

CHEMICAL KINETICS

- (1) 1) Stoichiometric coefficient (ν) is -ve for reactants and positive for products.
- 2) For time-independent stoichiometry,
 $aA + bB + \dots \rightarrow \dots yY + zZ$
- $$\frac{n_A - n_A^0}{-a} = \frac{n_B - n_B^0}{-b} = \dots = \frac{n_Y - n_Y^0}{y} = \frac{n_Z - n_Z^0}{z}$$
- 3) Extent of the reaction, $\xi = \frac{n - n^0}{\nu}$.
- 4) Rate of reaction: $\text{Rate} = \frac{1}{V} \frac{d\xi}{dt} = \frac{\dot{\xi}}{V}$
- $$= \frac{1}{\nu_i} \frac{d[P]}{dt}$$
- (if volume does not change)

(2) 1) When volume is not constant,

$$\text{rate} = \frac{1}{\nu_i} \frac{dc_i}{dt} + \frac{c_i}{\nu_i V} \frac{dV}{dt}$$

2) zero order: $aA \rightarrow P \Rightarrow [A] = -akt + [A_0]$
 $t_{1/2} = \frac{[A_0]}{2ak}$

3) First order: $[A] = [A_0] e^{-akt}$; $t_{1/2} = \frac{\ln 2}{ak}$

4) Second order: $\frac{1}{[A]} = akt + \frac{1}{[A_0]}$; $\frac{1}{ak[A_0]}$

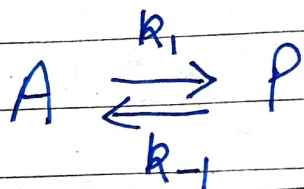
5) For n^{th} order reaction:

$$\frac{1}{[A]^{n-1}} = \frac{1}{[A_0]^{n-1}} + (n-1)kt$$

where $n = \frac{1}{2}, \frac{3}{2}, 2, 3, \dots$ and $n \neq 1$.

$$t_{1/2} = \frac{2^{(n-1)} - 1}{ak(n-1)[A_0]^{(n-1)}}$$

(L3) \Rightarrow First order opposite reactions:



(a) Rate of reaction = Rate of consumption of A = Rate of formation of P

(b) Rate of fwd reaction $v_1 = k_1[A]$
 " " bkwd " $v_{-1} = k_{-1}[P]$

Total rate of reaction = $v_1 - v_{-1}$

(c) $[P] = [A_0] - [A]$

(d) $\frac{d[A]}{dt} = -k_1[A] + k_{-1}([A_0] - [A])$

$$[A_{eq}] = \frac{k_{-1}}{k_1 + k_{-1}} [A_0]$$

When $\frac{[P]}{[A]} = K = \frac{k_1}{k_{-1}}$, the reaction is at equilibrium and rate is zero.

Integrated rate equation :

$$\frac{d[A]}{dt} = -(k_1 + k_{-1}) ([A] - [A]_{eq})$$

gives

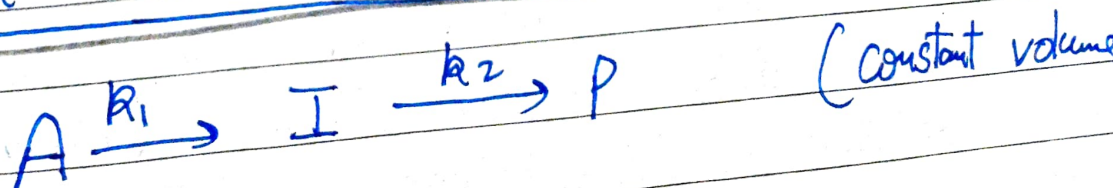
$$\rightarrow \ln ([A] - [A]_{eq}) = -(k_1 + k_{-1})t + \ln [A]_{eq}$$

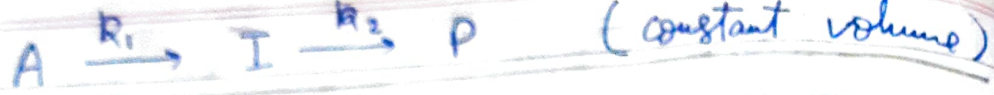
$$\rightarrow \ln \frac{[A]_{eq} - [A]}{[A]_{eq}} = -(k_1 + k_{-1})t$$

$$\rightarrow [A] = \frac{k_{-1}[A]_0}{(k_1 + k_{-1})} \left(1 + \left(\frac{k_1}{k_{-1}} \right) e^{-(k_1 + k_{-1})t} \right)$$

$$\rightarrow [P] = \frac{k_1[A]_0}{(k_1 + k_{-1})} (1 - e^{-(k_1 + k_{-1})t})$$

Consecutive first order reactions (Irreversible) :





(L4) \Rightarrow

(a) $[A] = [A_0] e^{-k_1 t}$

(b) $[I] = [A_0] \frac{k_1}{(k_2 - k_1)} (e^{-k_1 t} - e^{-k_2 t})$

(c) $[P] = [A_0] \left\{ 1 - \frac{k_2 e^{-k_1 t} - k_1 e^{-k_2 t}}{k_2 - k_1} \right\}$

(d) At all times, $[A] + [I] + [P] = [A_0]$

(e) $[I]_{\text{max.}} = [A]_0 \left(\frac{k_1}{k_2} \right) \left(\frac{k_2}{k_2 - k_1} \right)$

at
time $t_{\text{max.}} = \frac{\ln(k_2/k_1)}{(k_2 - k_1)}$

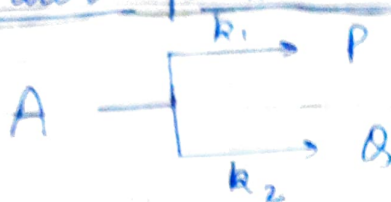
When $\frac{k_1}{k_2} \ll 1$, I acts as an unstable intermediate and $\frac{d[I]}{dt} \approx 0$

$$\Rightarrow k_1[A] - k_2[I] = 0$$

$$\Rightarrow [I]_{ss} = \frac{k_1}{k_2} A = \frac{k_1}{k_2} [A_0] e^{-k_1 t}$$

When the concentrations of intermediates (I) remain small and hardly change during most of the course of the reaction, then we can write $\frac{d[I]}{dt} \approx 0$ (The steady state approximation)

(L4) \Rightarrow First order parallel reactions:



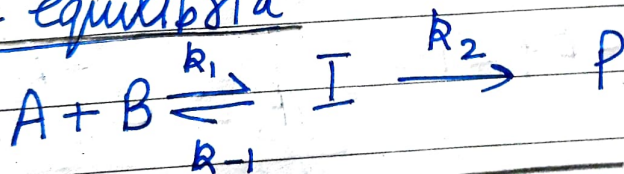
$$(a) [A] = [A]_0 e^{-(k_1 + k_2)t}$$

$$(b) [P] = \frac{k_1 [A]_0}{(k_1 + k_2)} (1 - e^{-(k_1 + k_2)t})$$

$$(c) \frac{[P]}{[Q]} = \frac{k_1}{k_2}$$

This means the composite reaction involves a pre-equilibrium.

2) \Rightarrow Pre-equilibrium



Case I: $k_{-1} \gg k_2$

$$K = \frac{k_1}{k_{-1}} = \frac{[I]}{[A][B]}$$

$$\frac{d[P]}{dt} = k_2 [I] = \frac{k_2 k_1}{k_{-1}} [A][B]$$

\therefore 2nd order.

Case II: What if "I" to "P" conversion is not too slow

$$\frac{d[P]}{dt} = k_2 [I]$$

$$\frac{d[I]}{dt} = k_1 [A][B] - k_{-1} [I] - k_2 [I]$$

$$\text{SSA} \Rightarrow [I] \approx \frac{k_1 [A][B]}{k_2 + k_{-1}}$$

~~2nd order~~

$$\Rightarrow \frac{d[P]}{dt} = k_2 [I] = \frac{k_1 k_2}{k_2 + k_{-1}} [A][B]$$

∴ 2nd order

(5) $k = A e^{-E_a/RT} = \underbrace{p}_{\text{Pre-exponential factor or frequency factor}} \underbrace{Z}_{\text{Orientation factor}} e^{-E_a/RT}$

$\underbrace{\hspace{10em}}_{\text{Collision frequency}}$

2) $A \rightarrow$ Number of times the reactants approach the activation barrier per unit time

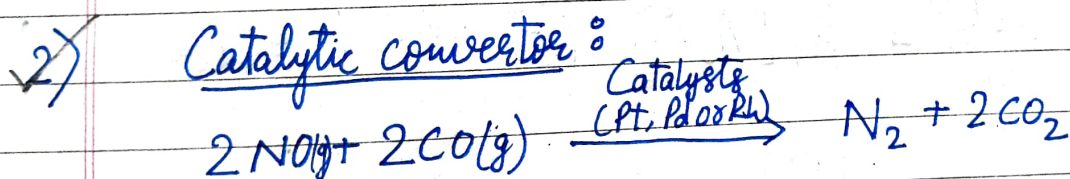
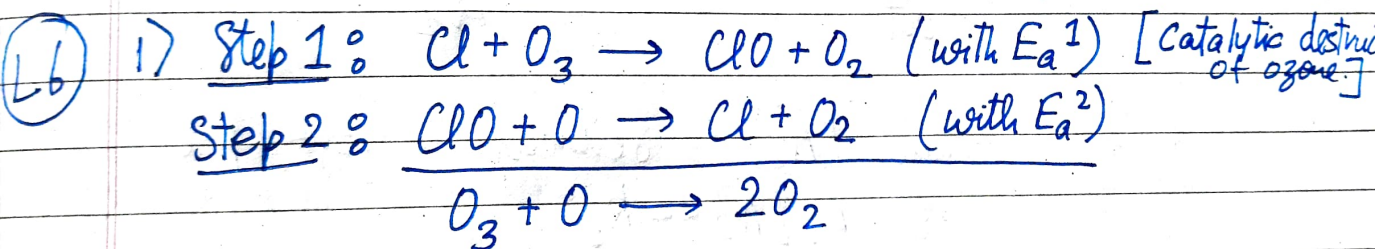
3) $e^{-E_a/RT} \rightarrow$ represents the fraction of molecules with enough energy to make it over the activation barrier on a given approach

4) $\ln\left(\frac{k_2}{k_1}\right) = \frac{E_a}{R} \left(\frac{1}{T_1} - \frac{1}{T_2}\right)$

5) Catalyst does not modify the standard Gibbs free energy change for the reaction: $\Delta G^\circ = -RT \ln K$

6) $k_{\text{catalyzed}} = k_{\text{uncatalyzed}} e^{-\Delta E_a/RT}$

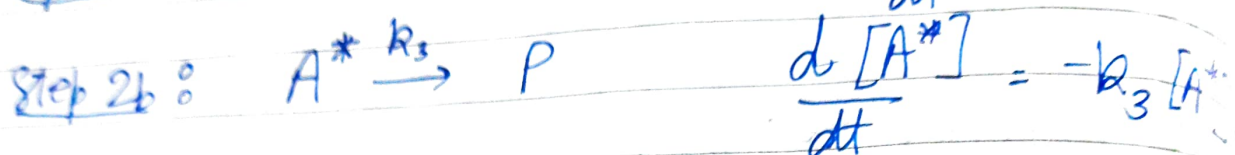
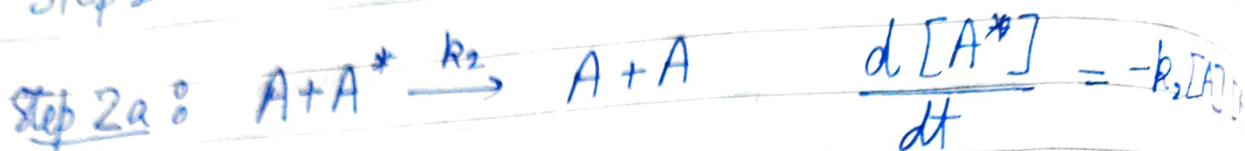
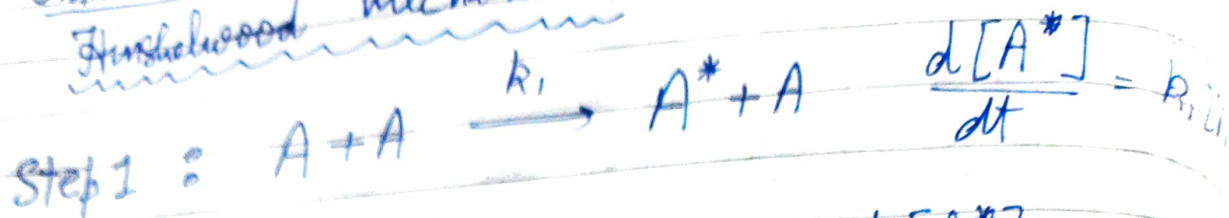
7) Degree of inhibition: $\varepsilon_i = \frac{v_0 - v}{v_0} = 1 - \frac{v}{v_0}$
($v_0 \rightarrow$ rate without inhibitor)
($v \rightarrow$ rate with inhibitor)



3) Hydrogenation of double bonds is a four-step process:
(a) Adsorption (b) Diffusion (c) Reaction (d) Desorption

4) Sucrase enzyme catalyzes breaking up of sucrose (table sugar) into glucose and fructose within the during digestion.

5/ Unimolecular Reaction Mechanism : The Lindemann-Hinshelwood mechanism



Case 1 : If step 2b is slow enough, it is overall 1st order kinetics i.e.

$$\frac{d[P]}{dt} = k[A] = \frac{k_1 k_3}{k_2} [A]$$

Case 2 : When $[A]$ is reduced to low pressure i.e. $k_2[A] \ll k_3$

$$\frac{d[P]}{dt} = k_1[A]^2 \quad \text{i.e. second order}$$

Full rate law : $\frac{d[P]}{dt} = k[A]$ where

$$\frac{1}{k} = \frac{k_2}{k_1 k_3} + \frac{1}{k_1[A]}$$