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MyMainScript

```
clc; clear;
tic;
```

NOTE

```
% Please ensure that image processing toolbox is installed as well.
% The ellipses may not be closed due to the pointset generation
  procedure
% used.
% The .mat files for ellipse, leaf and brain dataset are generated
% manually using traceBoundaries.m which is included in the folder.
```

Reading ellipse data

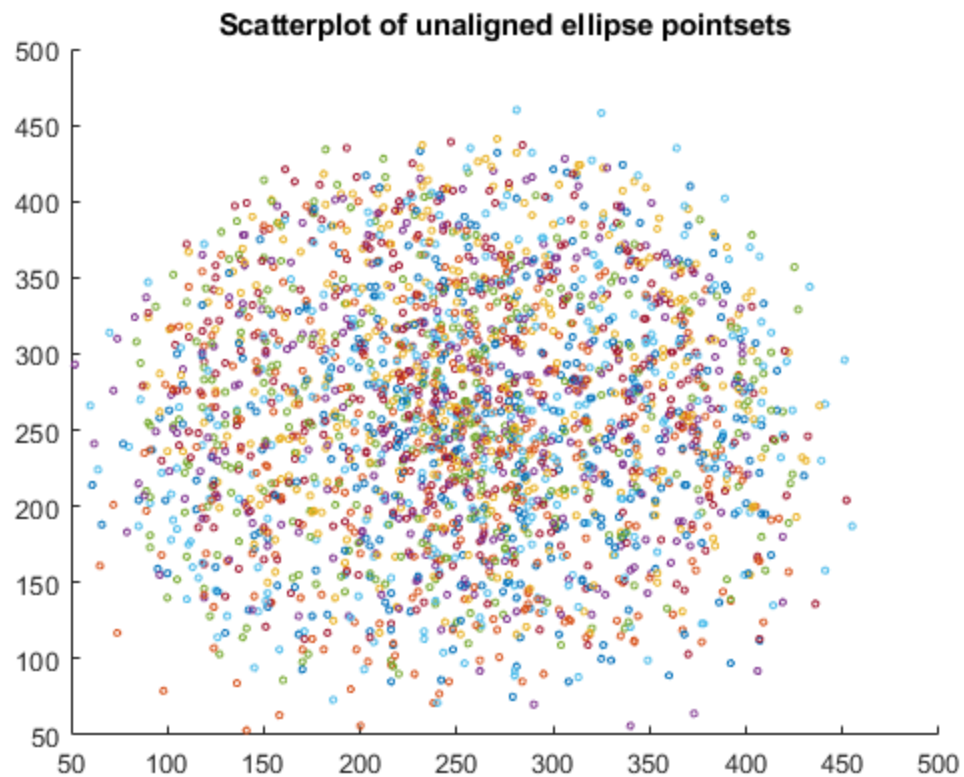
```
filePath = "../data/ellipse/data/";
%tracingBoundaries(".jpg", 150, 16, filePath);
data = load("../data/ellipse.mat");
imgs = data.shapes;

[dims, m, n] = size(imgs);
```

```

% plotting all the ellipses
figure
hold on
for i = 1:n
    scatter(imgs(1, :, i), imgs(2, :, i), 6);
end
title("Scatterplot of unaligned ellipse pointsets");
hold off

```

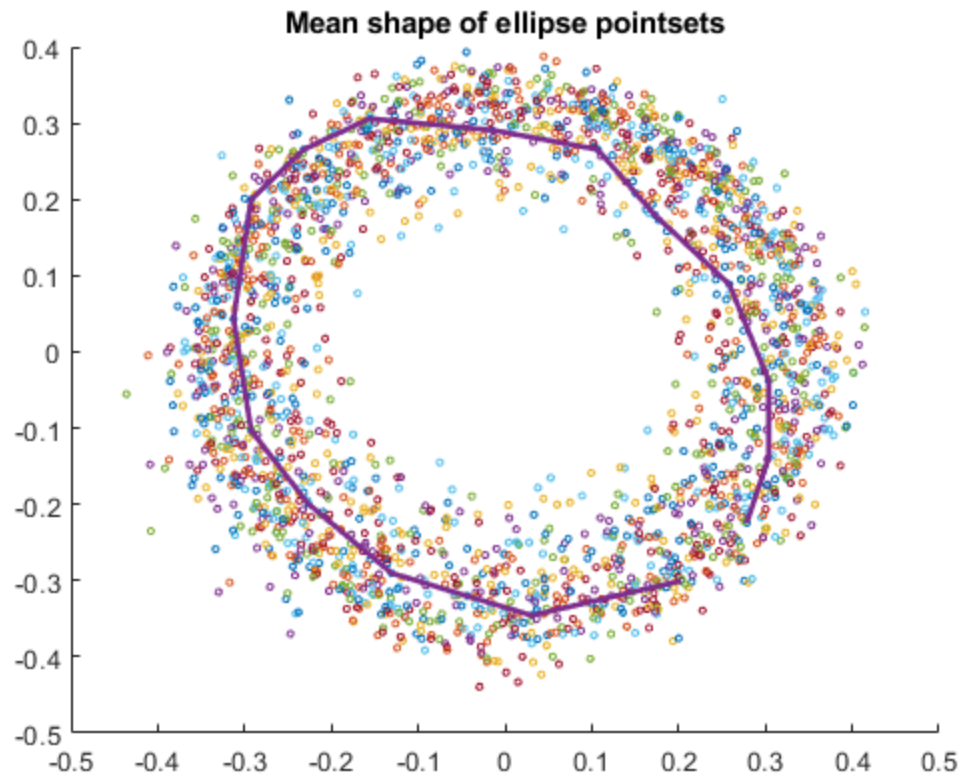


Mean shape of ellipse data

```

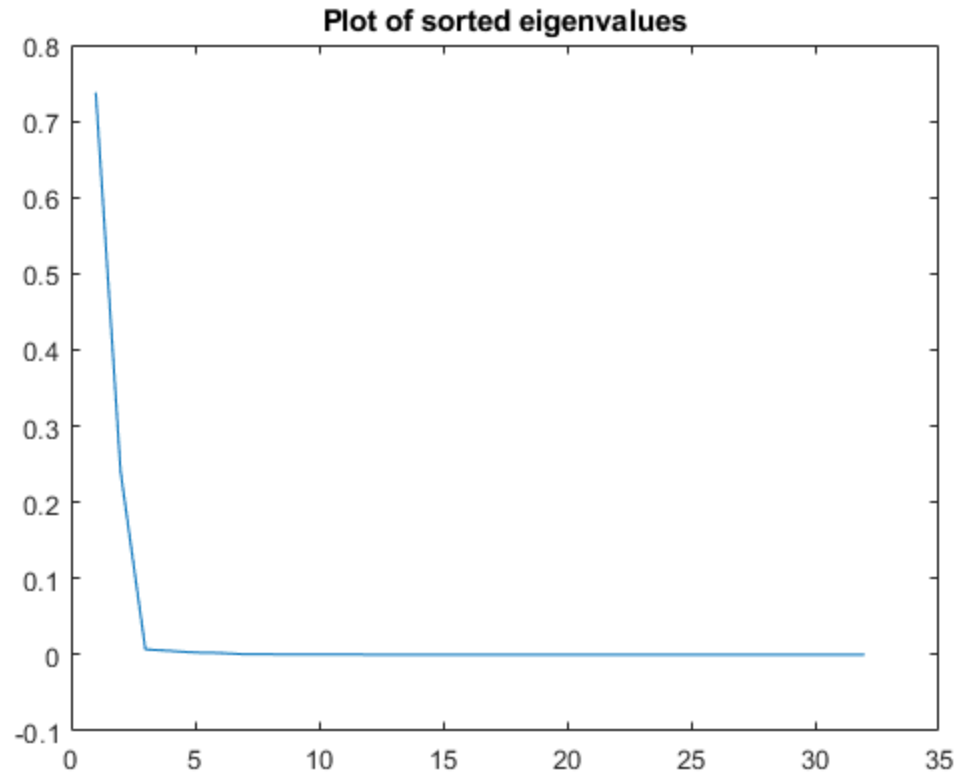
[ms, newPS] = meanShape(imgs);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
plot(ms(1, :), ms(2, :), 'LineWidth', 2);
title("Mean shape of ellipse pointsets");
hold off

```



Eigenvalues calculation

```
[D, W] = eigenCalc(newPS);  
figure  
plot(D);  
title("Plot of sorted eigenvalues");
```



Top 3 modes of variations

```
% 1st eigenvalue
ms1 = ms + 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
ms2 = ms - 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 1st eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off

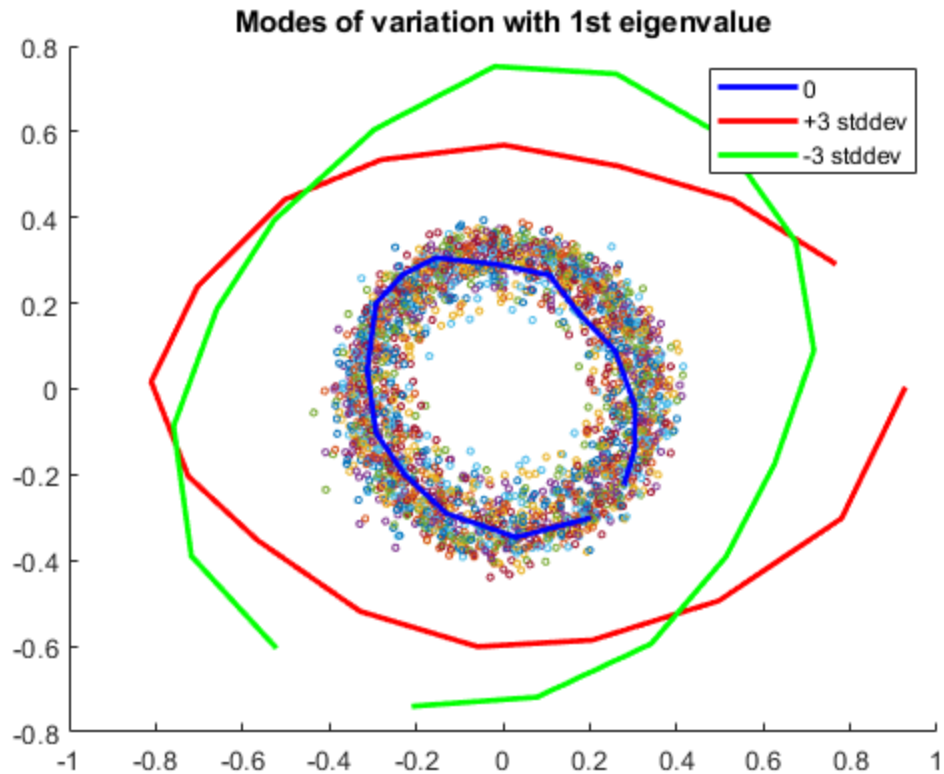
% 2nd eigenvalue
ms1 = ms + 3 * sqrt(D(2)) * reshape(W(:, 2), [2, m]);
ms2 = ms - 3 * sqrt(D(2)) * reshape(W(:, 2), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
```

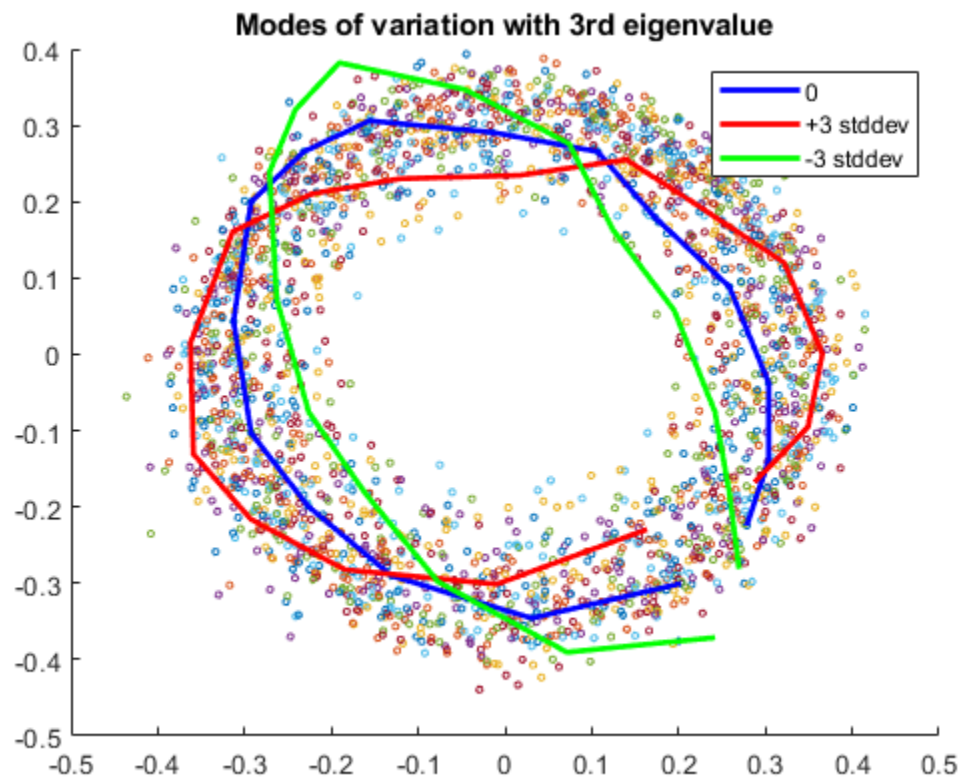
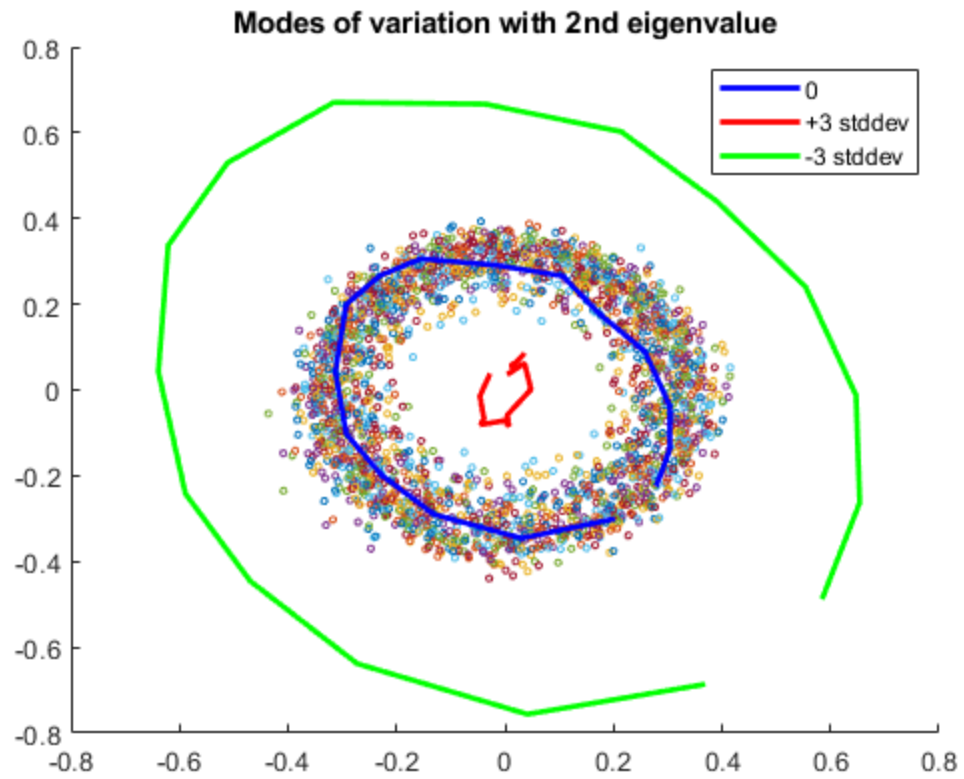
```

p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 2nd eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off

% 3rd eigenvalue
ms1 = ms + 3 * sqrt(D(3)) * reshape(W(:, 3), [2, m]);
ms2 = ms - 3 * sqrt(D(3)) * reshape(W(:, 3), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 3rd eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off

```





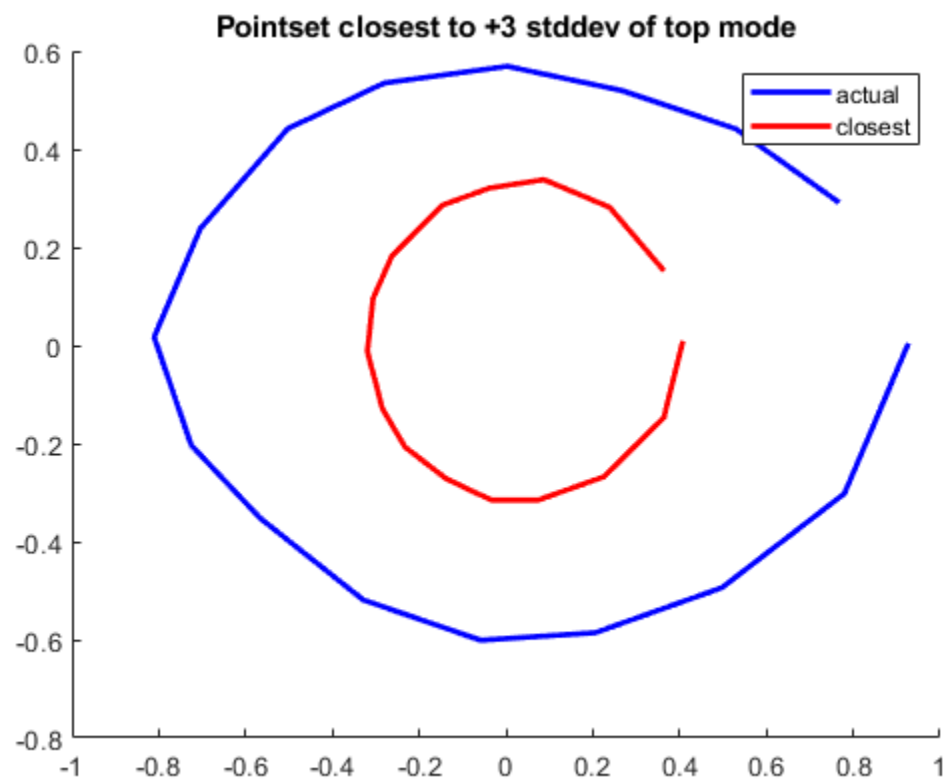
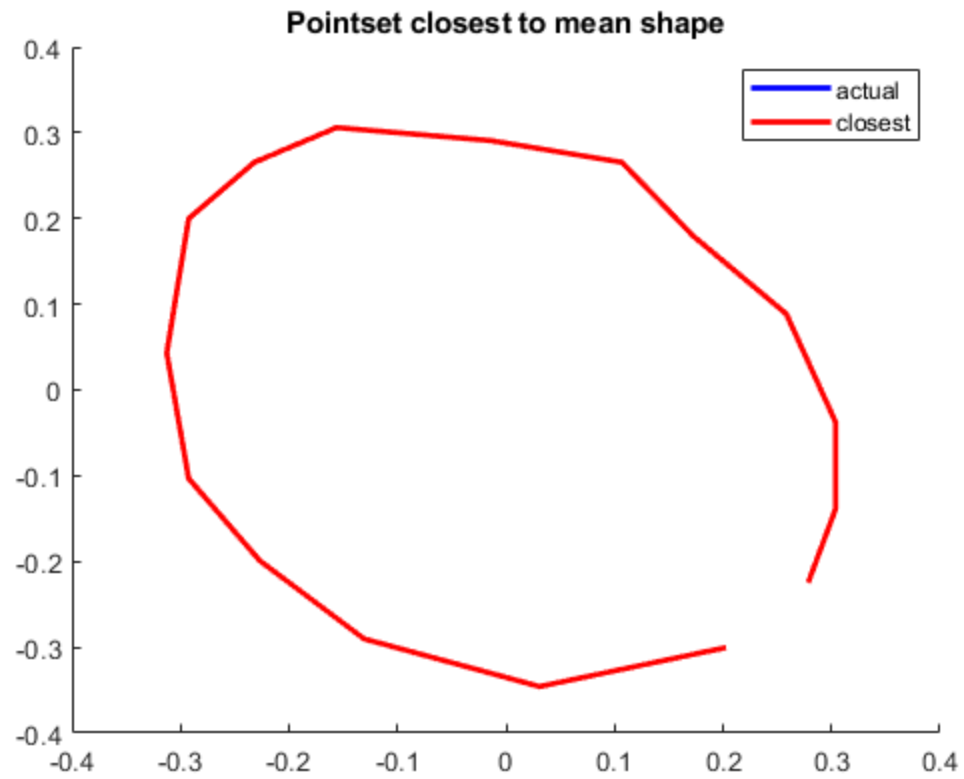
Closest pointsets

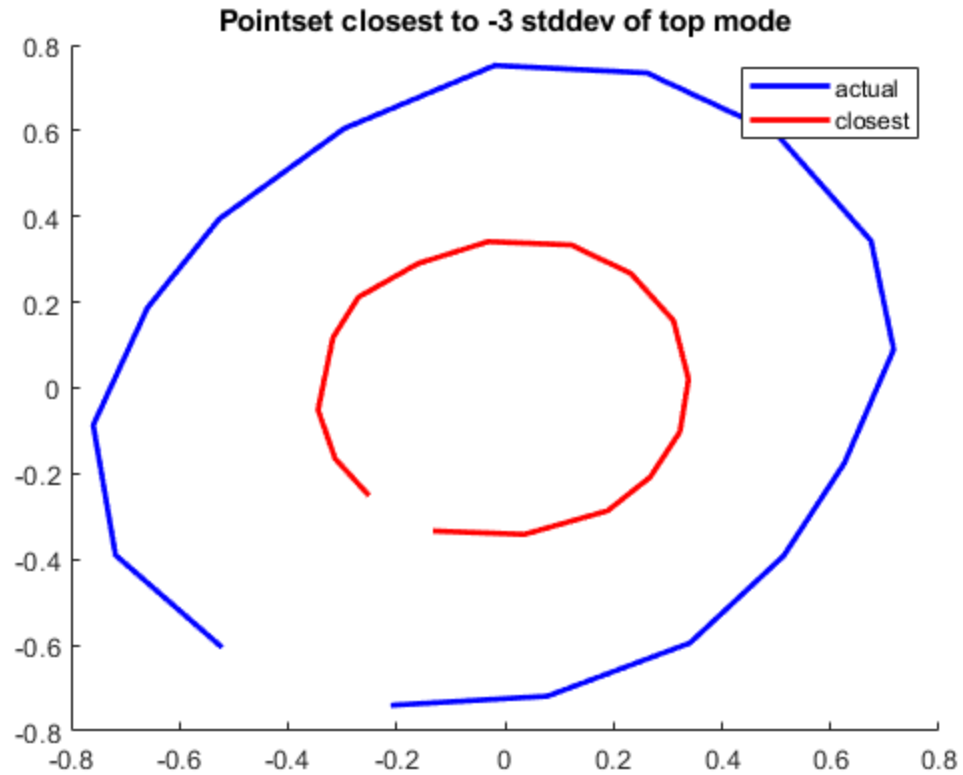
```
ms1 = ms + 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
ms2 = ms - 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);

% Closest to mean shape
ps = findMinErrorPS(newPS, ms);
figure
hold on
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to mean shape");
legend([p1, p2], "actual", "closest");
hold off

% Closest to +3 stddev
ps = findMinErrorPS(newPS, ms1);
figure
hold on
p1 = plot(ms1(1, :), ms1(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to +3 stddev of top mode");
legend([p1, p2], "actual", "closest");
hold off

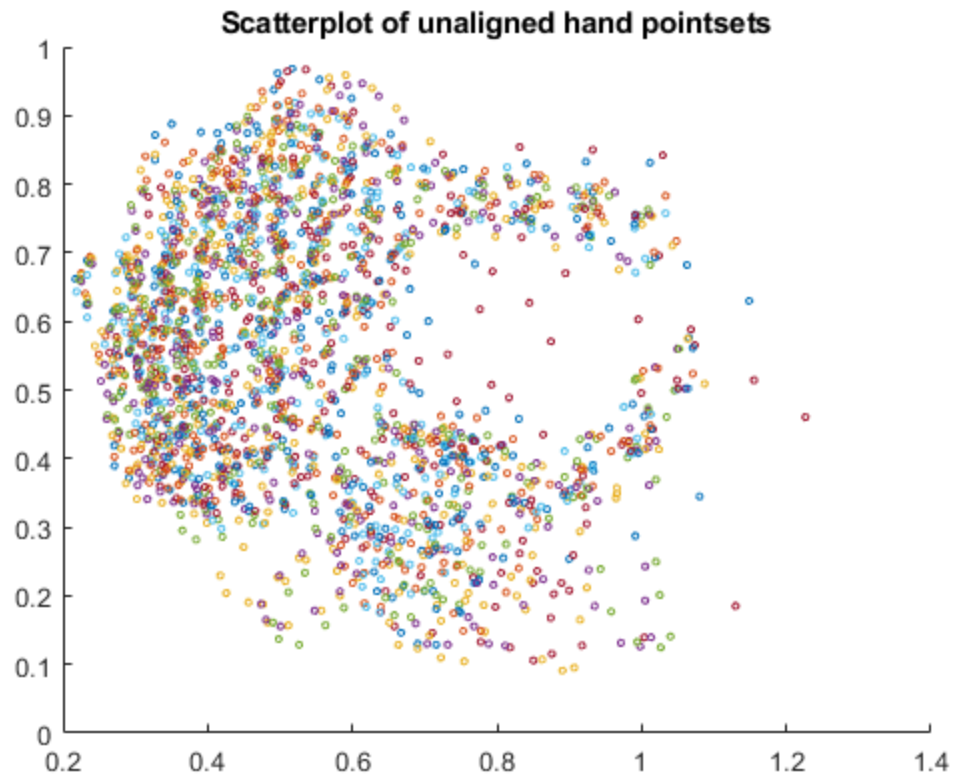
% Closest to -3 stddev
ps = findMinErrorPS(newPS, ms2);
figure
hold on
p1 = plot(ms2(1, :), ms2(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to -3 stddev of top mode");
legend([p1, p2], "actual", "closest");
hold off
```





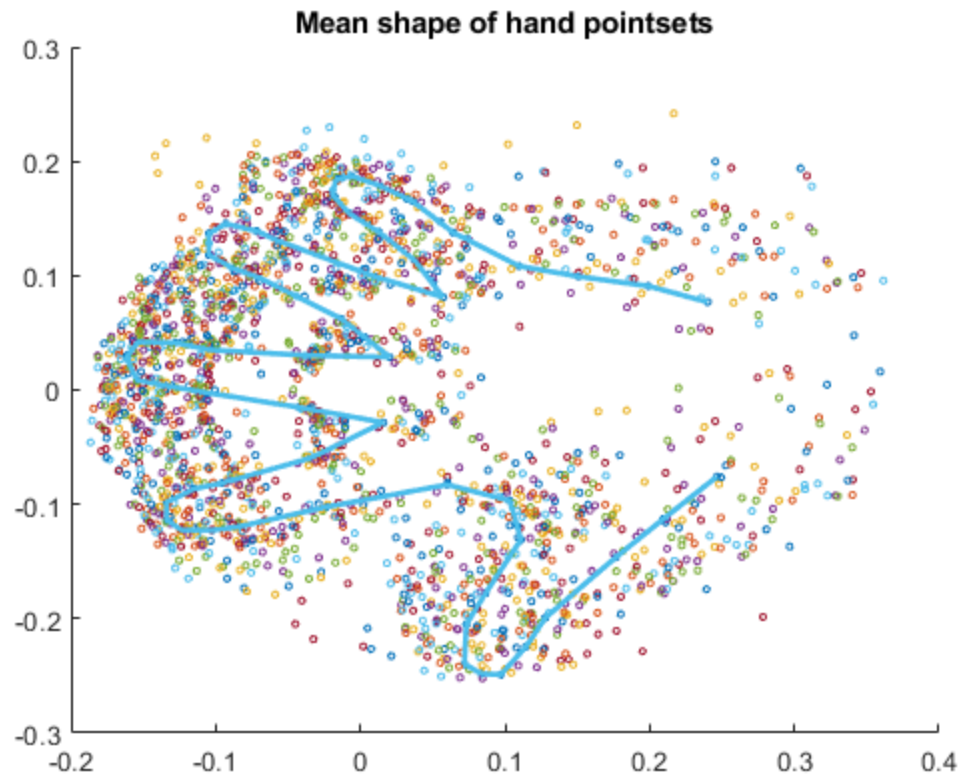
Reading hand data

```
data = load("../data/hand/data.mat");  
imgs = data.shapes;  
  
[dims, m, n] = size(imgs);  
  
% plotting all the hands  
figure  
hold on  
for i = 1:n  
    scatter(imgs(1, :, i), imgs(2, :, i), 6);  
end  
title("Scatterplot of unaligned hand pointsets");  
hold off
```



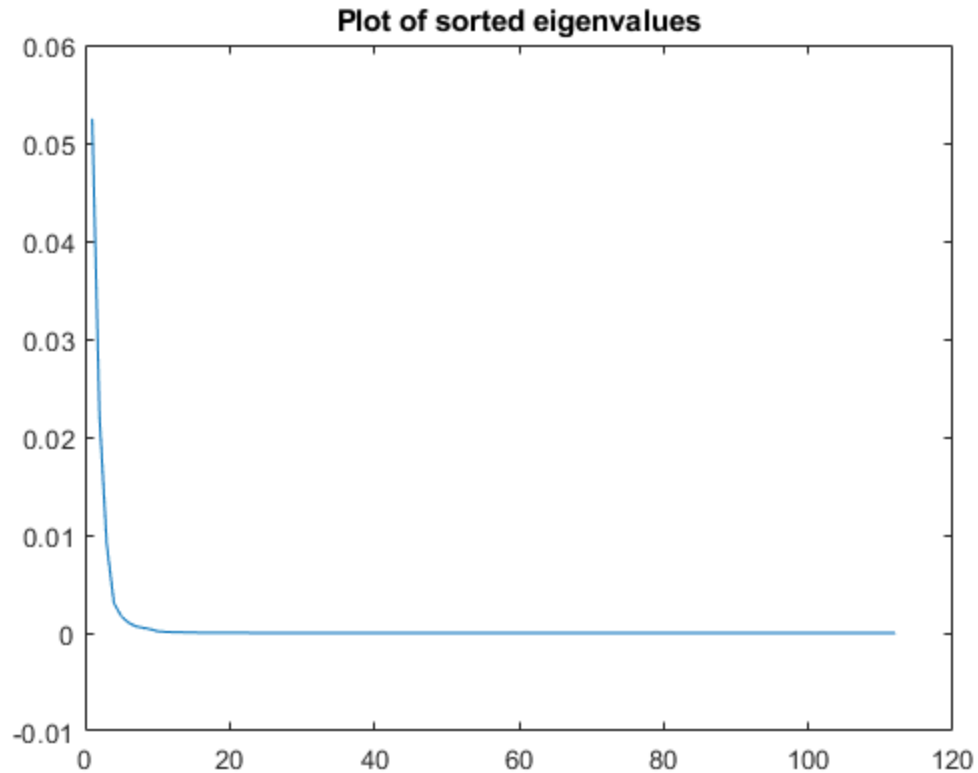
Mean shape of hand data

```
[ms, newPS] = meanShape(imgs);  
figure  
hold on  
for i = 1:n  
    scatter(newPS(1, :, i), newPS(2, :, i), 6);  
end  
plot(ms(1, :), ms(2, :), 'LineWidth', 2);  
title("Mean shape of hand pointsets");  
hold off
```



Eigenvalues calculation

```
[D, W] = eigenCalc(newPS);  
figure  
plot(D);  
title("Plot of sorted eigenvalues");
```



Top 3 modes of variations

```
% 1st eigenvalue
ms1 = ms + 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
ms2 = ms - 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 1st eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off

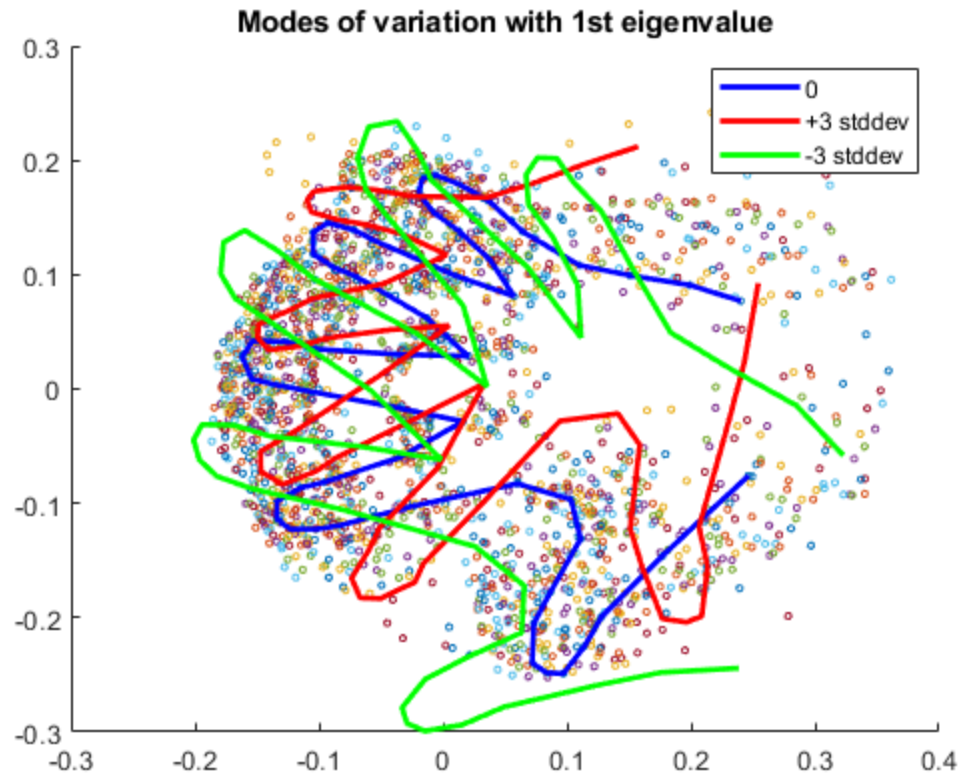
% 2nd eigenvalue
ms1 = ms + 3 * sqrt(D(2)) * reshape(W(:, 2), [2, m]);
ms2 = ms - 3 * sqrt(D(2)) * reshape(W(:, 2), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
```

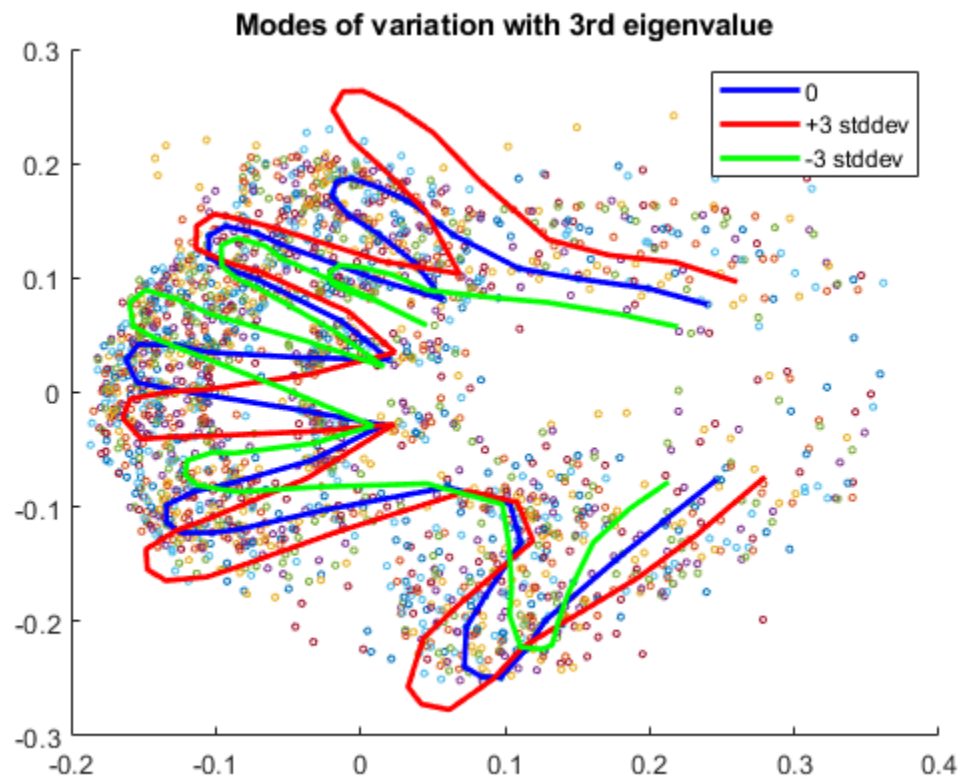
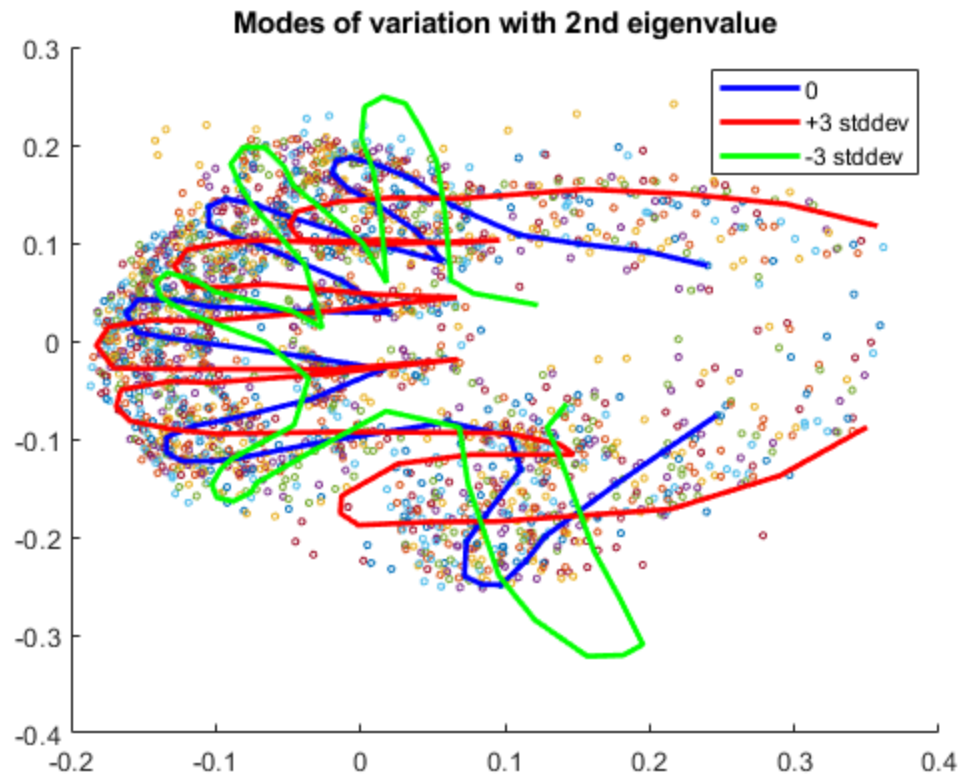
```

p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 2nd eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off

% 3rd eigenvalue
ms1 = ms + 3 * sqrt(D(3)) * reshape(W(:, 3), [2, m]);
ms2 = ms - 3 * sqrt(D(3)) * reshape(W(:, 3), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 3rd eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off

```





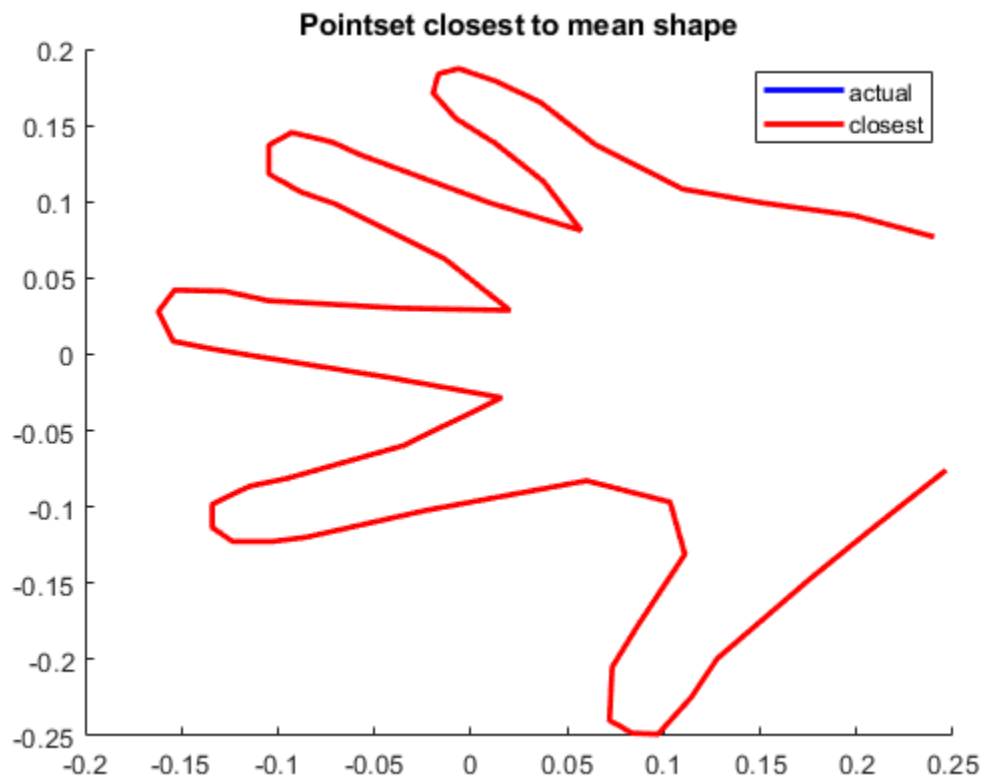
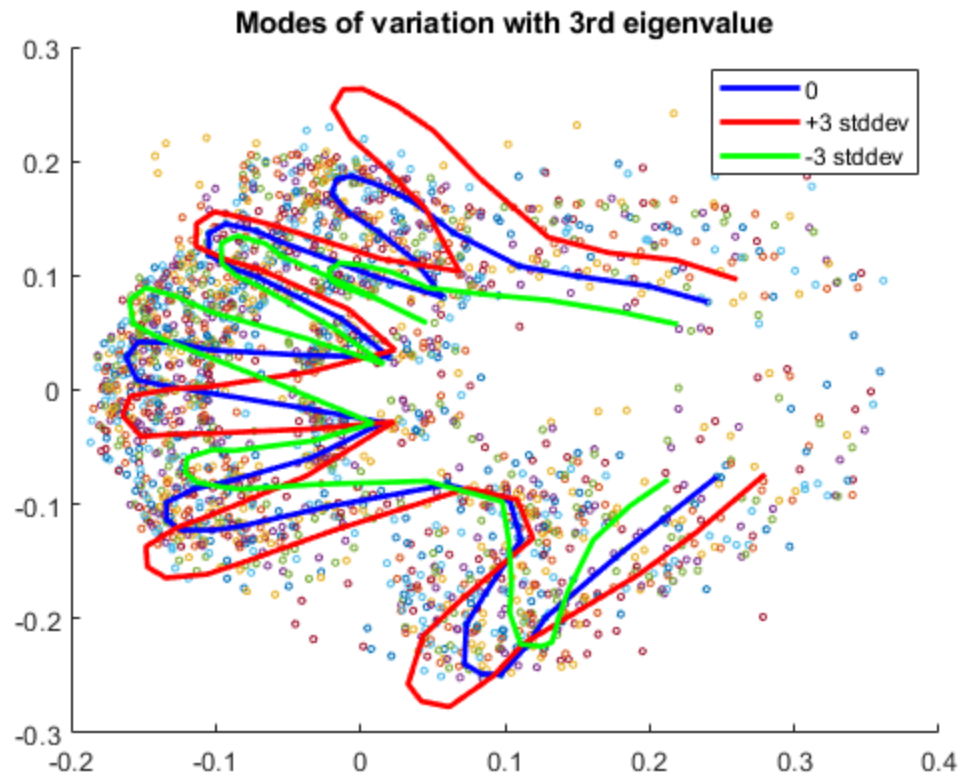
Closest pointsets

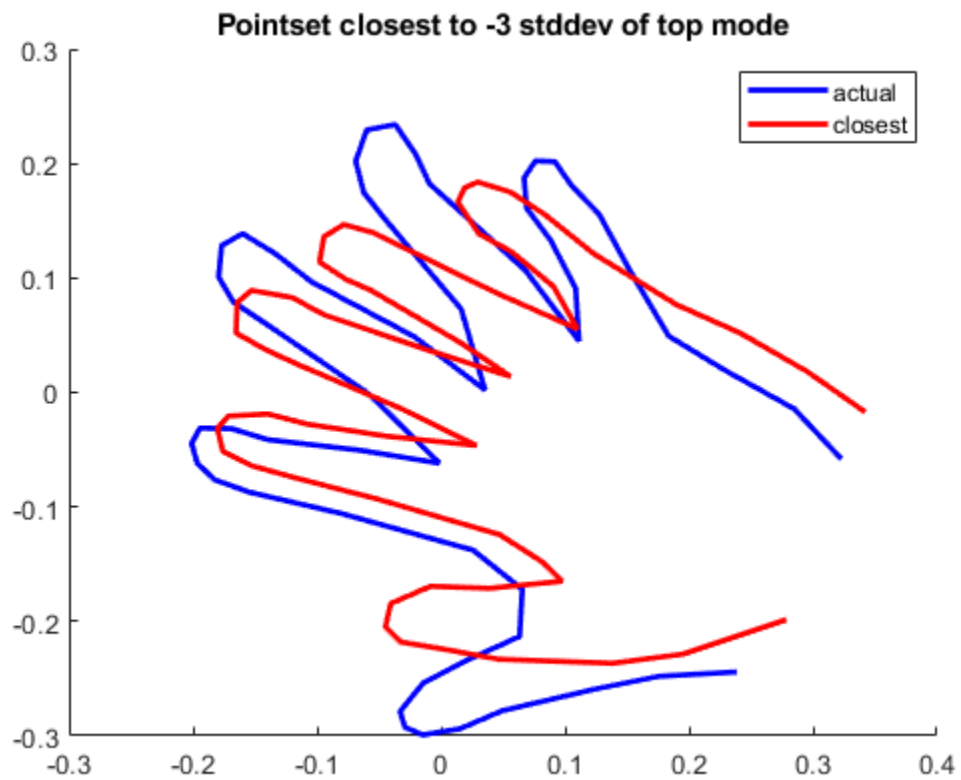
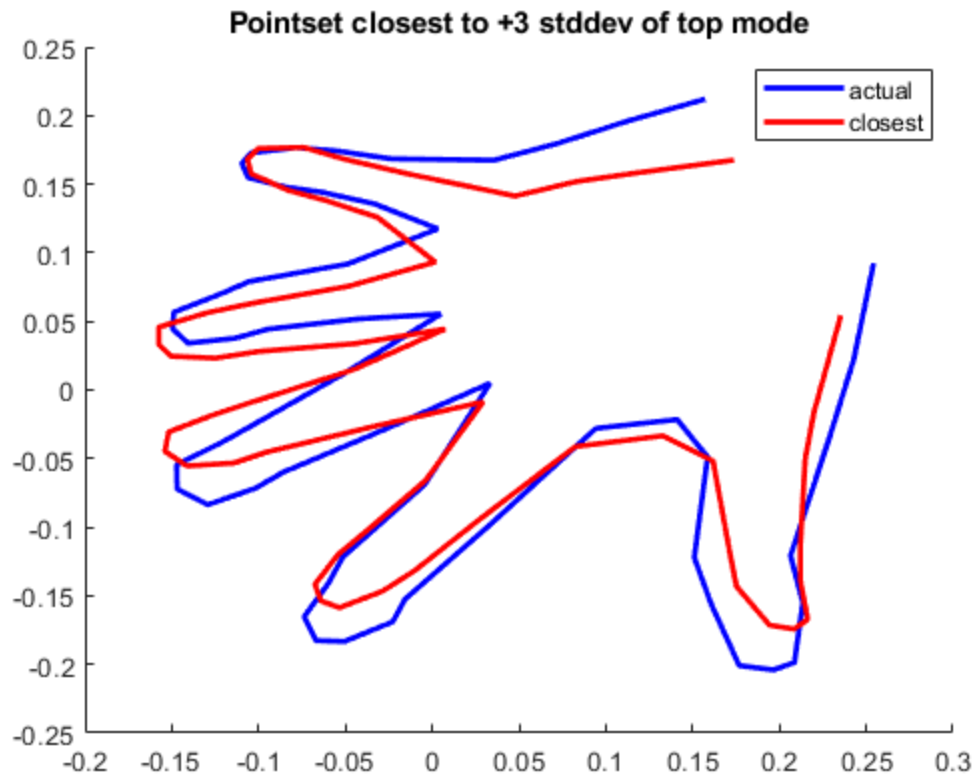
```
ms1 = ms + 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
ms2 = ms - 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);

% Closest to mean shape
ps = findMinErrorPS(newPS, ms);
figure
hold on
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to mean shape");
legend([p1, p2], "actual", "closest");
hold off

% Closest to +3 stddev
ps = findMinErrorPS(newPS, ms1);
figure
hold on
p1 = plot(ms1(1, :), ms1(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to +3 stddev of top mode");
legend([p1, p2], "actual", "closest");
hold off

% Closest to -3 stddev
ps = findMinErrorPS(newPS, ms2);
figure
hold on
p1 = plot(ms2(1, :), ms2(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to -3 stddev of top mode");
legend([p1, p2], "actual", "closest");
hold off
```



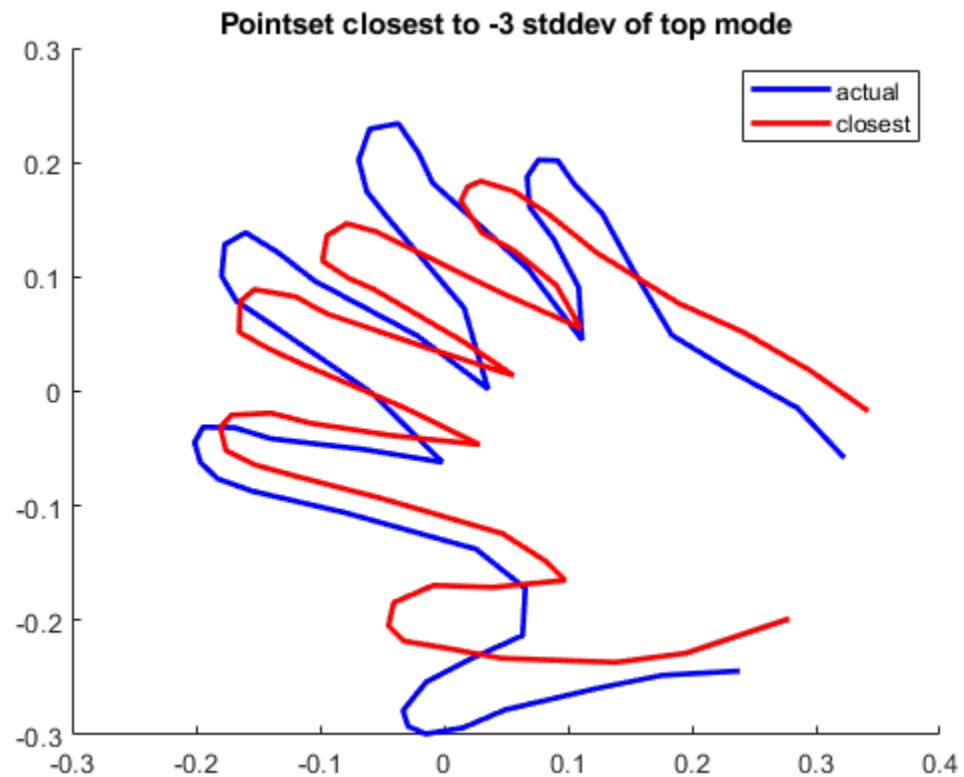


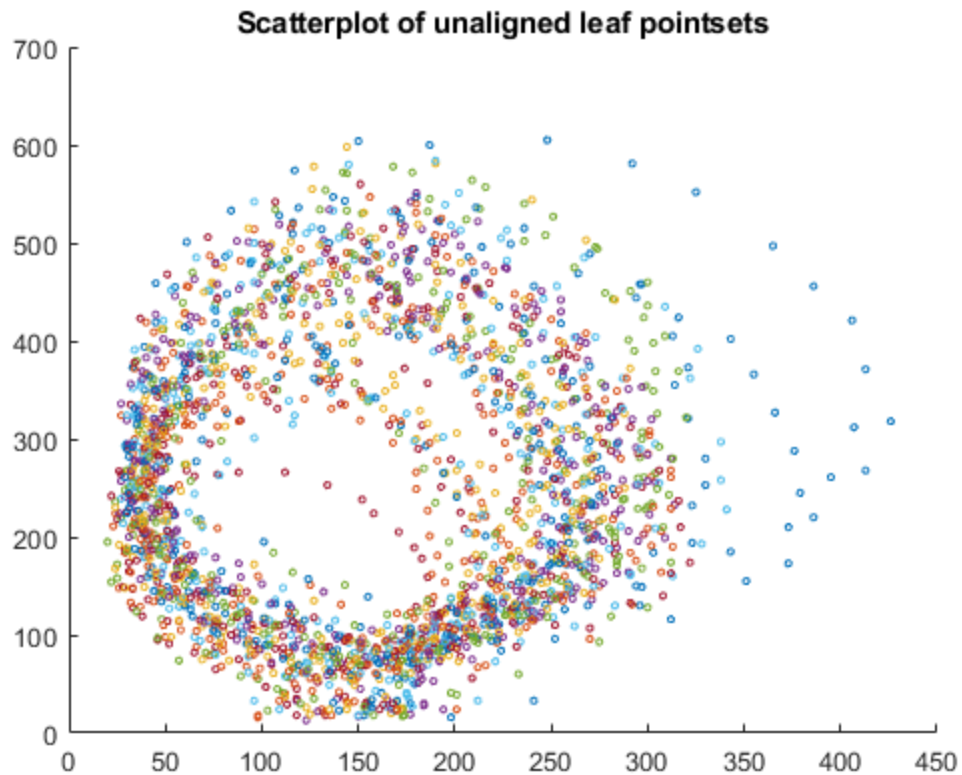
Reading leaf data

```
filePath = "../data/leaf/data/leaf_";
%tracingBoundaries(".png", 75, 32, filePath);
data = load("../data/leaf.mat");
imgs = data.shapes;

[dims, m, n] = size(imgs);

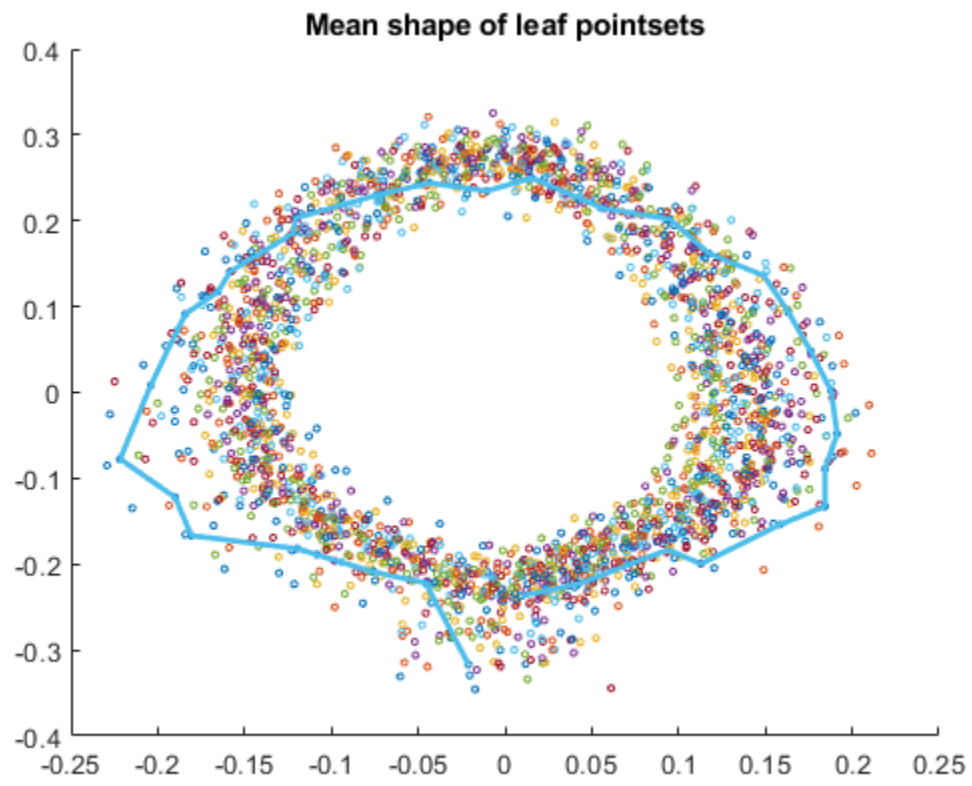
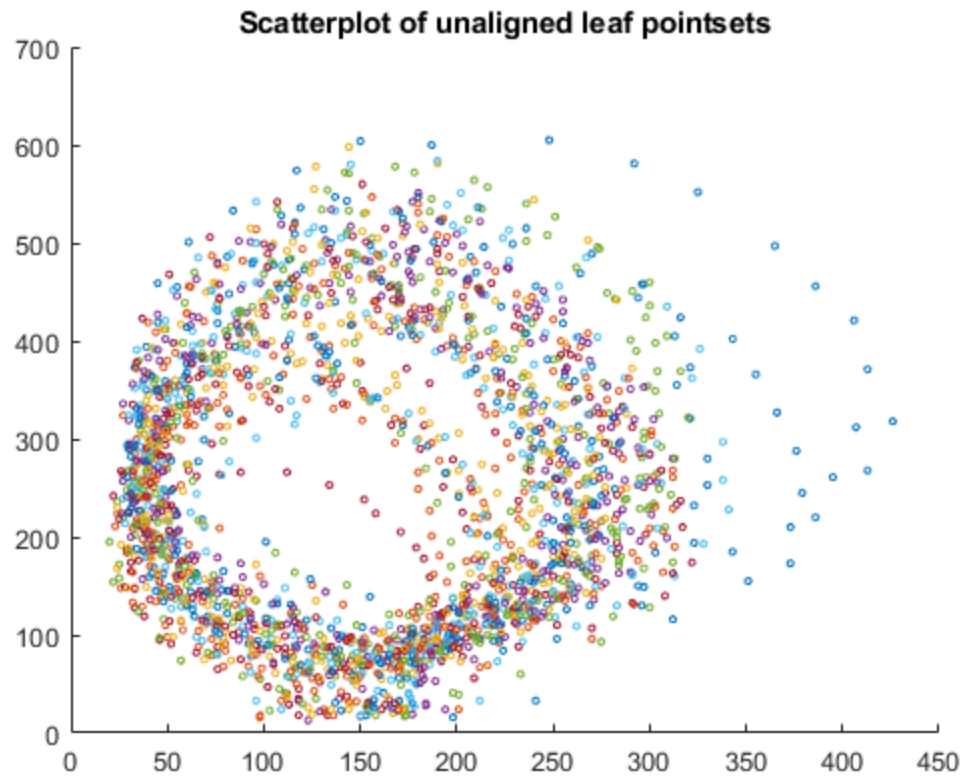
% plotting all the hands
figure
hold on
for i = 1:n
    scatter(imgs(1, :, i), imgs(2, :, i), 6);
end
title("Scatterplot of unaligned leaf pointsets");
hold off
```





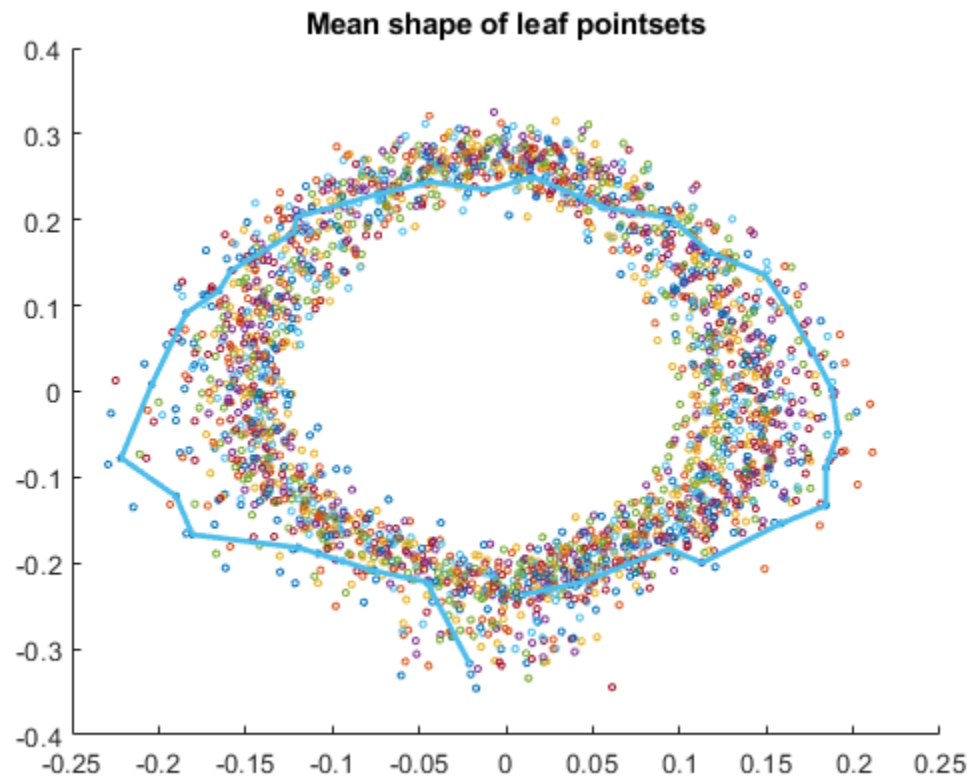
Mean shape of leaf data

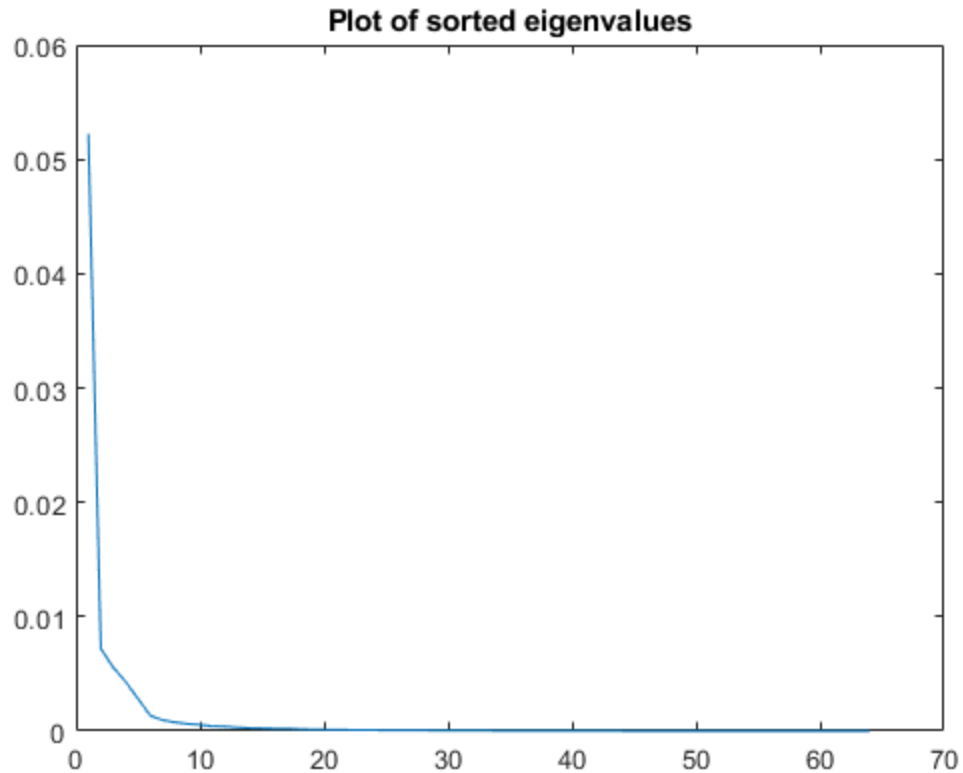
```
[ms, newPS] = meanShape(imgs);  
figure  
hold on  
for i = 1:n  
    scatter(newPS(1, :, i), newPS(2, :, i), 6);  
end  
plot(ms(1, :), ms(2, :), 'LineWidth', 2);  
title("Mean shape of leaf pointsets");  
hold off
```



Eigenvalues calculation

```
[D, W] = eigenCalc(newPS);  
figure  
plot(D);  
title("Plot of sorted eigenvalues");
```





Top 3 modes of variations

```
% 1st eigenvalue
ms1 = ms + 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
ms2 = ms - 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 1st eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off

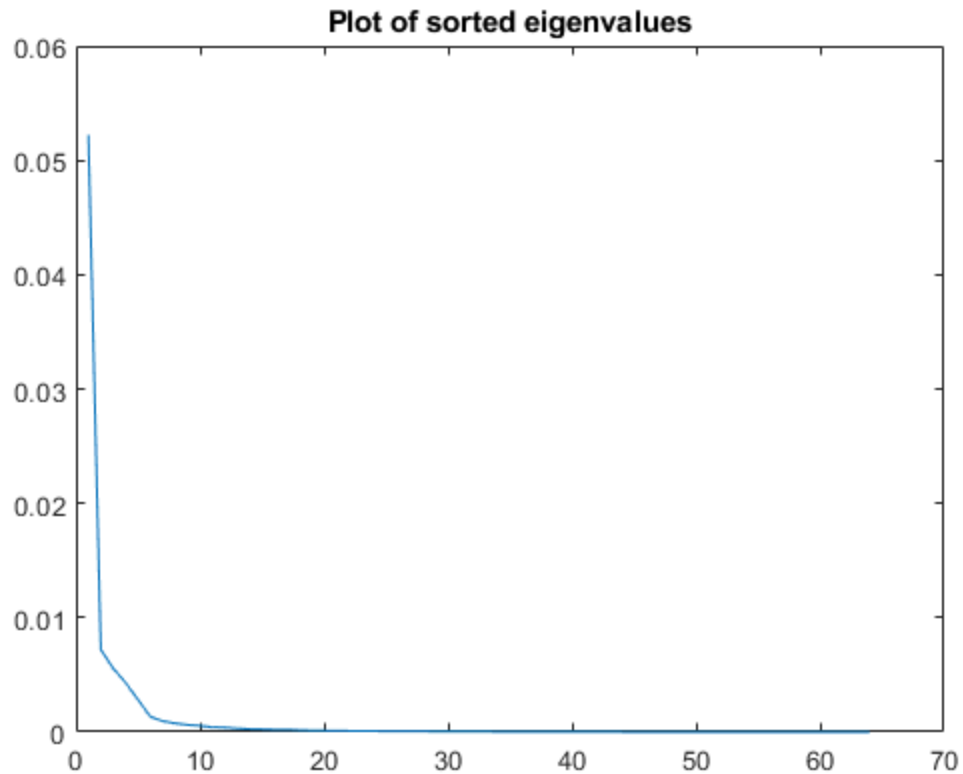
% 2nd eigenvalue
ms1 = ms + 3 * sqrt(D(2)) * reshape(W(:, 2), [2, m]);
ms2 = ms - 3 * sqrt(D(2)) * reshape(W(:, 2), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
```

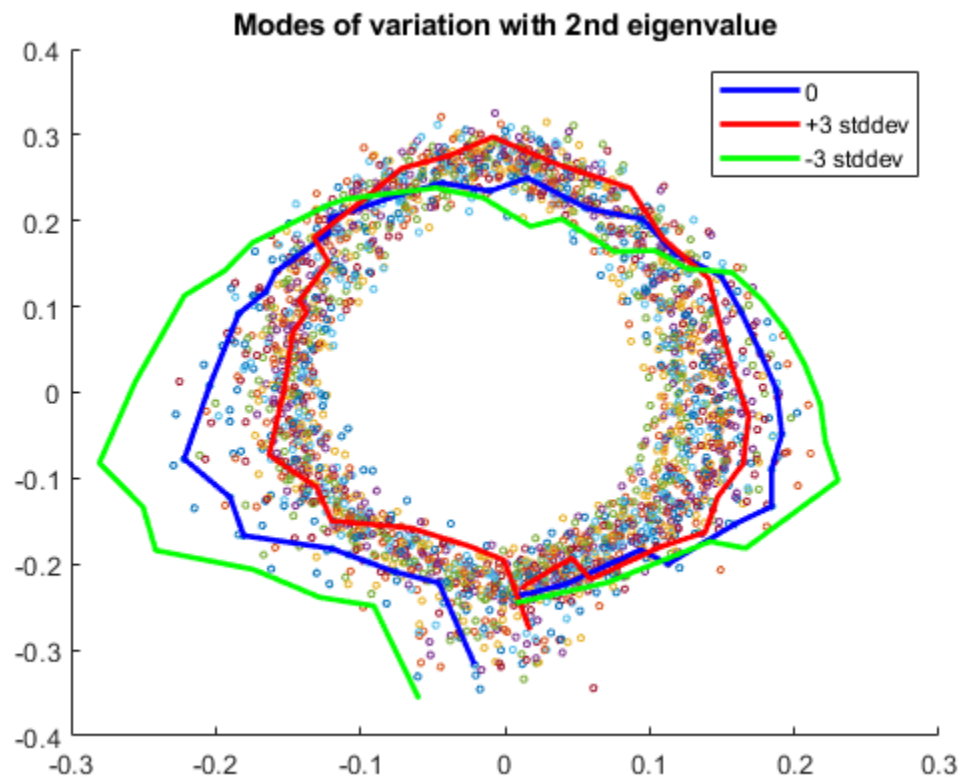
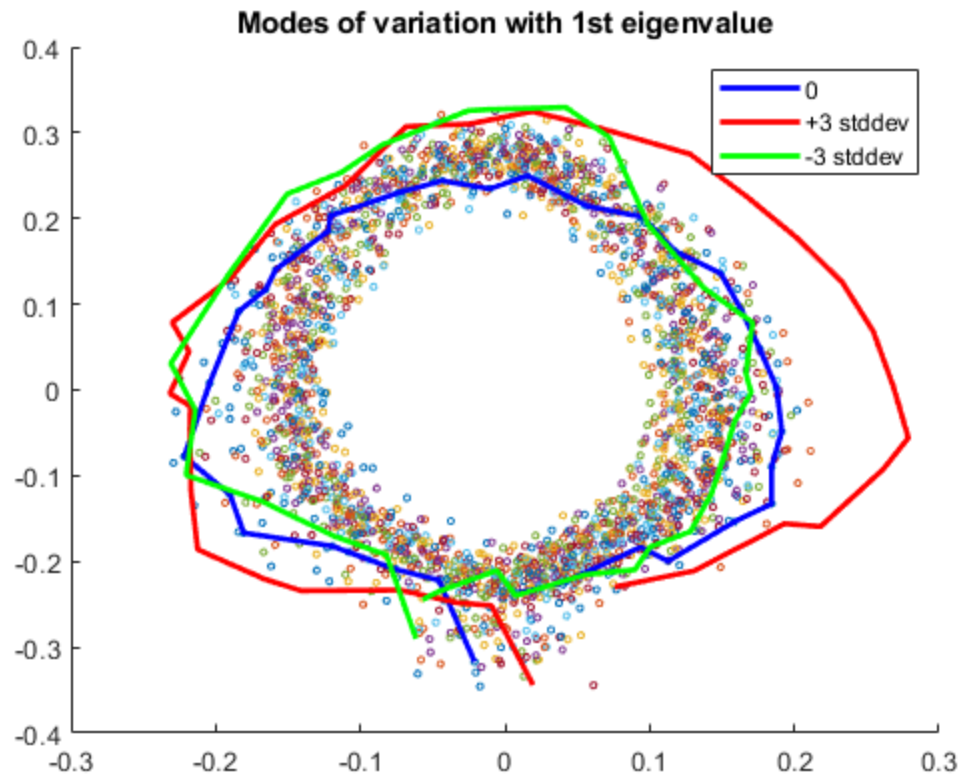
```

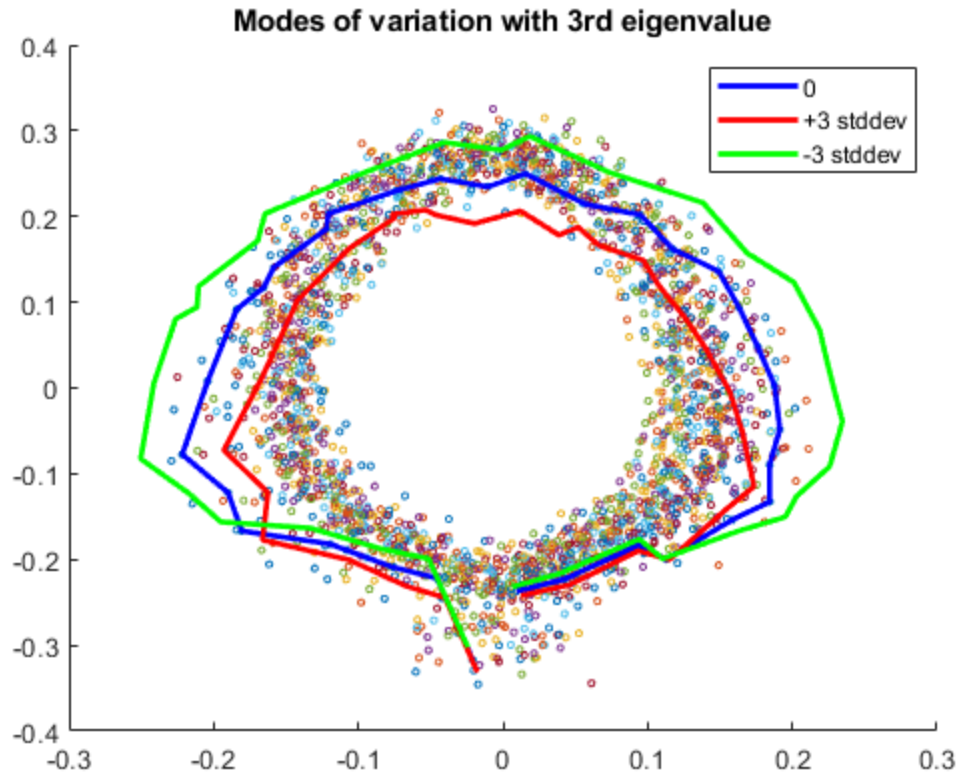
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 2nd eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off

% 3rd eigenvalue
ms1 = ms + 3 * sqrt(D(3)) * reshape(W(:, 3), [2, m]);
ms2 = ms - 3 * sqrt(D(3)) * reshape(W(:, 3), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 3rd eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off

```







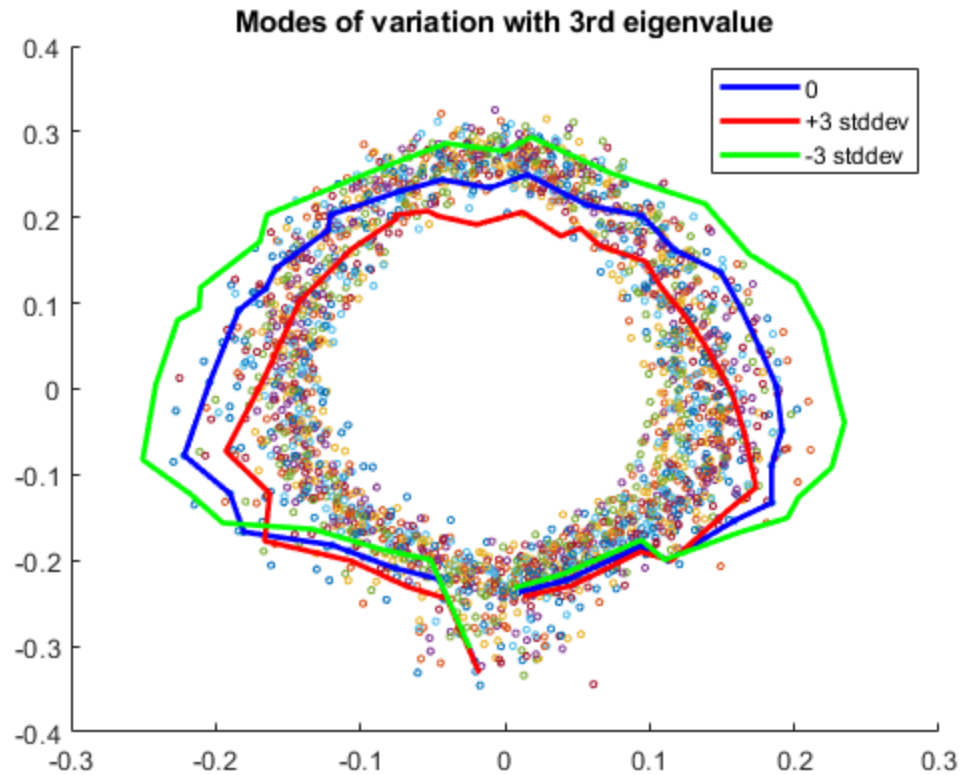
Closest pointsets

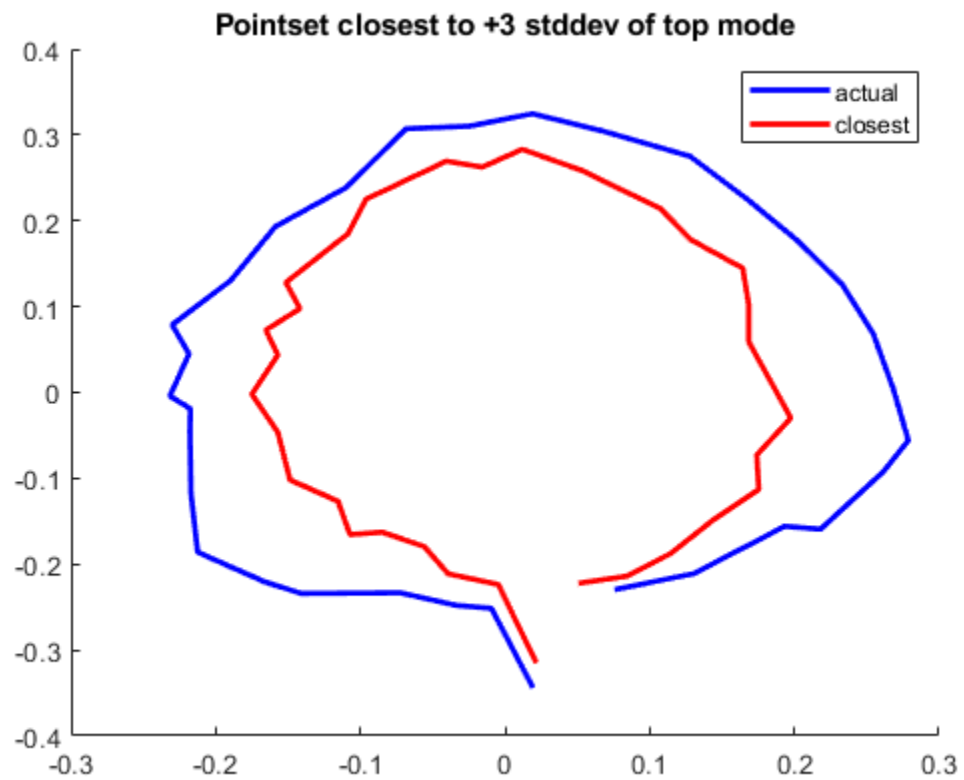
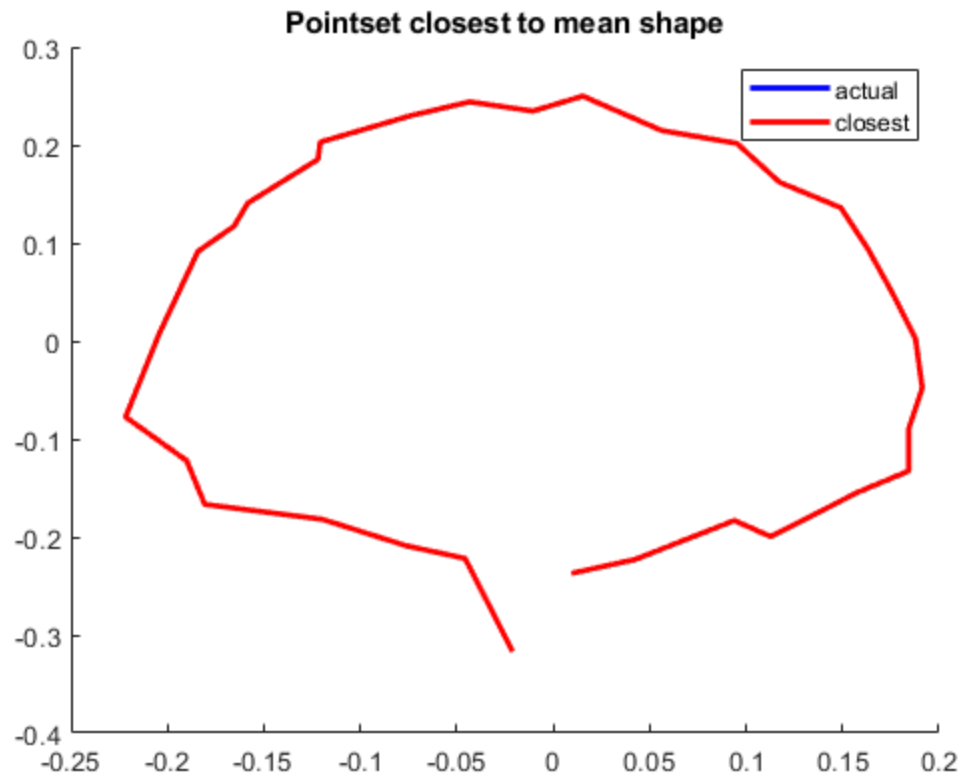
```
ms1 = ms + 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
ms2 = ms - 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);

% Closest to mean shape
ps = findMinErrorPS(newPS, ms);
figure
hold on
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to mean shape");
legend([p1, p2], "actual", "closest");
hold off

% Closest to +3 stddev
ps = findMinErrorPS(newPS, ms1);
figure
hold on
p1 = plot(ms1(1, :), ms1(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to +3 stddev of top mode");
legend([p1, p2], "actual", "closest");
hold off
```

```
% Closest to -3 stddev
ps = findMinErrorPS(newPS, ms2);
figure
hold on
p1 = plot(ms2(1, :), ms2(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to -3 stddev of top mode");
legend([p1, p2], "actual", "closest");
hold off
```





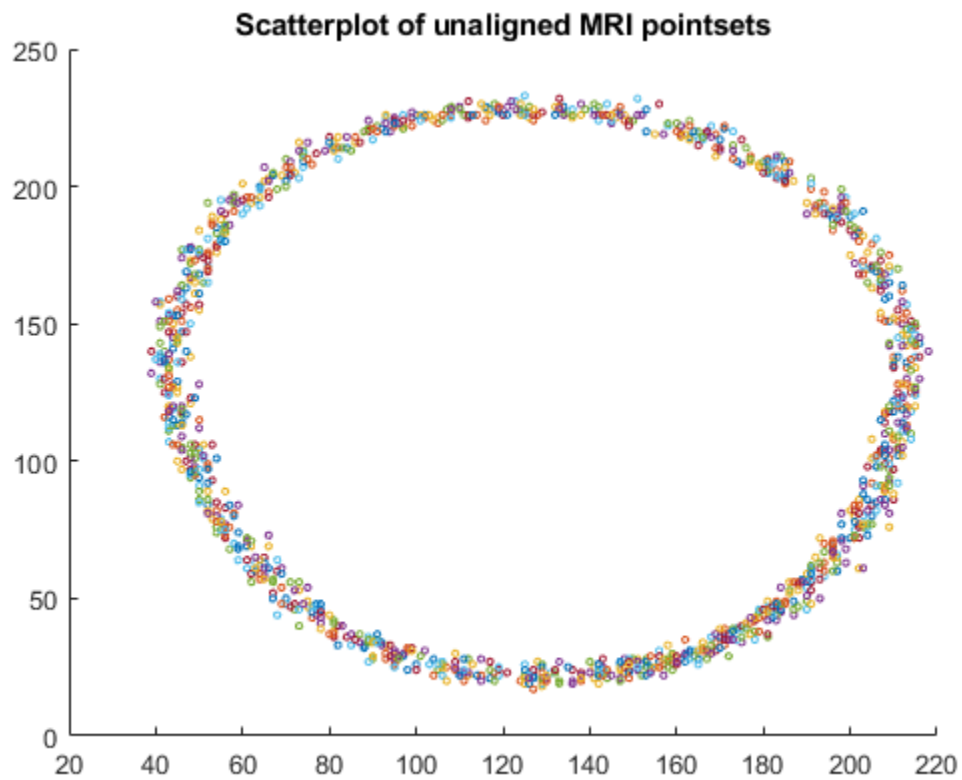


Reading MRI data

```
filePath = "../data/brain/data/mri_image_";
%tracingBoundaries(".png", 40, 32, filePath);
data = load("../data/brain.mat");
imgs = data.shapes;

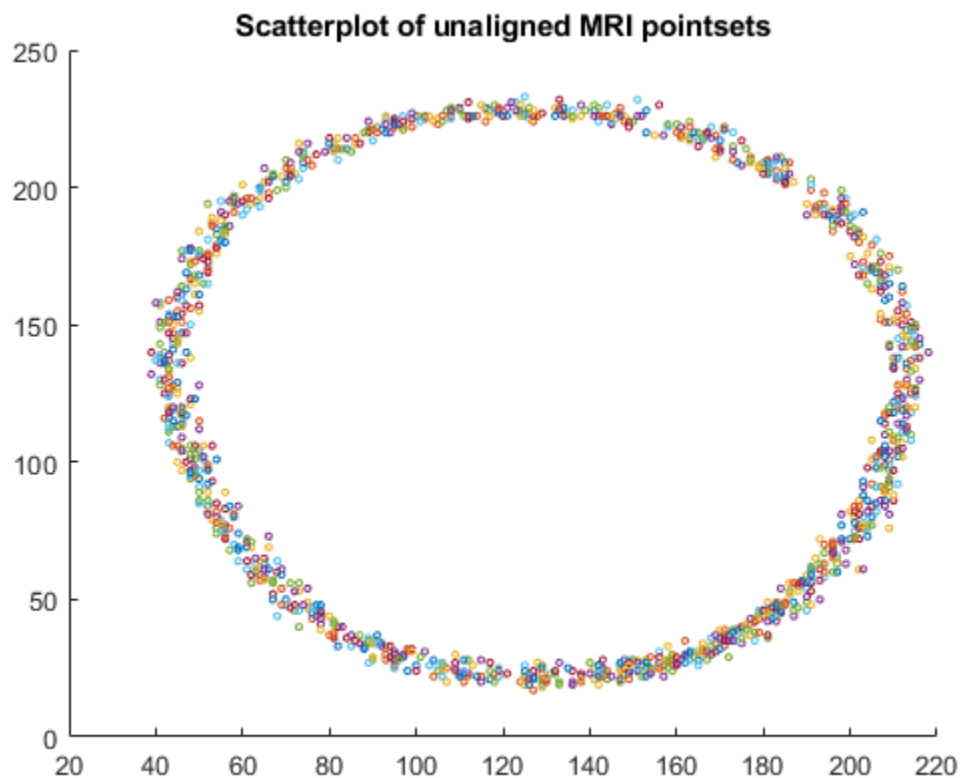
[dims, m, n] = size(imgs);

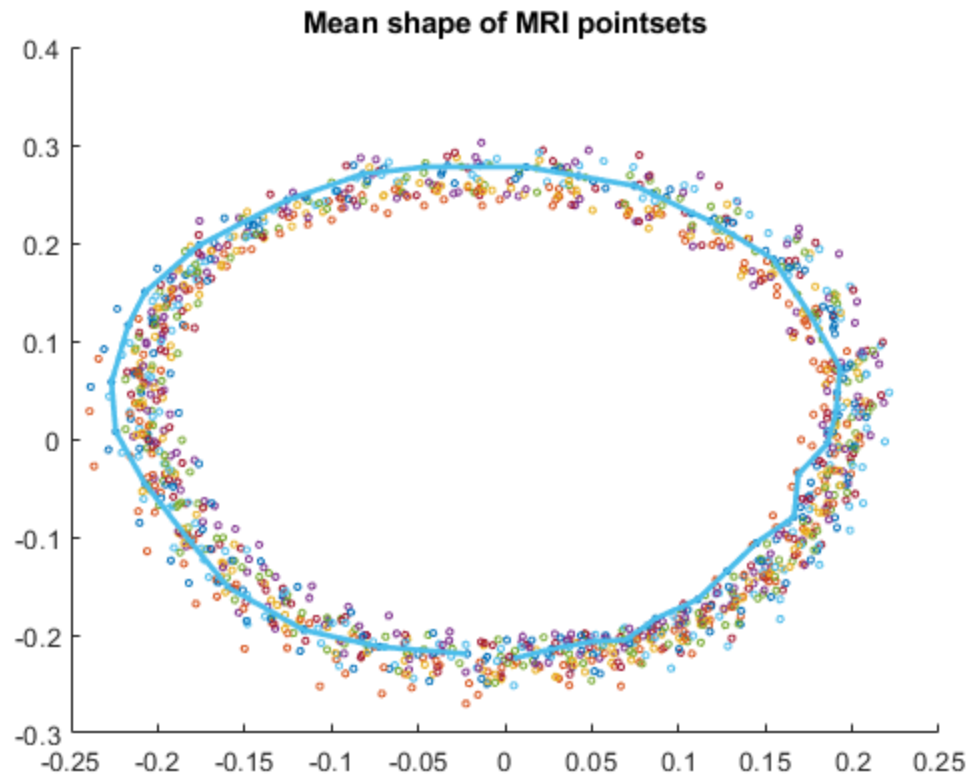
% plotting all the hands
figure
hold on
for i = 1:n
    scatter(imgs(1, :, i), imgs(2, :, i), 6);
end
title("Scatterplot of unaligned MRI pointsets");
hold off
```



Mean shape of MRI data

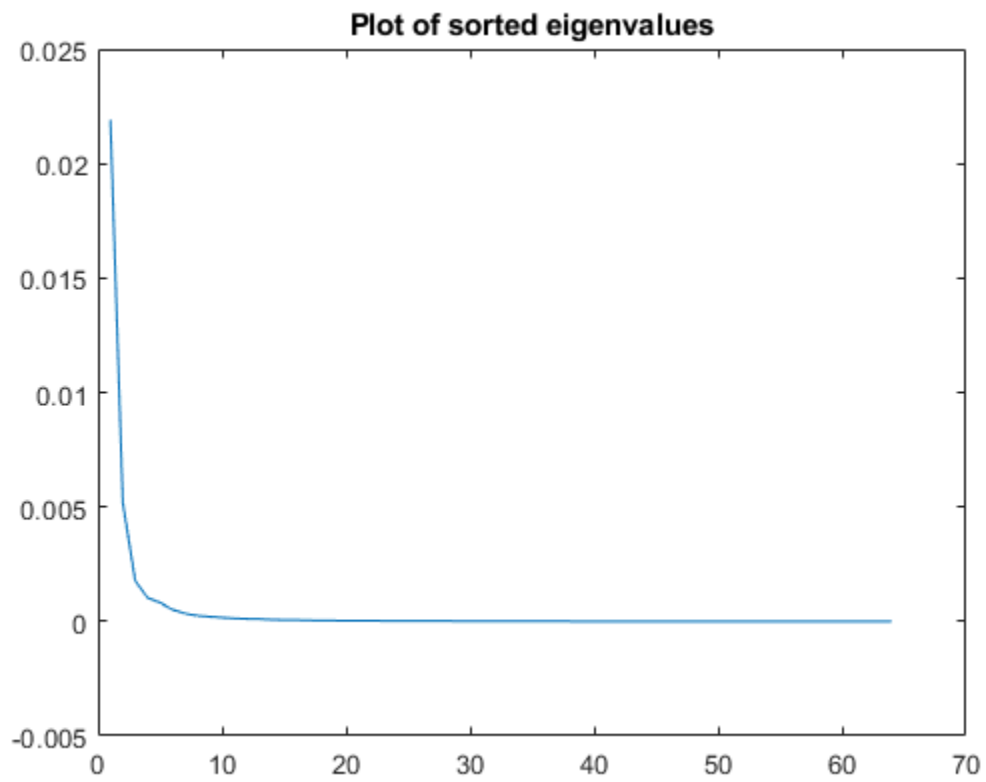
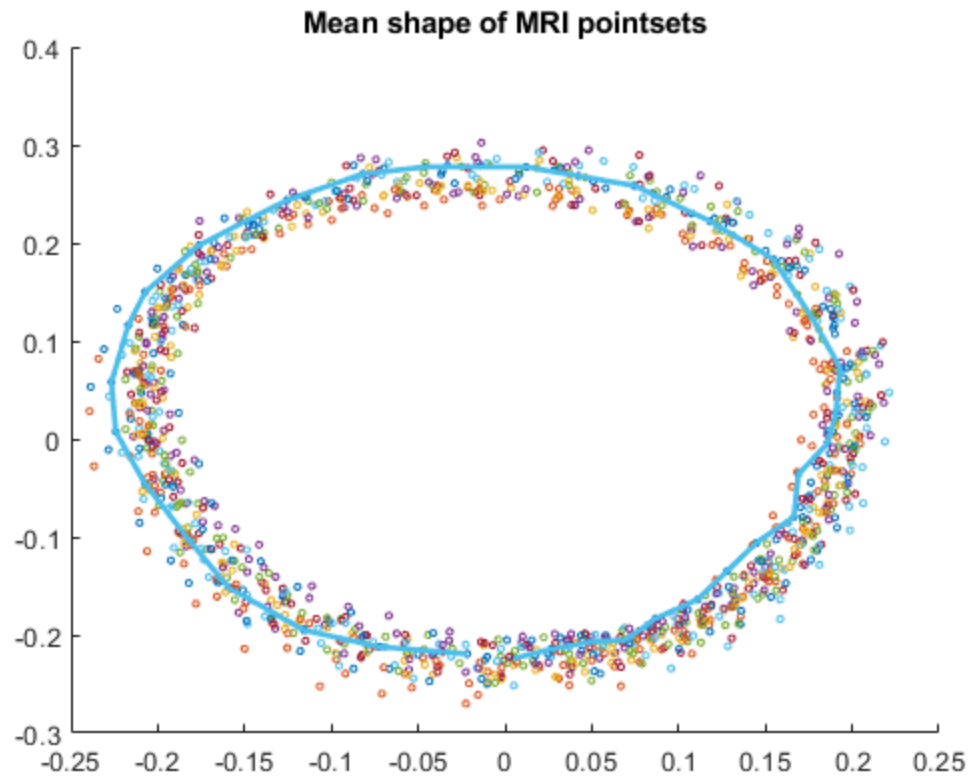
```
[ms, newPS] = meanShape(imgs);  
figure  
hold on  
for i = 1:n  
    scatter(newPS(1, :, i), newPS(2, :, i), 6);  
end  
plot(ms(1, :), ms(2, :), 'LineWidth', 2);  
title("Mean shape of MRI pointsets");  
hold off
```





Eigenvalues calculation

```
[D, W] = eigenCalc(newPS);  
figure  
plot(D);  
title("Plot of sorted eigenvalues");
```

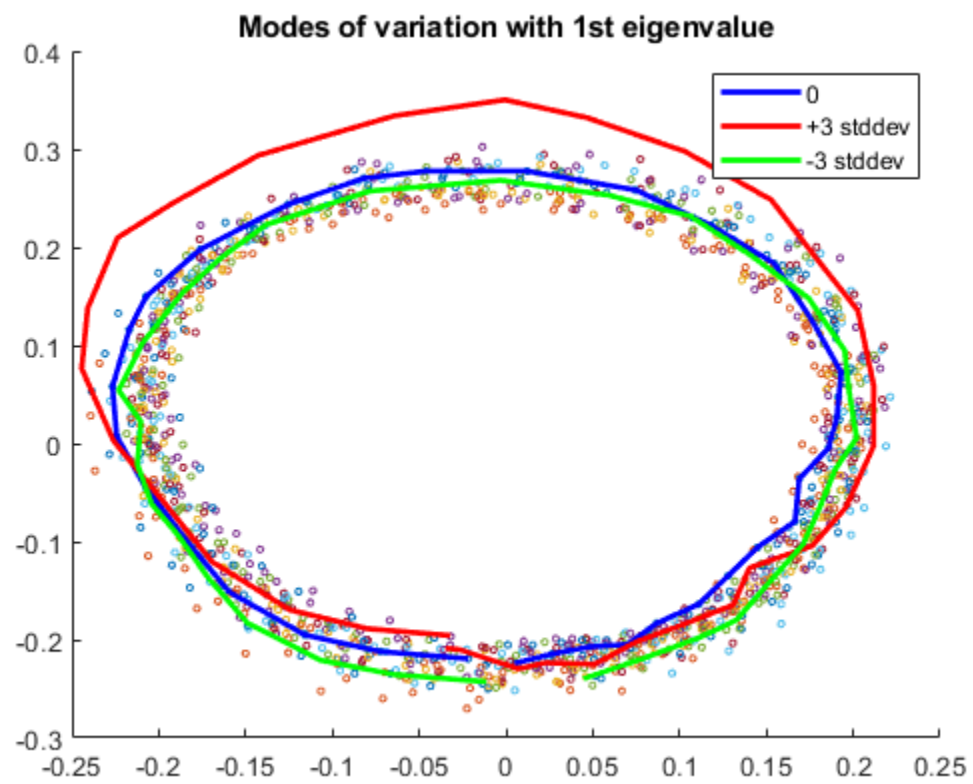
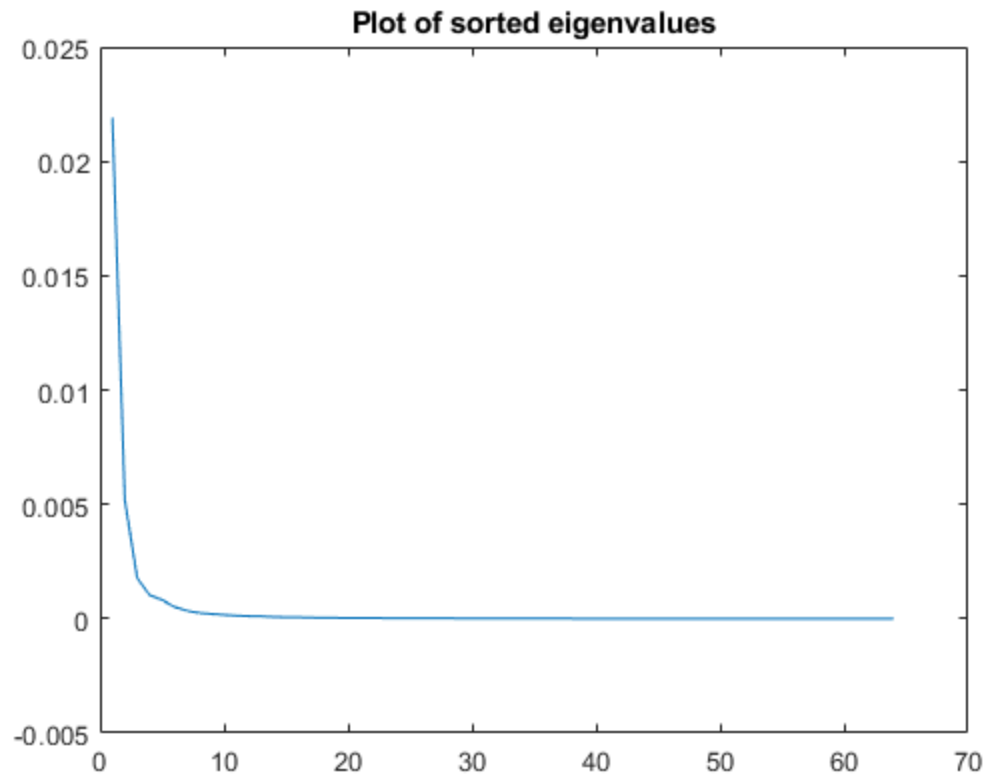


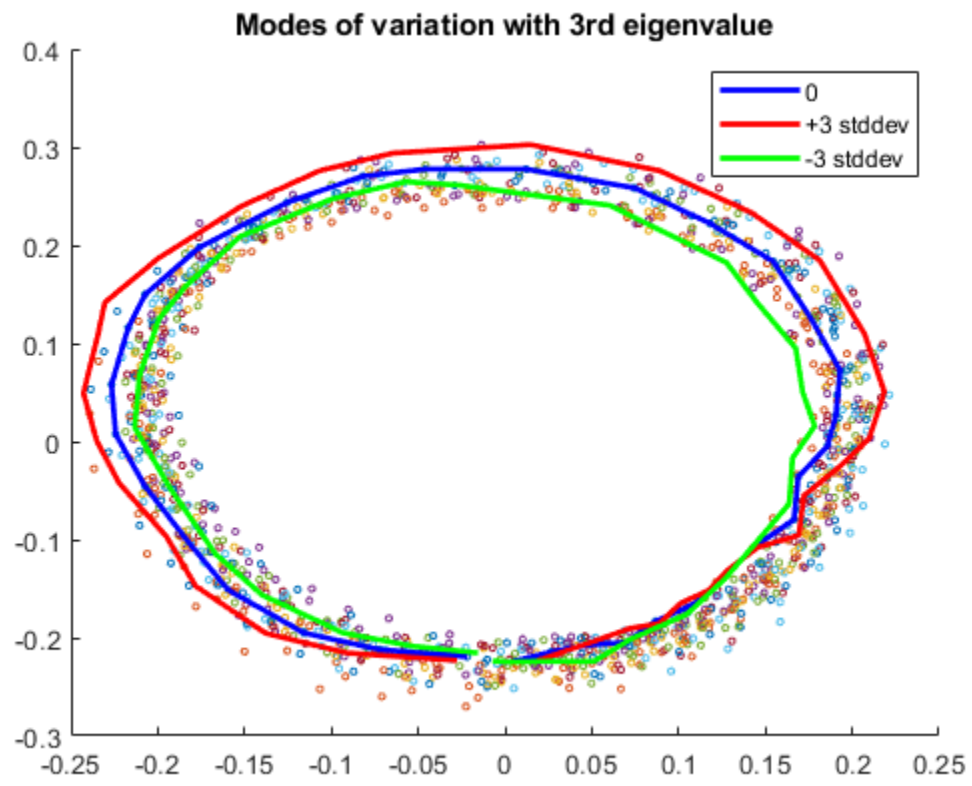
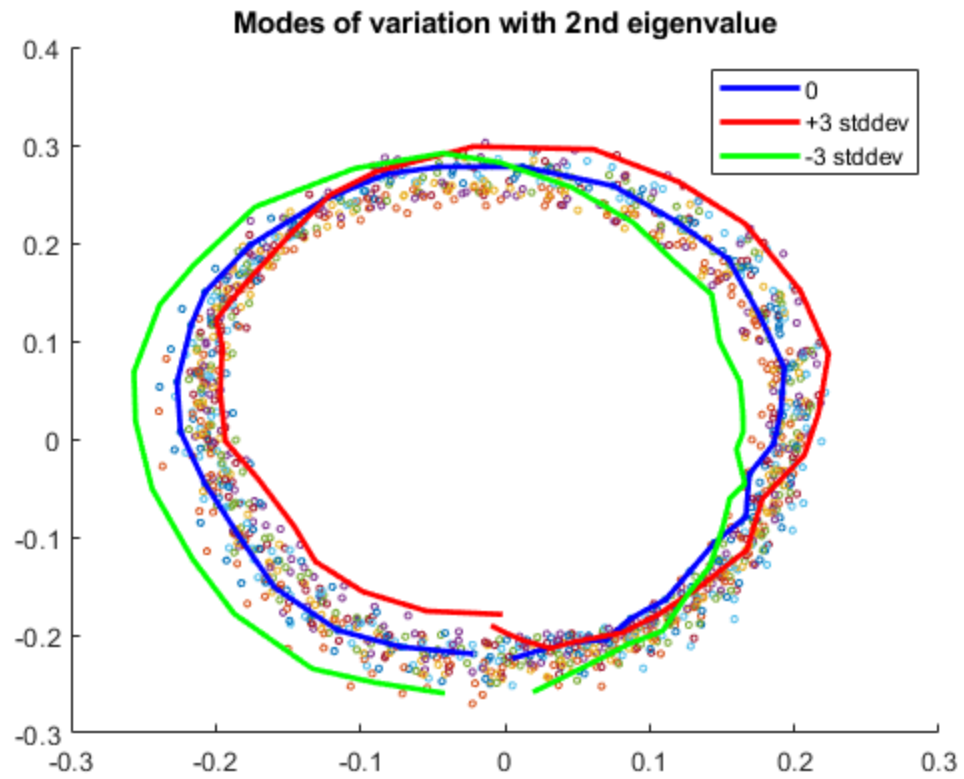
Top 3 modes of variations

```
% 1st eigenvalue
ms1 = ms + 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
ms2 = ms - 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 1st eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off

% 2nd eigenvalue
ms1 = ms + 3 * sqrt(D(2)) * reshape(W(:, 2), [2, m]);
ms2 = ms - 3 * sqrt(D(2)) * reshape(W(:, 2), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 2nd eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off

% 3rd eigenvalue
ms1 = ms + 3 * sqrt(D(3)) * reshape(W(:, 3), [2, m]);
ms2 = ms - 3 * sqrt(D(3)) * reshape(W(:, 3), [2, m]);
figure
hold on
for i = 1:n
    scatter(newPS(1, :, i), newPS(2, :, i), 6);
end
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ms1(1, :), ms1(2, :), 'Color', 'red', 'LineWidth', 2);
p3 = plot(ms2(1, :), ms2(2, :), 'Color', 'green', 'LineWidth', 2);
title("Modes of variation with 3rd eigenvalue");
legend([p1, p2, p3], "0", "+3 stddev", "-3 stddev");
hold off
```





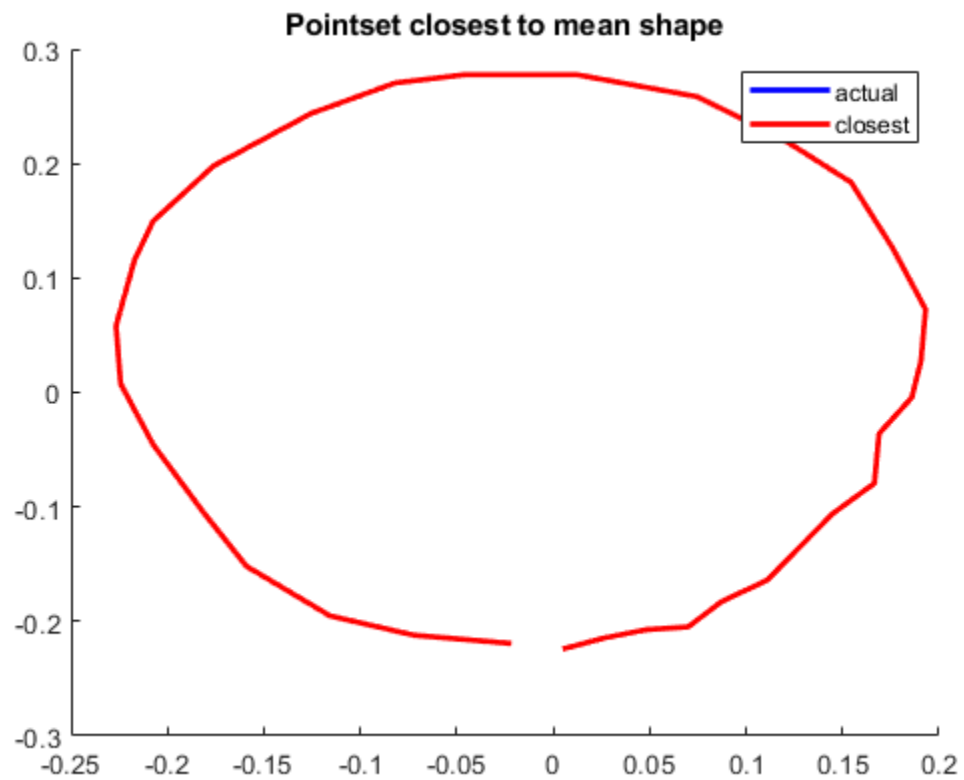
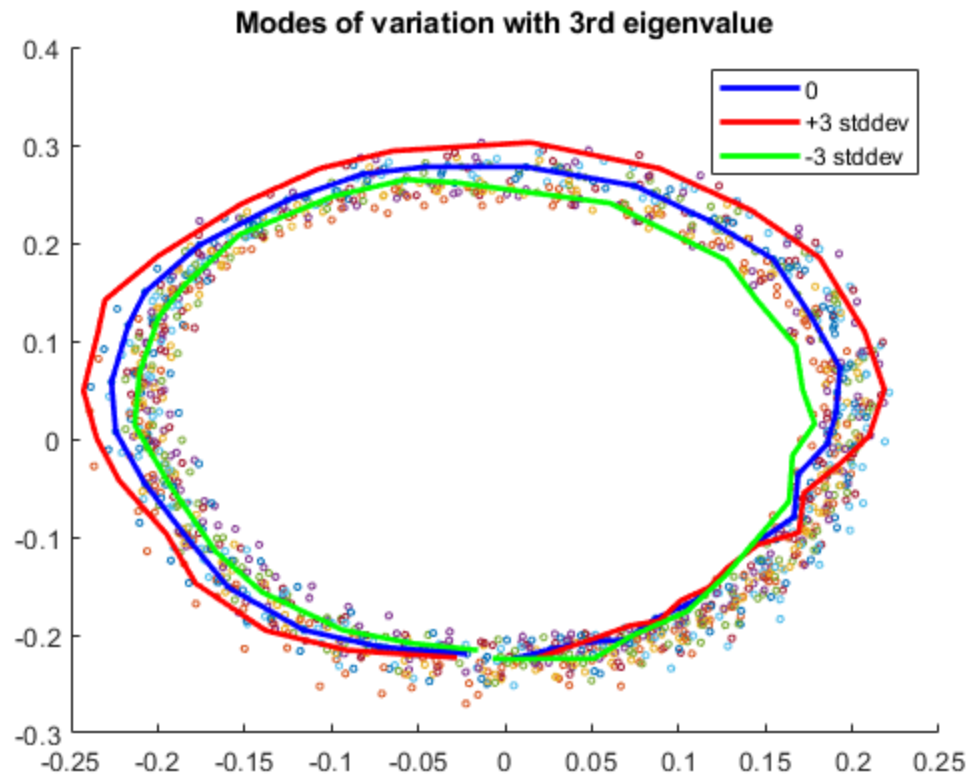
Closest pointsets

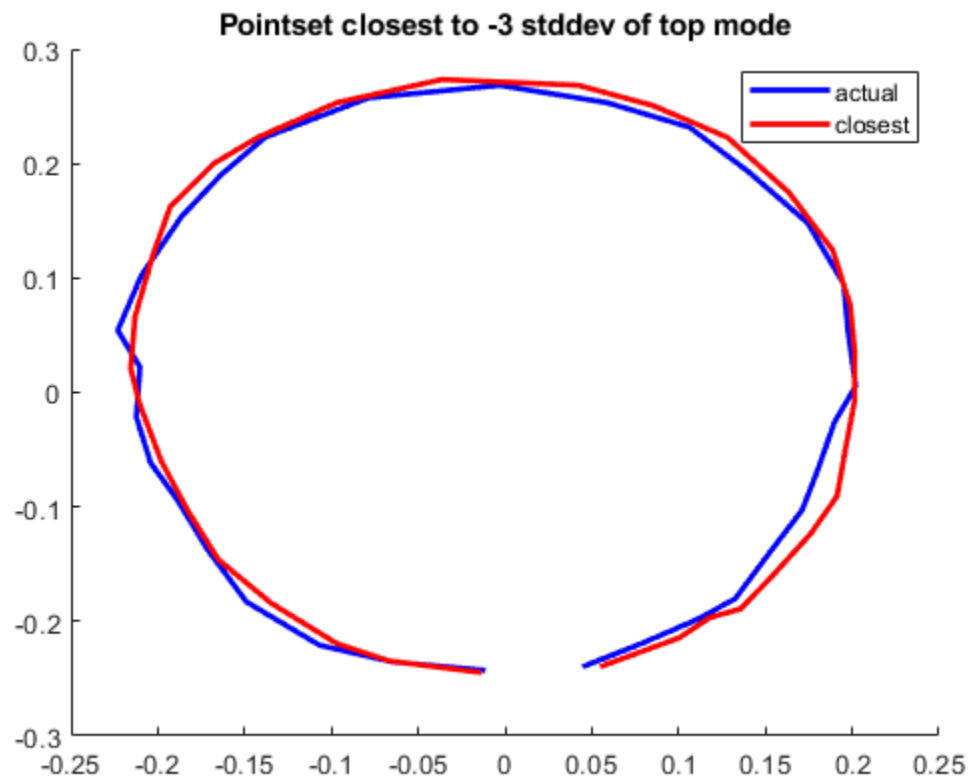
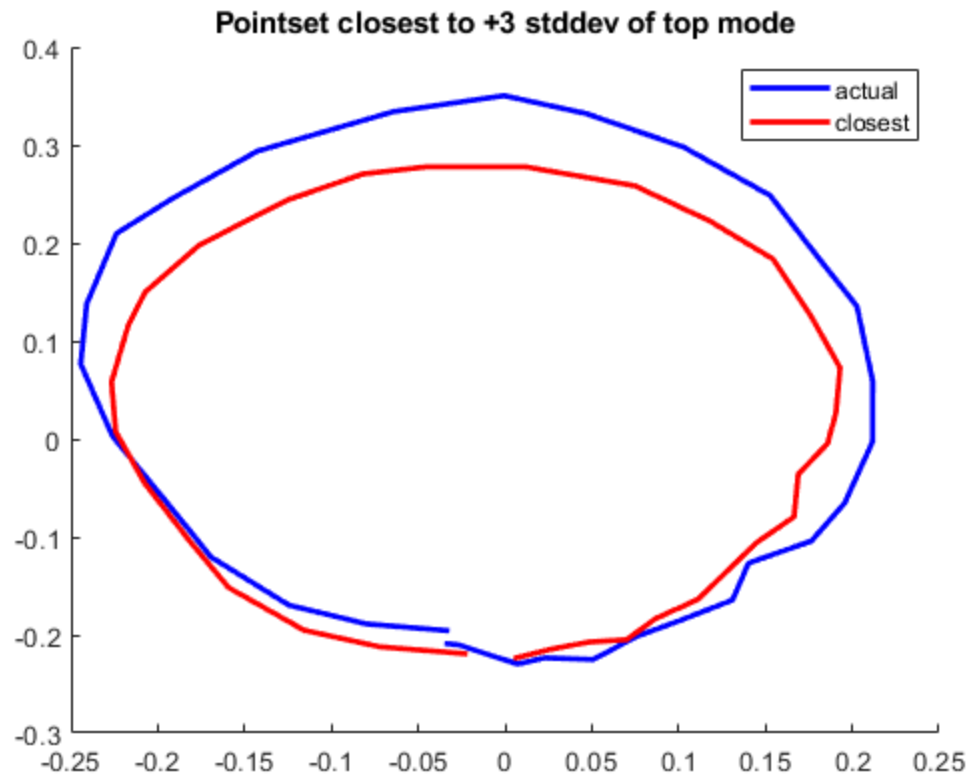
```
ms1 = ms + 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);
ms2 = ms - 3 * sqrt(D(1)) * reshape(W(:, 1), [2, m]);

% Closest to mean shape
ps = findMinErrorPS(newPS, ms);
figure
hold on
p1 = plot(ms(1, :), ms(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to mean shape");
legend([p1, p2], "actual", "closest");
hold off

% Closest to +3 stddev
ps = findMinErrorPS(newPS, ms1);
figure
hold on
p1 = plot(ms1(1, :), ms1(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to +3 stddev of top mode");
legend([p1, p2], "actual", "closest");
hold off

% Closest to -3 stddev
ps = findMinErrorPS(newPS, ms2);
figure
hold on
p1 = plot(ms2(1, :), ms2(2, :), 'Color', 'blue', 'LineWidth', 2);
p2 = plot(ps(1, :), ps(2, :), 'Color', 'red', 'LineWidth', 2);
title("Pointset closest to -3 stddev of top mode");
legend([p1, p2], "actual", "closest");
hold off
```





```
toc;
```

```
Elapsed time is 76.551501 seconds.
```

```
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```