

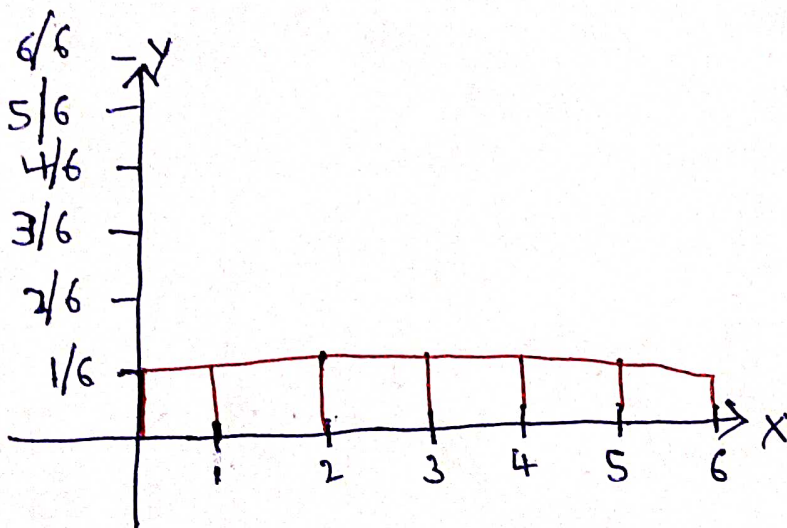
## Probability Mass Function:

\* used to Represent Discrete Random variables

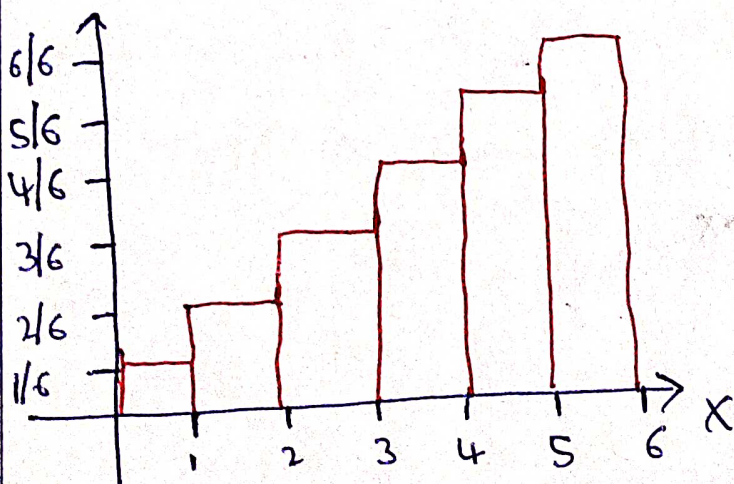
For eg: Rolling a Dice

$$X = \{1, 2, 3, 4, 5, 6\}$$

$$P_X(1) = 1/6, P_X(2) = 1/6, \dots$$



cumulative probability:



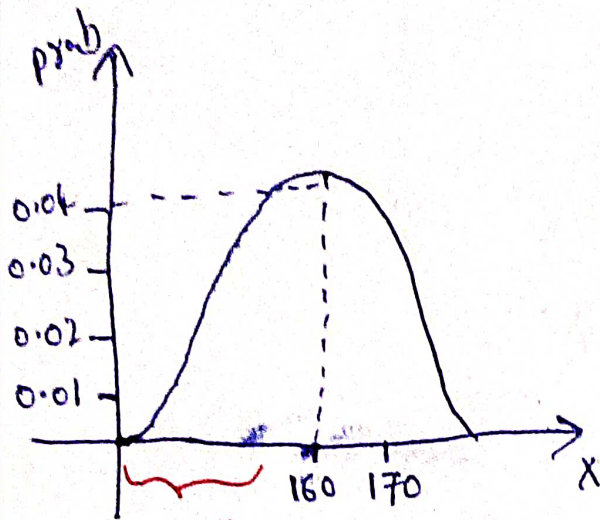
\* It's the cumulative sum of all the Data points.



# Probability Density Function:

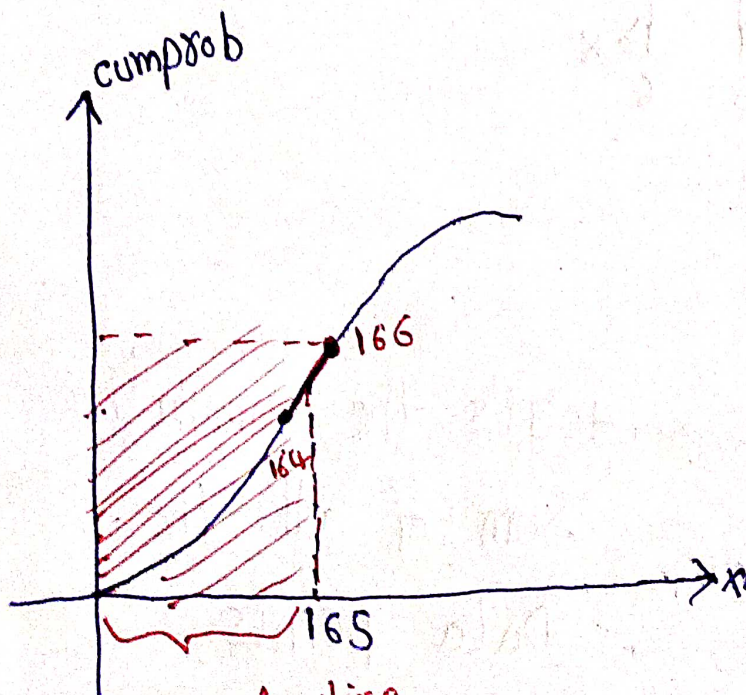
\* used to represent continuous Random variables.

Eg: Heights



50% of  
Entire Distribution

CDF:



50% of Entire  
Distribution.

## Bernoulli Distribution:

\* It is the Distribution where two discrete outcomes will be represented by  $P$  and  $1-P$

eg: Tossing a coin

$$P(H) = P = 0.50$$

$$\Rightarrow P(T) = 1 - P \Rightarrow q$$

mean of Bernoulli Distribution :  $P$

Variance :  $Pq$

std deviation :  $\sqrt{Pq}$

## Binomial Distribution:

\* It is same as Bernoulli, But two discrete outcomes will be done for  $n$  number of Times.

eg: Toss a coin 13 Times

Mean :  $np$

Variance :  $npq$

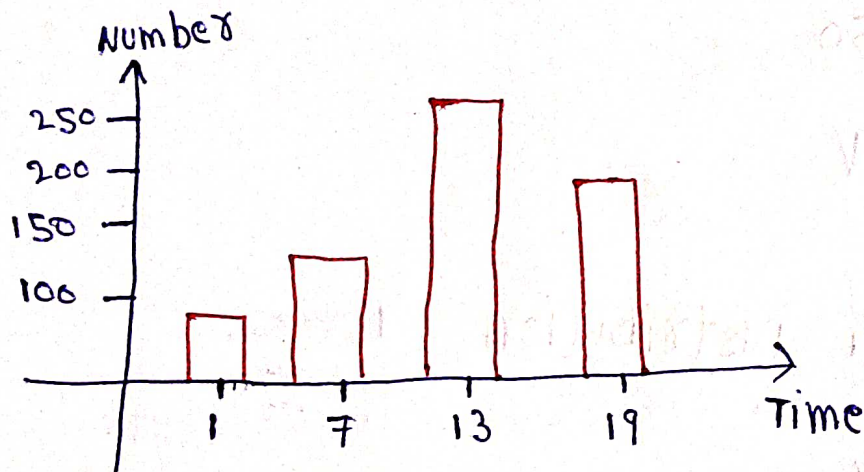
std Deviation :  $\sqrt{npq}$



## Poisson Distribution:

\* Describes the number of events occurring at a certain period of Time.

eg: No of people visiting Hospital every 6 hours.



$$\lambda = 135$$

\* ( $\lambda$ ) Represents Expected no. of events at every Time Interval

mean  $\rightarrow \lambda t$

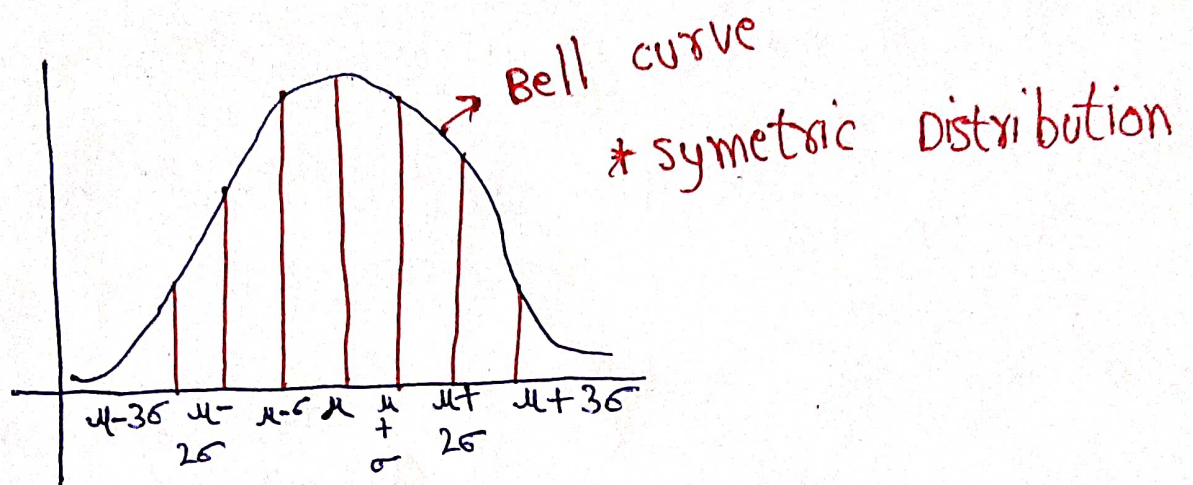
Variance  $\rightarrow \lambda t$

\*  $t$  = time Interval

$\lambda$  = Expected no. of Events



## Normal ( $\sigma$ ) Gaussian Distribution:



### Empirical Rule :

- \* 68% Data lies b/w  $\mu - \sigma$  and  $\mu + \sigma$
- \* 95% Data lies b/w  $\mu - 2\sigma$  and  $\mu + 2\sigma$
- \* 99.7% Data lies b/w  $\mu - 3\sigma$  and  $\mu + 3\sigma$

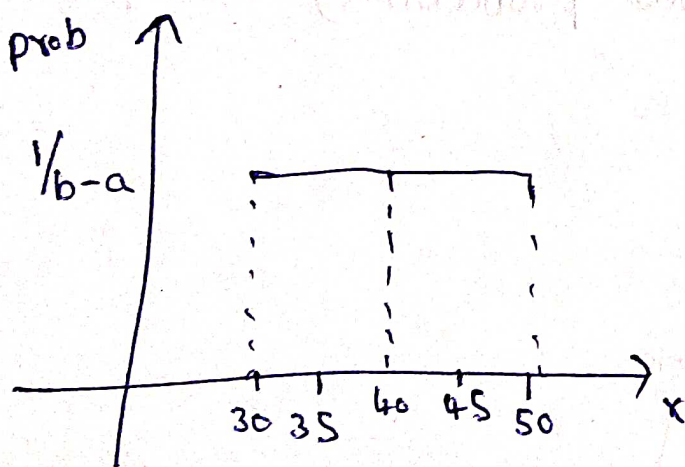
eg: Based on so much of Analysis, Researchers Found Height, weight, iris, etc... will mostly have gaussian distribution



## uniform Distribution

### continuous uniform Distribution:

- \* In uniform Distribution, the probability of getting outcomes is equal
- \* In continuous uniform distribution, In between a specified Range the probability of getting outcomes is same.



$$P_x = (x_2 - x_1) * \frac{1}{b-a}$$

$a$  = lower bound

$b$  = higher bound

$x_1, x_2$  are datapoints.

$$P_x(x \text{ b/w } 40 \text{ \& } 45) = (\cancel{45} x_2 - x_1) * \frac{1}{b-a}$$

$$= (45 - 40) * \frac{1}{50 - 30}$$

$$= 5/20$$

$$= 1/4 \Rightarrow 0.25 \Rightarrow 25\%$$

$$P(X \text{ b/w } 30 \text{ \& } 35) = (35-30) * \frac{1}{20}$$

$$= 0.25 \Rightarrow \boxed{25\%}$$

$$P(X \text{ b/w } 30 \text{ \& } 45) = (45-30) * \frac{1}{20}$$

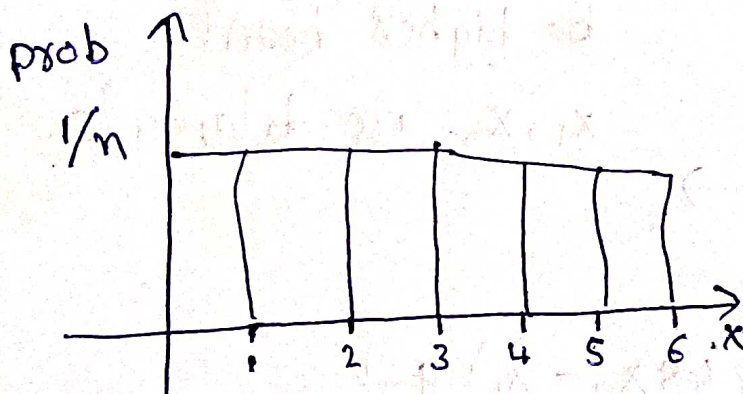
$$\text{Mean} : a-b/2 = 15/20$$

$$\text{Variance} : (b-a)^2/12 = 0.75 \Rightarrow \boxed{75\%}$$

Discrete uniform distribution:

\* All the data has equal probability i.e,  $1/n$

eg: Rolling a die



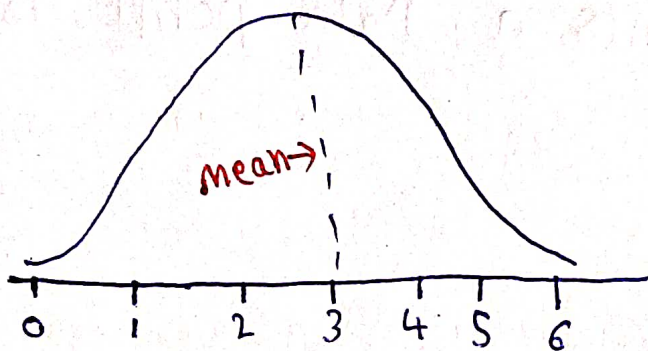
$$P(X=1) = 1/n \Rightarrow 1/6$$



## standard Normal distribution:

\* It is the process of converting Normal Distribution into -ve, zero and +ve Data

For eg this is Normal distribution:



$$\Rightarrow \mu = 0$$
$$\sigma = 1$$

Let's Apply z score on all data

$$z = \frac{x_i - \mu}{\sigma}$$

$$\mu = \text{mean} = 3$$

$$\sigma = \text{std deviation} = 2$$

data

0

1

2

3

4

5

6

z-Score

-1.5

-1

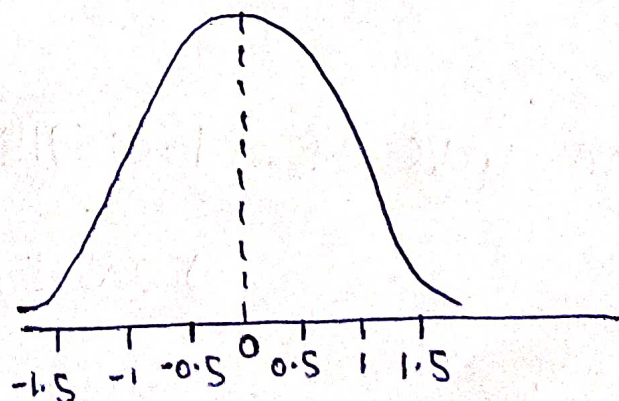
-0.5

0

0.5

1

1.5





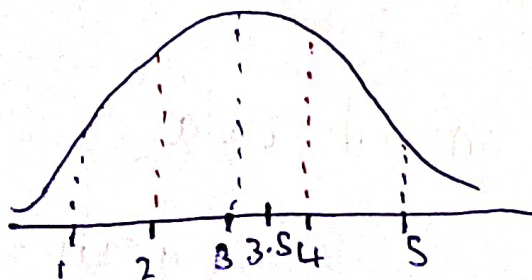
## z-scores :

\* z-score is used to standardize the data.

$$* z = \frac{x_i - \mu}{\sigma}$$

\* we can also relate 'z' with how many std deviation points a data point is away from mean.

eg :



\* Find px of Region above 3.5  $\Rightarrow$

$$z = \frac{3.5 - 3}{1} \Rightarrow \boxed{0.5} \rightarrow \text{Find its value in z-table}$$

0.6915 } its the region out of 1  
Before 3.5

$$\rightarrow \text{Region above 3.5} = 1 - 0.6915 \Rightarrow 0.3085$$

$$\Rightarrow 30.85\%$$