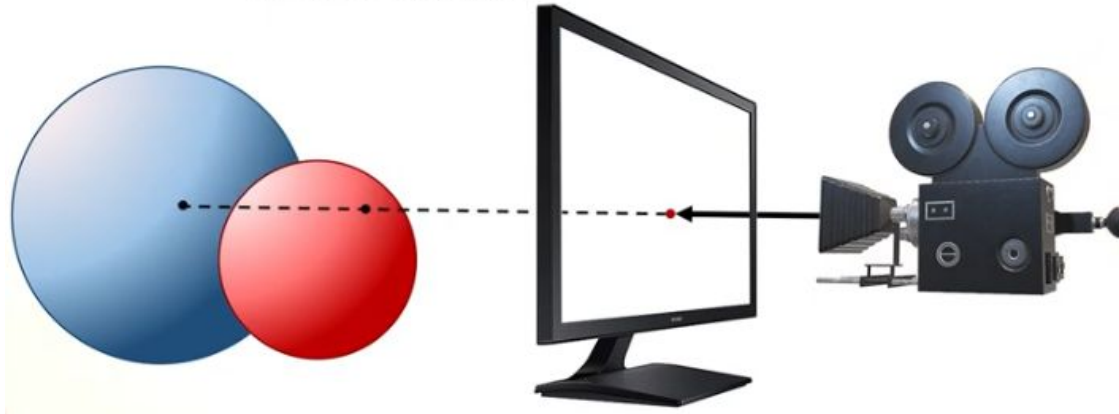
How

for each *ray*
find the *closest primitive*

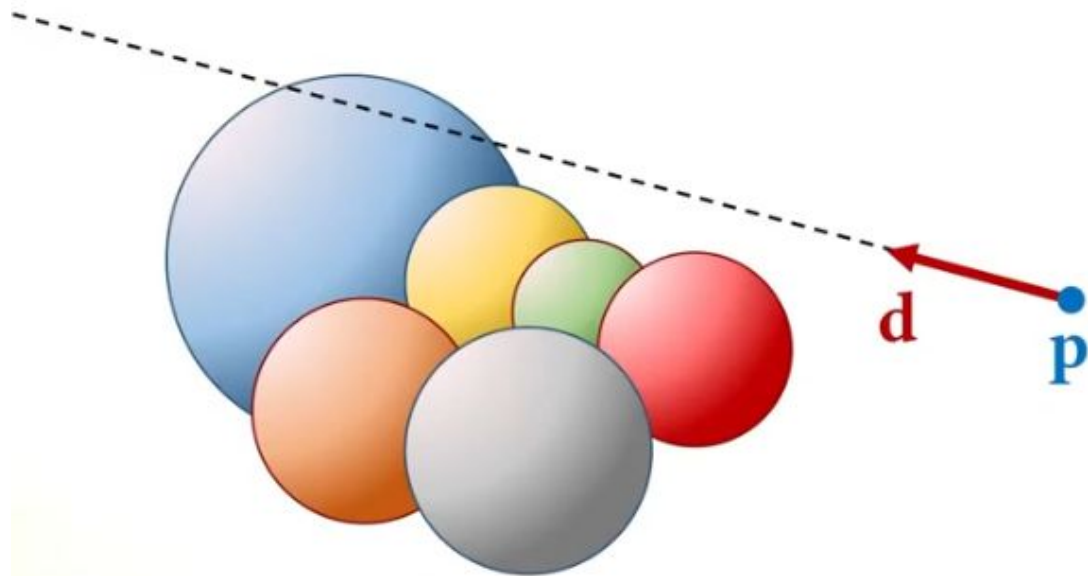


How

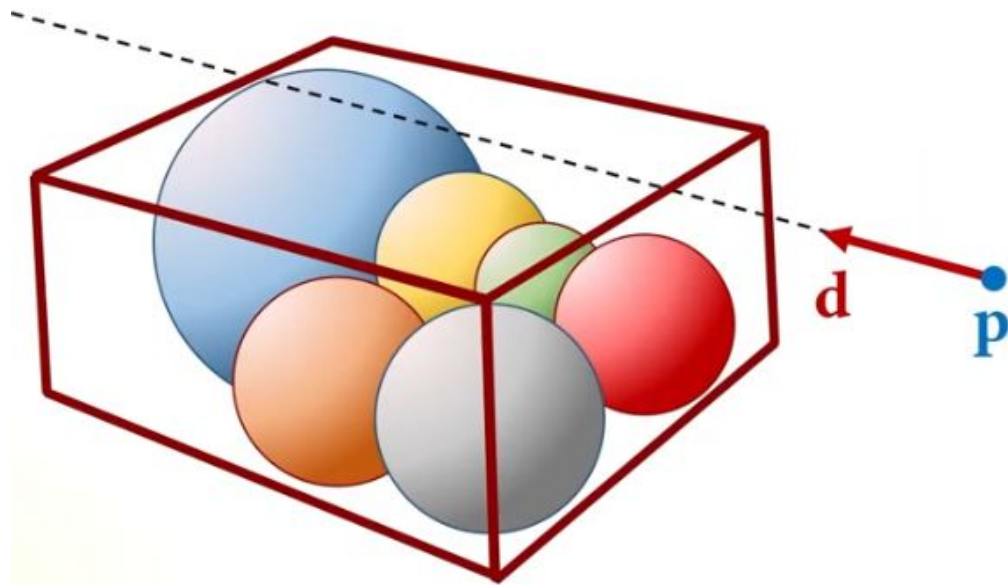
for each ray
 for each primitive
 if ray intersects primitive
 if *closest* hit



Accelerating ray tracing

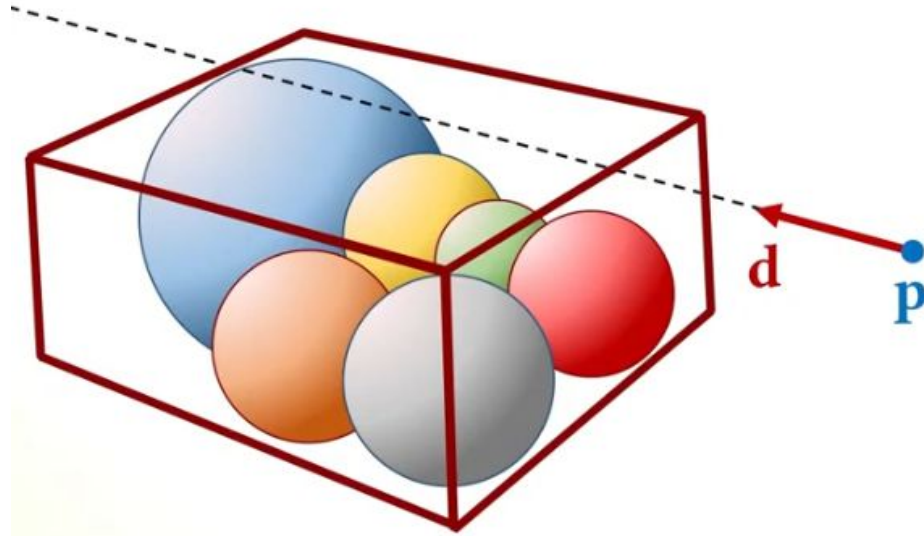


Accelerating ray tracing



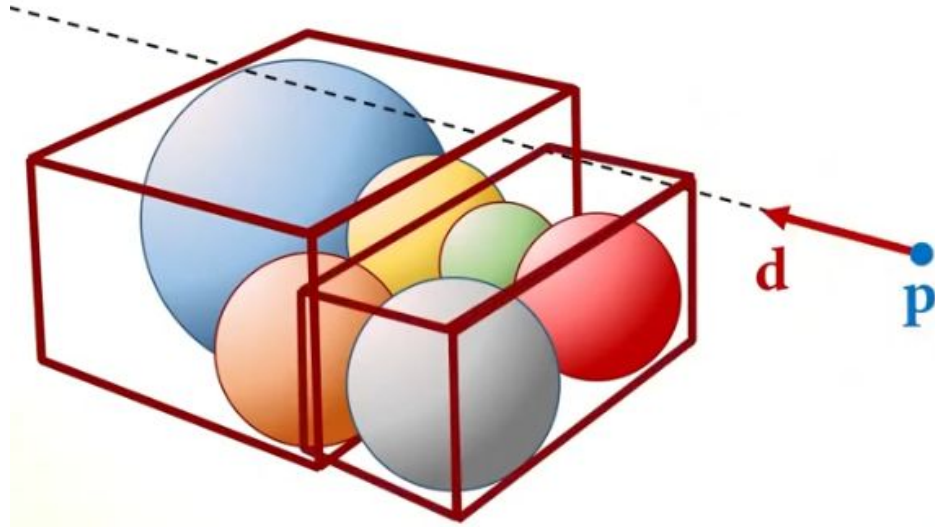
Accelerating ray tracing

Axis-Aligned Bounding Box

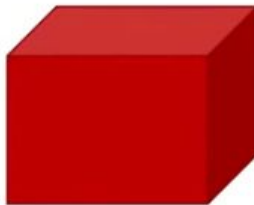


Accelerating ray tracing

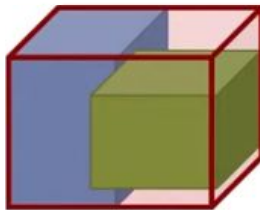
Axis-Aligned Bounding Box



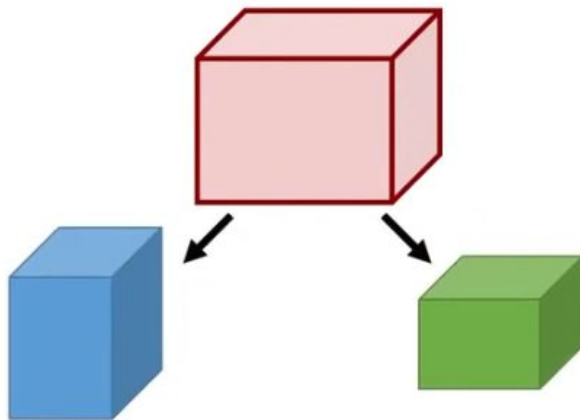
BVH



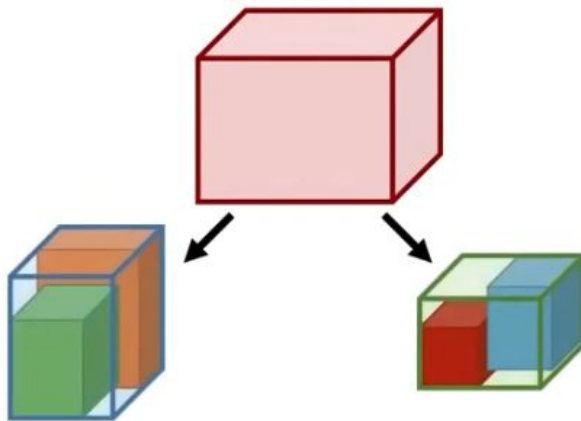
BVH



BVH



BVH



BVH

