

$$1) \quad P(X=k) = \frac{e^{-16} \times 16^k}{k!} \quad k = 0, 1, 2, \dots, \infty$$

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$$a) \quad P\{X \leq 8\} \leq \frac{1}{4}$$

$$= e^{-16} \sum_{k=0}^8 P(X=k) = \sum_{k=0}^8 e^{-16} \times \frac{16^k}{k!}$$

$$b) \quad \sum_{k=32}^{\infty} P(X=k) = \sum_{k=32}^{\infty} \frac{e^{-16} \times 16^k}{k!}$$

Now since $k \geq 32$

$$\frac{e^{-16} \times 16}{k} < 1$$

$$< \frac{E(X)}{32} \quad \text{By Markov's inequality}$$

$$\Rightarrow < 16 \sum_{k=32}^{\infty} \frac{e^{-16} 16^{k-1}}{32(k-1)!} < \frac{1}{2}$$

$$P \{ |x - 16| \geq k \} \leq \frac{\sigma^2}{k^2}$$

$$\sigma^2 = E(x^2) - E(x)^2$$

$$= \frac{e^{-16} 16^k k^2}{k}$$

$$\Rightarrow \frac{e^{-16} 16^k k}{k-1}$$

$$\Rightarrow \frac{\sum e^{-16} 16^k k}{k-2} + \frac{\sum e^{-16} 16^k k}{k-1}$$

$$= (16^2) + 16 - (16)^2 \rightarrow \left(E(x) \right)^2_{\text{term}}$$

$$\Rightarrow P(|x - 16| \geq 16) \leq \frac{1}{16}$$

Now $X \geq 0$

$$\text{So } P(X - 16 \geq 16) < \frac{1}{16}$$

$$P\{X \geq 32\} < \frac{1}{16}$$