

STAT 6338

Advanced Statistical Methods II

Project 1

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Ans 1)

a. Hypotheses:

Null Hypothesis (H_0): The mean infection risk is the same across all four regions.

Alternative Hypothesis (H_a): The mean infection risk is not the same across all four regions.

ANOVA Results:

F-value: 3.21 Pr > F: 0.0201

Conclusion: Since the p-value (0.0201) is less than the significance level of $\alpha = 0.05$, we reject the null hypothesis. We conclude that there is a statistically significant difference in the mean infection risk among the four geographic regions.

b. Pairwise comparisons are between each combination of means.

Regions 1 vs 2: Lower CL diff

Regions 1 vs 3: Lower CL diff

Regions 1 vs 4: Lower CL diff

Regions 2 vs 3: Lower CL diff

Regions 2 vs 4: Lower CL diff

Regions 3 vs 4: Lower CL diff

For Tukey's test to reveal a difference, the "diff" column (i.e. differences in means) must not cross 0. If they cross 0 or 0 is in between Upper CL and Lower CL, the analysis cannot show anything.

Ans 2)

Effect of average age of patient (variable 3) on mean infection risk (variable 4) is to be studied. For purposes of this ANOVA study, average age is to be classified into four categories: under 50, 50-54.9, 55.0-59.9, 60.0 and over. Assume that ANOVA model is applicable.

Test whether or not the mean infection risk differs for the four age groups. Control the α risk at .10.

We categorized average patient age into four groups and performed ANOVA to determine if there were significant differences in mean infection risk among these groups.

The results from the PDF show the following:

F Value: 0.56

Pr > F: 0.6412

Conclusion:

Since the p-value is not below 0.10, we fail to reject the null hypothesis and conclude that there is no significant difference in mean infection risk across the four age groups.

Ans 3)

b. Brown-Forsythe Test Results:

F Value: 4.33

Pr > F: 0.0064

Explanation: The Brown-Forsythe test assesses whether the variances in length of stay are equal across the four geographic regions. A significant p-value suggests unequal variances.

Conclusion:

The Brown-Forsythe test's p-value is 0.0064, which is less than the conventional alpha level of 0.05. Therefore, we reject the null hypothesis and conclude that the variances in length of stay are not equal across the regions.

c. Mean Length of Stay by Region:

Region 1: 11.0889

Region 2: 9.6834

Region 3: 9.1914

Region 4: 8.1138

Standard Deviation of Length of Stay by Region:

Region 1: 2.6696

Region 2: 1.1929

Region 3: 1.2250

Region 4: 1.0031

Explanation: Calculated the means (Y_i) and standard deviations (s_i) for length of stay in each region to determine the appropriate transformation. Comparing Y_i and s_i the s_i increases as Y_i increases, we would consider transformations (logarithmic) to stabilise the variance.

e. Transformed Data ANOVA Results:

F Value: 14.79

Pr > F: <.0001

Explanation: Fitted an ANOVA model to the reciprocal transformed length of stay data to assess differences across geographic regions. The very low p-value indicates significant differences.

Conclusion:

The F is 14.79 and the $p < 0.0001$ which is highly significant, we reject the null hypothesis and conclude that the mean reciprocal transformed length of stay differs significantly across the four regions.