

Q 1)

$$f(\text{schedule}, n) = g(\text{schedule}, n, 1, \text{sumdays}, \text{sum}, \text{count})$$

$$g(\text{schedule}, n, 1, 0, 0, 0)$$

$$g(\text{schedule}, n, i, \text{sumdays}, \text{sum}, \text{count})$$

$$= \begin{cases} (\text{sumdays} + i) = (\text{sum} + \text{schedule}(i)) & i = n \\ g(\text{schedule}, n, i+1, \text{sumdays}+i, \text{sum} + \text{schedule}(i), \\ \text{if } (\text{sumdays} + i) = \text{sum} + \text{schedule}(i) \text{ then count} + 1 \text{ else count} & i < n \end{cases}$$

if the sum of  $n$  days till any  $k =$   
 $\text{the sum of } \sum_{i=1}^k \text{schedule}(i)$  then ~~that~~

that  $i$  has all topics well studied.

so that is what this algorithm does,

and iterates from  $i=1$  to  $i=n$ ,  
 therefore its  $O(n)$ .

Q2)

a = stk.top()

b = stk.pop()

c = x in op1

d = op1[index(op2, x)]

e = ~~Base~~ ~~is~~ ~~empty~~ stk.size() == 0

3) ~~def remove\_all(l, x):  
 if l.pop() == x:  
     remove\_all(l, x)  
 else~~

3) 1) def remove\_all(l, x):  
 a = l.pop()  
 if l == []:  
     return []  
 elif a == x:  
     return remove\_all(l, x)  
 else  
     return remove\_all(l, x).append(a)

2) Time complexity analysis:

let  $n = \text{len}(l)$

Base Case: For  $n = 0$

$T(0) = k$  (some constant)

Induction hypothesis:

~~Let  $T_n = T_{n-1} + k$  be true for  $n$~~

We claim that  $T(n) = kn + c = O(n)$

Let  $T(n)$  be true for  $n$

Induction step:

We know that during recursion, when we receive the output from the function called before, we just append 'a' to the list or not, both taking  $O(1)$  operation

Therefore

$$T_{n+1} = T_n + \textcircled{\textcircled{\textcircled{k}}}$$

$$= kn + c + k$$

$$T_{n+1} = k(n+1) + c = O(n+1)$$

Hence Proved, Time complexity is of ~~and~~  
 $O(n)$

Q4) We know that  $\sqrt{b^2 - 4ac}$  (which is used in both cases) is positive (assuming real roots)

$\therefore$  We have to take caution while we are subtracting either two positive numbers or two negative numbers both of which result in a high relative error.

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Case 1:  $b > 0$

then  $-b < 0$

In this case ~~to~~  $-b + \sqrt{b^2 - 4ac}$  is like subtracting two positive numbers, so we need to avoid this. ~~while~~ we don't need to ~~avoid~~ avoid  $-b - \sqrt{b^2 - 4ac}$

$\therefore$  when  $b > 0$

We find the roots using the formulas

$$\frac{2c}{-b - \sqrt{b^2 - 4ac}} \quad \text{and} \quad \frac{-b - \sqrt{b^2 - 4ac}}{2a}$$

Case 2:  $b < 0$

then  $-b > 0$

So in this case we have to reverse the operation and therefore we use

$$\frac{-b + \sqrt{b^2 - 4ac}}{2a} \quad / \quad \frac{2c}{-b + \sqrt{b^2 - 4ac}} \quad \left( \text{since both are additional function} \right)$$

Ahel these cases will give us ~~more~~ stable  
roots.



Q5) 1) def isReachable( $x_1, y_1, x_2, y_2$ ) :

if  $x_1 == x_2$  and  $y_1 == y_2$  :

~~then~~ return ~~True~~ True

elif  $x_1 > x_2$  or  $y_1 > y_2$  :

return ~~False~~ False

else

return isReachable( $x_1 + y_1, y_1, x_2, y_2$ ) or

isReachable( $x_1, x_1 + y_1, x_2, y_2$ )

2) Correctness proof

Base case :

$x_1 > x_2$  or  $y_1 > y_2 = \text{False}$

$x_1 == x_2$  and  $y_1 == y_2 = \text{True}$

~~Induction~~

We use recursion to show that if both the base cases are not the current case, we

go along both the paths ( $x+y, y$ ) and ( $x, x+y$ )

So finally we will have output of all paths separated by (or)

i.e. Path1 or Path2 or Path3 or ... or Path $n$

if even 1 of these Paths are true (can make us reach airport), we return true

If none of the Paths are true,

we return false. Hence we get correct output

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6) 1) def nonOverlappingIntervals(intervals):
    a = [intervals[0]]
    for i intervals in range(1, len(intervals)):
        if intervals[i][0] <= a[-1][1]:
            a[-1][1] = intervals[i][1]
            if intervals[i][1] > a[-1][1]:
                a[-1][1] = intervals[i][1]
        else:
            do
            a.append(intervals[i])
    return a

```

2) Correctness Proof:

We first initialise  $a$  with first element of intervals.

We know that intervals ~~is~~ is sorted according to the starts i.

If the start of  $i^{\text{th}}$  element  $<$  end of  $i-1^{\text{th}}$  element, we merge them.

So we iterate  $i$  from 1 to  $\text{len(intervals)}-1$

Now if the last element of  $a = c$  (i.e.  $a[-1] = c$ )  
 if  $c[1] \geq \text{intervals}[i][0]$  we have to merge them; Now if intervals[i] is totally included in  $c$ , we don't need to alter  $c$



but if the intervals  $[i]$ 's end is larger than  $[i]$ 's end (intervals  $[i][i] > c[i]$ )

we have to increase  $c[i]$  to intervals  $[i][i]$ ,  
so that's what we do.

We do this ~~set~~ till  $i = \text{len}(l)$ , and  
we get a ~~merged~~ non overlapping intervals  
list.

Hence Proved.

Q7) def getLargest(self):

~~x~~ x = None  
y = None

if ~~root~~ ~~self~~ is instance (~~self~~.left, ~~TreeNode~~):  
~~x = self.getLargest()~~  
x = ~~self~~.left.getLargest()

~~if isInstance (root, int)~~  
elif isinstance (~~self~~.left, int)  
x = ~~self~~.left

~~if~~ if isinstance (~~self~~.right, ~~TreeNode~~):  
y = ~~self~~.right.getLargest()  
elif isinstance (~~self~~.right, int):  
y = ~~self~~.right

if x != None and y != None:  
return max(x, y)

elif x == None and y != None:  
return y

elif x != None and y == None:  
return x

else  
return None

## 2) Correctness Proof :

First we check that if ~~either of~~ <sup>self</sup> left ~~is~~ is a node or not, if it is, we find the max of that node and assign  $x = \text{self.left.getLargest()}$ .  
If its an integer we assign  $x = \text{self.left}$ .  
else  $x = \text{None}$

similarly we get values for y recursively

~~Now~~ Now ~~of~~ having both the value of max of left and right node,

We check that if both are not None, we ~~give~~ <sup>return</sup>  $\max(x, y)$

if one of them is None,  
we return the other one,  
else we return None.

So we recursively obtain the maximum of all the nodes ~~of~~ as ~~the~~  $x$  and  $y$  themselves with the max of <sup>left</sup> branch and right branch respectively.