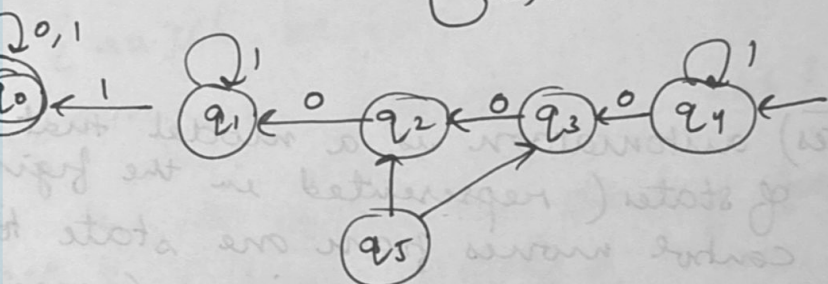
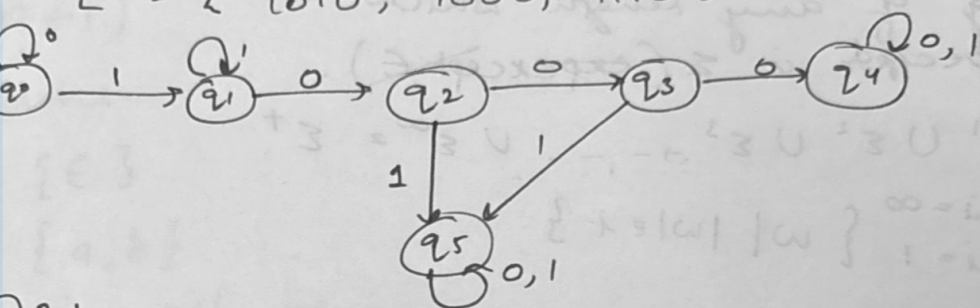


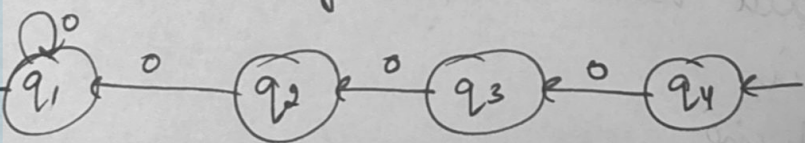
a) $L = \{ w \mid w \in \{0,1\}^*, \text{ 4th symbol from beginning of } w \text{ is } 0 \}$

$L = \{ 1010, 1000, 1110, \dots \}$



, it is valid in finite automata cause it both final & initial state. It is NFA
 cause in NFA, there is more than 1 transition for input 1 in DFA there is only transition from each input.

minimize \rightarrow q_5 is unreachable since it has no incoming edge, the new diagram is -



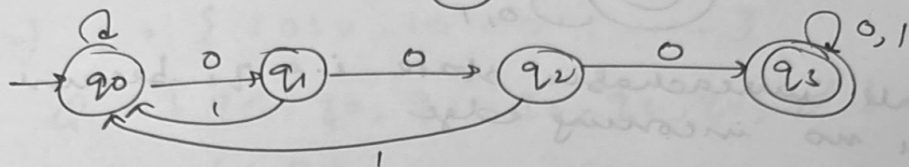
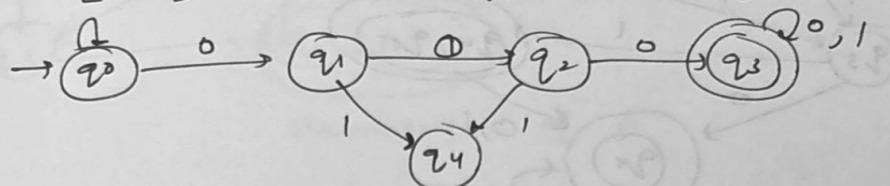
$|w| \geq 4$

begins with $\rightarrow 01$

ends with $\rightarrow 10$

$$\Sigma = \{0, 1\}$$

$$L = \{1000, 0001, 1000 \dots\}$$

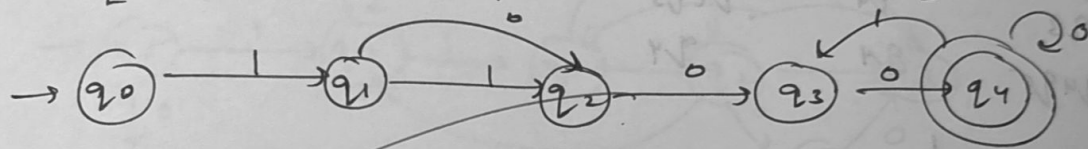


$$\Sigma = \{0, 1\}$$

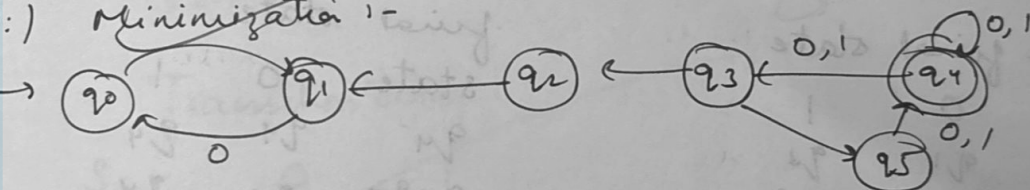
even no. of zero

even no. of ones

$$L = \{0011, 1100, 11110000 \dots\}$$



Minimization :-

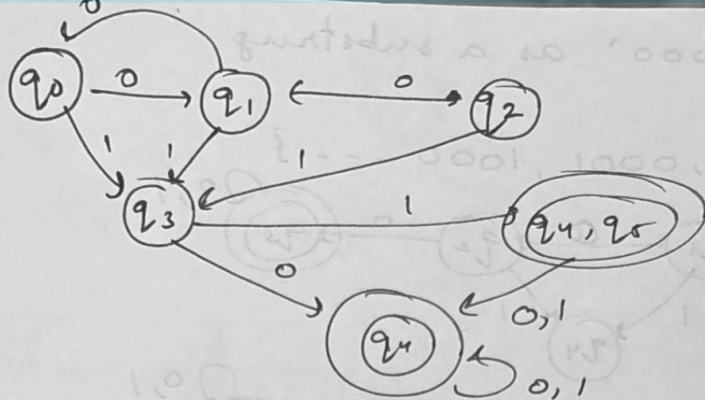


Transition table :-

state	0	1
q ₀	q ₁	q ₂
q ₁	q ₀	q ₃
q ₂	q ₁	q ₃
q ₃	q ₁	q ₄ q ₅
q ₄	q ₄	q ₄
q ₅		

DFA transition table :-

state	0	1
q ₀	q ₁	q ₃
q ₁	q ₀	q ₃
q ₂	q ₁	q ₄ q ₅
q ₃	q ₄	q ₄
q ₄	q ₄	q ₄
q ₄ q ₅		



Remove all unreachable state i.e. q_2 because there is no incoming edge

state	0	1
q_0	q_1	q_3
q_1	q_0	q_3
q_4	q_4	q_4
q_3	q_4	$q_4 q_5$
$q_4 q_5$	q_4	q_4

minimized

non-final state

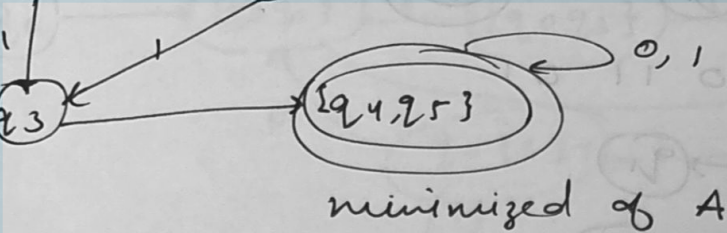
state	0	1
q_0	q_1	q_3
q_1	q_0	q_3
q_3	q_4	$q_4 q_5$

final state

state	0	1
q_4	q_4	q_4
$q_4 q_5$	q_4	q_4

now we will remove the duplicate rows and merge them into one and once again both the tables

state	0	1
q_0	q_1	q_3
q_1	q_0	q_3
q_3	$q_4 q_5$	$q_4 q_5$
$q_4 q_5$	$q_4 q_5$	$q_4 q_5$



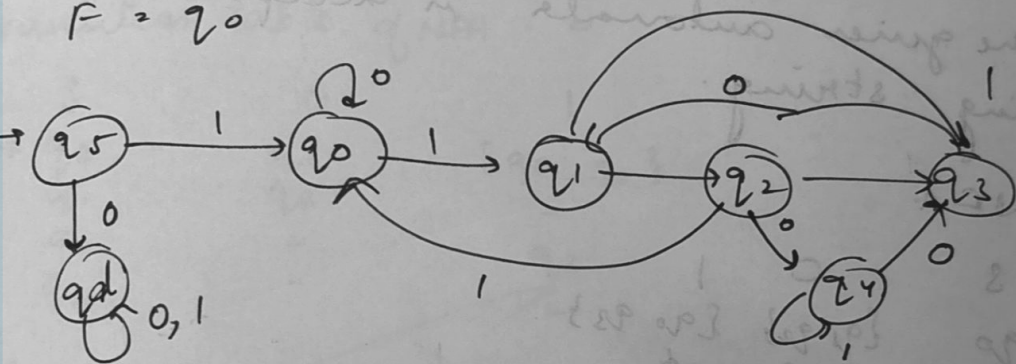
$$L = \{1010, 101001, \dots\}$$

$$Q = \{q_5, q_0, q_1, q_2, q_3, q_4, q_d\}$$

$$\Sigma = \{1, 0\}$$

$$q_0 = 20$$

$$F = 20$$

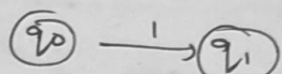


Transition table

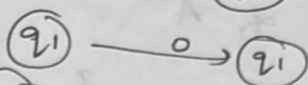
0	1
qd	q0
q0	q1
q2	q3
q4	q0
q1	q2
q3	q4
qd	qd

checking for 101101

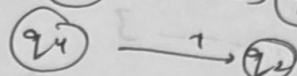
for 1



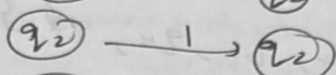
for 0



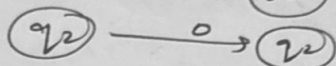
for 1



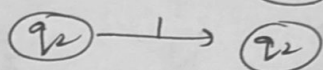
for 1



for 0



for 1



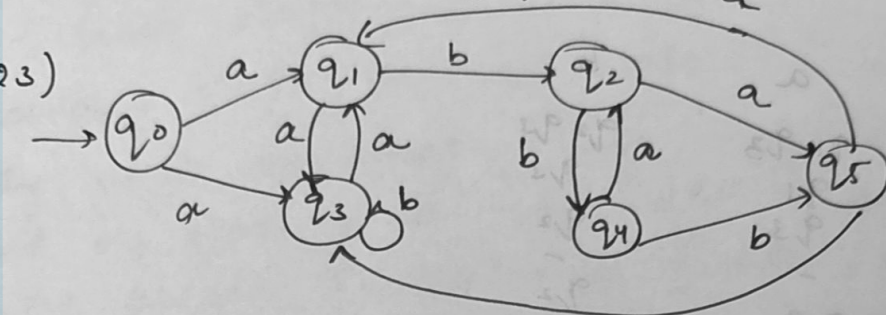
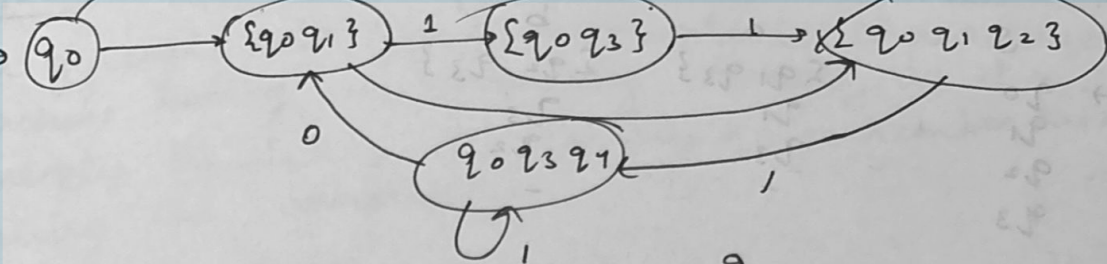
Hence, the given automata is acceptable for a given string.

20). NFA

S	0	1
q ₀	{q ₁ , q ₂ }	{q ₀ , q ₃ }
q ₁	{q ₁ }	∅
q ₂	∅	∅
q ₃	∅	{q ₄ }
q ₄	∅	∅

DFA

S	0	1
q ₀	q ₀ q ₁	q ₀ q ₃
{q ₀ , q ₁ }	q ₀ q ₁ q ₂	q ₀ q ₃
{q ₀ , q ₃ }	q ₀ q ₁	q ₀ q ₃ q ₄
q ₀ q ₁ q ₂	q ₀ q ₁ q ₂	q ₀ q ₃
q ₀ q ₃ q ₄	q ₀ q ₁	q ₀ q ₃ q ₄

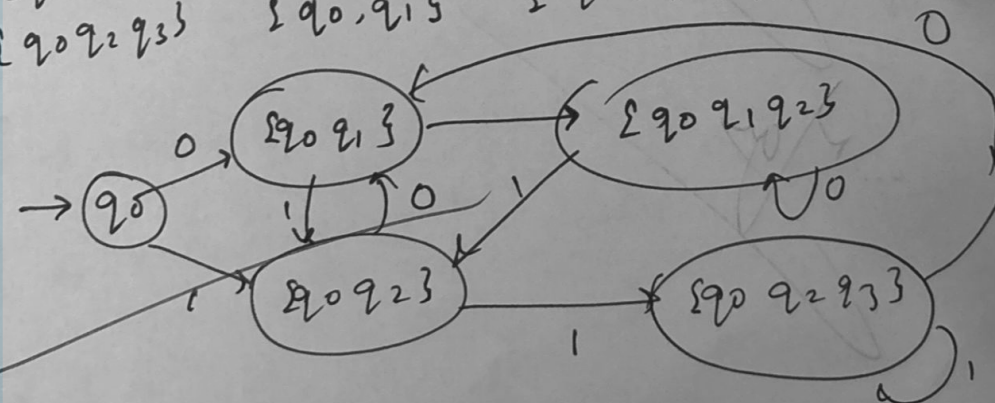


Transition table of NFA

S	0	1
→ q ₀	q ₁	{q ₀ , q ₁ }
q ₁	q ₂	-
q ₂	-	q ₃
q ₃	-	-

DFA

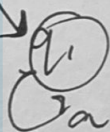
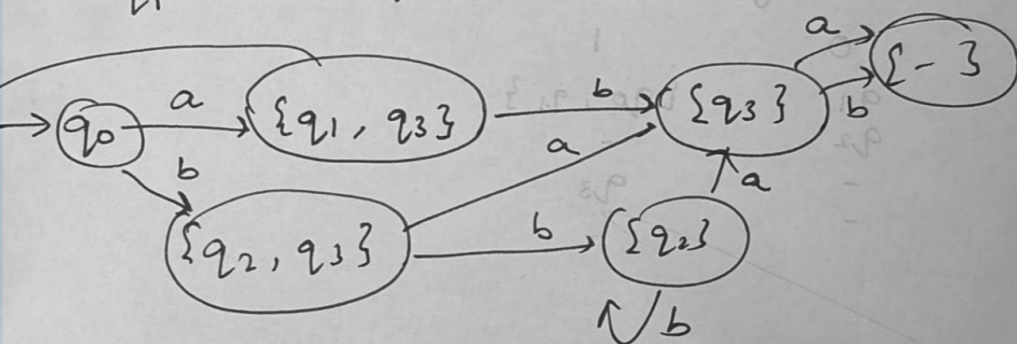
S	0	1
→ q ₀	{q ₀ , q ₁ }	{q ₀ , q ₂ }
{q ₀ , q ₁ }	{q ₀ q ₁ q ₃ }	{q ₀ , q ₂ }
{q ₀ q ₁ }	{q ₀ q ₁ }	{q ₀ , q ₂ , q ₃ }
{q ₀ q ₂ }	{q ₀ q ₁ q ₃ }	{q ₀ , q ₂ }
{q ₀ q ₁ q ₃ }	{q ₀ , q ₁ }	{q ₀ , q ₂ , q ₃ }
{q ₀ q ₂ q ₃ }		



S	a	b
$\rightarrow q_0$	$\{q_1, q_3\}$	$\{q_2, q_3\}$
q_1	q_1	q_3
q_2	q_3	q_2
q_3	-	-

DFA table

S	a	b
q_0	q_1, q_3	q_2, q_3
$\{q_1, q_3\}$	q_1	q_3
$\{q_2, q_3\}$	q_3	-
q_3	-	q_2
q_2	q_3	q_3
q_1	q_1	-



May