Discrete-Time Signals and Systems

Lecture 25

$$y[n] = x[n] - x[n-1]$$

Low pass filter
High pass filter

3) All pass filter 4) Band pass filter

$$y[n] = x[n] - x[n-1]$$

1) Low pass filter	2) High pass filter
3) All pass filter	4) Band pass filter

$$y[n] = x[n] - x[n-1]$$

$$h[n] = \delta[n] - \delta[n-1]$$

$$H(e^{j\Omega}) = \sum_{k=-\infty}^{\infty} (\delta[k] - \delta[k-1])e^{-j\Omega k}$$

$$H(e^{j\Omega}) = \sum_{k=-\infty}^{\infty} (\delta[k] - \delta[k-1])e^{-j\Omega k}$$

$$H(e^{j\Omega}) = 1 - e^{-j\Omega}$$

$$H(e^{j\Omega}) = e^{-j\Omega/2} \left(e^{j\Omega/2} - e^{-j\Omega/2} \right)$$

$$H(e^{j\Omega}) = 2je^{-j\Omega/2}\sin(\Omega/2)$$

$$\left| H(e^{j\Omega}) \right| = 2|\sin(\Omega/2)|$$

$$y[n] = \frac{1}{2}(x[n] + x[n-1])$$

1) Low pass filter

2) High pass filter

3) All pass filter

4) Band pass filter

$$y[n] = \frac{1}{2}(x[n] + x[n-1])$$

1) Low pass filter

2) High pass filter

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4) Band pass filter

$$H(e^{j\Omega}) = \frac{1}{2} \sum_{k=-\infty}^{\infty} (\delta[k] + \delta[k-1])e^{-j\Omega k}$$

$$H(e^{j\Omega}) = \frac{1}{2}(1 + e^{-j\Omega})$$

$$H(e^{j\Omega}) = e^{-j\Omega/2}\cos(\Omega/2)$$

$$y[n] - ay[n-1] = x[n]$$

1) Low pass filter2) High pass filter

3) All pass filter 4) Band pass filter

$$y[n] - ay[n-1] = x[n]$$

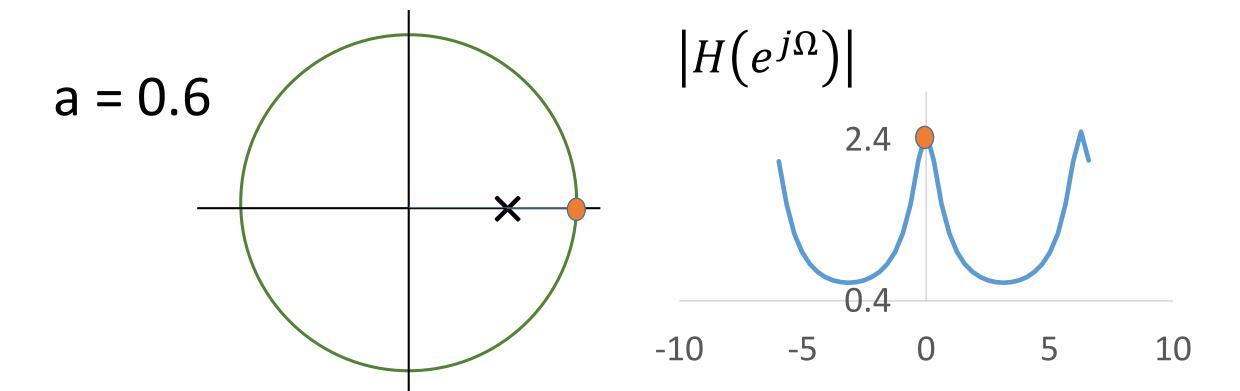
1) Low pass filter	2) High pass filter
3) All pass filter	4) Band pass filter

$$y[n] - ay[n-1] = x[n]$$

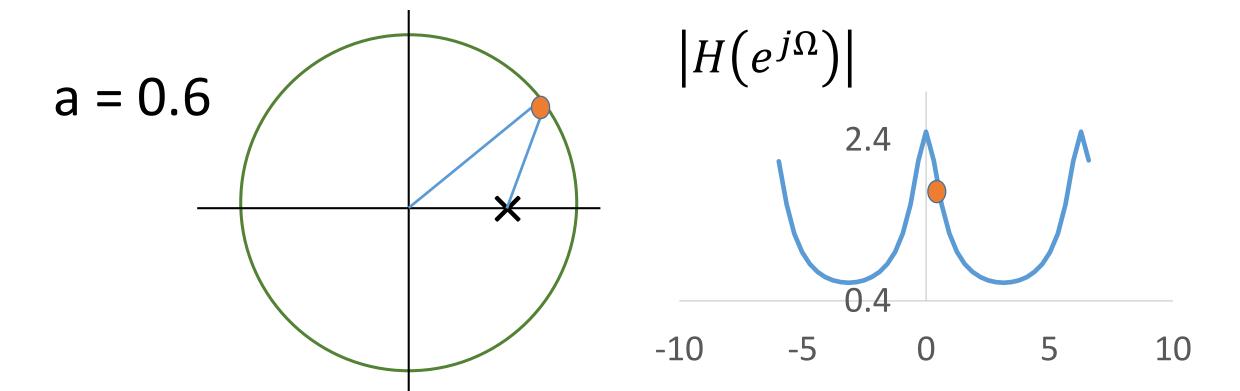
$$H(e^{j\Omega})e^{j\Omega n} - aH(e^{j\Omega})e^{j\Omega(n-1)} = e^{j\Omega n}$$

$$H(e^{j\Omega}) = \frac{1}{1 - ae^{-j\Omega}} = \frac{e^{j\Omega}}{e^{j\Omega} - a}$$

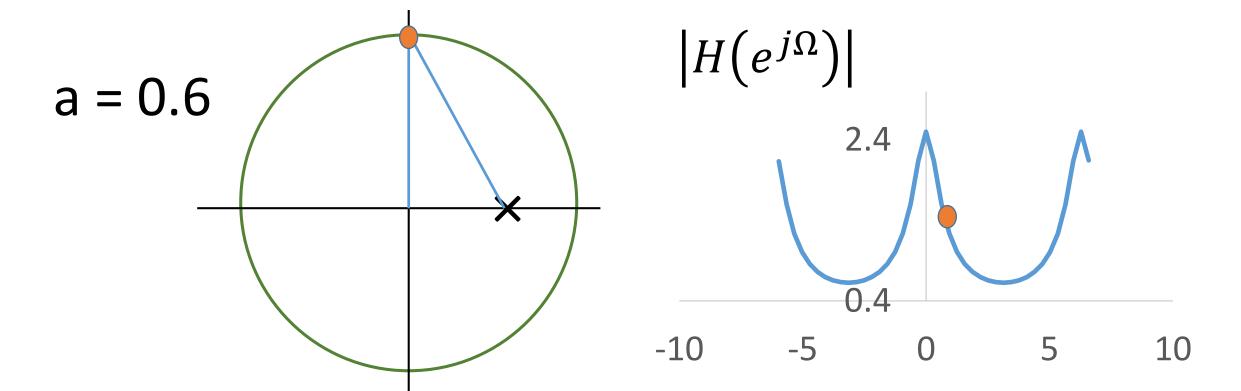
$$H(e^{j\Omega}) = \frac{e^{j\Omega}}{e^{j\Omega} - a} \quad |H(e^{j\Omega})| = \frac{Mag(Num)}{Mag(Denom)}$$



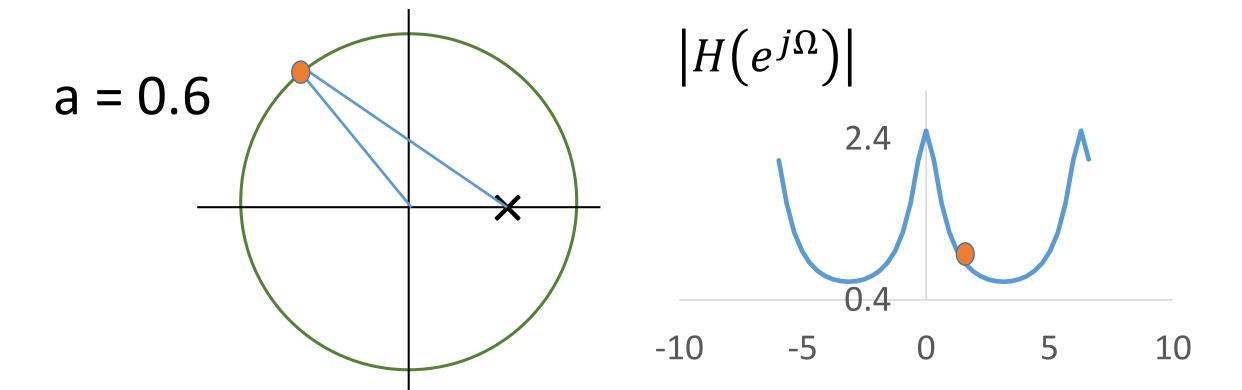
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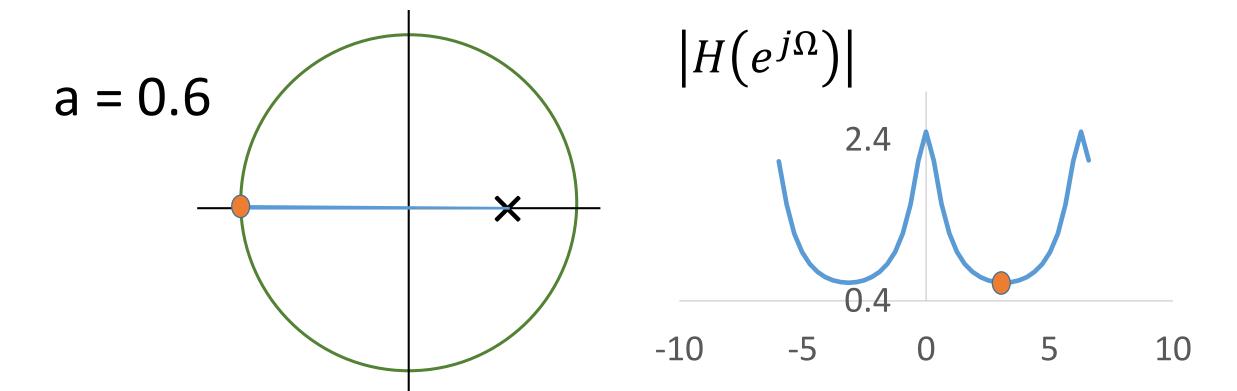
$$H(e^{j\Omega}) = \frac{e^{j\Omega}}{e^{j\Omega} - a} \quad |H(e^{j\Omega})| = \frac{Mag(Num)}{Mag(Denom)}$$



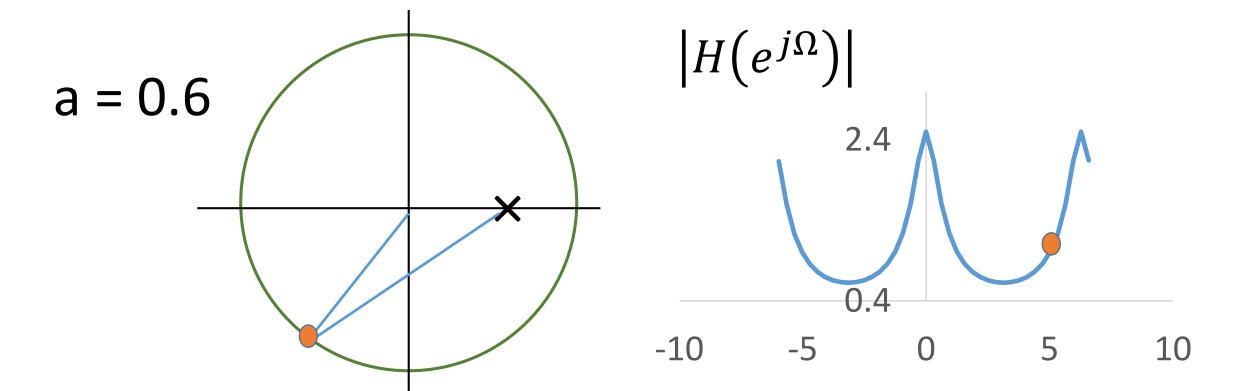
$$H(e^{j\Omega}) = \frac{e^{j\Omega}}{e^{j\Omega} - a} \quad |H(e^{j\Omega})| = \frac{Mag(Num)}{Mag(Denom)}$$



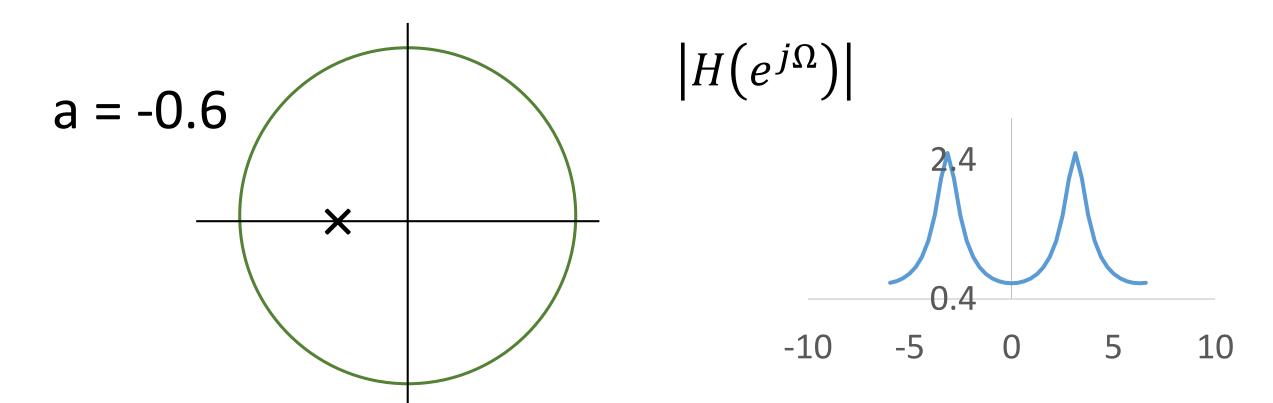
$$H(e^{j\Omega}) = \frac{e^{j\Omega}}{e^{j\Omega} - a} \quad |H(e^{j\Omega})| = \frac{Mag(Num)}{Mag(Denom)}$$



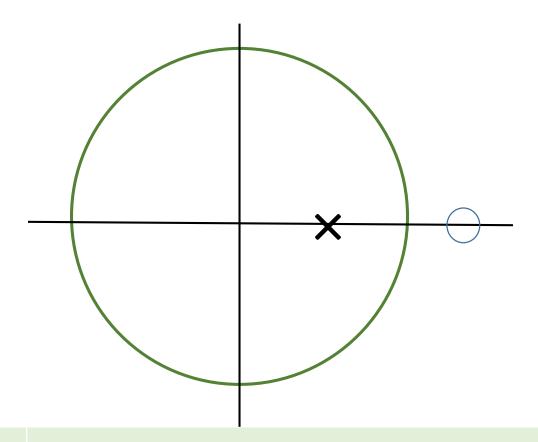
$$H(e^{j\Omega}) = \frac{e^{j\Omega}}{e^{j\Omega} - a} \quad |H(e^{j\Omega})| = \frac{Mag(Num)}{Mag(Denom)}$$



$$H(e^{j\Omega}) = \frac{e^{j\Omega}}{e^{j\Omega} - a} \quad |H(e^{j\Omega})| = \frac{Mag(Num)}{Mag(Denom)}$$



$$H(e^{j\Omega}) = \frac{e^{j\Omega} - \frac{1}{a}}{e^{j\Omega} - a}$$



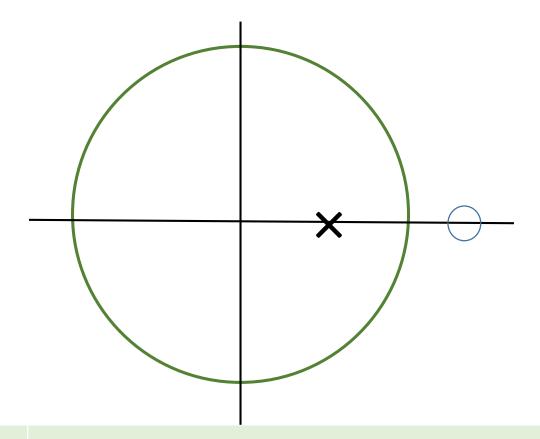
1	Low	pass filter
		pass inter

2) High pass filter

3) All pass filter

4) Band pass filter

$$H(e^{j\Omega}) = \frac{e^{j\Omega} - \frac{1}{a}}{e^{j\Omega} - a}$$



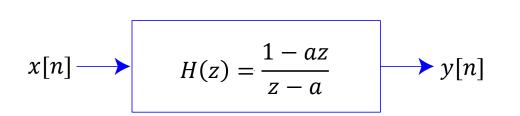
- 1) Low pass filter
- 3) All pass filter

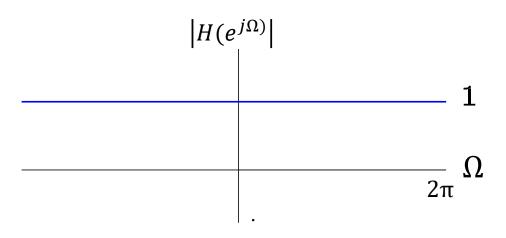
- 2) High pass filter
- 4) Band pass filter

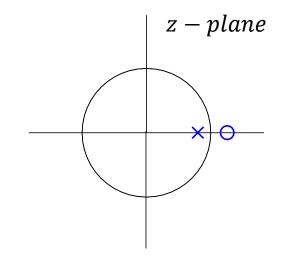
$$H(e^{j\Omega}) = \frac{e^{j\Omega} - \frac{1}{a}}{e^{j\Omega} - a} \qquad H(e^{j\Omega}) = \frac{1}{a} \frac{ae^{j\Omega} - 1}{e^{j\Omega} - a}$$

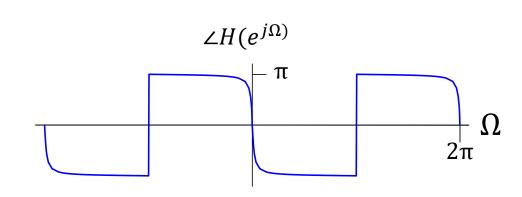
$$H(e^{j\Omega}) = \frac{1}{a} e^{j\Omega} \frac{a - e^{-j\Omega}}{e^{j\Omega} - a} \qquad |H(e^{j\Omega})| = \left| \frac{1}{a} \right|$$

Effect of all-pass filter









How does applications react to amplitude and phase distortions?

x(t) All pass filters y(t)

- Music (without phase distortions)
- Music (with phase distortions)
- Speech ('bat' without phase distortions)
- Speech ('bat' with phase distortions)

- Music (without phase distortions)
- Music (with phase distortions)
- Speech ('bat' without phase distortions)
- Speech ('bat' with phase distortions)



- Music (without phase distortions)
- Music (with phase distortions)
- Speech ('bat' without phase distortions)
- Speech ('bat' with phase distortions)



- Music (without phase distortions)
- Music (with phase distortions)
- Speech ('bat' without phase distortions)



Speech ('bat' with phase distortions)

- Music (without phase distortions)
- Music (with phase distortions)
- Speech ('bat' without phase distortions)
- Speech ('bat' with phase distortions)

