

## Assignment-1 Instructions

1. Last date of submission 5-February-2019
2. For question number (2), you have to submit program (.m or .py file) and plot.
3. For question number (1, 3, 4), you have to submit a pdf file.
4. Upload all the documents (program, plot, pdf) as a single zip file with your name and roll number in the file name (e.g. Rahul\_16126.zip)

## Assignment-1 - 10Marks

(1) For what value of 'a' in the equation below will give rise to (a) stable equilibrium point (asymptote), (b) stable oscillations, and (c) unstable oscillations.

$$N(t+1) = a N(t) (1 - N(t))$$

**Note:** For the stable asymptote the eigen value  $\lambda$  should be  $0 < \lambda < 1$ . For stable oscillations eigen value  $\lambda$  should be  $-1 < \lambda < 0$ . For unstable oscillations eigen value  $\lambda$  should be  $-1 > \lambda$ . (2M)

(2) (a) Write MATLAB/Python codes to get the cobweb plots ( $N(t+1)$  Vs  $N(t)$  space) for each of the cases mentioned in Q(1).  
(b) Also provide the  $N(t+1)$  vs  $t$  for the corresponding 'a' values.  
(c) Draw the bifurcation diagram ( $N(t)$  Vs 'a') for a values ranging from 1.4 to 4 in steps of 0.01. (4M)

(3) For the equation  $N(t+1) = N(t) e^{(r(K-N(t))/K)}$ , find the value of 'r' for which the equation will exhibit oscillations. (2M)

(4) For the continuous logistic equation the solution is given as

$$N(t) = \frac{K}{1 + \left( \frac{K - N(0)}{N(0)} \right) e^{-rt}}.$$

Express  $N(t+1)$  as a function of  $N(t)$  (2M)