

Artificial Intelligence

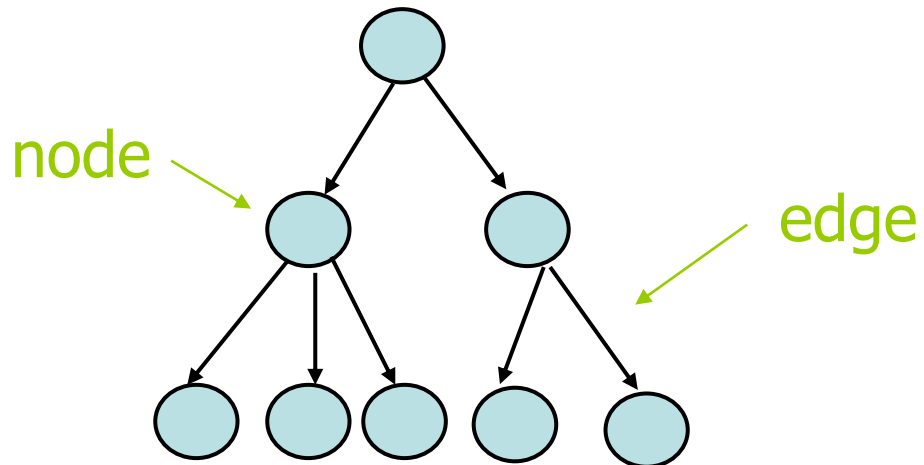
Tutorial 0



Trees

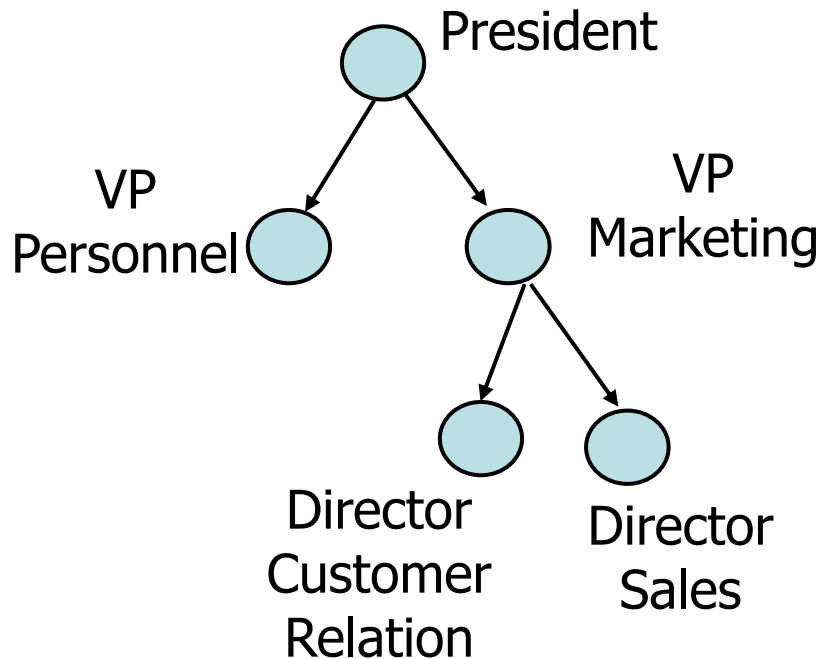
What is a tree?

- Trees are structures used to represent hierarchical relationship
- Each tree consists of nodes and edges
- Each node represents an object
- Each edge represents the relationship between two nodes.

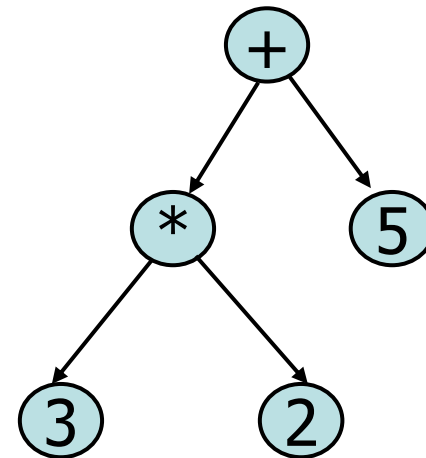


Some applications of Trees

Organization Chart

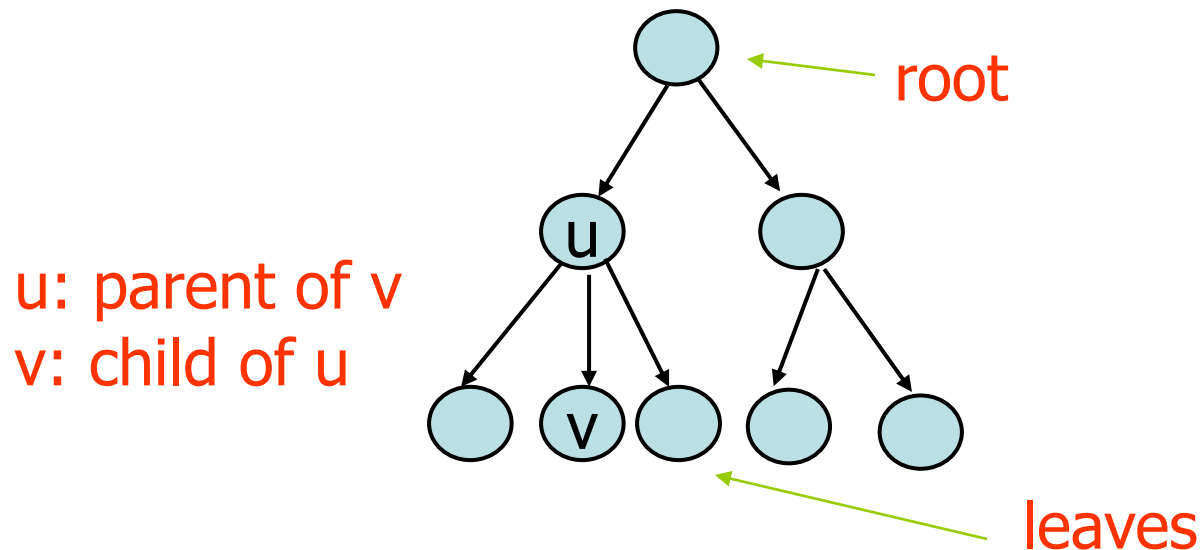


Expression Tree



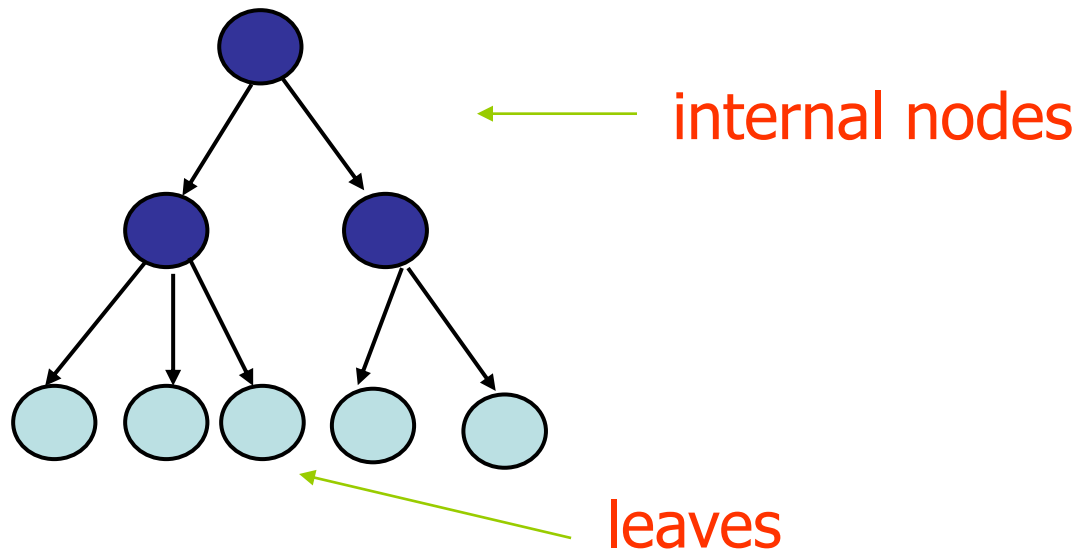
Terminology I

- For any two nodes u and v , if there is an edge pointing from u to v , u is called the **parent** of v while v is called the **child** of u . Such edge is denoted as (u, v) .
- In a tree, there is exactly one node without parent, which is called the **root**. The nodes without children are called **leaves**.



Terminology II

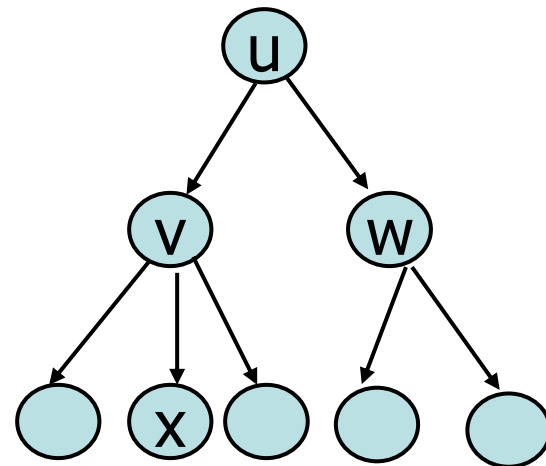
- In a tree, the nodes without children are called **leaves**. Otherwise, they are called **internal nodes**.



Terminology III

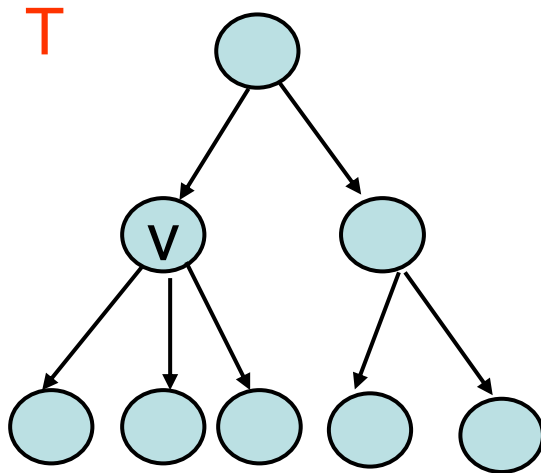
- If two nodes have the same parent, they are **siblings**.
- A node u is an **ancestor** of v if u is parent of v or parent of parent of v or ...
- A node v is a **descendent** of u if v is child of u or child of child of u or ...

v and w are siblings
 u and v are ancestors of x
 v and x are descendants of u

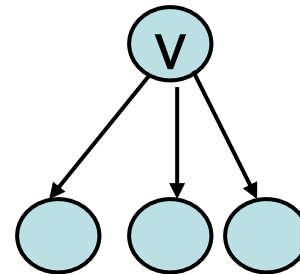


Terminology IV

- A **subtree** is any node together with all its descendants.

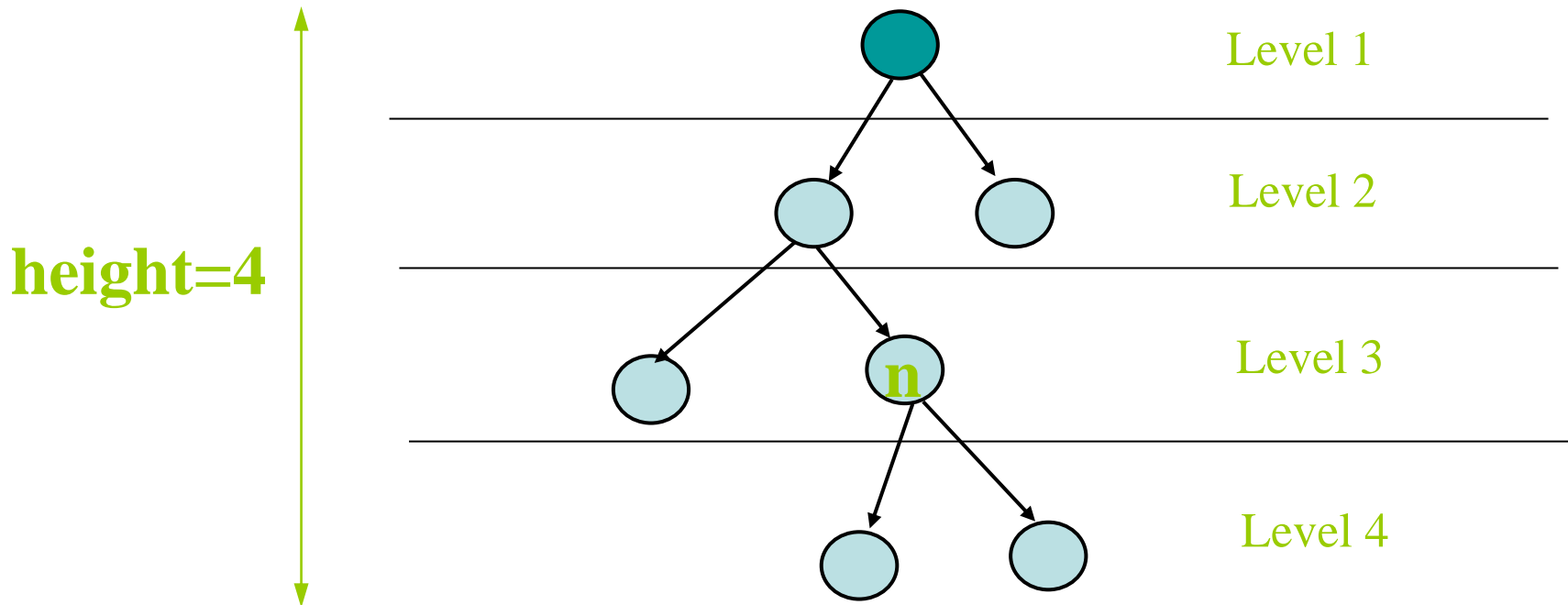


A subtree of T



Terminology V

- **Level of a node n:** number of nodes on the path from root to node n
- **Height of a tree:** maximum level among all of its node



Tree Traversal

- Given a binary tree, we may like to do some operations on all nodes in a binary tree. For example, we may want to double the value in every node in a binary tree.
- To do this, we need a traversal algorithm which visits every node in the binary tree.

Ways to traverse a tree

- There are three main ways to traverse a tree:
 - Pre-order:
 - (1) visit node, (2) recursively visit left subtree, (3) recursively visit right subtree
 - In-order:
 - (1) recursively visit left subtree, (2) visit node, (3) recursively visit right subtree
 - Post-order:
 - (1) recursively visit left subtree, (2) recursively visit right subtree, (3) visit node
 - Level-order:
 - Traverse the nodes level by level
- In different situations, we use different traversal algorithm.

Examples for expression tree

- By pre-order, (prefix)

+ * 2 3 / 8 4

- By in-order, (infix)

2 * 3 + 8 / 4

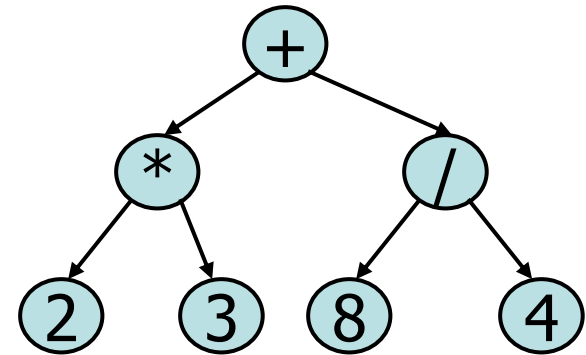
- By post-order, (postfix)

2 3 * 8 4 / +

- By level-order,

+ * / 2 3 8 4

- Note 1: Infix is what we read!
- Note 2: Postfix expression can be computed efficiently using stack



Preorder, Postorder and Inorder

- Preorder traversal
 - node, left, right
 - prefix expression
 - $++a*bc*+*defg$

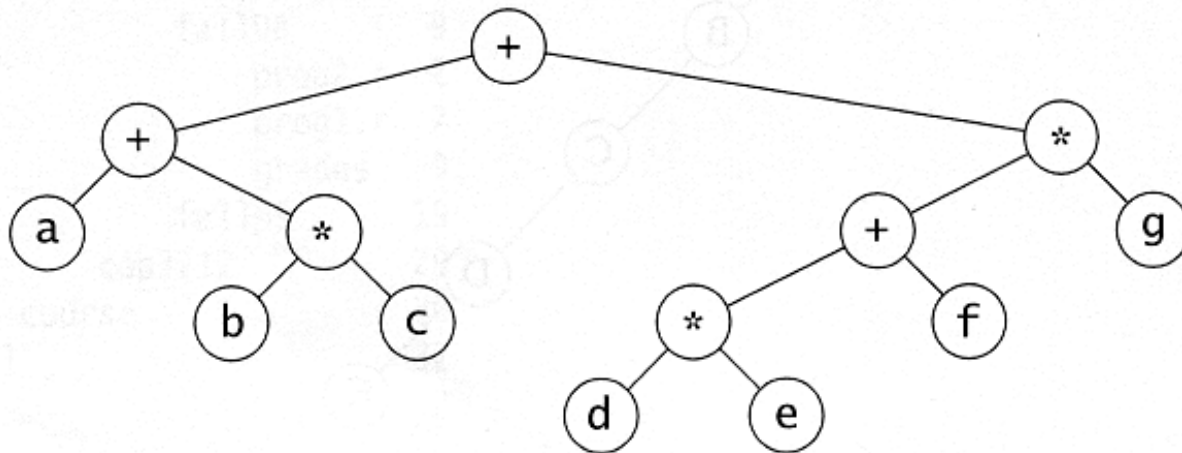


Figure 4.14 Expression tree for $(a + b * c) + ((d * e + f) * g)$

Preorder, Postorder and Inorder

- Postorder traversal

- left, right, node
- postfix expression
 - $abc^*+de^*f+g^*+$

- Inorder traversal

- left, node, right.
- infix expression
 - $a+b*c+d*e+f*g$

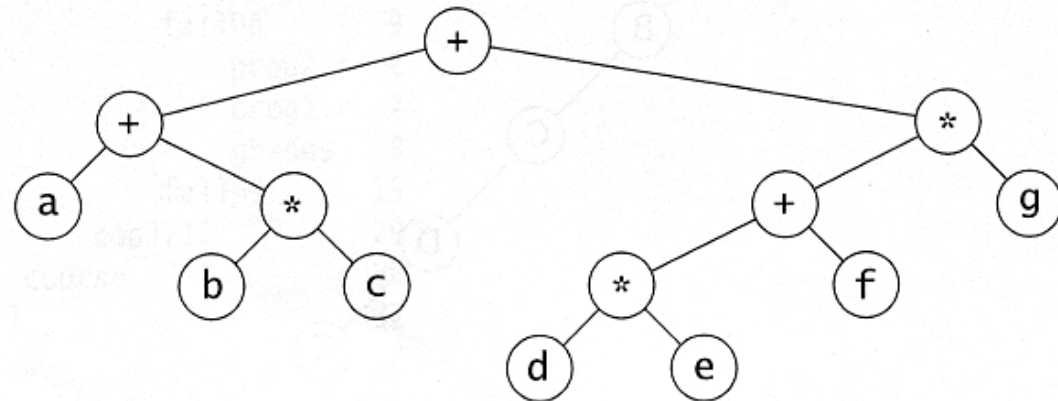
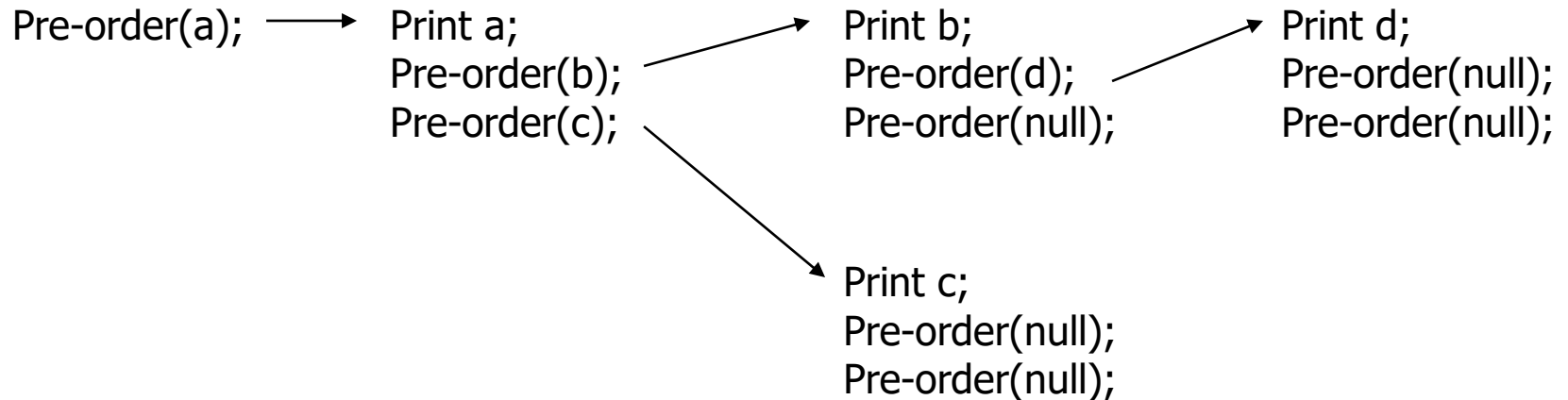
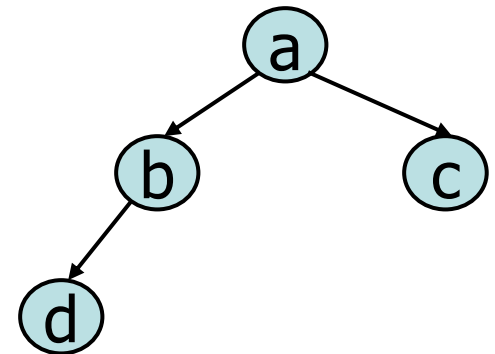


Figure 4.14 Expression tree for $(a + b * c) + ((d * e + f) * g)$

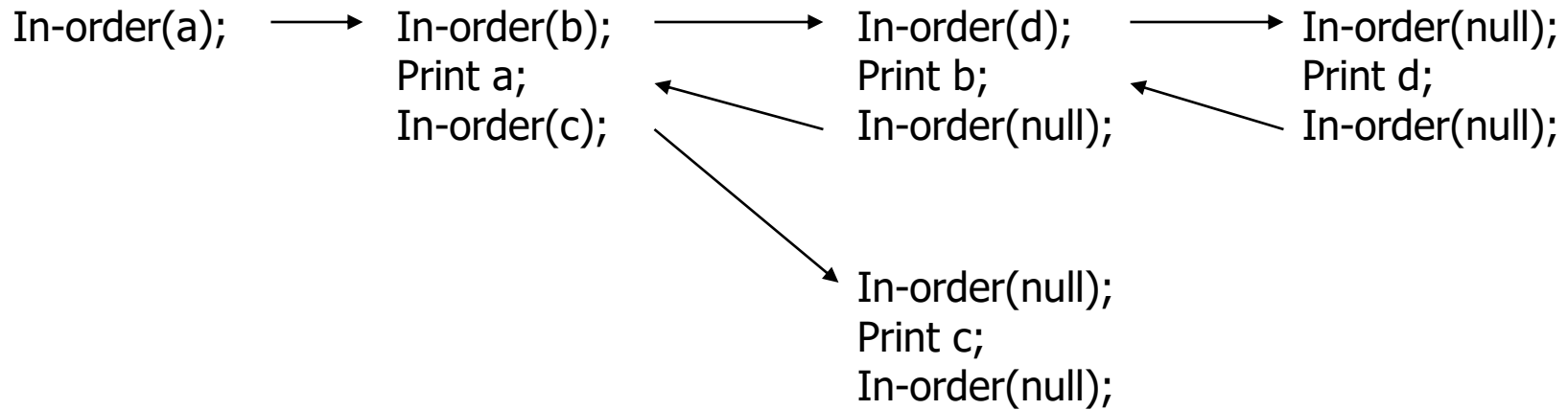
Pre-order example



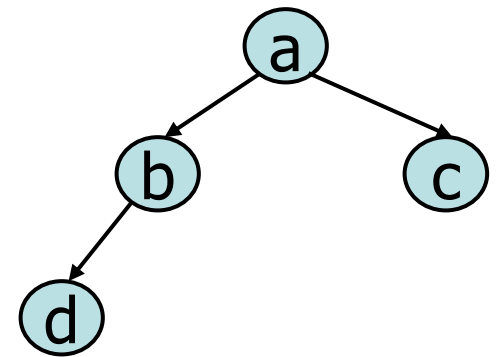
a b d c



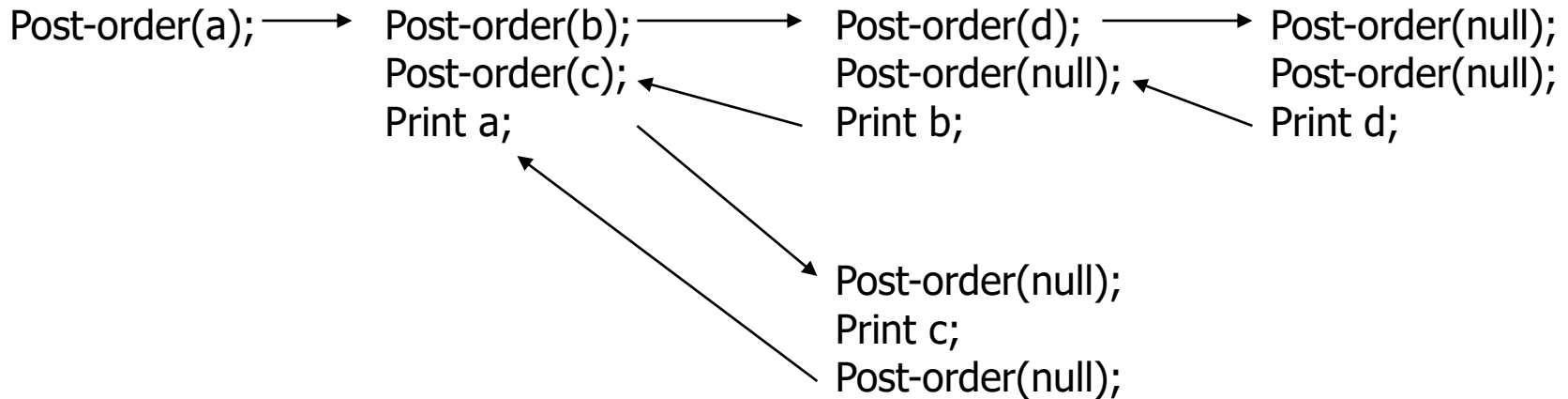
In-order example



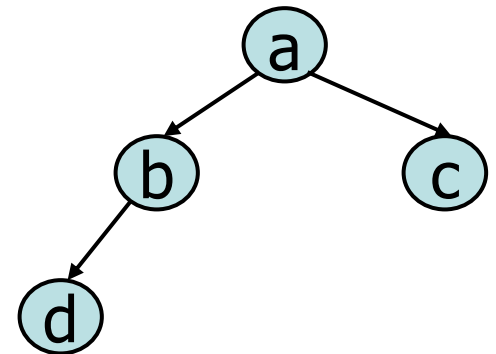
d b a c



Post-order example



d b c a

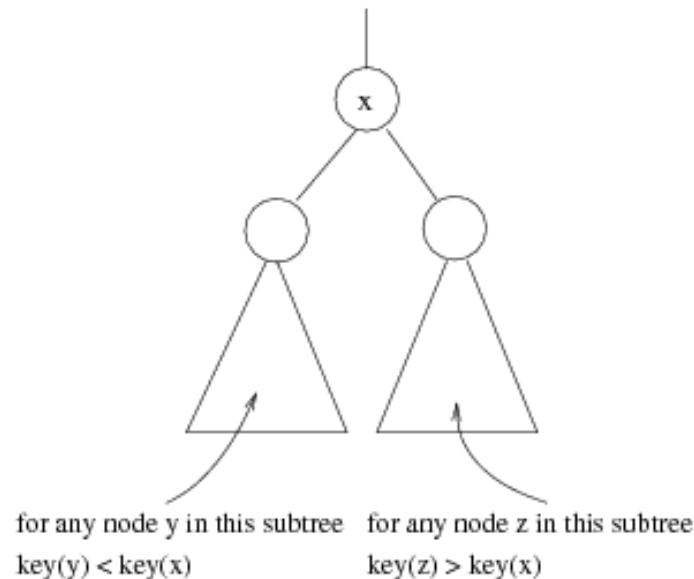


Binary Search Trees

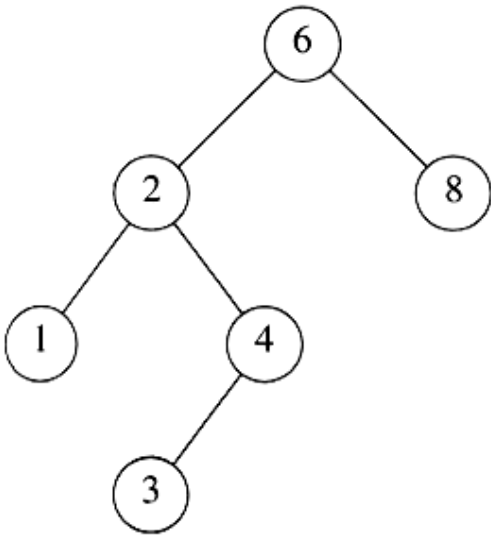
- Stores keys in the nodes in a way so that searching, insertion and deletion can be done efficiently.

Binary search tree property

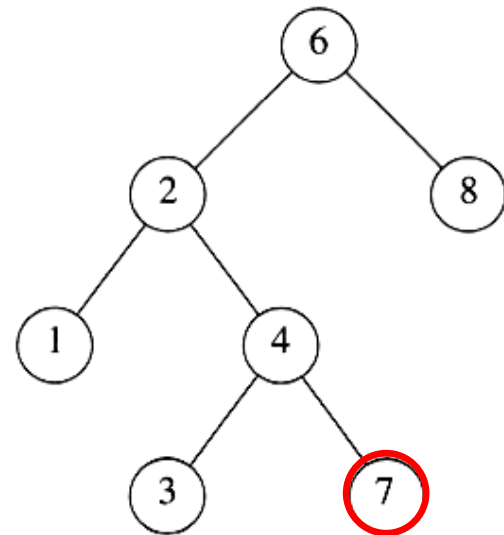
- For every node X , all the keys in its left subtree are smaller than the key value in X , and all the keys in its right subtree are larger than the key value in X



Binary Search Trees



A binary search tree

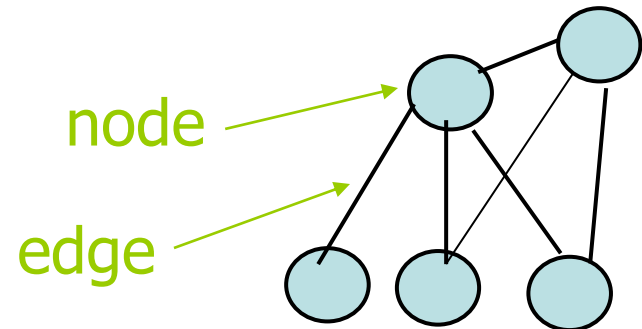


Not a binary search tree

Graphs

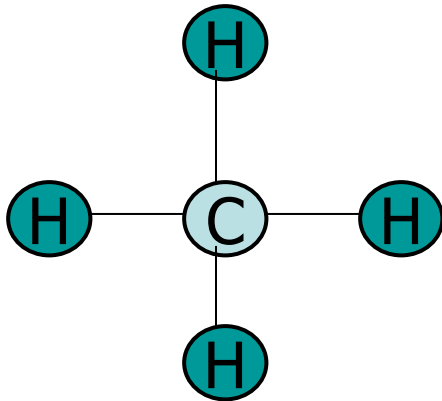
What is a graph?

- Graphs represent the relationships among data items
- A graph G consists of
 - a set V of nodes (vertices)
 - a set E of edges: each edge connects two nodes
- Each node represents an item
- Each edge represents the relationship between two items

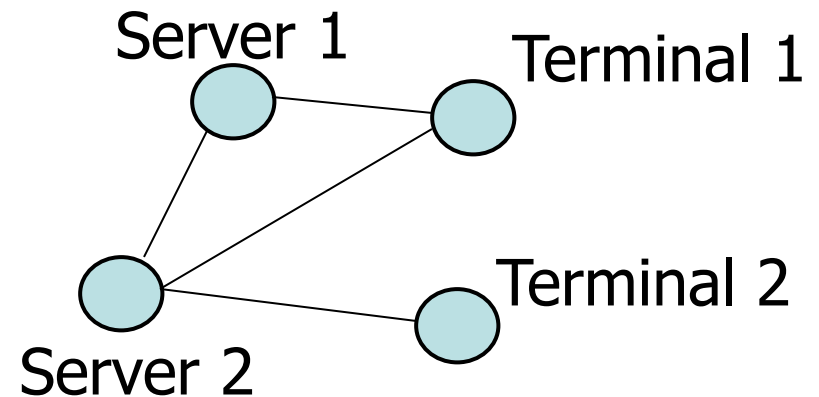


Examples of graphs

Molecular Structure



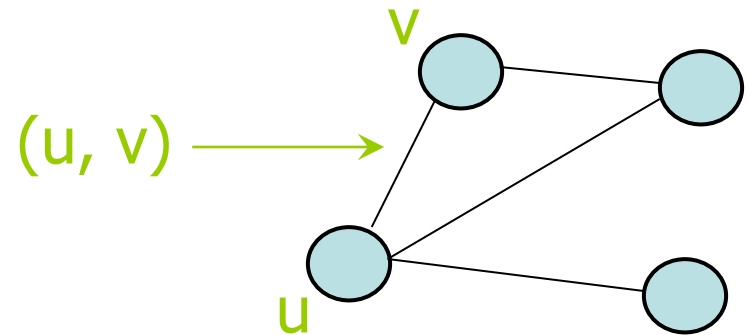
Computer Network



Other examples: electrical and communication networks, airline routes, flow chart, graphs for planning projects

Formal Definition of graph

- The set of nodes is denoted as V
- For any nodes u and v , if u and v are connected by an edge, such edge is denoted as (u, v)



- The set of edges is denoted as E
- A graph G is defined as a pair (V, E)