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# MLL 100

## Introduction to Materials Science and Engineering

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*Lecture-19 (February 23, 2022)*

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IIT Delhi

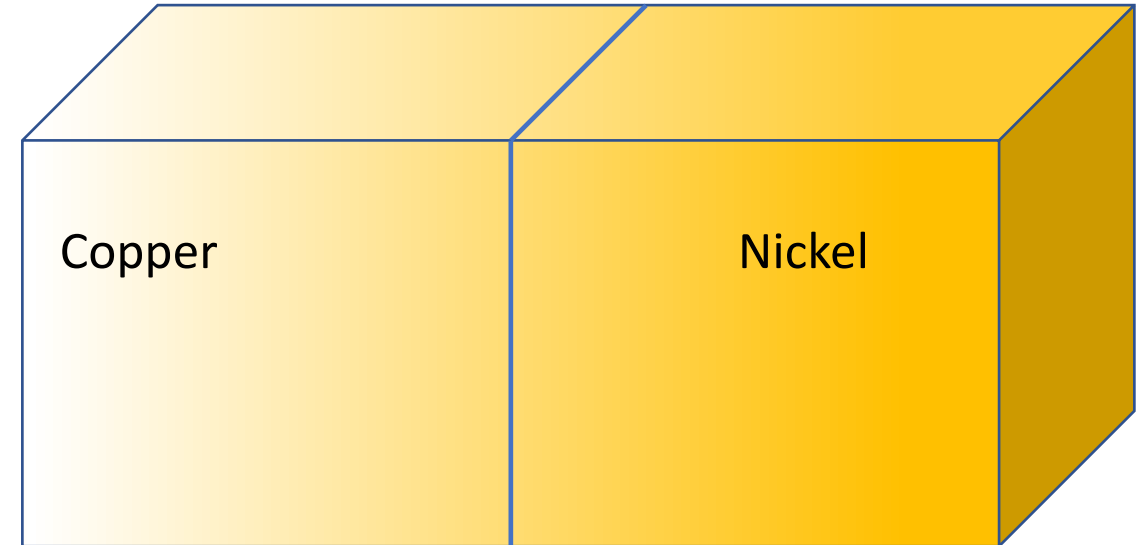
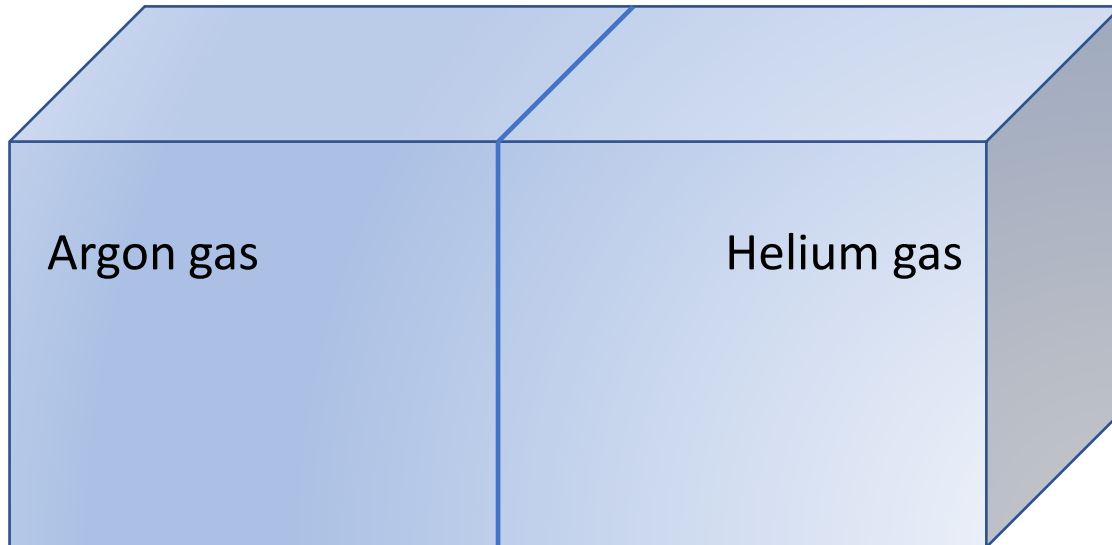
Department of Materials Science and Engineering

# What have we learnt in Lecture-18?

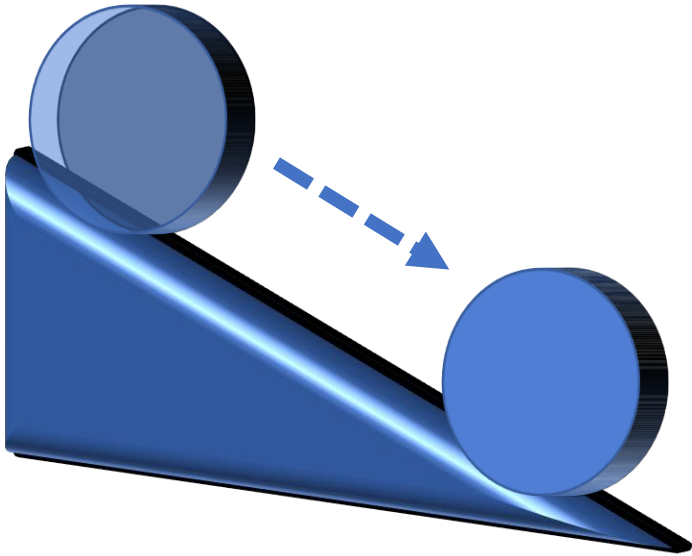
- ❑ TTT diagram (Transformation-temperature-time)
- ❑ Avrami equation
- ❑ Bainite, Martensite
- ❑ Different kinds of cooling rates: Annealing, Normalizing, Austempering, Quenching

**Imagine a chamber with a partition in the middle. Either side of the partition contains two different gases, Argon and Helium. What happens if the partition gets removed?**

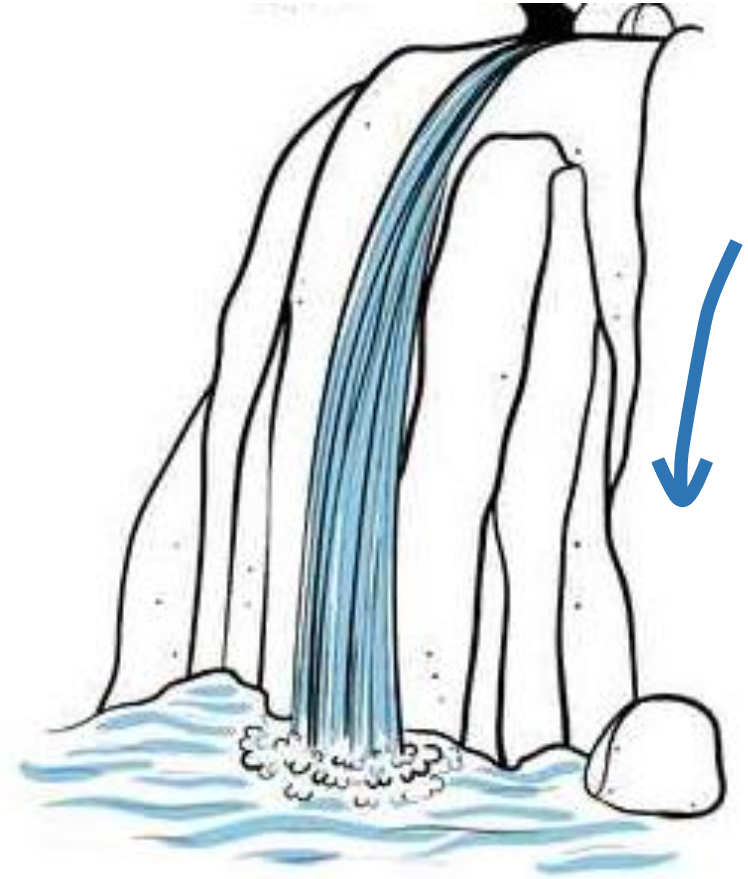
**In the second case, consider two single solid crystals, copper and nickel. What happens after the removal of partition?**



# Diffusion



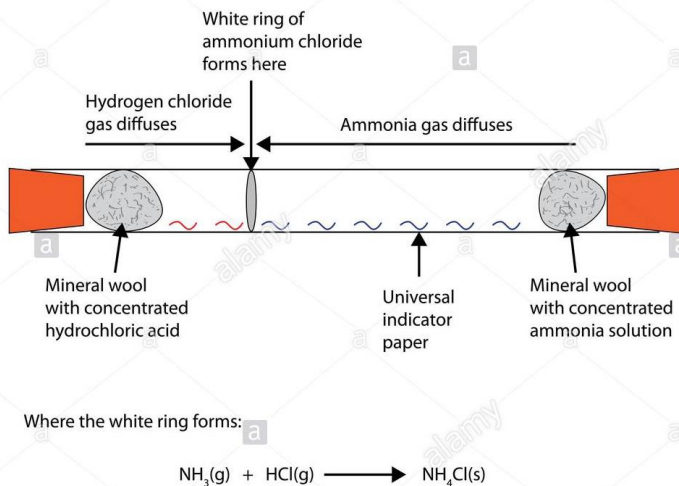
Disc rolling down the slope



Water falling down the hill slope

# What is diffusion?

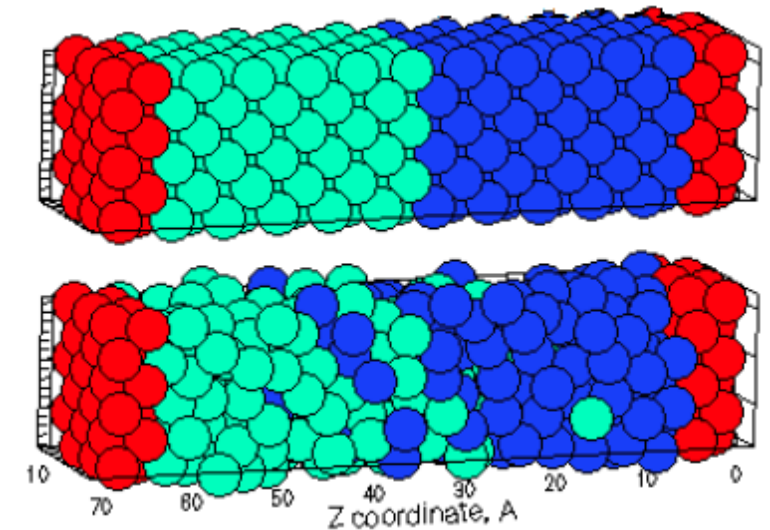
- Flow of atoms under the influence of a gradient, i.e. from a higher potential region to a lower potential region.



*Gas: Diffusion of ammonia*



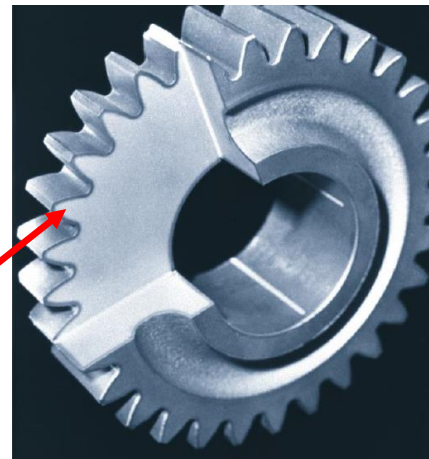
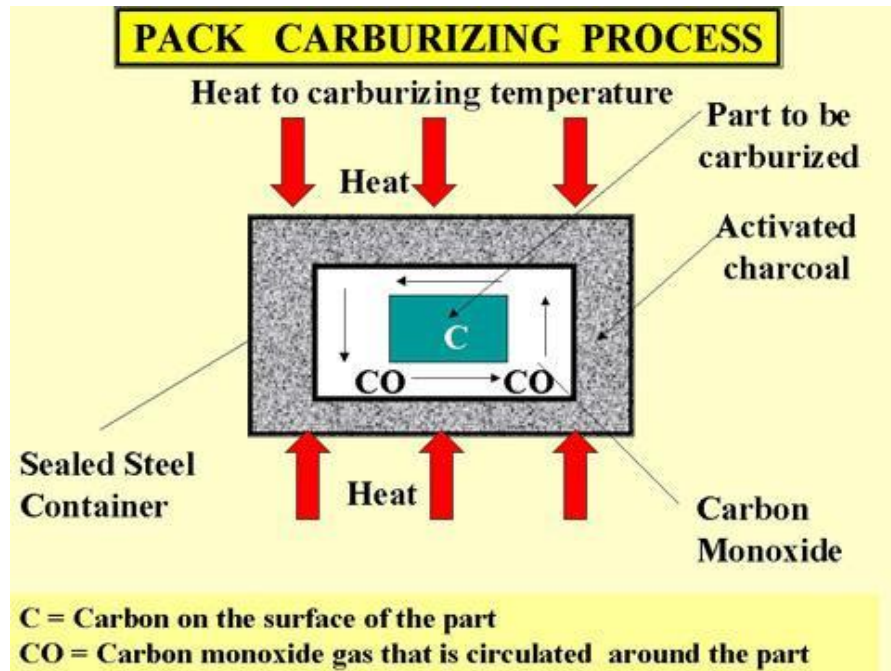
*Liquid: Diffusion of ink in water*



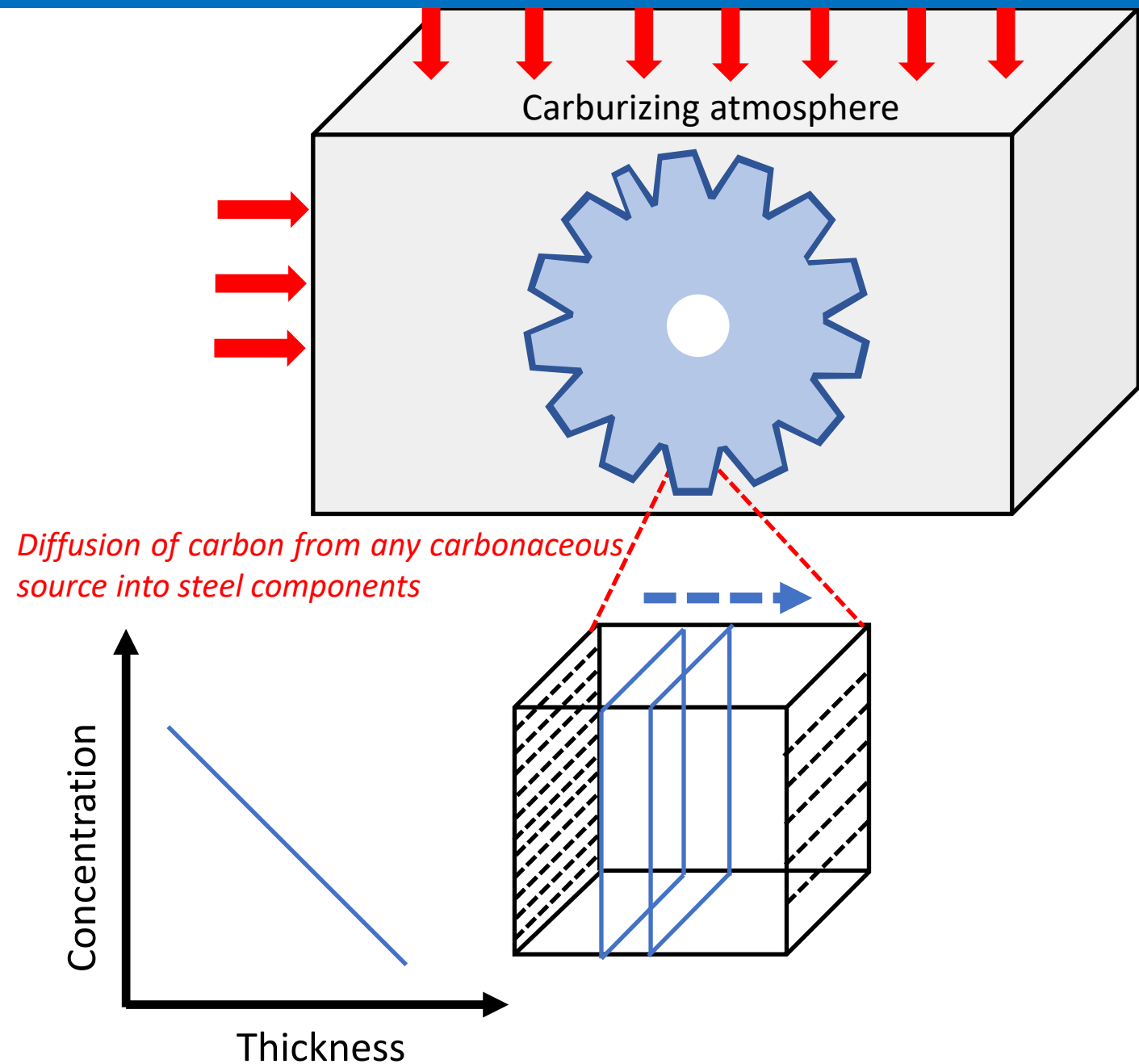
*Solid: Diffusion of atoms in copper and brass*

Diffusion in solids occur very slowly compared to those in liquids and gases, and also, is very restricted.

# How was diffusion exploited to engineer gears?

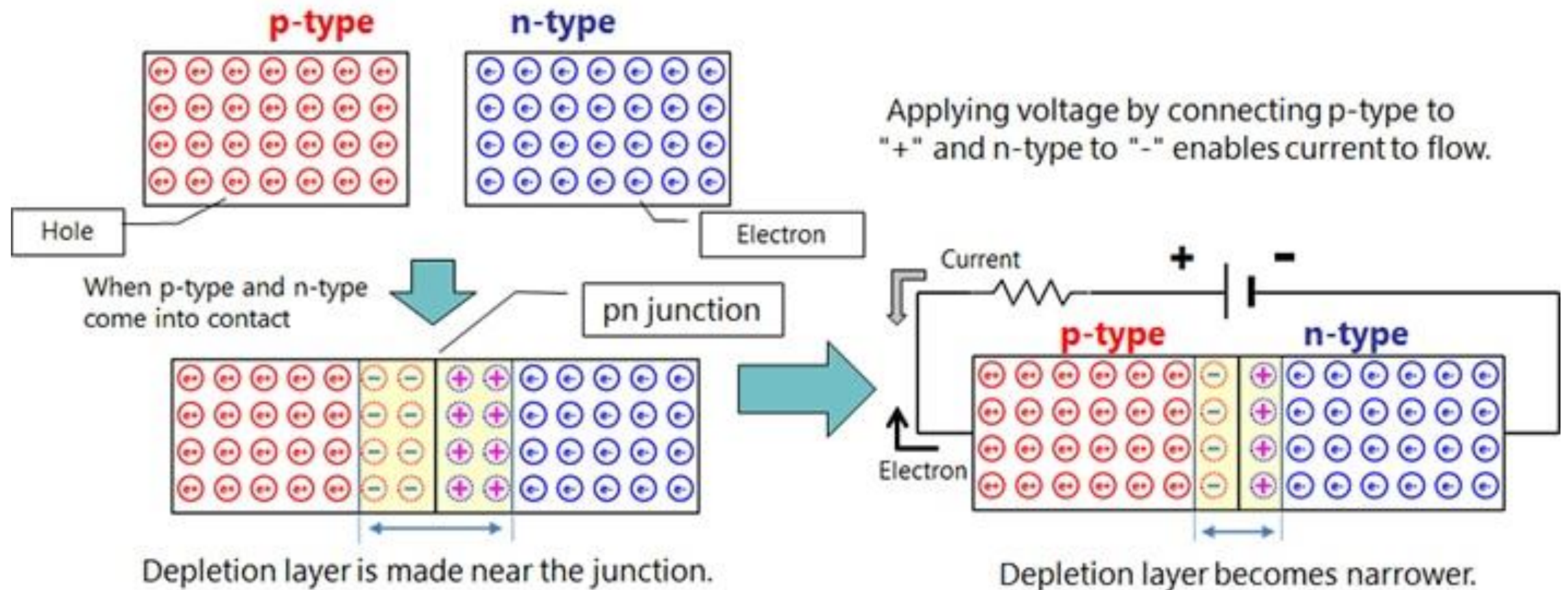


*Hardening of teeth of gears*



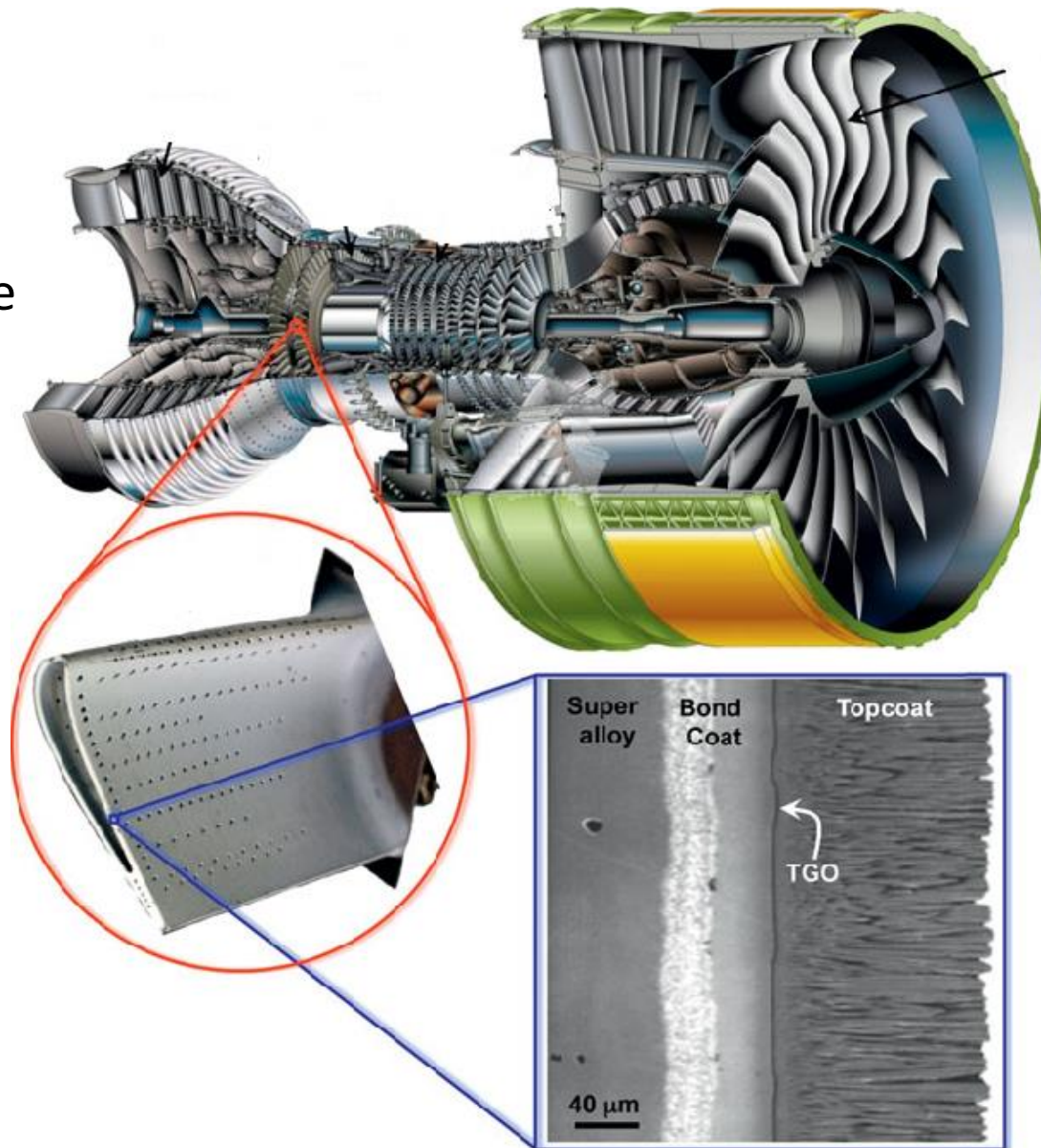


# Diffusion in semiconductor applications



# Aircraft engine

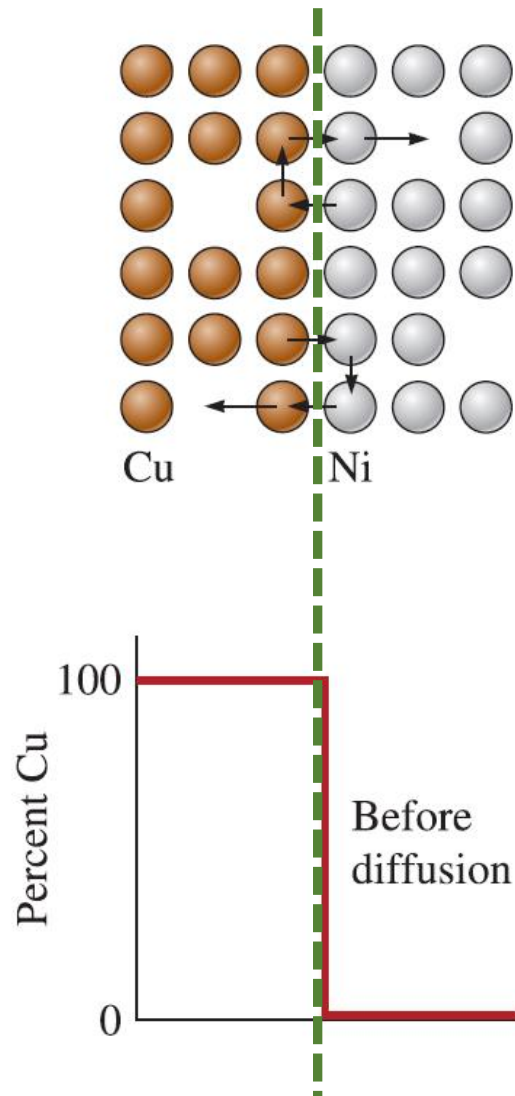
Turbine blade



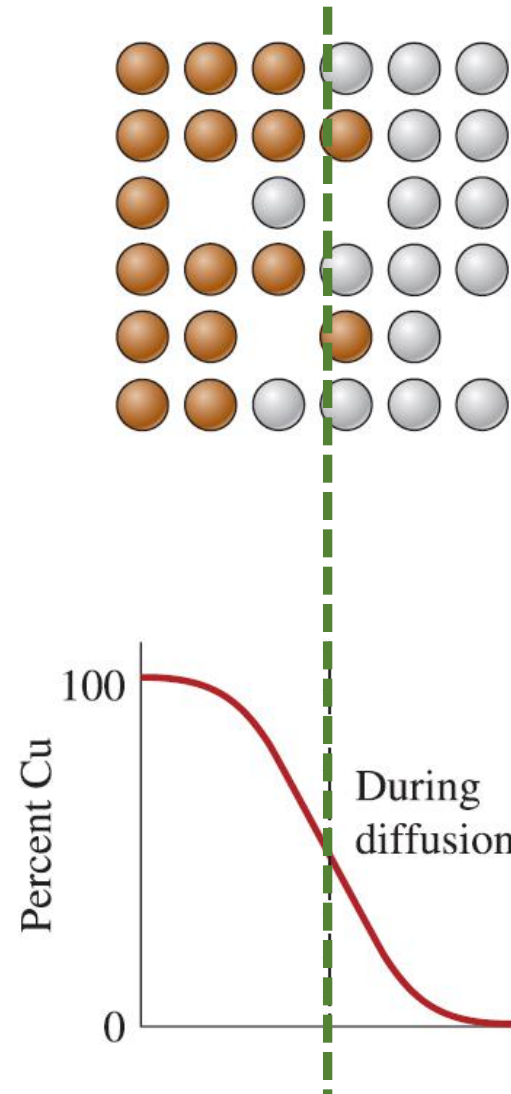


# How was the study of diffusion started off?

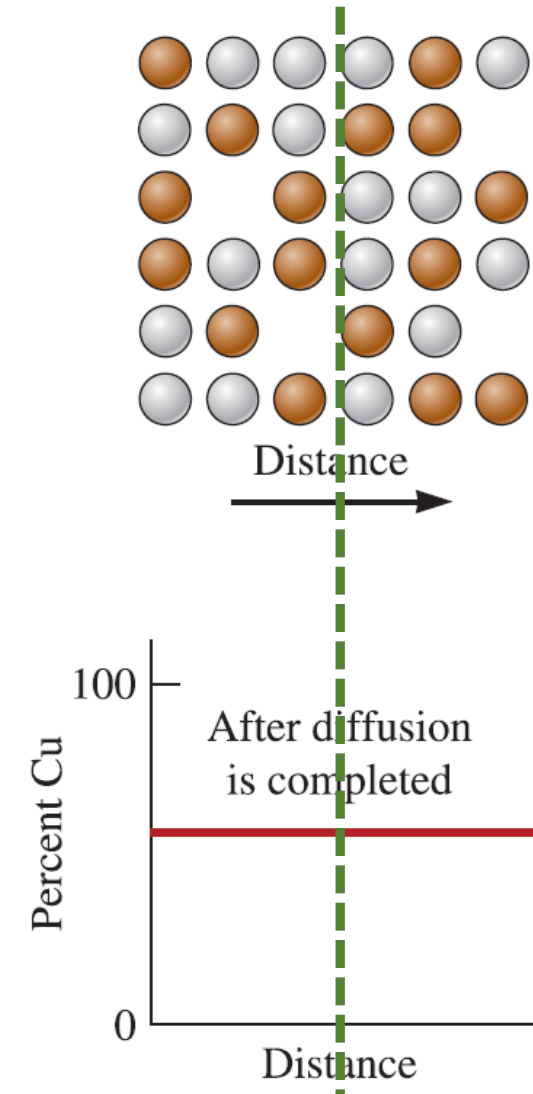
Initial stage



During diffusion



Completion of diffusion



# What drives diffusion?

- Temperature and a chemical potential gradient.

- Thermal energy -----> Atomic vibrations in lattice -----> Atomic jumps

- Gradient: Chemical potential (*What about the concentration gradient??*)

Gibbs Free energy (Minimized)

$$\Delta G = +\Delta H - T\Delta S$$

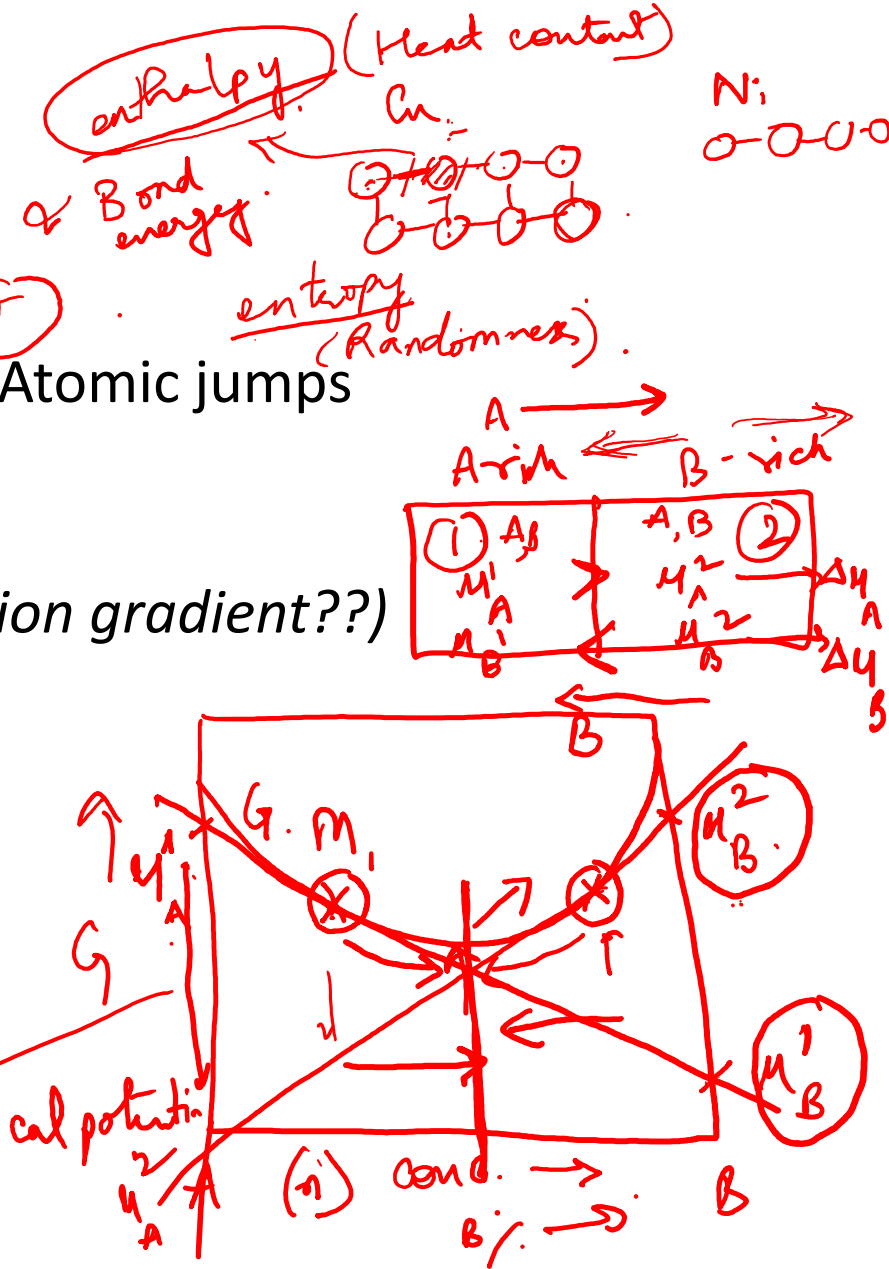
( $G_{\text{ini}}$   $G_{\text{fin}}$ )      enthalpy      entropy

( $G_{\text{ini}}$   $G_{\text{min}}$ )

$\frac{dG}{d\eta} = \mu$

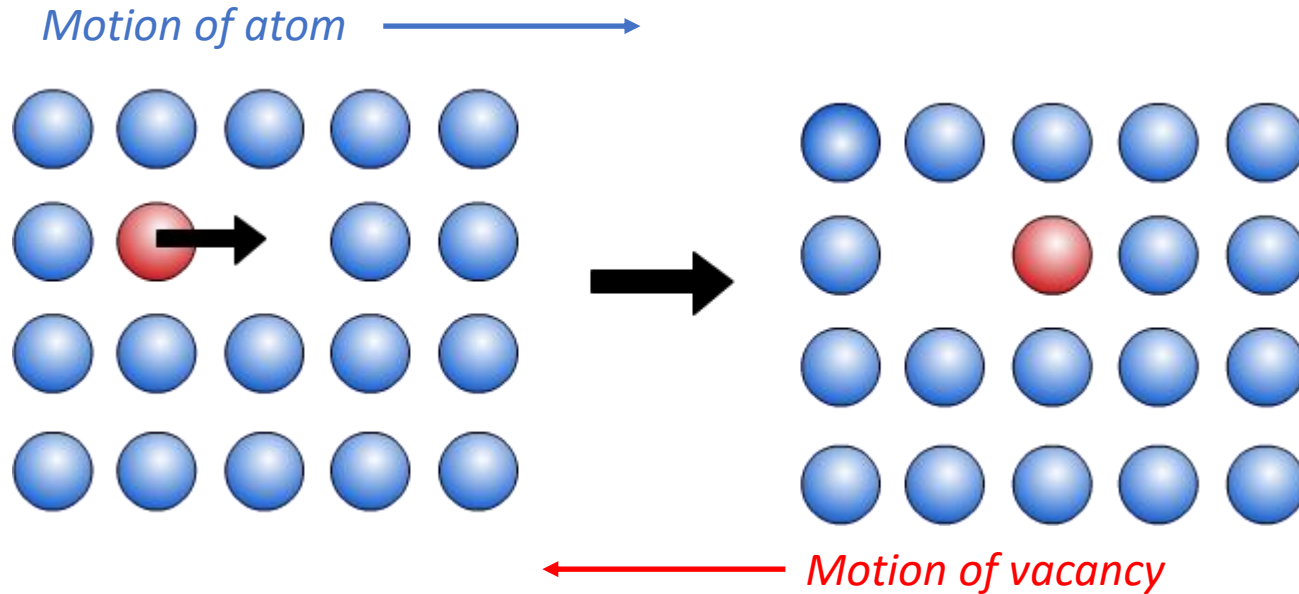
Chemical potential  $\mu$

Chemical potential gradient

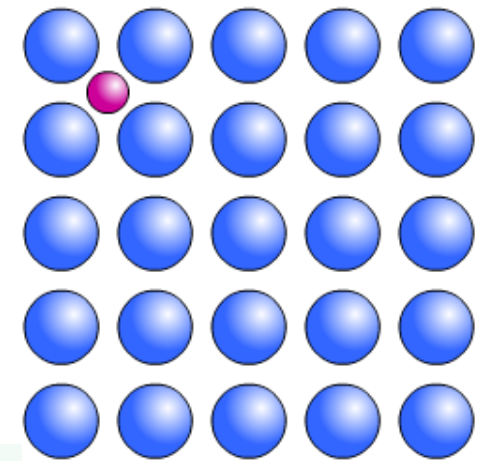


# How does diffusion occur in a solid?

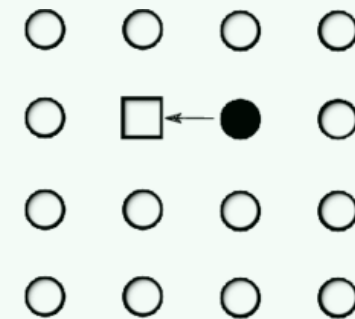
## Substitutional diffusion



## Interstitial diffusion



### Vacancy-mediated diffusion



❑ Diffusion of an atom via vacancy depends on two factors:

- How easily vacancies can form in the lattice?
- How easy it is for an atom to move into a vacancy?

❑ The dependence upon the presence of vacancies makes substitutional diffusion slower than interstitial diffusion.

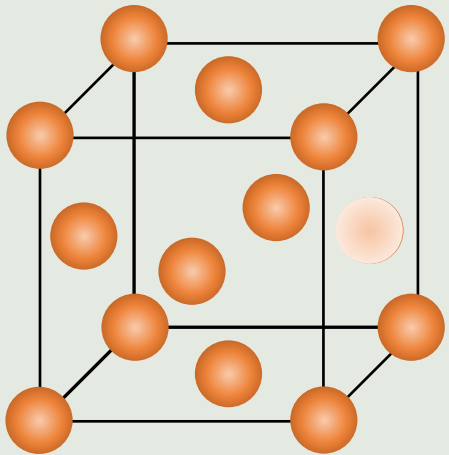
# Defects (Imperfections) in crystalline solid

Disruption in the regular arrangement of internal constituents of a solid.

Classification based on: (i) Dimensionality, (ii) Thermodynamics, (iii) Sources

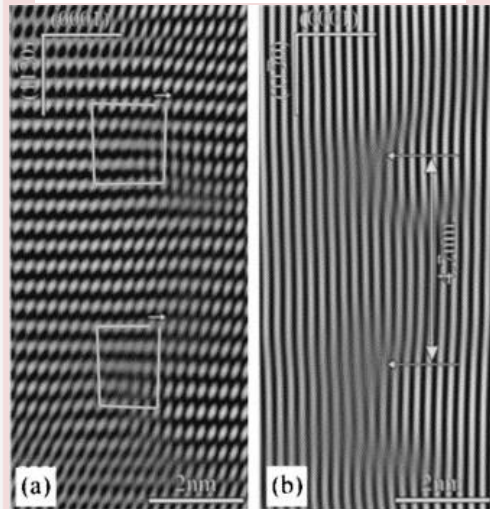
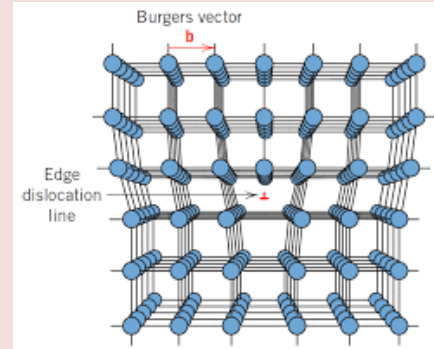
**Equilibrium defects**  
(Decreases free energy of the system)

## 0-D: Point defect

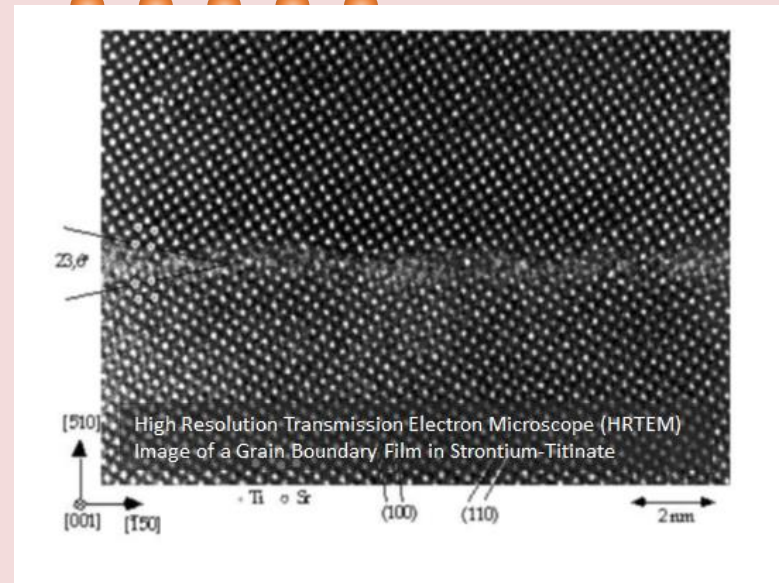


- Vacancies
- Self-interstitials

## 1-D: Line defect



## 2-D: Planar defect

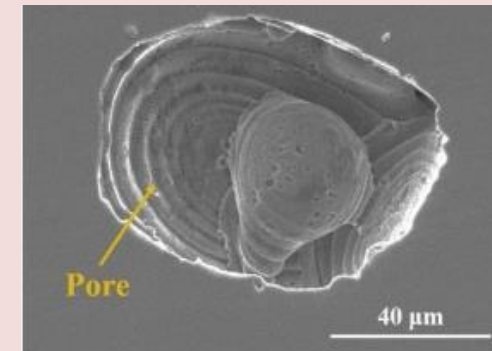


- Dislocations

**Non-equilibrium defects**

(Increases free energy of the system)

## 3-D: Volumetric defect



- Voids
- Precipitates

- Grain boundaries
- Interfaces

# Point Defects in crystalline solid

## 1. Vacancy

*(Entity missing from regular lattice site)*

## 2. Self-interstitial

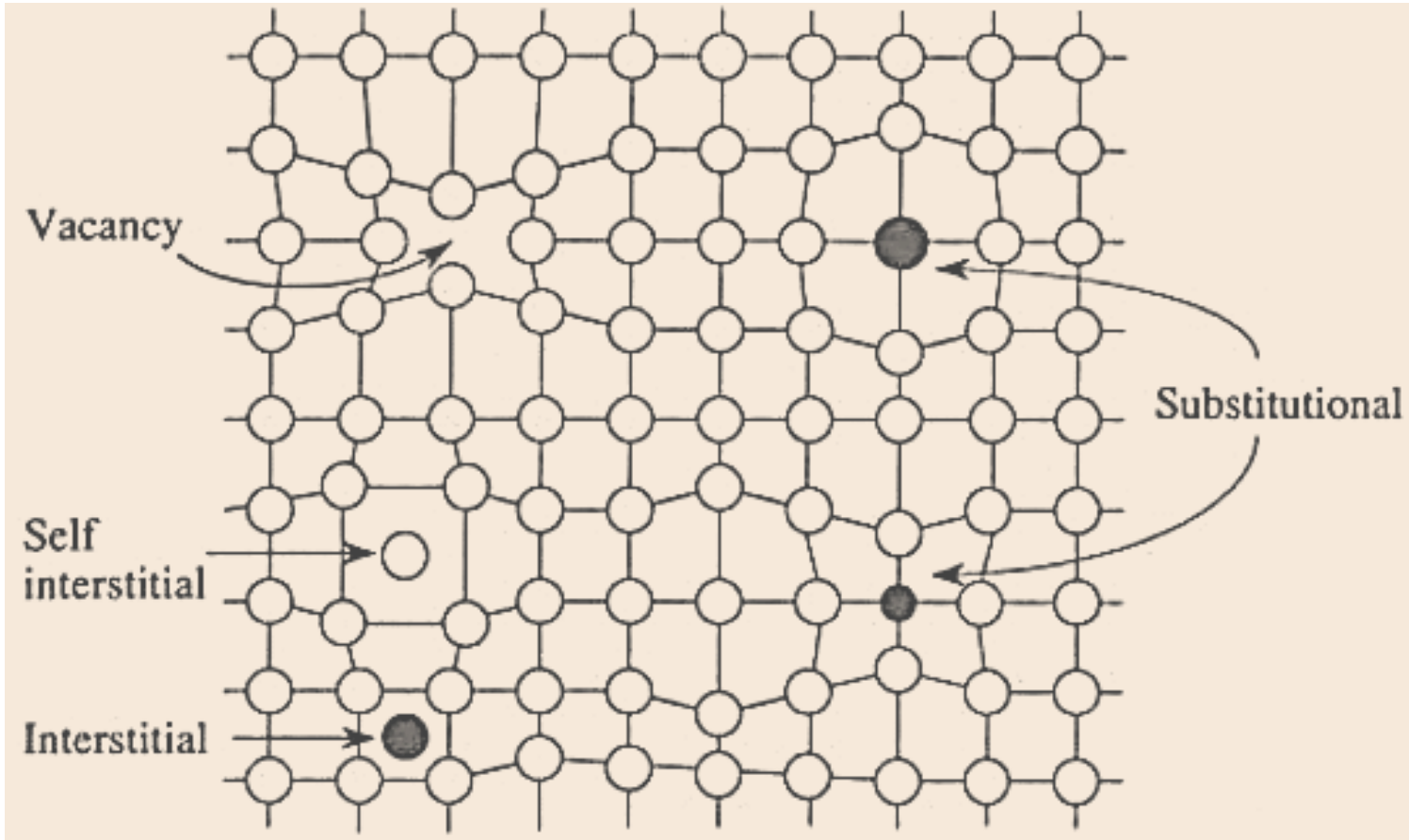
*(Lattice atoms present at interstitial sites)*

## 3. Substitutional solute

*(Foreign atoms occupying regular lattice site)*

## 4. Interstitial solute

*(Foreign atoms typically with a size much smaller than the regular atoms occupying the interstitial sites)*





# Why a vacancy is thermodynamically stable defect?

Stability of a system at a constant pressure:

Let's assume that a system at state '1' has a free energy of ' $G_1$ ' and ' $G_2$ ' at state '2':

$$G = H - T.S$$

$$G_1 = H_1 - T.S_1$$

$$G_2 = H_2 - T.S_2$$

The system would like to attain state '2' only if:

$$\text{Change in 'Free Energy'} \rightarrow \Delta G = \Delta H - T.\Delta S$$

(Energy which is available/free to do work or to transform from one phase to another)

Enthalpy change (Heat content)

Entropy change (Randomness)

*Perfect crystal*

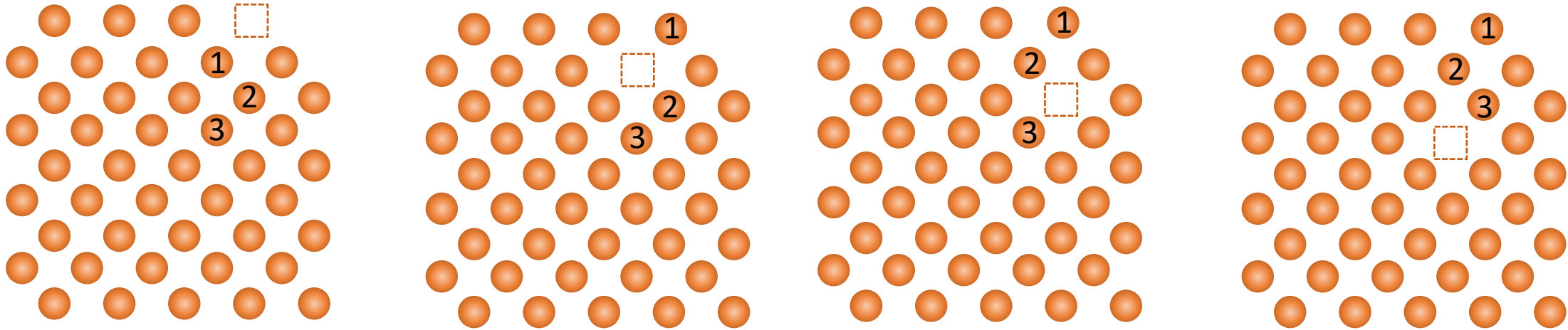


*Remove balls from random positions (vacancies)*



*Remove balls from a line (dislocations)*

## Formation of a vacancy

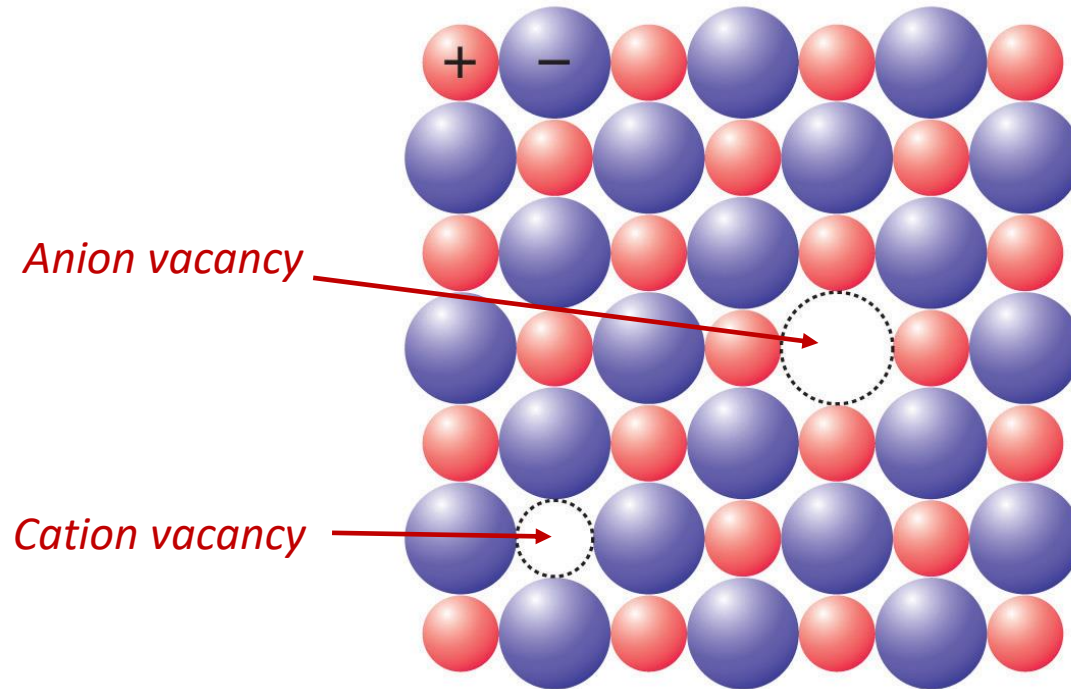


- ❑ When atoms diffuse from the interior of a crystal to the free surface, thermal vacancies get created.
- ❑ Bonds are broken because of the creation of vacancies  $\rightarrow$  Increase in enthalpy, (+ve  $H_v$ )  $\rightarrow$  Unfavourable for the system.
- ❑ Increase in entropy  $\rightarrow$  irregular vibration of atoms surrounding the vacancies and entropy of mixing (configurational entropy), i.e., different possibilities of mixing arrangements of components and vacancies.

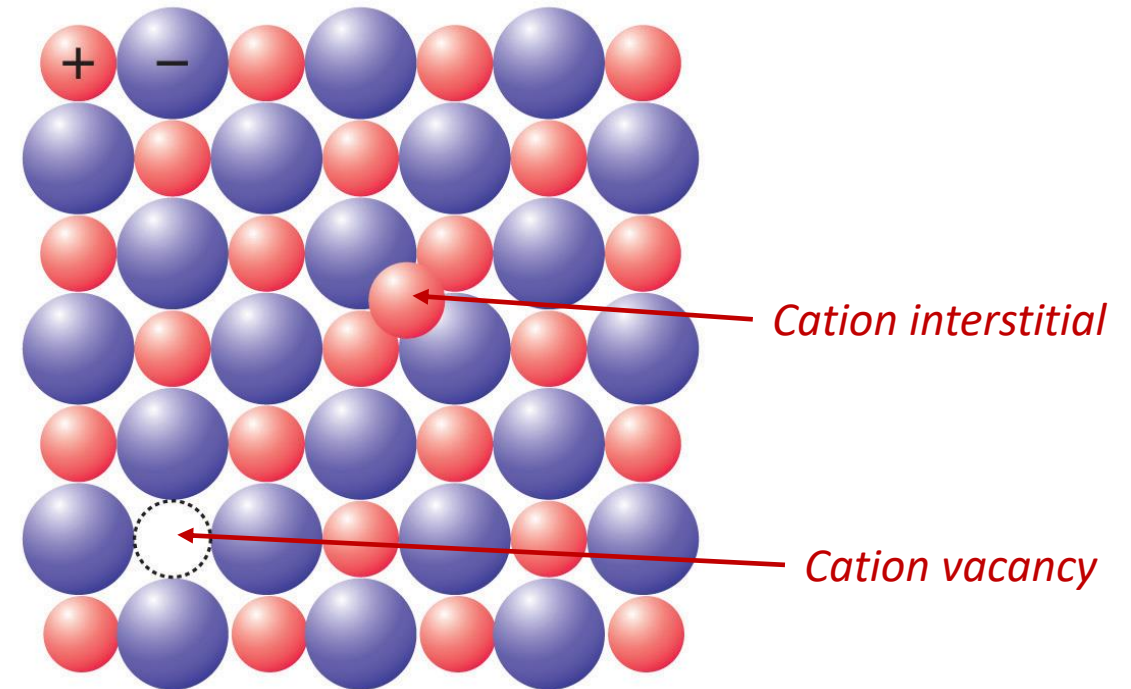
# Point defects in ionic solids

Defects in semiconductors:

- (i) Intrinsic defects (Present in a pure material at equilibrium)
- (ii) Extrinsic defects (Defects resulting because of doping/alloying)



**(a) Schottky defect**



**(b) Frenkel defect**

Creation of a vacancy in an ionic solid: Charge neutrality ----> anion vacancy + cation vacancy (Schottky defect)

----> Cation vacancy + interstitial (Frenkel defect)

# Laws of diffusion



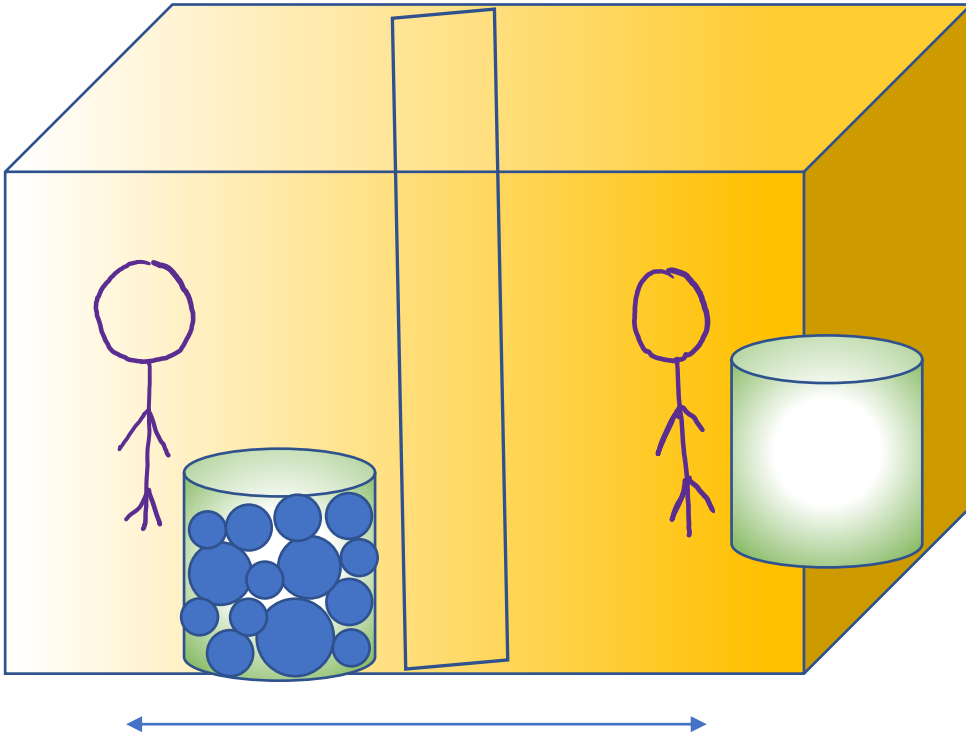
Fick's first law of diffusion

*(Empirical law)*



Fick's second law of diffusion

*(First Law + Mass balance)*



- Area of window (A) ↑
- Distance between two persons (x) ↓
- Time (t) ↑
- No. of balls (B) ↑

$$\text{Number of balls reaching to your friend} \propto \frac{(B_1 - B_2) \cdot A \cdot t}{\Delta x}$$

$$\frac{(\text{Number of balls reaching to your friend})}{A \cdot t} \propto \frac{(B_1 - B_2)}{\Delta x}$$

$$\frac{(\text{Number of balls reaching to your friend})}{A \cdot t} = (\text{property of a ball}) \cdot \frac{(B_1 - B_2)}{\Delta x}$$