



# AKTU

## B.Tech I-Year



### Electrical Engg.

### ONE SHOT Revision

#### Unit-1

#### DC Circuits



Avinash Sir

# Fundamentals of Electrical Engineering

## Unit-1 : DC Circuits

### AKTU Syllabus

Electrical circuit elements (R, L and C), Concept of active and passive elements,  
Voltage and current sources, concept of linearity, unilateral and bilateral  
elements.  
Kirchhoff's laws, Mesh and nodal methods of analysis.

# Active Elements & Passive Elements

① **Active Elements**:- Elements that can provide energy to the networks.

Examples: Voltage Source & Current Source, Battery

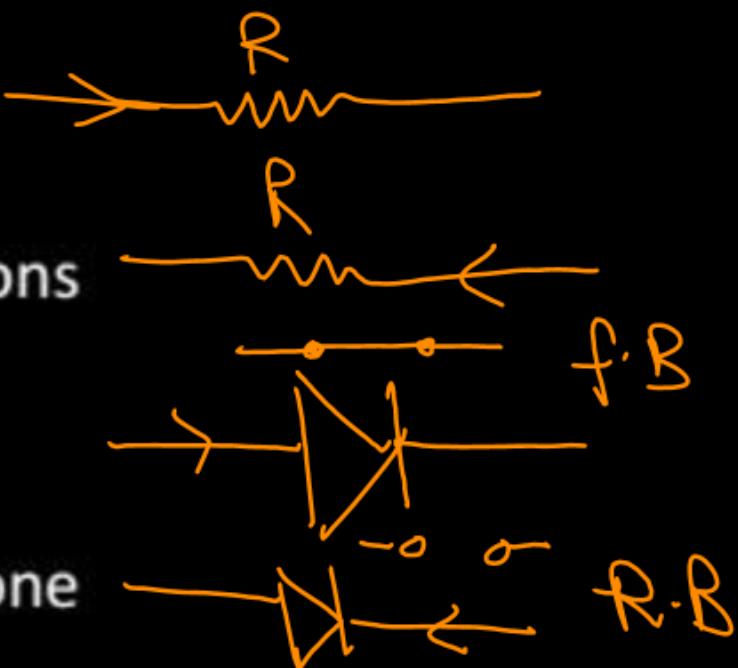
- **Passive Elements**:- Elements that can which can only receive energy, which it can either dissipate, absorb or store it in an electric field or a magnetic field.

Examples: R,L,C - Resistance - dissipate , Inductor & Capacitor → Energy store

② **Bilateral Element & Unilateral Element**

**Bilateral Element**:- Elements which allows current to flow from both directions are known as Bilateral Element. (Examples: Resistance)

**Unilateral Element**:- Elements which allows current to flow only from one direction are known as Unilateral Element . (Examples: Diode)

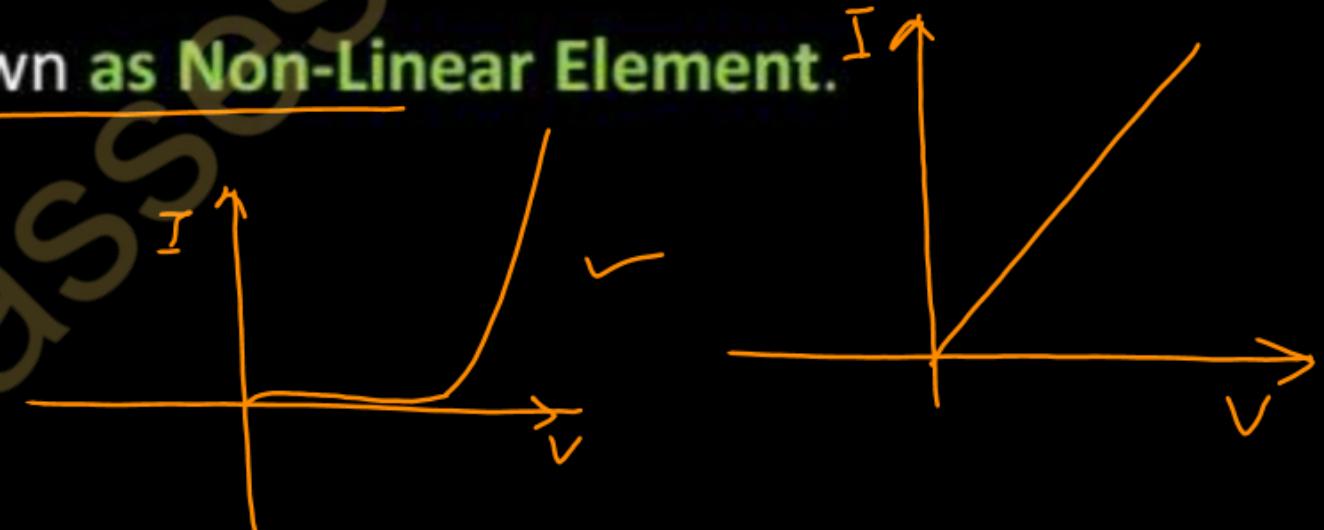


## Linear and Non Linear Elements

③ **Linear & Non Linear Element** - An Element is said to be linear, if it obeys the principle of homogeneity and superposition, Otherwise it is known as Non-Linear Element.

**Examples:** Resistance (Linear) , diodes (Non-Linear)

Lumped and Distributed network  
Semi conductor



**Lumped Network**:-A network in which all the network elements are physically separable is known as a lumped network.

**Examples:** - Network having Resistance ,Inductor or Capacitor etc

**Distributed Network** - A network in which network elements can not be physically separable is known as **Distributed network** like Transmission Line.

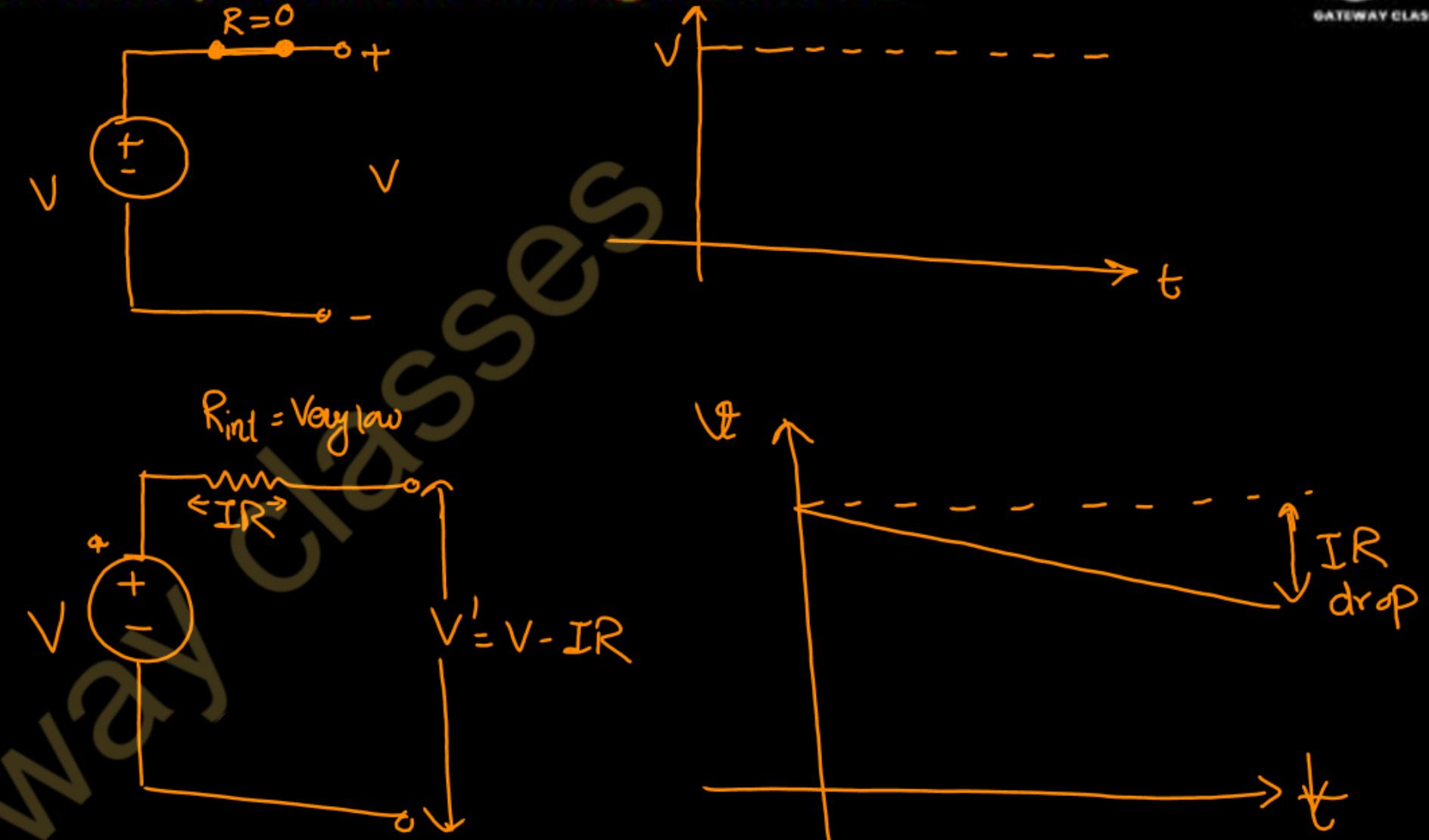
# Voltage Source: Ideal and practical Voltage source

**Ideal Voltage source:-** Energy Source

which provide constant voltage across its terminals irrespective of current drawn through its terminals.

It has Zero Internal Resistance

**Practical Voltage Source:-** A practical voltage source has small internal resistance due to which voltage across terminals decrease slightly with increase in current.



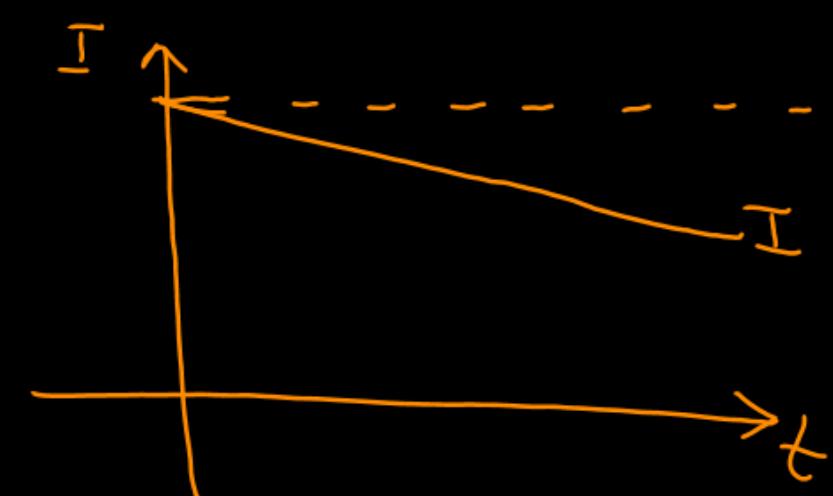
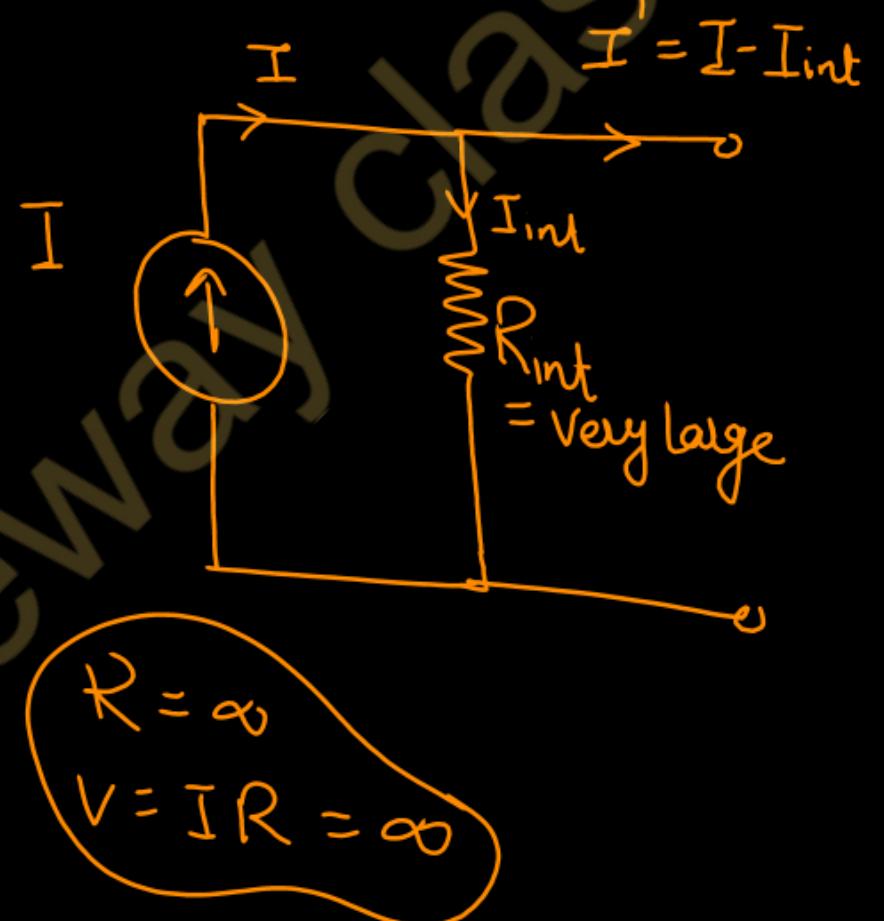
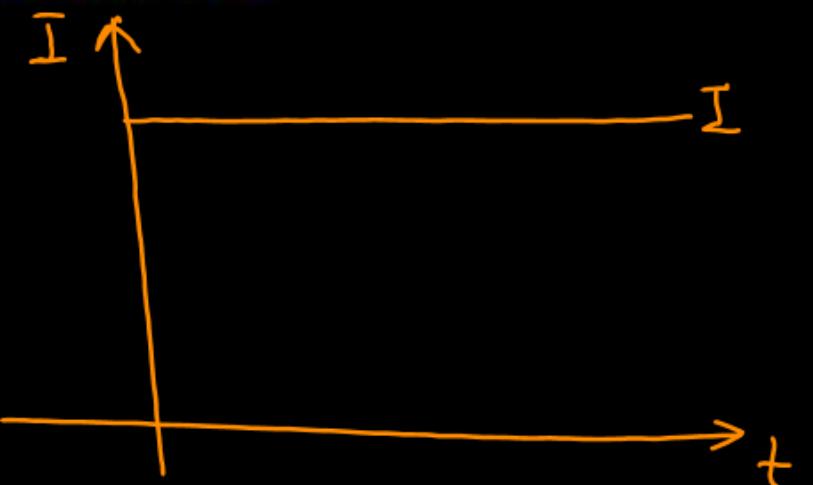
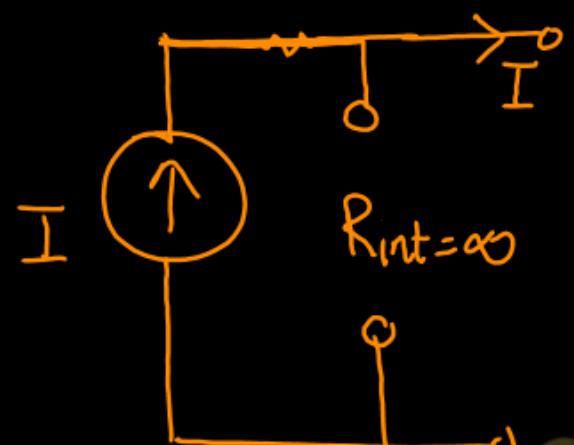
# Current Source: Ideal and Practical Current source

**Ideal Current source:-** Energy

Source which provide constant Current across its terminals irrespective of current drawn through its terminals.

*It has infinite Internal Resistance.*

**Practical Current Source:-** A practical Current source has very high internal resistance due to which Current across terminals decrease slightly with increase in voltage.



$$\begin{aligned} I_1 + I_2 + I_3 \\ = I_4 + I_5 \end{aligned}$$

**Kirchhoff's Current Law:-** According to Kirchhoff's Current Law, algebraic sum of ALL the currents entering and leaving a node must be equal to zero,  $I_{(\text{exiting})} + I_{(\text{entering})} = 0$ .

Nodal Analysis

$$(I_4 + I_5) - I_1 - I_2 - I_3 = 0$$

**Kirchhoff's Voltage Law:-** According to Kirchhoff's Voltage Law, The voltage around a loop equals the sum of every voltage drop in the same loop for any closed network and equals zero.

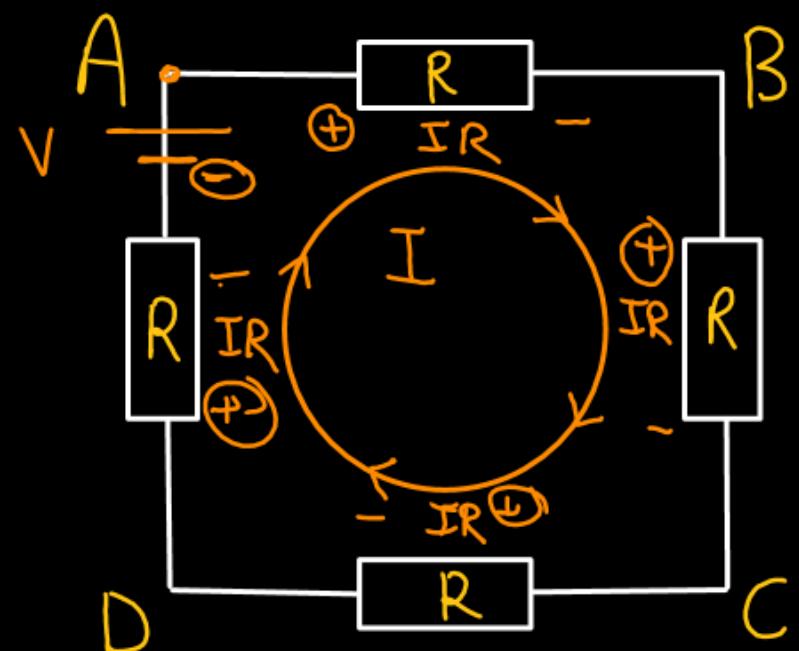
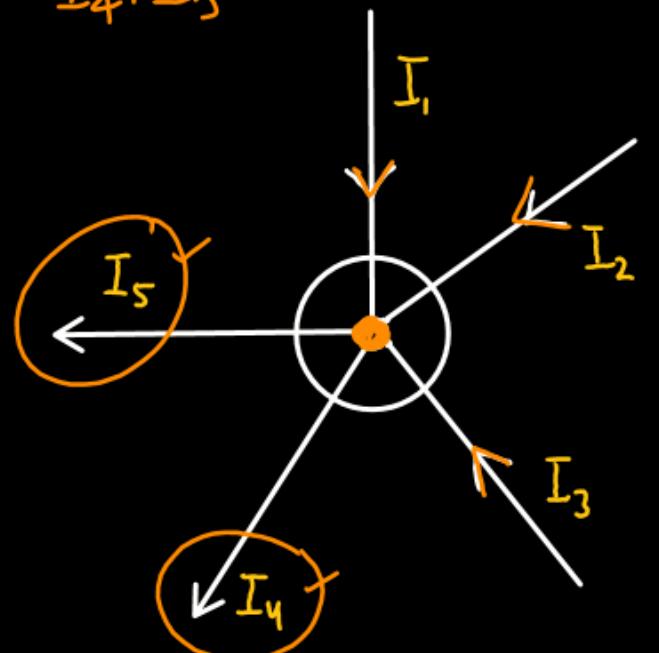
Mesh Analysis

**Why We can not apply KVL in a loop having Current Source.**

**Ans.**

NO

$$IR + JR + IR + IR - V = 0$$



# Ques. Explain the procedure of mesh analysis with the help of an example

Step-1- Identify loops in given circuit

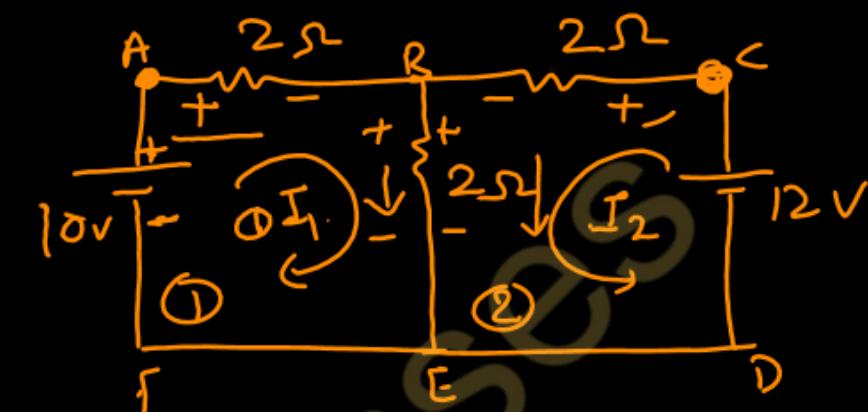
Step-2 Consider loop current in mesh ( $I_1, I_2$ )

Step-3 (optional) → mark polarity on each resistance

Step-4 Apply KVL in each ~~loop~~ mesh one by one

Step-5 - Now we have one equation from each mesh

Step-6 Solve all equations to find mesh currents.



Apply KVL in mesh ①

$$+2I_1 + 2(I_1 + I_2) - 10 = 0$$

$$4I_1 + 2I_2 = 10 \quad \text{---} ①$$

Apply KVL in mesh ②

$$+2I_2 + 2(I_2 + I_1) = 12$$

$$2I_1 + 4I_2 = 12 \quad \text{---} ②$$

(AKTU-2023-24)

Loop → Any closed path

Mesh → shortest closed path loop that does not contain any other loop

$$I_1 = 1.33 \text{ A}$$

$$I_2 = 2.33 \text{ A}$$

# Ques. Explain the procedure of Nodal analysis with the help of an example.

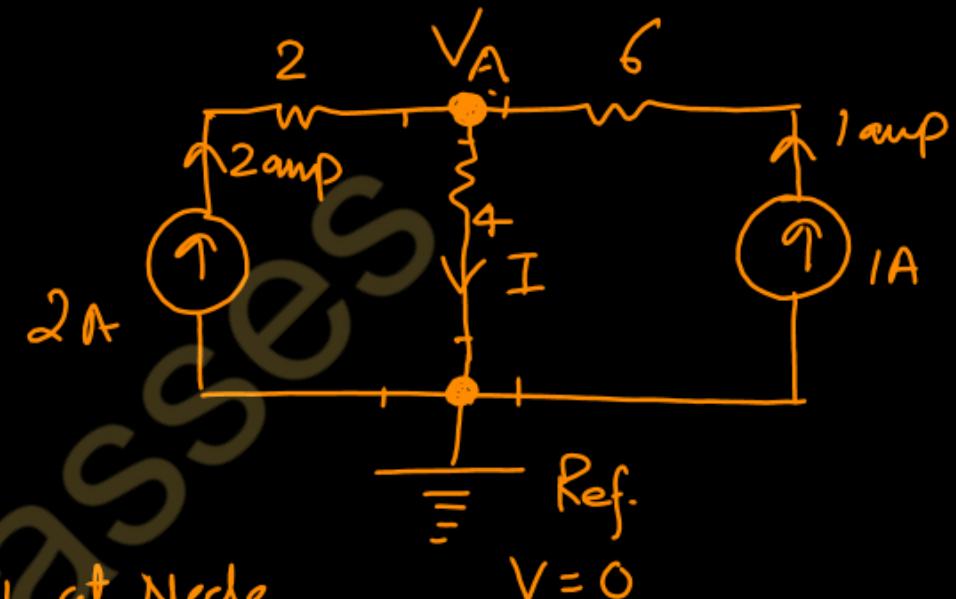
Step-1 Identify junction in the circuit

Step-2 Consider one junction at reference ( $V=0$ )  
and rest junction voltages should be considered

Step-3 Now assume random branch current with random direction

Step-4 Now apply KCL at each node

Step-5 Solve these equations to find Node Voltages and currents.



Apply KCL at Node

$$1+2 = I$$

$$\boxed{I = 3} \text{ amp}$$

$$I = \frac{V_A - 0}{4} = \frac{V_A}{4}$$

$$V_A = 4I = 4 \times 3 = 12 \text{ Volt}$$


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Junction - where 3 or more branches meets

Node → where 2 or more branches meets

# Mesh Analysis(KVL): Numerical Problems

**Q.1 Using Mesh Analysis Find Current in all branches.**

Apply KVL in Supermesh

$$+5I + 2(I+5) + 6(I+5+I_1) - 60 = 0$$

$$5I + 2I + 10 + 6I + 30 + 6I_1 - 60 = 0$$

$$13I + 6I_1 = 20 \quad \text{--- } \textcircled{1}$$

Apply KVL in loop  $\textcircled{3}$

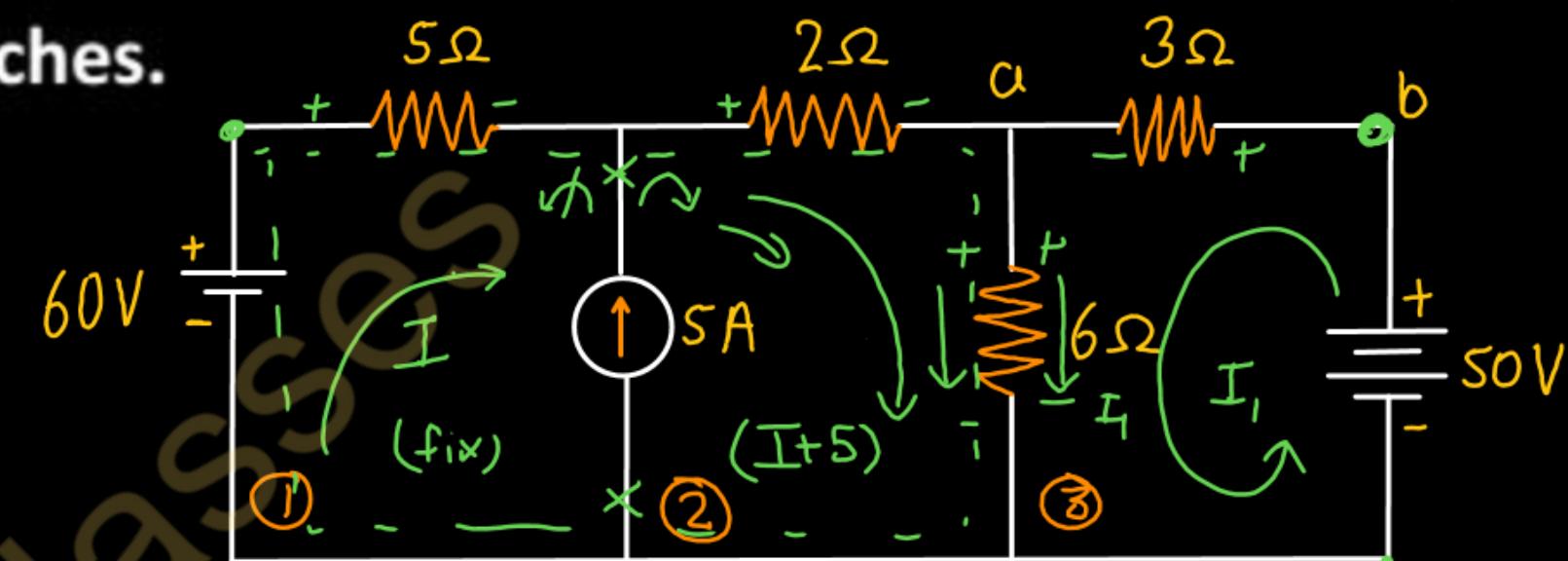
$$+3(I_1) + 6(I_1 + I + 5) - 50 = 0$$

$$3I_1 + 6I_1 + 6I + 30 - 50 = 0$$

$$6I + 9I_1 = 20 \quad \text{--- } \textcircled{2}$$

Solve Eqn  $\textcircled{1} \& \textcircled{2}$

$$\begin{aligned} I &= 0.74 \text{ Amp} \\ I_1 &= 1.72 \text{ Amp} \end{aligned} \quad \left\{ \text{Ans} \right.$$



# Mesh Analysis(KVL): Numerical Problems

**Q.2 Using Mesh Analysis Find Current in  $20\Omega$  resistance. ( AKTU-2023-24)**

Apply KVL in Loop ①

$$5I_1 + 10(I_1 - I_2) = 20$$

$$15I_1 - 10I_2 = 20 \quad \text{---} ①$$

Apply KVL in Loop ②

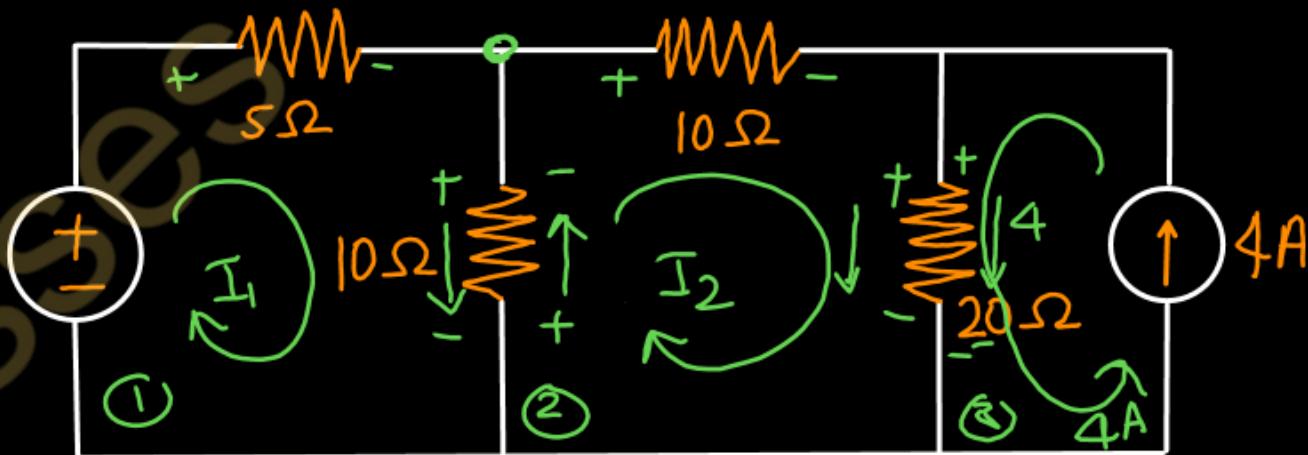
$$+10(I_2) + 20(I_2 + 4) + 10(I_2 - I_1) = 0$$

$$-10I_1 + 40I_2 = -80 \quad \text{---} ②$$

Solve Eqn ① & ②,

$$I_1 = 0$$

$$I_2 = -2 \text{ Amp}$$



$$I_{20\Omega} = I_2 + 4$$

$$\boxed{I_{20\Omega} = 2 \text{ Amp}}$$

Amp

# Mesh Analysis(KVL): Numerical Problems

**Q.3 Using Mesh Analysis Find Current in 6 ohm Resistance.**

Apply KVL in Loop ①

$$+3I_1 + 6(I_1 - I_2) = 6$$

$$9I_1 - 6I_2 = 6 \quad \text{---} ①$$

Apply KVL in Loop (2 & 3) (supermesh)

$$2(I_2) + 1(I_2 + 3) + 4(I_2 + 3) + 6(I_2 - I_1) = 0$$

$$-6I_1 + 13I_2 + 15 = 0$$

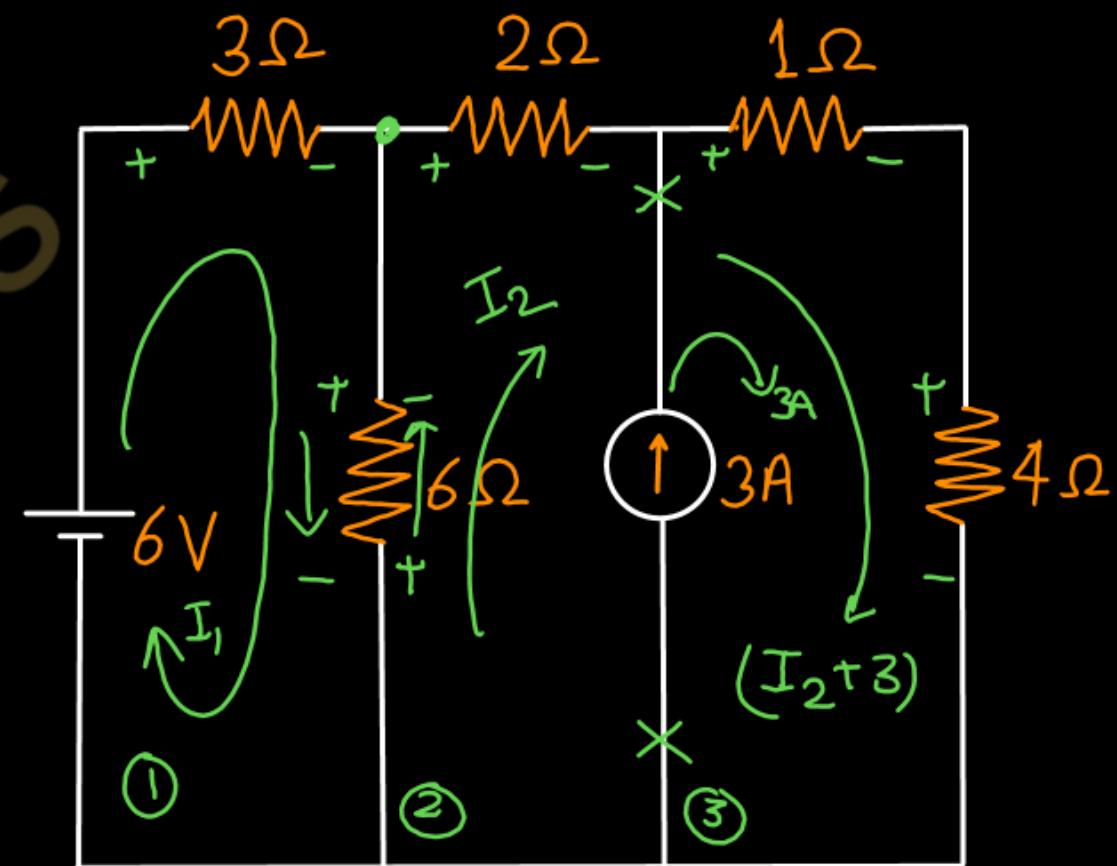
$$-6I_1 + 13I_2 = -15 \quad \text{---} ②$$

Solve Eqn ① & ②

$$I_1 = -0.148 \text{ A}$$

$$I_2 = -1.22 \text{ Amp}$$

$$\begin{aligned} I_{6\Omega} &= (I_1 - I_2) \\ &= -0.148 + 1.22 \\ I_{6\Omega} &= 1.072 \end{aligned}$$



## Q.4 Determine the currents in all branches of the circuit as shown in below figure,

using Mesh current method? (AKTU 2023-24)

Apply KVL in loop ①

$$+30(I_1 - I_3) + 50(I_1 - I_2) + 20 - 100 + 60(I_1) = 0$$

$$140I_1 - 50I_2 - 30I_3 = 80 \quad \text{---} ①$$

Apply KVL in Loop ②

$$+40(I_2 - I_3) + 10(I_2) - 50 - 20 + 50(I_2 - I_1) = 0$$

$$-50I_1 + 100I_2 - 40I_3 = 70 \quad \text{---} ②$$

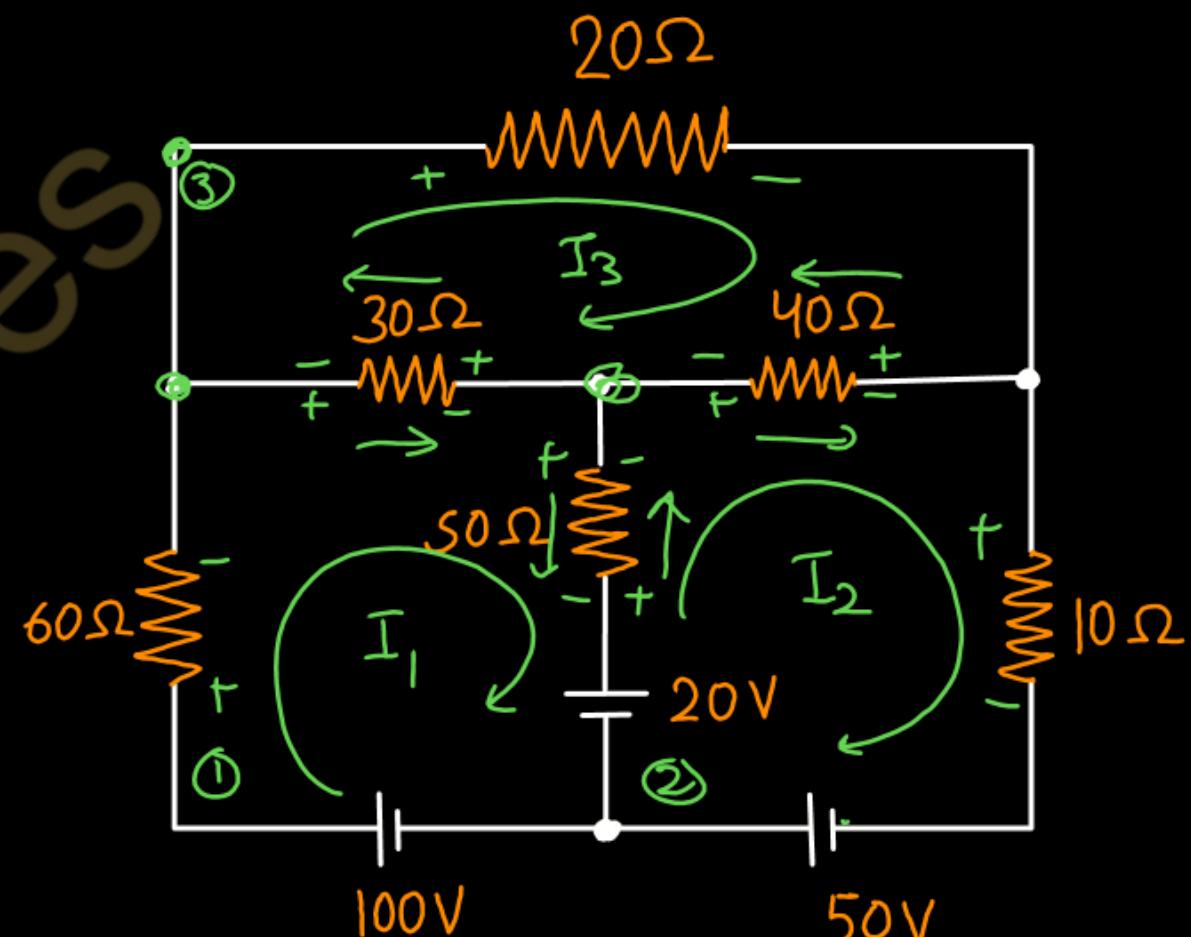
Apply KVL in loop ③

$$+20I_3 + 40(I_3 - I_2) + 30(I_3 - I_1) = 0$$

$$-30I_1 - 40I_2 + 90I_3 = 0 \quad \text{---} ③$$

Solve eqn ①, ② &amp; ③

$$I_1 = 1.65A, I_2 = 2.12A, I_3 = 1.49A$$



**Q.5 Determine the set of Mesh equations that are required to solve the network given in below circuit diagram. AKTU 2022-23**

Apply KVL in Loop ①  $I_3 = -3A$

$$+2I - 12 + 5(I_1 + 3) = 0$$

$$2I + 5I_1 = 27 - 3 \quad ①$$

Apply KVL in Loop ②

$$+6 - 2I + 6(I_2 + 3) = 0$$

$$6 - 2I + 6I_2 + 18 = 0$$

$$-2I + 6I_2 = -24 \quad ②$$

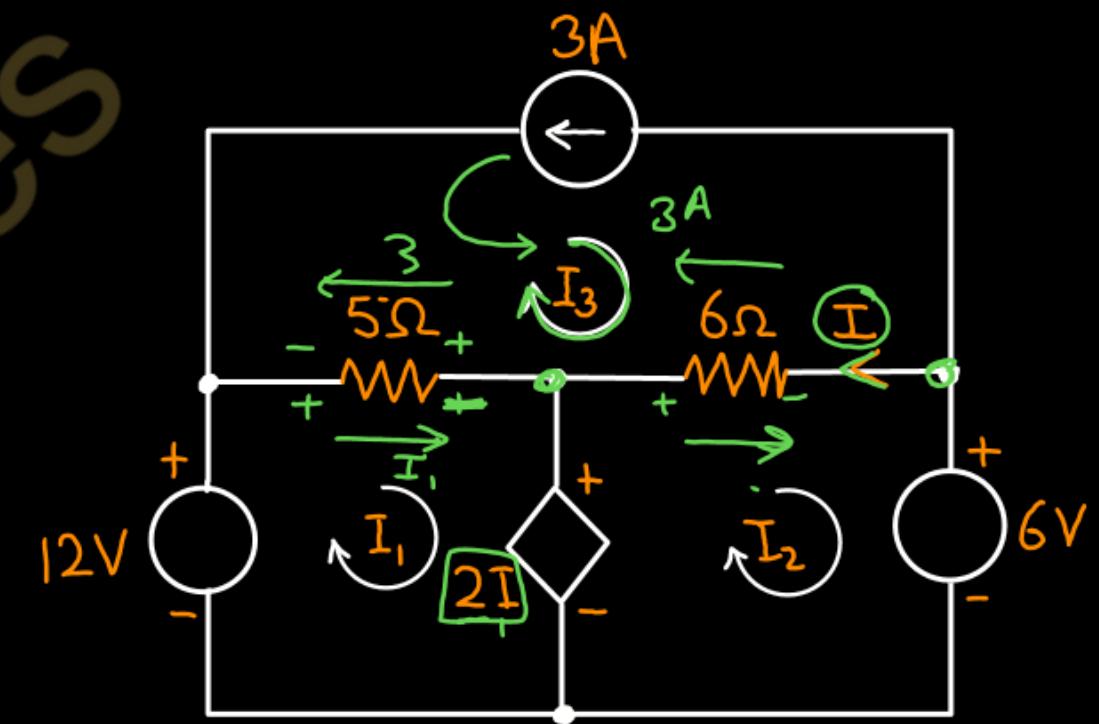
Now we have

$$\begin{aligned} I &= -3 - I_2 \\ I + 0I_1 + I_2 &= 3 \quad ③ \end{aligned}$$

$$I = 0.75$$

$$I_1 = 8.25 - 0.9 \quad A$$

$$I_2 = 8.25 - 3.75 \quad A$$



**Q.6 Use nodal analysis to find the currents in various resistors of the circuit shown below.**

$$i_1 = \frac{V_A - 0}{2} = \frac{V_A}{2}, i_2 = \frac{V_A - V_C}{5}, i_3 = \frac{V_A - V_B}{3}, i_4 = \frac{V_B}{5}, i_5 = \frac{(V_B - V_C)}{1}, i_6 = \frac{V_C}{4} = \frac{3 \cdot 8}{4} =$$

**AKTU- 2022-23**

Apply KCL at Node (A)

$$i_1 + i_2 + i_3 = 10$$

$$\frac{V_A}{2} + \frac{V_A - V_C}{5} + \frac{V_A - V_B}{3} = 10$$

$$V_A \left( \frac{1}{2} + \frac{1}{5} + \frac{1}{3} \right) - \frac{V_B}{3} - \frac{V_C}{5} = 10$$

$$V_A \left( \frac{31}{30} \right) - \frac{V_B}{3} - \frac{V_C}{5} = 10 \quad (1)$$

Apply KCL at Node (B)

$$i_3 = i_4 + i_5 \\ i_3 - i_4 - i_5 = 0$$

$$\frac{V_A - V_B}{3} - \frac{V_B}{5} - V_B + V_C = 0$$

$$\frac{V_A - V_B}{3} \left( \frac{1}{3} + \frac{1}{5} + 1 \right) + V_C = 0$$

$$\frac{V_A - V_B}{3} \left( \frac{23}{15} \right) + V_C = 0 \quad (2)$$

Apply KCL at Node (C)

$$i_2 + i_5 = i_6 + 2$$

$$i_2 + i_5 - i_6 = 2$$

$$\frac{V_A - V_C}{5} + V_B - V_C - \frac{V_C}{4} = 2$$

$$\frac{V_A}{5} + V_B - V_C \left( \frac{1}{5} + 1 + \frac{1}{4} \right) = 2$$

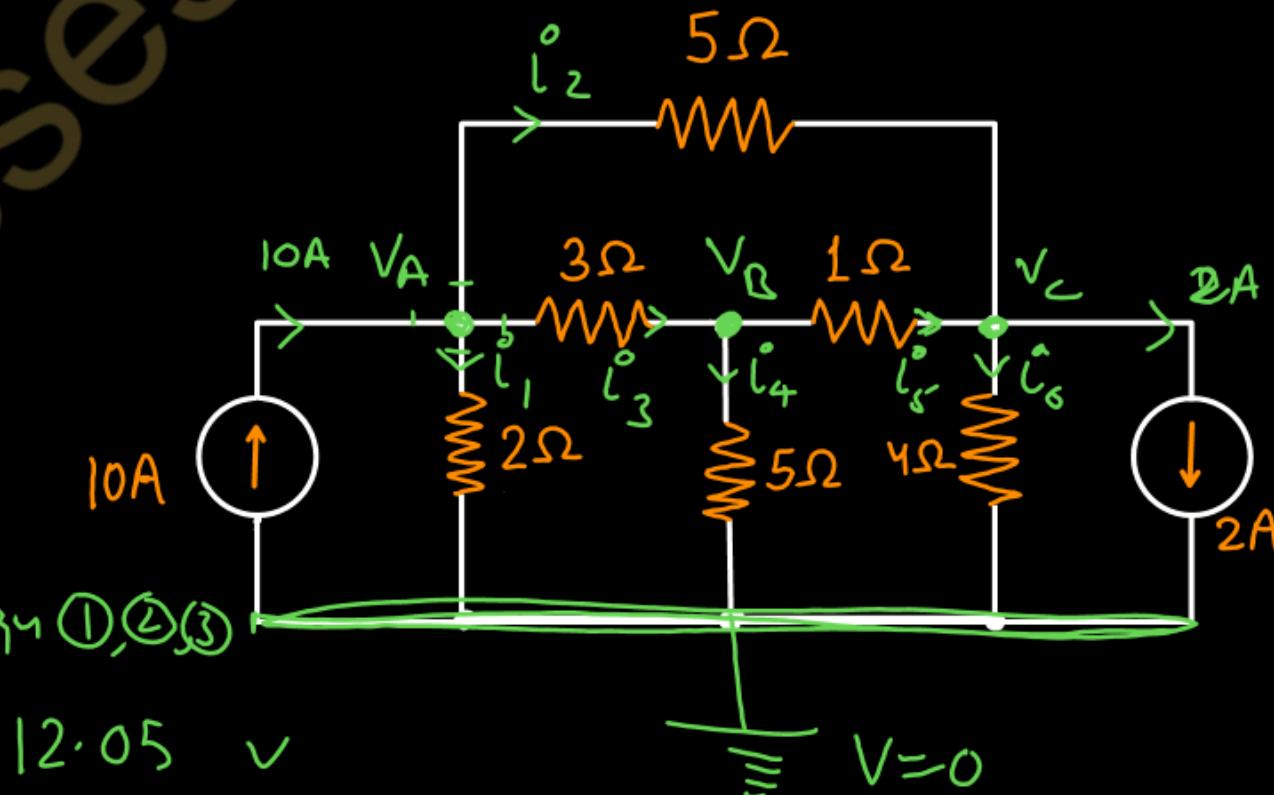
$$\frac{V_A}{5} + V_B - V_C \left( \frac{29}{20} \right) = 2 \quad (3)$$

Solve eqn (1), (2), (3)

$$V_A = 12.05 \text{ V}$$

$$V_B = 5.1 \text{ V}$$

$$V_C = 3.8 \text{ V}$$



**Q.7 Determine the currents in the various branches of the circuit shown in Figure by nodal analysis? (AKTU 2022-23)**

$$I_1 = \frac{0 - V_B + 100}{20} = \frac{100 - V_B}{20}, \quad I_2 = \frac{V_B}{10}, \quad I_3 = \frac{V_B - V_C}{15}, \quad I_4 = \frac{V_C}{10}$$

$$I_5 = \frac{V_C - 80}{10}$$

Apply KCL at Node B

$$I_1 = I_2 + I_3$$

$$I_1 - I_2 - I_3 = 0$$

$$\frac{100 - V_B}{20} - \frac{V_B}{10} - \frac{V_B - V_C}{15} = 0$$

$$\frac{100}{20} - V_B \left( \frac{1}{20} + \frac{1}{10} + \frac{1}{15} \right) + \frac{V_C}{15} = 0$$

$$-V_B \left( \frac{13}{60} \right) + \frac{V_C}{15} = -5 \quad \text{---(1)}$$

Apply KCL at Node C

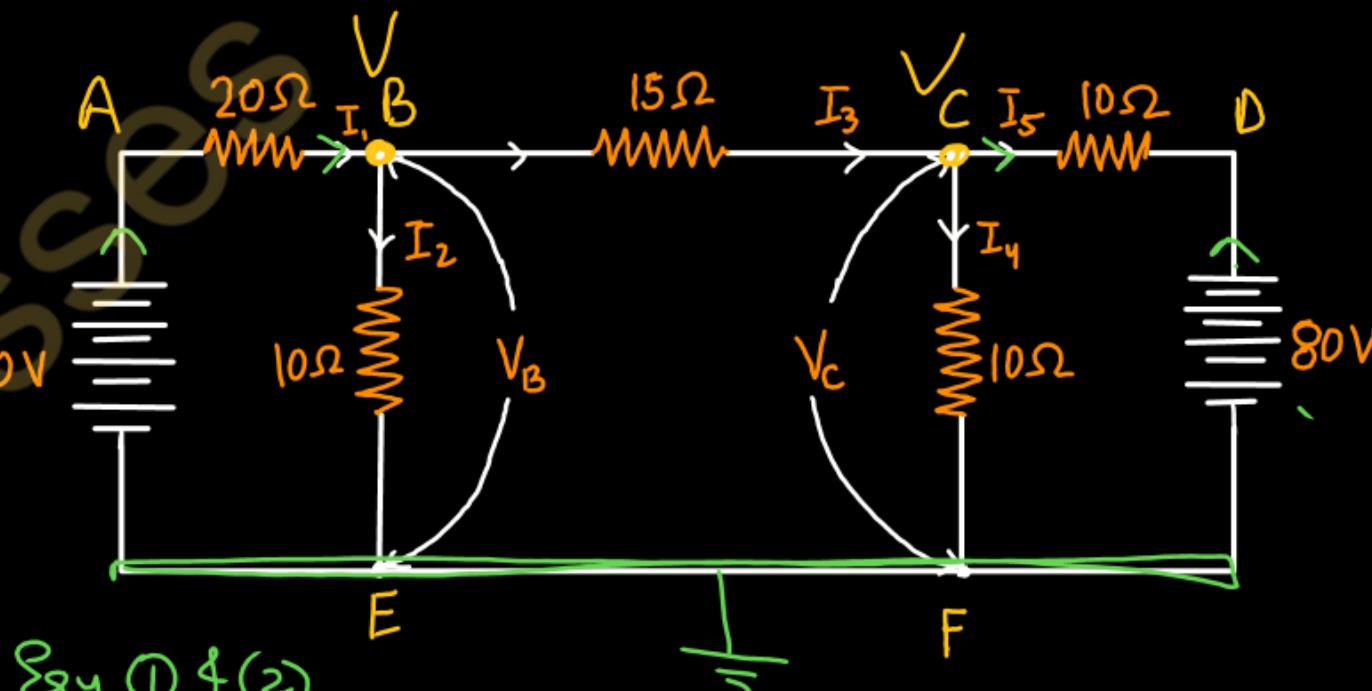
$$I_3 = I_4 + I_5$$

$$I_3 - I_4 - I_5 = 0$$

$$\frac{V_B - V_C}{15} - \frac{V_C}{10} - \frac{V_C - 80}{10} = 0$$

$$\frac{V_B}{15} - V_C \left( \frac{1}{15} + \frac{1}{10} + \frac{1}{10} \right) = -8$$

$$\frac{V_B}{15} - V_C \left( \frac{8}{30} \right) = -8 \quad \text{---(2)}$$



Solve Equ ① & ②

$$V_B = 35 \text{ V}$$

$$V_C = 38.75 \text{ V}$$

**Q.8 Determine the current by Nodal method, through 2 ohm resistor for the network shown below? (AKTU 2023-24)**

$$I_1 = \frac{20 - V_A}{2}, \quad I_2 = V_A, \quad I_3 = \frac{(V_A - V_B)}{0.5} = 2(V_A - V_B), \quad I_4 = \frac{V_B}{2}, \quad I_5 = (20 - V_B)$$

KCL at A

$$I_1 = I_2 + I_3$$

$$20 - V_A = V_A + 2V_A - 2V_B$$

$$20 = 4V_A - 2V_B \rightarrow \textcircled{1}$$

KCL at Nod (B)

$$I_3 + I_5 = I_4$$

$$2V_A - 2V_B + 20 - V_B = 0.5V_B$$

$$2V_A - 3V_B - 0.5V_B = -20$$

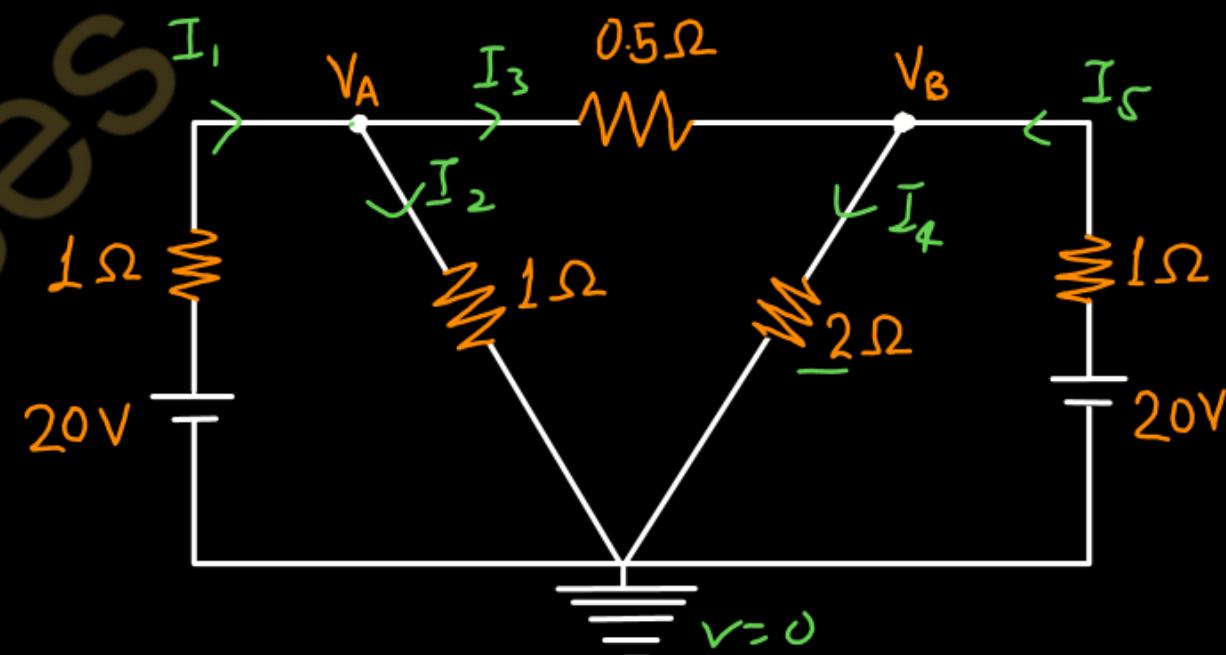
$$2V_A - 3.5V_B = -20 \rightarrow \textcircled{2}$$

Solve Eqn ① & ②

$$\left. \begin{array}{l} V_A = 11 \text{ V} \\ V_B = 12 \text{ V} \end{array} \right\}$$

RN

$$I_4 = \frac{V_B}{2} = \frac{12}{2} = 6 \text{ amp}$$



**Q.9 Calculate the current across  $6\Omega$  resistor in the following circuit using: (AKTU 2023-24 )**

Mesh Analysis

Nodal Analysis

$$I_1 = \frac{(18 - V_A)}{3}, I_2 = \frac{V_A}{6}, I_3 = \frac{12 - V_A}{7}$$

Apply KCL at Node

$$I_1 + I_3 - I_2 = 0$$

$$\left(\frac{18 - V_A}{3}\right) + \left(\frac{12 - V_A}{7}\right) - \frac{V_A}{6} = 0$$

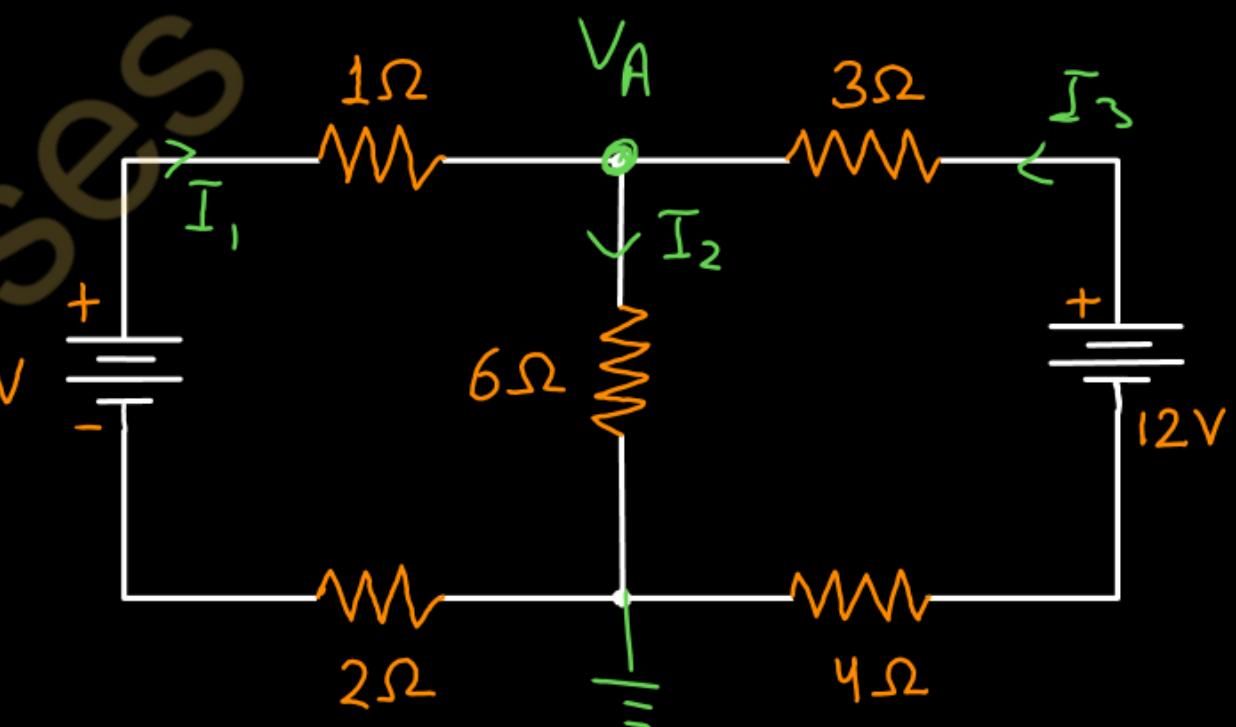
$$\frac{18 - V_A}{3} + \frac{12 - V_A}{7} - \frac{V_A}{6} = 0$$

$$7 \cdot 7 I_1 - V_A \left( \frac{1}{3} + \frac{1}{7} + \frac{1}{6} \right) = 0$$

$$\therefore 7 \cdot 7 I_1 = 0.64 V_A$$

$$V_A = 11.99 \approx 12 V$$

$$I_2 = \frac{V_A}{6} = \frac{12}{6} = 2 \text{ A}$$



**Q.10 Find the value of current in  $8\Omega$  resistance using Nodal Analysis**

$$I_1 = \frac{15 - V_B}{20}, \quad I_2 = \frac{15 - V_B}{8}, \quad I_3 = \frac{V_B - 0 + 25}{20} = \frac{V_B + 25}{20}$$

Apply KCL at Node

$$I_1 + I_2 - I_3 = 0$$

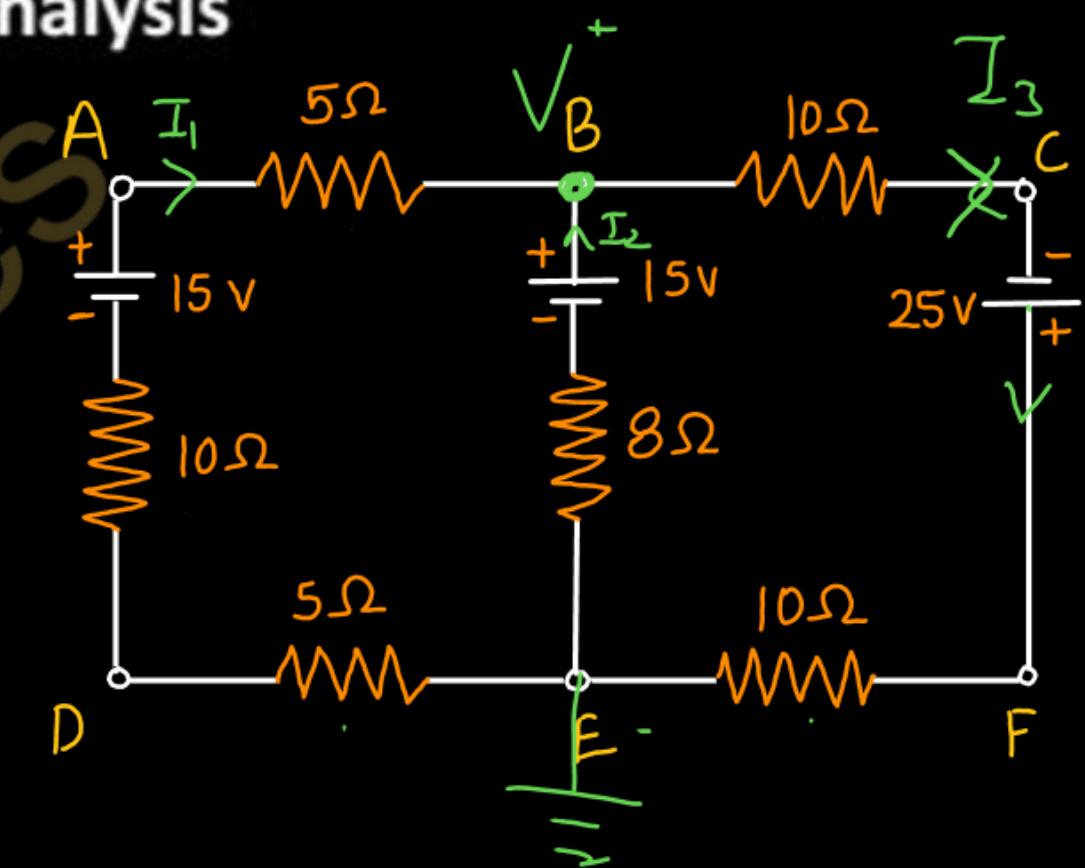
$$\frac{15 - V_B}{20} + \frac{15 - V_B}{8} - \frac{V_B + 25}{20} = 0$$

$$\left( \frac{15}{20} + \frac{15}{8} - \frac{25}{20} \right) - V_B \left( \frac{1}{20} + \frac{1}{8} + \frac{1}{20} \right) = 0$$

$$1.375 - V_B (0.225) = 0$$

$$V_B = \frac{1.375}{0.225} = 6.11 \text{ Volt}$$

$$\begin{aligned} I_{8\Omega} &= I_2 = \frac{15 - 6.11}{8} \\ &= 1.11 \text{ Amp} \end{aligned}$$



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**Thank You**