

MTL101  
LINEAR ALGEBRA AND DIFFERENTIAL EQUATIONS  
QUIZ 1

Total Marks: 10

Time: 30 Minutes

**Question 1: (4 Marks)** If  $A$  and  $B$  are two  $n \times n$  invertible matrices, such that  $A^{-1}B^{-1}AB = cI_{n \times n}$  where  $c$  is a complex number and  $I_{n \times n}$  is the identity matrix. What is the value of  $c^n$ ?

**Question 2: (3 Marks)** What is the value of the determinant

$$\det \left( \begin{bmatrix} 2a + 4b & 2a + 5b & 2a + 6b \\ 2a + 5b & 2a + 6b & 2a + 7b \\ 2a + 6b & 2a + 7b & 2a + 8b \end{bmatrix} \right)$$

**Question 3: (3 Marks)** Prove that  $W = \{(x, y, z) \in \mathbb{R}^3 \mid ax + by + cz = d\}$  is a subspace of  $\mathbb{R}^3$  if and only if  $d = 0$ .