

**MANAV RACHNA UNIVERSITY, FARIDABAD**  
**Department of Mathematics**

**Course: B.Tech. CSE**  
**Session: 2020-2021**

**Semester: IV**  
**Subject: Probability and Statistics (MAH202B-T)**

**TUTORIAL - 03**

1. Is the function given below a density function?

$$f(x) = \begin{cases} 0 & \text{for } x < 2 \\ \frac{3+2x}{18} & \text{for } 2 \leq x \leq 4 \\ 0 & \text{for } x > 4 \end{cases}$$

Also find  $P(2 \leq X \leq 3)$ .

2. If  $f(x) = \begin{cases} \frac{x+1}{2}, & -1 < x < 1 \\ 0, & \text{elsewhere} \end{cases}$  represents the density function of a random variable X.  
Find  $E(X)$  and  $VAR(X)$ .

3. The frequency distribution of a measurable characteristic varying between 0 and 2 is as under:

$$f(x) = \begin{cases} x^3, & 0 \leq x \leq 1 \\ (2-x)^3 & 1 \leq x \leq 2 \end{cases}$$

Calculate the standard deviation and also the mean deviation about mean.

4. Let X be a random variable defined by the density function

$$f(x) = \begin{cases} 3x^2, & 0 \leq x \leq 1 \\ 0, & \text{otherwise} \end{cases}$$

Find  $E(X)$ ,  $E(3X - 2)$ ,  $E(X^2)$

5. The probability density  $p(x)$  of a continuous random variable is given by

$$p(x) = y_0 e^{-|x|}, -\infty < x < \infty$$

Find  $y_0$