



## **DEPARTMENT OF MATHEMATICS**

## **ODD SEMESTER (JAN-MAY-2021)**

## T1 Examination, February 2021

**FACULTY NAME: Ms Savitta** Saini/Ms Seema Aggarwal/Dr Kalpana Shukla

NAME OF THE COURSE COORDINATOR: Ms Savitta Saini

**COURSE NAME: Probability** and Statistics MAH202B-T

**COURSE** CODE:

**CREDIT:** 04

**MAX. MARKS: 30** 

TIME DURATION: 90 min.

**DATE OF EXAM:** 09/02/2021 9:30 AM - 11:00 AM

Note: ALL QUESTIONS ARE COMPULSORY.

Q.NO.		QUESTIONS	MAR KS		BLOOM'S TAXONOMY LEVEL	ΡI
PART-A	Q1(A)	Suppose that $X$ is a random variable with $E[X] = 10$ and $VAR[X] = 25$ . Find the positive numbers $a$ and $b$ such that $Y = aX + b$ has mean 0 and variance 1.	2	CO1	вт3	
	Q1(B)	Find the constant $k$ such that the following is a p.d.f. $f(x) = \begin{cases} 0, & \text{if } 0 \le x < 2\\ 2k, & \text{if } 2 \le x < 4\\ -kx + 6k, & \text{if } 4 \le x < 6 \end{cases}$	2	CO1	ВТ3	
	Q1(C)	Can a binomial distribution have mean 3 and variance 4? Justify your answer.	2	CO2	BT2	
	Q1(D)	Let Y be the absolute difference of the upturned faces in the experiment of tossing two dice. Find $E[Y]$	2	CO1	ВТ3	

	Q1(E)	Prove or disprove if $P(A) = 0$ , then $P(A \cap B) = 0$	2	CO1	ВТ3	
	Q2(A)	<ul> <li>A bombing plane flies directly above a rail road track. Assume that if a small bomb falls within 15 feet of the track, the track will be sufficiently damaged so that traffic will be disrupted. Let X denotes the perpendicular distance from the track that a bomb falls. Assume that f<sub>X</sub>(x) = 100-x/5000 ,0 ≤ x ≤ 100</li> <li>(i) Find the probability that a small bomb will disrupt the traffic.</li> <li>(ii) If a plane can carry 8 small bombs and uses all the eight, what is the probability that traffic will be disrupted?</li> </ul>	5	CO1	BT3	
PART-B	Q2(B)	An Urn contains balls numbered 1, 2 and 3. First a ball is drawn from the urn and then a fair coin is tossed the number of times as the number shown on the drawn ball. Find the expected number of heads.	5	CO1	ВТ3	
	Q3(A)	Suppose that flaws in plywood occur at random with an average of one flaw per 50 square feet. What is the probability that a 4 foot × 8 foot sheet will have no flaws? At most one flaw? (Assume that the number of flaws per unit area is Poisson distributed).	5	CO2	BT3	
	Q3(B)	If on the average rain falls on 10 days in every 30 days, obtain the probability that	5	CO2	ВТ3	

	(i) rain will fall on at least 3 days of a given week (ii) first three days of a given week will be fine and the remaining 4 days wet.
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