Scilab Manual for Digital Signal Processing by Prof R.Senthilkumar, Assistant Professor Electronics Engineering Institute of Road and Transport Technology¹

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Generation of Discrete Signals

Scilab code Solution 1.1 Unit Sample Sequence

```
//Caption:Unit Sample Sequence
clear;
clc;
close;
L = 4; //Upperlimit
n = -L:L;
x = [zeros(1,L),1,zeros(1,L)];
b = gca();
b.y_location = "middle";
plot2d3('gnn',n,x)
a = gce();
a.children(1).thickness = 4;
xtitle('Graphical Representation of Unit Sample Sequence', 'n', 'x[n]');
```

Scilab code Solution 1.2 Unit Step Sequence

```
1 // Caption: Unit Step Sequence
```

```
2 clear;
3 clc;
4 close;
5 L = 4; //Upperlimit
6 \quad n = -L:L;
7 x = [zeros(1,L), ones(1,L+1)];
8 a=gca();
9 a.y_location = "middle";
10 plot2d3('gnn',n,x)
11 title ('Graphical Representation of Unit Step Signal'
12 xlabel('
                                                         n'
     );
13 ylabel('
                                                          Х
      [n]');
```

Scilab code Solution 1.3 Discrete Ramp Sequence

```
//Caption: Discrete Ramp Sequence
clear;
clc;
close;
L = 4; //Upperlimit
n = -L:L;
x = [zeros(1,L),0:L];
b = gca();
b.y_location = 'middle';
plot2d3('gnn',n,x)
a = gce();
a.children(1).thickness = 2;
xtitle('Graphical Representation of Discrete Unit Ramp Sequence', 'n', 'x[n]');
```

Scilab code Solution 1.4 Exponentially Decreasing Signal

```
//Caption: Exponentially Decreasing Signal
clear;
clc;
close;
a = 0.5;
n = 0:10;
x = (a)^n;
a = gca();
a.x_location = "origin";
a.y_location = "origin";
plot2d3('gnn',n,x)
a.thickness = 2;
xtitle('Graphical Representation of Exponentially Decreasing Signal', 'n', 'x[n]');
```

Scilab code Solution 1.5 Exponentially Increasing Signal

```
//Caption: Exponentially Increasing Signal
clear;
clc;
close;
a =1.5;
n =1:10;
x = (a)^n;
a=gca();
a.thickness = 2;
plot2d3('gnn',n,x)
xtitle('Graphical Representation of Exponentially Increasing Signal', 'n', 'x[n]');
```

Linear and Circular Convolution of two sequences

Scilab code Solution 2.1 Program for Linear Convolution

```
1 // Caption: Program for Linear Convolution
2 clc;
3 clear all;
4 close;
5 x = input('enter x seq');
6 h = input('enter h seq');
7 m = length(x);
8 n = length(h);
9 // Method 1 Using Direct Convolution Sum Formula
10 \text{ for } i = 1:n+m-1
11
       conv_sum = 0;
12
       for j = 1:i
           if (((i-j+1) \le n) & (j \le m))
13
14
                conv_sum = conv_sum + x(j)*h(i-j+1);
15
           end;
           y(i) = conv_sum;
16
17
       end;
18 end;
19 disp(y', 'Convolution Sum using Direct Formula Method
```

```
= , )
20 //Method 2 Using Inbuilt Function
21 f = convol(x,h)
22 disp(f, 'Convolution Sum Result using Inbuilt Funtion
23 //Method 3 Using frequency Domain multiplication
24 \quad N = n+m-1;
25 \times = [x \times zeros(1,N-m)];
26 h = [h zeros(1,N-n)];
27 f1 = fft(x)
28 	ext{ f2} = 	ext{fft(h)}
29 f3 = f1.*f2;
                    // freq domain multiplication
30 	ext{ f4} = ifft(f3)
31 disp(f4, 'Convolution Sum Result DFT - IDFT method ='
32 / f4 = real (f4)
33 subplot (3,1,1);
34 plot2d3 ('gnn',x)
35 xtitle('Graphical Representation of Input signal x')
36 subplot (3,1,2);
37 plot2d3('gnn',h)
38 xtitle ('Graphical Representation of Impulse signal h
      <sup>'</sup>);
39 subplot(3,1,3);
40 plot2d3('gnn',y)
41 xtitle ('Graphical Representation of Output signal y'
      );
42 / Result
43 // \text{enter x seq} [1 \ 1 \ 1 \ 1]
44 //enter h seq [1 2 3]
45 // Convolution Sum using Direct Formula Method =
46 //
                       6.
                                     5.
                              6.
47 // Convolution Sum Result using Inbuilt Funtion =
                3.
                       6.
                              6.
                                     5.
49 // Convolution Sum Result DFT - IDFT method =
                       6.
50 //
          1.
                 3.
                              6.
                                     5.
                                            3.
```

Scilab code Solution 2.2 Program to find the Cicrcular Convolution

```
1 // Caption: Program to find the Cicrcular Convolution
       of given
2 // discrete sequences using Matrix method
3
4 clear;
5 clc;
6 \times 1 = [2,1,2,1]; //First sequence
7 \text{ x2} = [1,2,3,4]; //Second sequence
8 m = length(x1); //length of first sequence
9 n = length(x2); //length of second sequence
10 //To make length of x1 and x2 are Equal
11 if (m >n)
12
      for i = n+1:m
13
        x2(i) = 0;
14
      end
15 elseif (n>m)
16
      for i = m+1:n
17
        x1(i) = 0;
18
      end
19 end
20 N = length(x1);
21 x3 = zeros(1,N); //x3 = Circular convolution result
22 a(1) = x2(1);
23 \text{ for } j = 2:N
24
     a(j) = x2(N-j+2);
25 end
26 \quad \text{for i} = 1:N
     x3(1) = x3(1)+x1(i)*a(i);
27
28 end
29 X(1,:)=a;
30 // Calculation of circular convolution
31 \quad for \quad k = 2:N
```

```
32
       for j = 2:N
           x2(j) = a(j-1);
33
34
       end
           x2(1) = a(N);
35
36
           X(k,:) = x2;
       for i = 1:N
37
            a(i) = x2(i);
38
            x3(k) = x3(k)+x1(i)*a(i);
39
40
       end
41 end
42 disp(X, 'Circular Convolution Matrix x2[n]=')
43 disp(x3, 'Circular Convolution Result x3[n] = ')
44 // Result
45 // Circular Convolution Matrix x2[n]=
46 //
                              2.
          1.
                 4.
                       3.
47 //
          2.
                 1.
                       4.
                              3.
48 //
49 //
          3.
                 2.
                       1.
                              4.
50 //
          4.
                 3.
                       2.
                              1.
51 //
52 // Circular Convolution Result x3[n] =
53 //
          14.
                  16.
                                  16.
54 //
                          14.
```

Circular convolution using FFT

Scilab code Solution 3.1 Performing Circular COnvolution Using DFT IDFT method

```
1 // Caption: Performing Circular COnvolution Using DFT-
      IDFT method
2 clear all;
3 clc;
4 close;
5 L = 4; //Length of the Sequence
6 N = 4; // N - point DFT
7 \times 1 = [2,1,2,1];
8 \times 2 = [1,2,3,4];
9 //Computing DFT
10 X1 = fft(x1,-1);
11 X2 = fft(x2,-1);
12 disp(X1, 'DFT of x1[n] is X1(k)=')
13 disp(X2, 'DFT of x1[n] is X2(k)=')
14 // Multiplication of 2 DFTs
15 \times 3 = X1.*X2;
16 disp(X3, 'DFT of x3[n] is X3(k)=')
17 // Circular Convolution Result
18 \times 3 = abs(fft(X3,1))
19 \operatorname{disp}(x3, '\operatorname{Circular} \operatorname{Convolution} \operatorname{Result} x3[n]=')
```

```
20 // Result
21 // DFT of x1[n] is X1(k)=
23 // 6. 0 2. 0
24 //
25 // DFT of x1[n] is X2(k)=
27 \ // \ \ 10. \ - \ 2. \ + \ 2. \ i \ - \ 2. \ - \ 2. \ - \ 2. \ i
28 //
29 // DFT of x3[n] is X3(k)=
30 //
       60. \quad 0 - 4. \quad 0
31 //
32 //
33 // Circular Convolution Result x3[n]=
34 //
       14. 16. 14.
35 //
                                16.
```

Linear Convolution using Circular Convolution

Scilab code Solution 4.1 Performing Linear Convolution using Circular Convolution

```
1 // Caption: Performing Linear Convolution using
     Circular Convolution
3 clear;
4 clc;
5 close;
6 h = [1,2,3]; //Impulse Response of LTI System
7 x = [1,2,2,1];
                   //Input Response of LTI System
8 N1 = length(x);
9 N2 = length(h);
10 N = N1 + N2 - 1
11 disp(N, 'Length of Output Response y(n)')
12 //Padding zeros to Make Length of 'h' and 'x'
13 //Equal to length of output response 'y'
14 h1 = [h, zeros(1, N-N2)];
15 	 x1 = [x, zeros(1, N-N1)];
16 //Computing FFT
17 H = fft(h1,-1);
```

```
18 X = fft(x1,-1);
19 // Multiplication of 2 DFTs
20 \quad Y = X.*H
21 //Linear Convolution Result
22 y = abs(fft(Y,1))
23 disp(X, 'DFT of i/p X(k)=')
24 disp(H, 'DFT of impulse sequence H(k)=')
25 disp(Y, 'DFT of Linear Filter o/p Y(k)=')
26 disp(y, 'Linear Convolution result y[n]=')
27 //Result
28 // Length of Output Response y(n)
29 //
30 //
         6.
31 //
32 // DFT of i/p X(k)=
33 //
34 //
       6. - 3.4641016i 0
                                     0 3.4641016 i
35 //
36 // DFT of impulse sequence H(k)=
37 //
38 //
       6. 0.5 - 4.330127i - 1.5 + 0.8660254i
      2. - 1.5 - 0.8660254i 0.5 + 4.330127i
39
40 // DFT of Linear Filter o/p Y(k)=
41 //
         36. - 15. - 1.7320508i 0
42 //
                                        0 \quad 0 \quad - \quad 15.
     + 1.7320508 i
43 //
44 // Linear Convolution result y[n]=
45 //
46 //
         1.
               4.
                      9.
                            11.
                                   8.
                                         3.
```

Calculation of FFT and IFFT of a sequence

Scilab code Solution 5.5 Performing FFT and IFFT of a discrete sequence

```
1 // Caption: Performing FFT and IFFT of a discrete
     sequence
2 clear;
3 clc;
4 close;
5 L = 4; //Length of the Sequence
6 N = 4; // N - point DFT
7 x = [1,2,3,4];
8 //Computing DFT
9 X = fft(x,-1);
10 disp(X, 'FFT of x[n] is X(k)=')
11 x = abs(fft(X,1))
12 disp(x, 'IFFT of X(k) is x[n]=')
13 // Plotting the spectrum of Discrete Sequence
14 subplot (2,1,1)
15 a=gca();
16 a.data_bounds=[0,0;5,10];
17 plot2d3('gnn',0:length(x)-1,x)
18 \ b = gce();
```

```
19 b.children(1).thickness =3;
20 xtitle ('Graphical Representation of Discrete
     Sequence', 'n', 'x[n]');
21 subplot (2,1,2)
22 a=gce();
23 a.data_bounds=[0,0;5,10];
24 plot2d3('gnn',0:length(X)-1,abs(X))
25 b = gce();
26 b.children(1).thickness =3;
27 xtitle ('Graphical Representation of Discrete
     Spectrum', k', X(k));
28 //Result
29 //FFT of x[n] is X(k)=
30 //
        10. - 2. + 2.i - 2. - 2.i
31 //
32 //
33 //IFFT of X(k) is x[n]=
34 //
35 //
       1.
               2.
                     3. 4.
```

Time and Frequency Response of LTI systems

Scilab code Solution 6.1 Time and Frequency Response

```
1 //Caption: Program to generate and plot the impulse
     response and frequency
2 //response of a Linear constant coefficient first
     order Differential Equation
3 //[1]. Impulse response h(t) = \exp(-a*t)u(t), A>0
4 // [2]. Frequency response H(jw) = 1/(jw+a)
5 clear;
6 clc;
7 close;
8 //[1]. To generate and plot the impulse response
9 a =1; //Constant coefficient a =1
10 \text{ Dt} = 0.005;
11 t = 0:Dt:10;
12 ht = exp(-a*t);
13 figure(1)
14 a = gca();
15 a.y_location = "origin";
16 plot(t,ht);
17 xlabel('time t ---->');
```

```
18 ylabel('h(t)')
19 title ('Impulse Repsonse of Ist Order Linear Constant
       Coeff. Differential Equ.')
20 //
21 //[2]. Finding Frequency response using Continuous
      Time Fourier Transform
22 \text{ Wmax} = 2*\%pi*1;
                             //Analog Frequency = 1Hz
23 \text{ K} = 4;
24 k = 0: (K/1000):K;
25 W = k*Wmax/K;
26 \text{ HW} = \text{ht* } \exp(-\text{sqrt}(-1)*\text{t'*W}) * \text{Dt};
27 \text{ HW}_{Mag} = abs(HW);
28 W = [-mtlb_fliplr(W), W(2:1001)]; // Omega from -
      Wmax to Wmax
29 HW_Mag = [mtlb_fliplr(HW_Mag), HW_Mag(2:1001)];
30 [HW_Phase,db] = phasemag(HW);
31 HW_Phase = [-mtlb_fliplr(HW_Phase), HW_Phase(2:1001)
      ];
32 figure (2)
33 // Plotting Magnitude Response
34 subplot (2,1,1);
35 \ a = gca();
36 a.y_location = "origin";
37 plot(W,HW_Mag);
38 xlabel('Frequency in Radians/Seconds---> W');
39 ylabel('abs(H(jW))')
40 title ('Magnitude Response')
41 // Plotting Phase Reponse
42 subplot(2,1,2);
43 \ a = gca();
44 a.y_location = "origin";
45 a.x_location = "origin";
46 plot(W,HW_Phase*\%pi/180);
47 xlabel('
                                        Frequency in
      Radians/Seconds---> W');
48 ylabel('
                                                           <H
      (jW) ')
```

49 title('Phase Response in Radians')

Sampling, Verification of Sampling and Effect of aliasing

check Appendix AP 1 for dependency:

sincnew.sce

Scilab code Solution 7.1 Sampling and Reconstruction of a Signal

```
13 //Continuous Time Signal
14 xa = exp(-A*abs(t));
15 // Discrete Time Signal
16 Fs = input ('Enter the Sampling Frequency in Hertz');
      //Fs = 1Hz, 2Hz, 4Hz, 20Hz, 100Hz
17 \text{ Ts} = 1/\text{Fs};
18 \text{ nTs} = -2:Ts:2;
19 x = \exp(-A*abs(nTs));
20 // Analog Signal reconstruction
21 \text{ Dt} = 0.005;
22 t = -2:Dt:2;
23 Xa = x *sincnew(Fs*(ones(length(nTs),1)*t-nTs'*ones
      (1, length(t)));
24 // Plotting the original signal and reconstructed
      signal
25 subplot(2,1,1);
26 \ a = gca();
27 a.x_location = "origin";
28 a.y_location = "origin";
29 plot(t,xa);
30 xlabel('t in sec.');
31 \text{ ylabel('xa(t)')}
32 title ('Original Analog Signal')
33 subplot(2,1,2);
34 \ a = gca();
35 a.x_location = "origin";
36 a.y_location = "origin";
37 xlabel('t in sec.');
38 \text{ ylabel('}xa(t)')
39 title ('Reconstructed Signal using sinc function, Fs
      = 100 \,\mathrm{Hz}');
40 plot(t, Xa);
```

Design of FIR Filters Window Design

Scilab code Solution 8.1 Program to Design FIR Low Pass Filter

```
1 // Caption: Program to Design FIR Low Pass Filter
2 clc;
3 close;
4 M = input('Enter the Odd Filter Length =');
                   // Filter length
5 Wc = input('Enter the Digital Cutoff frequency =');
      // Digital Cutoff frequency
                    // Center Value
6 \text{ Tuo} = (M-1)/2
7 \quad for \quad n = 1:M
       if (n == Tuo+1)
9
         hd(n) = Wc/\%pi;
10
          hd(n) = sin(Wc*((n-1)-Tuo))/(((n-1)-Tuo)*%pi)
11
12
       end
13 end
14 // Rectangular Window
15 \text{ for } n = 1:M
16 \quad W(n) = 1;
```

```
17 \text{ end}
18 //Windowing Fitler Coefficients
19 h = hd.*W;
20 disp(h, 'Filter Coefficients are')
21
22 [hzm, fr] = frmag(h, 256);
23 \text{ hzm_dB} = 20*log10(hzm)./max(hzm);
24 subplot (2,1,1)
25 plot(2*fr,hzm)
26 xlabel('Normalized Digital Frequency W');
27 ylabel('Magnitude');
28 title ('Frequency Response Of FIR LPF using
      Rectangular window')
29 xgrid(1)
30 subplot (2,1,2)
31 plot(2*fr,hzm_dB)
32 xlabel('Normalized Digital Frequency W');
33 ylabel('Magnitude in dB');
34 title ('Frequency Response Of FIR LPF using
      Rectangular window')
35 xgrid(1)
36 //Result
37 //Enter the Odd Filter Length = 7
38 //Enter the Digital Cutoff frequency = %pi/2
39 //
40 // Filter Coefficients are
41 //
42 //
       -0.1061033
         1.949D-17
                    = 0.0
43 //
44 //
         0.3183099
         0.5
45 //
46 //
         0.3183099
47 //
         1.949D-17 = 0.0
48
        - 0.1061033
```

Scilab code Solution 8.2 rogram to Design FIR High Pass Filter

```
1 //Caption: Program to Design FIR High Pass Filter
2 clear;
3 clc;
4 close;
5 M = input('Enter the Odd Filter Length =');
                   //Filter length
6 Wc = input('Enter the Digital Cutoff frequency =');
      // Digital Cutoff frequency
   Tuo = (M-1)/2
                      //Center Value
  for n = 1:M
9
       if (n == Tuo+1)
10
         hd(n) = 1-Wc/\%pi;
11
       else
         hd(n) = (sin(\%pi*((n-1)-Tuo)) - sin(Wc*((n-1)-Tuo)))
12
            Tuo)))/(((n-1)-Tuo)*%pi);
13
       end
14 end
15 //Rectangular Window
16 \quad for \quad n = 1:M
17
     W(n) = 1;
18 end
19 //Windowing Fitler Coefficients
20 h = hd.*W;
21 disp(h, 'Filter Coefficients are')
22 [hzm,fr]=frmag(h,256);
23 \text{ hzm_dB} = 20*log10(hzm)./max(hzm);
24 subplot (2,1,1)
25 \text{ plot}(2*fr,hzm)
26 xlabel('Normalized Digital Frequency W');
27 ylabel('Magnitude');
28 title ('Frequency Response Of FIR HPF using
      Rectangular window')
29 xgrid(1)
30 subplot (2,1,2)
31 plot(2*fr,hzm_dB)
32 xlabel('Normalized Digital Frequency W');
```

```
33 ylabel('Magnitude in dB');
34 title ('Frequency Response Of FIR HPF using
      Rectangular window')
35 xgrid(1)
36 //Result
37 //Enter the Odd Filter Length = 5
38 //Enter the Digital Cutoff frequency = \%pi/4
39 // Filter Coefficients are
40 //
41 //
       -0.1591549
42 //
      -0.2250791
       0.75
43 //
44 //
      -0.2250791
       -0.1591549
```

Scilab code Solution 8.3 Program to Design FIR Band Pass Filter

```
1 //Caption: Program to Design FIR Band Pass Filter
2 clear;
3 clc;
4 close;
5 M = input('Enter the Odd Filter Length =');
                    //Filter length
6 // Digital Cutoff frequency [Lower Cutoff, Upper
      Cutoff
7 Wc = input('Enter the Digital Cutoff frequency =');
8 \text{ Wc2} = \text{Wc}(2)
9 \text{ Wc1} = \text{Wc}(1)
10 \text{ Tuo} = (M-1)/2
                        //Center Value
11 hd = zeros(1,M);
12 W = zeros(1,M);
13 \text{ for } n = 1:11
     if (n == Tuo+1)
14
15
         hd(n) = (Wc2-Wc1)/\%pi;
16
     else
```

```
17
        hd(n) = (sin(Wc2*((n-1)-Tuo)) - sin(Wc1*((n-1)-Tuo)))
18
           Tuo)))/(((n-1)-Tuo)*%pi);
19
     end
20
     if(abs(hd(n))<(0.00001))
21
       hd(n)=0;
22
     end
23 end
24 hd:
25 // Rectangular Window
26 \text{ for } n = 1:M
27
     W(n) = 1;
28 end
29 //Windowing Fitler Coefficients
30 h = hd.*W;
31 disp(h, 'Filter Coefficients are')
32 [hzm,fr]=frmag(h,256);
33 \text{ hzm_dB} = 20*\log 10 \text{ (hzm)./max(hzm)};
34 subplot (2,1,1)
35 plot (2*fr, hzm)
36 xlabel('Normalized Digital Frequency W');
37 ylabel('Magnitude');
38 title ('Frequency Response Of FIR BPF using
      Rectangular window')
39 xgrid(1)
40 subplot (2,1,2)
41 plot(2*fr,hzm_dB)
42 xlabel('Normalized Digital Frequency W');
43 ylabel('Magnitude in dB');
44 title ('Frequency Response Of FIR BPF using
      Rectangular window')
45 xgrid(1)
46 // Result
47 //Enter the Odd Filter Length = 11
48 //Enter the Digital Cutoff frequency = [\%pi/4,3*\%pi]
      /4
49 // Filter Coefficients are
50 // 0.
             0. \quad 0. \quad -0.3183099
                                     0 .
                                              0.5 	 0. -
```

Scilab code Solution 8.4 Program to Design FIR Band Reject Filter

```
1 //Caption: Program to Design FIR Band Reject Filter
2 clear;
3 clc;
4 close;
5 M = input('Enter the Odd Filter Length =');
                     //Filter length
6 // Digital Cutoff frequency [Lower Cutoff, Upper
      Cutoff]
7 Wc = input('Enter the Digital Cutoff frequency =');
8 \text{ Wc2} = \text{Wc}(2)
9 \text{ Wc1} = \text{Wc}(1)
10 \text{ Tuo} = (M-1)/2
                        //Center Value
11 hd = zeros(1,M);
12 W = zeros(1,M);
13 \text{ for } n = 1:M
14
   if (n == Tuo+1)
15
    hd(n) = 1-((Wc2-Wc1)/\%pi);
16
17
    hd(n) = (\sin(\%pi*((n-1)-Tuo))-\sin(Wc2*((n-1)-Tuo))+
        sin(Wc1*((n-1)-Tuo)))/(((n-1)-Tuo)*%pi);
18
     if(abs(hd(n))<(0.00001))</pre>
19
        hd(n)=0;
20
21
     end
22 \text{ end}
23
24 // Rectangular Window
25 \quad for \quad n = 1:M
     W(n) = 1;
26
27 \text{ end}
28 //Windowing Fitler Coefficients
```

```
29 h = hd.*W;
30 disp(h, 'Filter Coefficients are')
31 [hzm,fr]=frmag(h,256);
32 hzm_dB = 20*log10(hzm)./max(hzm);
33 subplot (2,1,1)
34 \text{ plot}(2*fr,hzm)
35 xlabel('Normalized Digital Frequency W');
36 ylabel('Magnitude');
37 title ('Frequency Response Of FIR BSF using
      Rectangular window')
38 xgrid(1)
39 subplot (2,1,2)
40 plot(2*fr,hzm_dB)
41 xlabel('Normalized Digital Frequency W');
42 ylabel ('Magnitude in dB');
43 title ('Frequency Response Of FIR BSF using
      Rectangular window')
44 xgrid(1)
45 // Result
46 //Enter the Odd Filter Length = 11
47 //Enter the Digital Cutoff frequency = [\%pi/3, 2*\%pi]
48 // Filter Coefficients are
49 //column 1 to 9
50 //
         0. - 0.1378322
                              0.
                                    0.2756644
                                                  0.
      0.6666667
                   0.
                          0.2756644
                                       0.
51 //column 10 to 11
52 // - 0.1378322
                       0.
```

Design of FIR Filters Frequency Sampling

Scilab code Solution 9.1 Design of FIR LPF Filter using Frequecny Sampling Technique

```
1 //Cpation: Design of FIR LPF Filter using Frequenny
      Sampling Technique
3 clear;
4 clc;
5 close;
6 M = 15;
7 \text{ Hr} = [1,1,1,1,0.4,0,0,0];
8 for k =1:length(Hr)
       G(k) = ((-1)^{(k-1)})*Hr(k);
10 \text{ end}
11 h = zeros(1,M);
12 U = (M-1)/2
13 \text{ for } n = 1:M
14
    h1 = 0;
     for k = 2:U+1
       h1 = G(k)*cos((2*\%pi/M)*(k-1)*((n-1)+(1/2)))+h1;
16
17
```

```
h(n) = (1/M)* (G(1)+2*h1);
18
19 end
20 disp(h, 'Filter Coefficients are h(n)=')
21 [hzm, fr] = frmag(h, 256);
22 \text{ hzm_dB} = 20*log10(hzm)./max(hzm);
23 subplot (2,1,1)
24 plot (2*fr, hzm)
25 \ a=gca();
26 xlabel('Normalized Digital Frequency W');
27 ylabel ('Magnitude');
28 title('Frequency Response Of FIR LPF using Frequency
       Sampling Technique with M = 15 with Cutoff
      Frequency = 0.466')
29 xgrid(2)
30 subplot (2,1,2)
31 plot(2*fr,hzm_dB)
32 \ a = gca();
33 xlabel('Normalized Digital Frequency W');
34 ylabel('Magnitude in dB');
35 title ('Frequency Response Of FIR LPF using Frequency
       Sampling Technique with M = 15 with Cutoff
      Frequency = 0.466')
36 xgrid(2)
37 //Result
38 // Filter Coefficients are h(n)=
39 //column 1 to 7
40 //
41 // -0.0141289 -0.0019453 0.04
                                      0.0122345
      -0.0913880 \quad -0.0180899
                               0.3133176
42 //
43 //column 8 to 14
44 //
45 //0.52
         0.3133176 - 0.0180899 - 0.0913880
                0.04 - 0.0019453
      0.0122345
46 //
47 //column 15
48 //
49 // - 0.0141289
```

Design of IIR Filters-Butterworth

Scilab code Solution 10.1 Digital IIR First Order Butterworth LPF Filter

```
1 //Caption: To design a digital IIR First Order
     Butterworth LPF Filter
2 //Using Bilinear Transformation
3 clear all;
4 clc;
5 close;
6 s = poly(0, 's');
                      // Cutoff frequency
7 Omegac = 0.2*\%pi;
8 H = Omegac/(s+Omegac); //Analog first order
     Butterworth filter transer function
9 T =1; // Sampling period T = 1 Second
10 z = poly(0, 'z');
11 Hz = horner(H, (2/T)*((z-1)/(z+1))) // Bilinear
     Transformation
12 HW = frmag(Hz(2), Hz(3), 512); // Frequency response
     for 512 points
13 W = 0:\%pi/511:\%pi;
14 a=gca();
```

Scilab code Solution 10.2 HPF Using Digital Filter Transformation

```
1 // Caption: To design First Order Butterworth Low
      Pass Filter and covert it into
2 // HPF Using Digital Filter Transformation
3 clear all;
4 clc;
5 close;
6 s = poly(0, 's');
7 Omegac = 0.2*%pi; //Filter cutoff frequency
8 H = Omegac/(s+Omegac); //First order Butterworth IIR
       filter
9 T =1; //Sampling period T = 1 Second
10 z = poly(0, z');
11 Hz_{LPF} = horner(H, (2/T)*((z-1)/(z+1))); //Bilinear
      Transformation
12 alpha = -(\cos((Omegac + Omegac)/2))/(\cos((Omegac -
     Omegac)/2));
13 HZ_HPF=horner(Hz_LPF,-(z+alpha)/(1+alpha*z))/LPF to
      HPF digital transformation
14 HW = frmag(HZ_HPF(2), HZ_HPF(3), 512); //Frequency
      response for 512 points
15 W = 0:\%pi/511:\%pi;
16 a=gca();
17 a.thickness = 1;
18 plot(W/%pi, HW, 'r')
```

Scilab code Solution 10.3 BPF using Digital Transformation

```
1 ///Caption:To Design a Digital IIR Butterworth LPF
      Filter from Analog IIR
2 //Butterworth Filter and LPF to BPF using Digital
      Transformation
3 clear all;
4 clc;
5 close;
6 omegaP = 0.2*%pi; //Filter cutoff frequency
7 omegaL = (1/5)*\%pi; //Lower Cutoff frequency for
     BSF
  omegaU = (3/5)*\%pi; //Upper Cutoff frequency for
     BSF
9 z = poly(0, 'z');
10 H_LPF = (0.245)*(1+(z^-1))/(1-0.509*(z^-1)); //
      Bilinear transformation
  alpha = (cos((omegaU+omegaL)/2)/cos((omegaU-omegaL)
11
     /2));//parameter 'alpha'
12 //parameter 'k'
13 k = (\cos((\text{omegaU - omegaL})/2)/\sin((\text{omegaU - omegaL}))
     /2))*tan(omegaP/2);
14 NUM =-((z^2)-((2*alpha*k/(k+1))*z)+((k-1)/(k+1)));
15 DEN = (1-((2*alpha*k/(k+1))*z)+(((k-1)/(k+1))*(z^2))
     );
16 HZ_BPF=horner(H_LPF, NUM/DEN); //LPF to BPF conversion
       using digital transformation
17 disp(HZ_BPF, 'Digital BPF IIR Filter H(Z) = ');
```

```
18 HW = frmag(HZ_BPF(2), HZ_BPF(3), 512); // frequency
    response
19 W = 0:%pi/511:%pi;
20 a=gca();
21 a.thickness = 1;
22 plot(W/%pi,HW,'r')
23 a.foreground = 1;
24 a.font_style = 9;
25 xgrid(1)
26 xtitle('Magnitude Response of BPF Filter cutoff
    frequency [0.2,0.6]', 'Normalized Digital
    Frequency—>', 'Magnitude');
```

Scilab code Solution 10.4 BSF using Digital Transformation

```
1 //Caption:To Design a Digital IIR Butterworth LPF
      Filter from Analog IIR
2 //Butterworth Filter and LPF to BSF using Digital
     Transformation
3 clear all;
4 clc;
5 close;
6 omegaP = 0.2*%pi; //Filter cutoff frequency
7 omegaL = (1/5)*\%pi; //Lower Cutoff frequency for
     BSF
  omegaU = (3/5)*\%pi; //Upper Cutoff frequency for
     BSF
9 z = poly(0, 'z');
10 H_LPF = (0.245)*(1+(z^-1))/(1-0.509*(z^-1))//
      Bilinear transformation
11 alpha = (cos((omegaU+omegaL)/2)/cos((omegaU-omegaL)
     /2)); //parameter 'alpha'
12 k = tan((omegaU - omegaL)/2)*tan(omegaP/2); //
     parameter 'k'
13 NUM = ((z^2) - ((2*alpha/(1+k))*z) + ((1-k)/(1+k))); //
```

```
Numerator
14 DEN = (1-((2*alpha/(1+k))*z)+(((1-k)/(1+k))*(z^2)));
      //Denominator
15 HZ_BSF=horner(H_LPF, NUM/DEN); //LPF to BSF
      conversion using digital transformation
16 HW = frmag(HZ_BSF(2), HZ_BSF(3), 512); //frequency
     response for 512 points
17 W = 0:\%pi/511:\%pi;
18 a=gca();
19 a.thickness = 1;
20 plot(W/%pi,HW,'r')
21 a.foreground = 1;
22 a.font_style = 9;
23 xgrid(1)
24 xtitle ('Magnitude Response of BSF Filter cutoff freq
       [0.2,0.6] ', 'Normalized Digital Frequency--->', '
     Magnitude');
```

Design of IIR Filters Chebyshev

Scilab code Solution 11.1 To Design the Digtial Chebyshev IIR Filter

```
1 //Program To Design the Digtial Chebyshev IIR Filter
2 clear;
3 clc;
4 close;
5 Wp = input('Enter the Digital Pass Band Edge
     Frequency');
6 Ws = input ('Enter the Digital Stop Band Edge
     Frequency');
7 T = input('Sampling Interval')
8 OmegaP = (2/T)*tan(Wp/2)
9 OmegaS = (2/T)*tan(Ws/2)
10 Delta1 = input('Enter the Pass Band Ripple');
11 Delta2 = input ('Enter the Stop Band Ripple');
12 Delta = sqrt(((1/Delta2)^2)-1)
13 Epsilon = sqrt(((1/Delta1)^2)-1)
14 N = (acosh(Delta/Epsilon))/(acosh(OmegaS/OmegaP))
15 N = ceil(N)
16 OmegaC = OmegaP/((((1/Delta1)^2)-1)^(1/(2*N)))
17 [pols,gn] = zpch1(N,Epsilon,OmegaP)
```

```
18 Hs = poly(gn, 's', 'coeff')/real(poly(pols, 's'))
19 z = poly(0, 'z');
20 Hz = horner(Hs,((2/T)*((z-1)/(z+1))))
21 HW = frmag(Hz(2), Hz(3), 512); // Frequency response
      for 512 points
22 W = 0:\%pi/511:\%pi;
23 a=gca();
24 a.thickness = 1;
25 plot(W/%pi,abs(HW), 'r')
26 a.foreground = 1;
27 a.font_style = 9;
28 xgrid(1)
29 xtitle ('Magnitude Response of Chebyshev LPF Filter',
      'Normalized Digital Frequency--->', 'Magnitude in
      dB');
30 //RESULT
31 //Enter the Digital Pass Band Edge Frequency 0.2*%pi
32 //Enter the Digital Stop Band Edge Frequency 0.6*%pi
33 //Sampling Interval 1
34 // T =
35 //
36 //
37 // \text{OmegaP} =
38 //
39 //
         0.6498394
40 // \text{OmegaS} =
41 //
         2.7527638
42 //
43 //Enter the Pass Band Ripple 0.8
44 //Enter the Stop Band Ripple 0.2
45 // Delta =
46 //
47 //
         4.8989795
48 // Epsilon =
49 //
50 //
         0.75
51 // N =
52 //
```

```
53 // 1.2079548
54 // N =
55 //
56 // 2.
57 // \text{OmegaC} =
58 //
59 // 0.7503699
60 // gn =
61 //
62 // 0.2815275
63 // pols =
64 //
65 // - 0.2652958 + 0.5305916 i - 0.2652958 -
     0.5305916i
66 // \text{Hs} =
67 //
68 //
                 0.2815275
69 //
70 //
71 //
       0.3519094 + 0.5305916s + s
72 // Hz =
73 //
74 //
75 //
       0.2815275 + 0.5630550z + 0.2815275z
76 //
77 //
78 //
       3.2907261 - 7.2961813z + 5.4130926z
79 //-->0.5*0.5629
80 // ans =
81 //
82 // 0.28145
83 //
84 //-->Hz(2)= Hz(2)/5.4130926
85 // Hz =
86 //
87 //
88 //
       0.0520086 + 0.1040172z + 0.0520086z
89 //
```

```
90 // 2
91 // 3.2907261 - 7.2961813z + 5.4130926z
92 //
93 //—>Hz(3) = Hz(3)/5.4130926
94 // Hz =
95 //
96 // 2
97 // 0.0520086 + 0.1040172z + 0.0520086z
98 //
99 // 0.6079198 - 1.3478767z + z
```

Decimation by polyphase decomposition

Scilab code Solution 12.1 Design of Ployphase Decimator

```
1 //Caption: Decimation by 2, Filter Length = 30
2 //Cutoff Frequency Wc = \%pi/2
\frac{3}{2} // Pass band Edge frequency fp = 0.25 and a Stop band
       edge frequency fs = 0.31
4 // Choose the number of cosine functions and create
      a dense grid
5 // \text{ in } [0,0.25] \text{ and } [0.31,0.5]
6 / magnitude for pass band = 1 & stop band = 0 (i.e)
7 // \text{Weighting function} = [2 \ 1]
8 clear;
9 clc;
10 close;
11 M = 30; // Filter Length
12 D = 2; //Decimation Factor = 2
13 Wc = %pi/2; //Cutoff Frequency
14 Wp = Wc/(2*%pi); //Passband Edge Frequency
15 Ws = 0.31; //Stopband Edge Frequency
16 hn=eqfir(M,[0 Wp; Ws .5],[1 0],[2 1]);
```

```
17 disp(hn, 'The LPF Filter Coefficients are: ')
18 //Obtaining Polyphase Filter Coefficients from hn
19 p = zeros(D, M/D);
20 \text{ for } k = 1:D
21
     for n = 1:(length(hn)/D)
22
       p(k,n) = hn(D*(n-1)+k);
23
     end
24 end
25 disp(p, 'The Polyphase Decimator for D = 2 are: ')
26 //Result
27 //The LPF Filter Coefficients are:
28 //column 1 to 7
29 / (0.0060203 - 0.0128037 - 0.0028534)
                                            0.0136687
     -0.0046761 -0.0197002
                                  0.0159915
30
31 //column 8 to 14
32 / 0.0213811 - 0.0349808 - 0.0156251
                                            0.0640230
     -0.0073600 -0.1187325 0.0980522
33 //column 15 to 21
                  0.4922476 0.0980522 - 0.1187325
34 / 0.4922476
     -0.0073600
                    0.0640230 \quad - \ 0.0156251
35 //column 22 to 28
                    0.0213811 \qquad 0.0159915 \quad - \ 0.0197002
36 //- 0.0349808
       -\ 0.0046761\ 0.0136687\ -\ 0.0028534
37
38 //column 29 to 30
39 //- 0.0128037
                    0.0060203
40
41 //The Polyphase Decimator for D = 2 are:
42 //column 1 to 7
43 / 0.0060203 - 0.0028534 - 0.0046761
                                            0.0159915
     -0.0349808
                   0.0640230 - 0.1187325
44 //- 0.0128037
                    0.0136687 - 0.0197002
                                              0.0213811
       45
46 //column 8 to 14
47 //0.4922476
                 0.0980522 \quad - \ 0.0073600 \quad - \ 0.0156251
        0.0213811 - 0.0197002 0.0136687
```

Periodogram based Spectral Estimation

Scilab code Solution 13.1 Periodogram Estimate of Given Discrete Sequence

```
1 //Caption: Periodogram Estimate of Given Discrete
      Sequence
2 //x(n) = \{1,0,2,0,3,1,0,2\}
3 //using DFT
4 clear;
5 clc;
6 close;
7 N =8; //8-point DFT
8 \times = [1,0,2,0,3,1,0,2]; //given discrete sequence
9 X = dft(x,-1); //8-point DFT of given discrete
      sequence
10 Pxx = (1/N)*(abs(X).^2); //Peridogram Estimate
11 disp(X, 'DFT of x(n) is X(k)=')
12 disp(Pxx, 'Peridogram of x(n) is Pxx(k/N)=')
13 figure(1)
14 \ a = gca();
15 a.data_bounds = [0,0;8,11];
16 plot2d3('gnn',[1:N],Pxx)
```

```
17 a.foreground = 5;
18 a.font_color = 5;
19 a.font_style = 5;
20 title('Peridogram Estimate')
21 xlabel('Discrete Frequency Variable K ---->')
22 ylabel('Periodogram Pxx (k/N) ---->')
23 // Result
24 //DFT of x(n) is X(k)=
25 //
26 //
         9.
27 //
       -1.2928932 + 0.1213203 i
28 //
         2. + i
29 //
       -2.7071068 + 4.1213203 i
30 //
         3. - 3.674D - 16i
       -2.7071068 - 4.1213203i
31 //
32 //
         2. - i
33 //
      -1.2928932 - 0.1213203 i
34 //
35 // Peridogram of x(n) is Pxx(k/N)=
36 //
37 //
         10.125
38 //
         0.2107864
39 //
         0.625
40 //
         3.0392136
41 //
         1.125
42 //
         3.0392136
43 //
         0.625
         0.2107864
44 //
```

Appendix

```
Scilab code AP 11 function [y]=sincnew(x)
2 i=find(x==0);
3 x(i)= 1;    // don't need this is /0 warning is
    off
4 y = sin(%pi*x)./(%pi*x);
5 y(i) = 1;
6 endfunction
sinc function
```