

# Time Series Analysis of dataset downloaded

```
//Time Series Analysis of dataset downloaded from  
https://www.kaggle.com/kanncaal/time-series-prediction-tutorial-with-eda
```

```
//We have used 2 libraries for this, i.e. sparkts and flint
```

```
/*1. Load the Data
```

```
It contains 2 files:
```

- i) Aerial Bombing Operations in WW2
  - ii) Weather Conditions in WW2(This data set has 2 subset in it. First one includes weather station locations like country, latitude and longitude. Second one includes measured min, max and mean temperatures from weather stations.)
- ```
*/
```

```
//importing sparkts and required java time classes
```

```
import java.time.{LocalDateTime, ZoneId, ZonedDateTime}
```

```
import com.cloudera.sparkts._
```

```
import com.cloudera.sparkts.stats.TimeSeriesStatisticalTests
```

```
import java.time.{LocalDateTime, ZoneId, ZonedDateTime}
```

```
import com.cloudera.sparkts._
```

```
import com.cloudera.sparkts.stats.TimeSeriesStatisticalTests
```

```

import org.apache.spark.sql.functions._
import org.apache.spark.sql.types._

//bombing data
var aerial = spark.read.
    format("csv")
    .option("header","true")
    .option("inferSchema","true")
    .option("timestampFormat","MM/dd/yyyy")
    .option("mode", "PERMISSIVE")

.load("dbfs:/FileStore/shared_uploads/harsh.vijaywat@gmail.com/operations.csv")
//weather data that includes locations like country, latitude and longitude.
var weather_station_locations = spark.read.
    format("csv")
    .option("header","true")
    .option("inferSchema","true")
    .option("timestampFormat","MM/dd/yyyy")
    .option("mode", "PERMISSIVE")

.load("dbfs:/FileStore/shared_uploads/harsh.vijaywat@gmail.com/Weather_Station_Locations.csv")

val weatherSchema = StructType(Array(StructField("STA", StringType),
StructField("Date", TimestampType), StructField("MeanTemp", DoubleType)))
//Second weather data that includes measured min, max and mean temperatures
var weather = spark.read.
    format("csv")
    .option("header","true")
    .schema(weatherSchema)
    .option("timestampFormat","yyyy/MM/dd")
    .option("mode", "PERMISSIVE")

.load("dbfs:/FileStore/shared_uploads/harsh.vijaywat@gmail.com/Summary_of_Weather.csv")

```

```

import org.apache.spark.sql.functions._
import org.apache.spark.sql.types._
aerial: org.apache.spark.sql.DataFrame = [Mission ID: int, Mission Date: timestamp ... 44 more fields]
weather_station_locations: org.apache.spark.sql.DataFrame = [WBAN: int, NAME: string ... 6 more fields]
weatherSchema: org.apache.spark.sql.types.StructType = StructType(StructField(STA,StringType,true), StructField(Date,TimestampType,true), StructField(MeanTemp,DoubleType,true))

```

```
weather: org.apache.spark.sql.DataFrame = [STA: string, Date: timestamp ...  
1 more field]
```

```
/*Data Description
```

#### 1. Aerial bombing Data description:

Mission Date: Date of mission

Theater of Operations: Region in which active military operations are in progress; "the army was in the field awaiting action"; Example: "he served in the Vietnam theater for three years"

Country: Country that makes mission or operation like USA

Air Force: Name or id of air force unity like 5AF

Aircraft Series: Model or type of aircraft like B24

Callsign: Before bomb attack, message, code, announcement, or tune that is broadcast by radio.

Takeoff Base: Takeoff airport name like Ponte Olivo Airfield

Takeoff Location: takeoff region Sicily

Takeoff Latitude: Latitude of takeoff region

Takeoff Longitude: Longitude of takeoff region

Target Country: Target country like Germany

Target City: Target city like Berlin

Target Type: Type of target like city area

Target Industry: Target industry like town or urban

Target Priority: Target priority like 1 (most)

Target Latitude: Latitude of target

Target Longitude: Longitude of target

#### 2. Weather Condition data description:

Weather station location:

WBAN: Weather station number

NAME: weather station name

STATE/COUNTRY ID: acronym of countries

Latitude: Latitude of weather station

Longitude: Longitude of weather station

#### 3. Weather:

STA: weather station number (WBAN)

Date: Date of temperature measurement

MeanTemp: Mean temperature \*/

```
/* Data Cleaning
```

Aerial Bombing data includes a lot of NaN value. Instead of using them, drop some NaN values. It does not only remove the uncertainty but it also ease visualization process.

Drop countries that are NaN

Drop if target longitude is NaN

Drop if takeoff longitude is NaN

Drop unused features

```
*/
```

```
//drop if target longitude, takeoff longitude ,Country are NaN
```

```
aerial = aerial.na.drop("any", Array("Country", "Target Latitude", "Takeoff Longitude"))
```

```
//drop unused features
```

```
aerial = aerial.drop("Mission ID", "Unit ID", "Target ID", "Altitude (Hundreds of Feet)", "Attacking Aircraft", "Bombing Aircraft", "Aircraft Returned", "Aircraft Failed", "Aircraft Damaged", "Aircraft Lost", "High Explosives", "High Explosives Type", "Mission Type", "High Explosives Weight (Pounds)", "High Explosives Weight (Tons)", "Incendiary Devices", "Incendiary Devices Type", "Incendiary Devices Weight (Pounds)", "Incendiary Devices Weight (Tons)", "Fragmentation Devices", "Fragmentation Devices Type", "Fragmentation Devices Weight (Pounds)", "Fragmentation Devices Weight (Tons)", "Total Weight (Pounds)", "Total Weight (Tons)", "Time Over Target", "Bomb Damage Assessment", "Source ID" )
```

```
//drop takeoff latitude=4248, takeoff longitude=1355
```

```
aerial = aerial.filter("`Takeoff Longitude` != 1355 AND `Takeoff Latitude` != 4248")
```

```
//select only important columns
```

```
weather_station_locations = weather_station_locations.select("WBAN", "NAME", "STATE/COUNTRY ID", "Latitude", "Longitude")
```

```
//select only important columns
```

```
weather = weather.select("STA", "Date", "MeanTemp")
```

```
//drop nan values in weather
```

```
weather = weather.na.drop
```

```
aerial: org.apache.spark.sql.DataFrame = [Mission Date: timestamp, Theater of Operations: string ... 16 more fields]
```

```
aerial: org.apache.spark.sql.DataFrame = [Mission Date: timestamp, Theater of Operations: string ... 16 more fields]
```

```
aerial: org.apache.spark.sql.DataFrame = [Mission Date: timestamp, Theater of Operations: string ... 16 more fields]
```

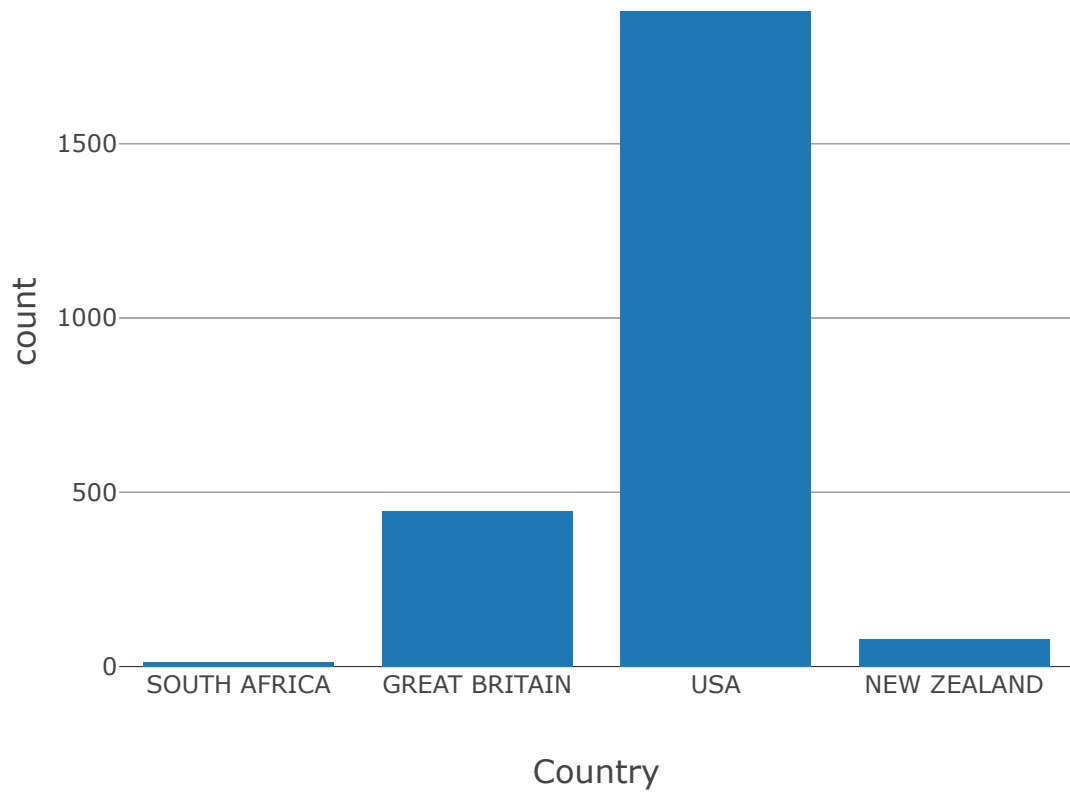
```
weather_station_locations: org.apache.spark.sql.DataFrame = [WBAN: int, NAME: string ... 3 more fields]
```

```
weather: org.apache.spark.sql.DataFrame = [STA: string, Date: timestamp ... 1 more field]
```

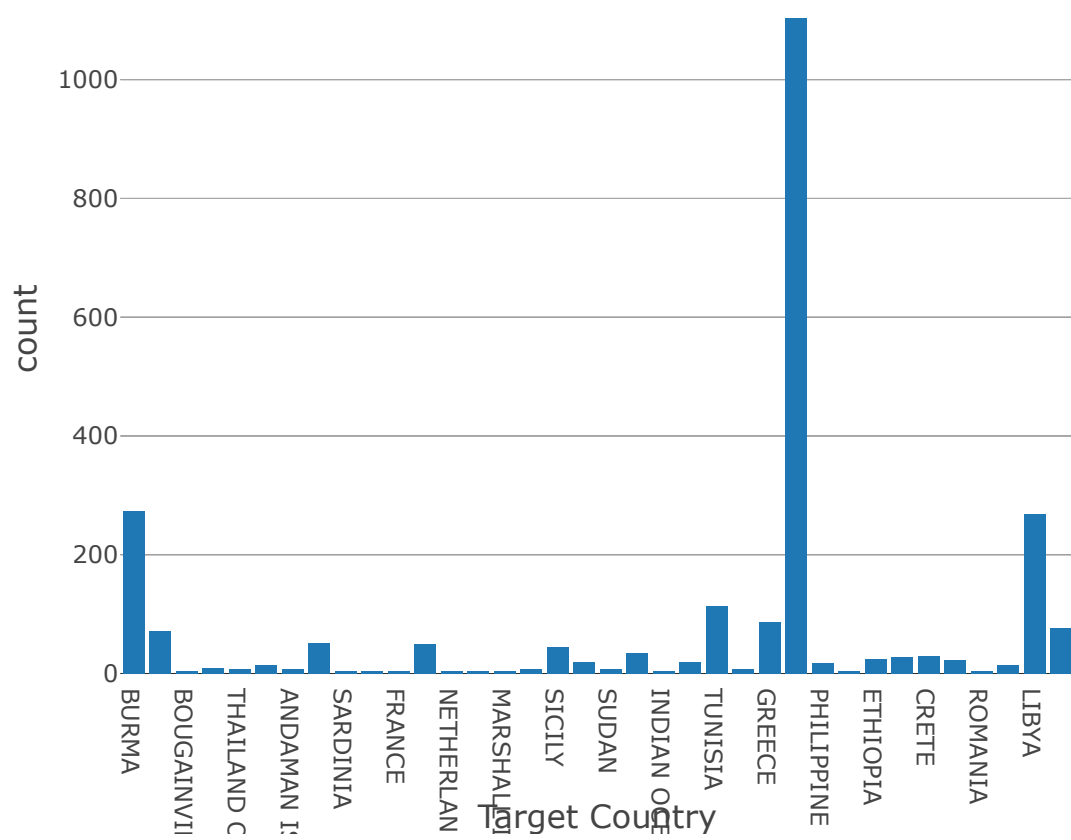
```
weather: org.apache.spark.sql.DataFrame = [STA: string, Date: timestamp ... 1 more field]
```

```
//Data Visualization
```

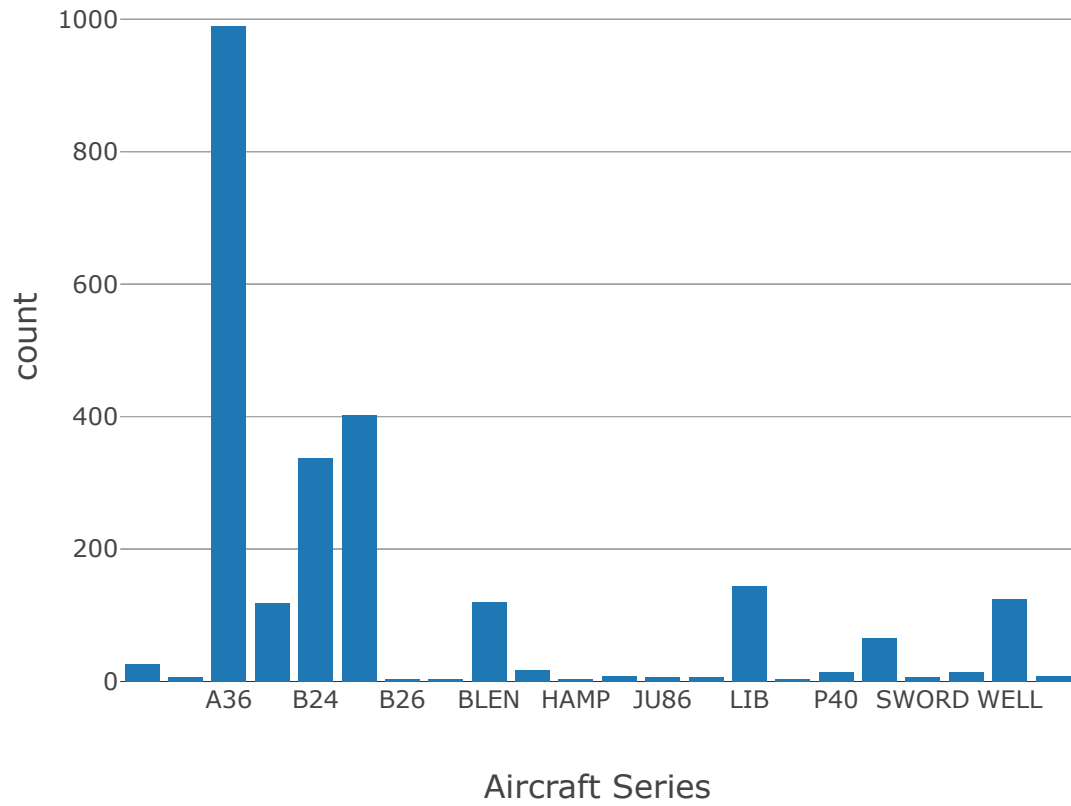
```
//How many country which attacks  
display(aerial.groupBy("Country").count())
```



```
//Top target countries  
display(aerial.groupBy("Target Country").count())
```

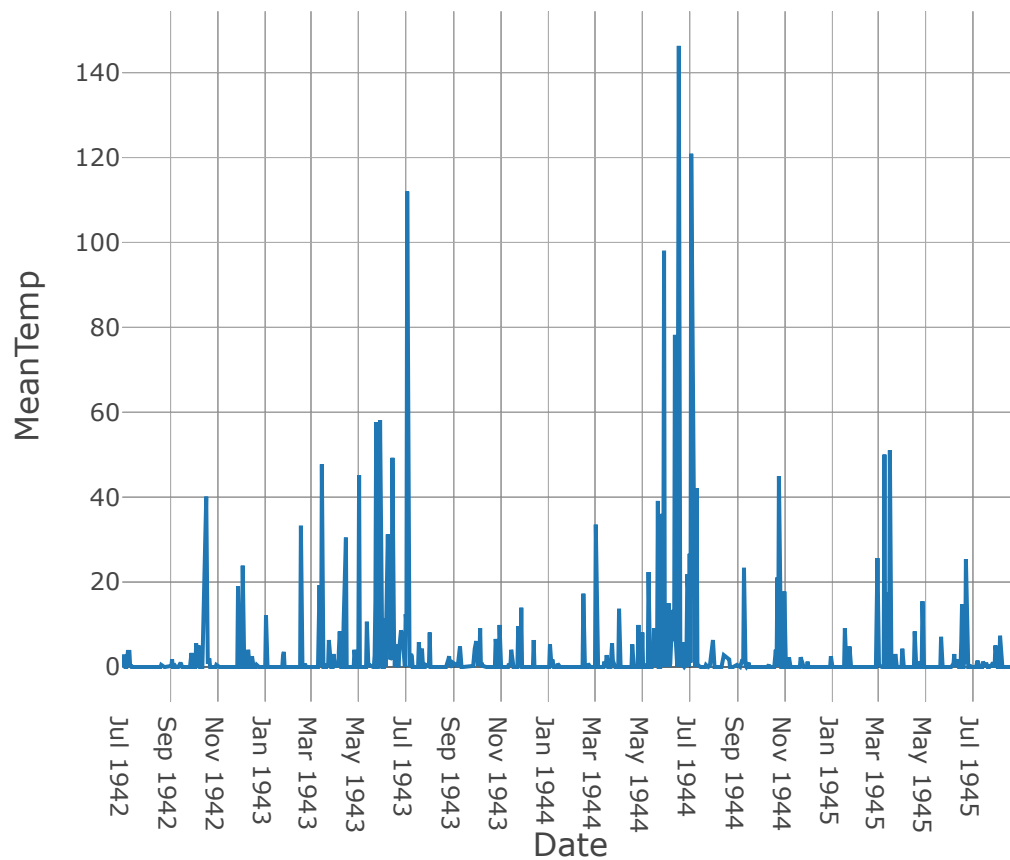


```
//Top 10 aircraft series
display(aerial.groupBy("Aircraft Series").count().orderBy("Aircraft
Series"))
```



```
//MeanTemp as function of date  
display(weather.select("Date", "MeanTemp"))
```

Showing sample based on the first 1000 rows.



```
weather.show(10)
```

| STA   | Date                | MeanTemp |
|-------|---------------------|----------|
| 10001 | 1942-07-01 00:00:00 | 1.016    |
| 10001 | 1942-07-02 00:00:00 | 0.0      |
| 10001 | 1942-07-03 00:00:00 | 2.54     |
| 10001 | 1942-07-04 00:00:00 | 2.54     |
| 10001 | 1942-07-05 00:00:00 | 0.0      |
| 10001 | 1942-07-06 00:00:00 | 0.0      |
| 10001 | 1942-07-08 00:00:00 | 3.556    |
| 10001 | 1942-07-10 00:00:00 | 3.556    |
| 10001 | 1942-07-11 00:00:00 | 0.0      |
| 10001 | 1942-07-12 00:00:00 | 0.508    |

only showing top 10 rows

```
//Time Series Prediction with ARIMA
```



## `/*Stationarity of a Time Series`

There are three basic criterion for a time series to understand whether it is stationary series or not.

Statistical properties of time series such as mean, variance should remain constant over time to call time series is stationary

constant mean

constant variance

autocovariance that does not depend on time. autocovariance is covariance between time series and lagged time series.

Lets visualize and check seasonality trend of our time series. \*/

`/*We can check stationarity using the following methods:`

1. Plotting Rolling Statistics: We have a window lets say window size is 6 and then we find rolling mean and variance to check stationary.

2. Dickey-Fuller Test: The test results comprise of a Test Statistic and some Critical Values for difference confidence levels. If the test statistic is less than the critical value, we can say that time series is stationary. \*/

`//importing flint packages/classes for rolling statistics`

`import com.twosigma.flint.timeseries.TimeSeriesRDD`

`import scala.concurrent.duration._ // for defined value of DAYS`

`val tsRdd = TimeSeriesRDD.fromDF(weather)(isSorted = false, timeUnit = DAYS, timeColumn = "Date")`

`import com.twosigma.flint.timeseries.TimeSeriesRDD`

`import scala.concurrent.duration._`

`tsRdd: com.twosigma.flint.timeseries.TimeSeriesRDD = com.twosigma.flint.timeseries.TimeSeriesRDDImpl@238674dc`

`tsRdd.toDF.show(10)`

```
+-----+-----+-----+
|           time|  STA|MeanTemp|
+-----+-----+-----+
1940-01-01 00:00:00	10701	7.62
1940-01-01 00:00:00	22504	2.286
1940-01-01 00:00:00	22508	0.254
1940-01-02 00:00:00	10701	15.24
1940-01-02 00:00:00	22504	5.334
1940-01-02 00:00:00	22508	10.16
1940-01-03 00:00:00	10701	25.4
1940-01-03 00:00:00	22504	0.0
1940-01-04 00:00:00	10701	0.0
1940-01-04 00:00:00	22504	7.112
+-----+-----+-----+
```

only showing top 10 rows

```
//Calculation of rolling mean and rolling std of MeanTemp
```

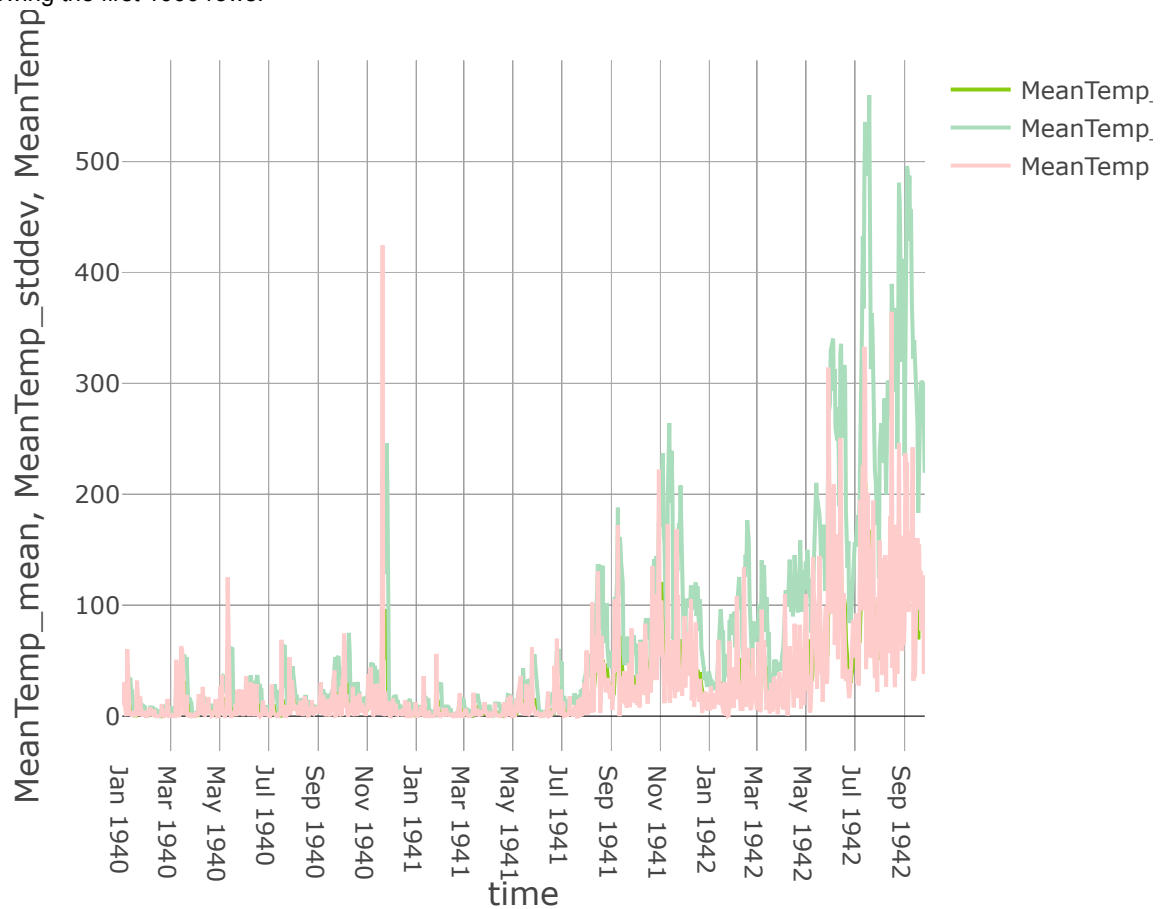
```
import com.twosigma.flint.timeseries._  
val result = tsRdd.summarizeWindows(  
  Windows.pastAbsoluteTime("6days"),  
  Summarizers.mean("MeanTemp")).summarizeWindows(  
    Windows.pastAbsoluteTime("6days"),  
    Summarizers.stddev("MeanTemp"))
```

```
import com.twosigma.flint.timeseries._  
result: com.twosigma.flint.timeseries.TimeSeriesRDD = com.twosigma.flint.timeseries.TimeSeriesRDDImpl@4c38ca5a
```

```
//visualisation of rolling stats  
display(result.toDF)
```

Aggregated (by sum) in the backend.

Showing the first 1000 rows.



```

/*Our first criteria for stationary is constant mean. So we fail because
mean is not constant as you can see from plot(black line) above . (no
stationary)
Second one is constant variance. We fail this too because std is not
constant.
As a result, we sure that our time series is not stationary.
Lets make time series stationary at the next part.
*/

```

```

result.toDF.show(10)

```

```

+-----+-----+-----+-----+-----+
|          time|  STA|MeanTemp|  MeanTemp_mean|  MeanTemp_stddev|
+-----+-----+-----+-----+-----+
1940-01-01 00:00:00	10701	7.62	3.3866666666666667	3.804351368279924
1940-01-01 00:00:00	22504	2.286	3.3866666666666667	3.804351368279924
1940-01-01 00:00:00	22508	0.254	3.3866666666666667	3.804351368279924
1940-01-02 00:00:00	10701	15.24	6.8156666666666667	5.451047520125528
1940-01-02 00:00:00	22504	5.334	6.8156666666666667	5.451047520125528
1940-01-02 00:00:00	22508	10.16	6.8156666666666667	5.451047520125528
1940-01-03 00:00:00	10701	25.4	8.28675	8.644466962828222
1940-01-03 00:00:00	22504	0.0	8.28675	8.644466962828222
1940-01-04 00:00:00	10701	0.0	6.8810909090909091	7.793665857021912
1940-01-04 00:00:00	22504	7.112	6.8810909090909091	7.793665857021912
+-----+-----+-----+-----+-----+

```

only showing top 10 rows

```

/*Make a Time Series Stationary?

```

First solve trend(constant mean) problem

Most popular method is moving average.

Moving average: We have window that take the average over the past 'n' sample. 'n' is window size.

```

//Moving average method

```

```

val o = result.toDF.withColumn("Moving_avg_diff", col("MeanTemp")-
col("MeanTemp_mean"))

```

```

val tsRdd2 = TimeSeriesRDD.fromDF(o)(isSorted = false, timeUnit = DAYS,
timeColumn = "time")

```

```

o: org.apache.spark.sql.DataFrame = [time: timestamp, STA: string ... 4 more
fields]

```

```

tsRdd2: com.twosigma.flint.timeseries.TimeSeriesRDD = com.twosigma.flint.tim
eseries.TimeSeriesRDDImpl@3849d15

```

```

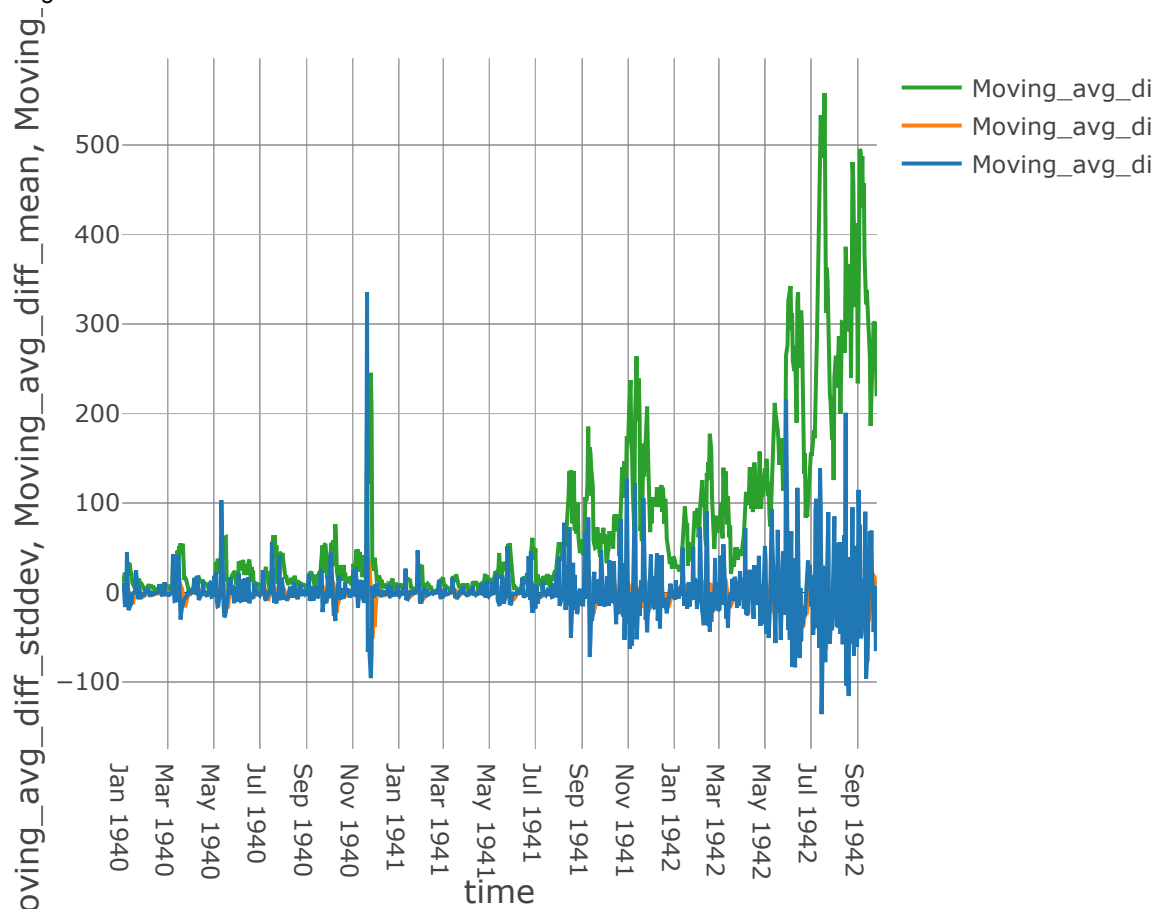
val result2 = tsRdd2.summarizeWindows(
  Windows.pastAbsoluteTime("6days"),
  Summarizers.mean("Moving_avg_diff")).summarizeWindows(
  Windows.pastAbsoluteTime("6days"),
  Summarizers.stddev("Moving_avg_diff"))

result2: com.twosigma.flint.timeseries.TimeSeriesRDD = com.twosigma.flint.timeseries.TimeSeriesRDDImpl@25e95692

display(result2.toDF.select("time","Moving_avg_diff","Moving_avg_diff_mean",
  "Moving_avg_diff_stddev"))
//Constant mean criteria: mean looks like constant as you can see from
plot(orange line) above . (yes stationary)

```

Aggregated (by sum) in the backend.  
Showing the first 1000 rows.



## `/*Forecasting a Time Series`

For prediction(forecasting) we will use `ts_diff` time series that is result of moving avg method.

Also prediction method is ARIMA that is Auto-Regressive Integrated Moving Averages.

AR: Auto-Regressive (p): AR terms are just lags of dependent variable. For example lets say p is 3, we will use  $x(t-1)$ ,  $x(t-2)$  and  $x(t-3)$  to predict  $x(t)$

I: Integrated (d): These are the number of nonseasonal differences. For example, in our case we take the first order difference. So we pass that variable and put `d=0`

MA: Moving Averages (q): MA terms are lagged forecast errors in prediction equation.

(p,d,q) is parameters of ARIMA model.

In order to choose p,d,q parameters we will use two different plots.

Autocorrelation Function (ACF): Measurement of the correlation between time series and lagged version of time series.

Partial Autocorrelation Function (PACF): This measures the correlation between the time series and lagged version of time series but after eliminating the variations already explained by the intervening comparisons.`*/`

`//we need array of double to calculate acf and pacf (due to scala APIs)`

`val cc =`

`result2.toDF.select("Moving_avg_diff").rdd.collect.map(_.getDouble(0))`

```
cc: Array[Double] = Array(4.233333333333333, -1.1006666666666667, -3.1326666666666667, 8.424333333333333, -1.4816666666666674, 3.344333333333333, 17.11325, -8.28675, -6.88109090909091, 0.2309090909090905, -4.59509090909091, -5.424714285714286, -5.424714285714286, -5.170714285714286, -4.746625, -4.746625, 15.536333333333333, 29.760333333333335, -9.186333333333334, 11.895666666666667, 8.847666666666665, -7.662333333333334, -5.122333333333334, -6.900333333333334, -5.948947368421053, -5.948947368421053, -5.440947368421053, -5.547894736842106, -4.785894736842106, -4.531894736842106, -5.8420000000000005, -5.8420000000000005, -5.8420000000000005, -2.7234444444444446, 1.5945555555555555, -0.5503333333333337, -0.5503333333333337, -0.5503333333333337, -0.38847058823529446, -0.38847058823529446, -0.460375000000000037, 0.8096249999999996, -0.1354666666666667, -0.3894666666666667, 0.9366249999999998, 15.668624999999999, 8.302624999999999, -2.7491764705882353, -2.2411764705882353, 5.632823529411764, -2.4951764705882353, -2.4951764705882353, -2.4951764705882353, -2.4951764705882353, -3.3584444444444445, 2.7375555555555555, 8.579555555555556, 1.6227777777777774, -1.4252222222222222, -3.6971111111111111, -3.6971111111111111, -2.1025555555555555, -0.8325555555555555, -0.070555555555555548, -1.6086666666666667, -1.6086666666666667, -1.6086666666666667, -0.5221111111111112, 0.23988888888888882, 1.0865555555555555, -1.9614444444444445, -1.9614444444444445, -0.9595555555555557, -0.9595555555555557, -0.9595555555555557, -0.5677647058823531, -0.5080000000000000)
```

```
//importing required dependencies
import org.apache.commons.math3.distribution.NormalDistribution
import com.cloudera.sparkts.models.Autoregression
import org.apache.spark.mllib.linalg._
//method for finding confident interval value (same for +ve and -ve)
def calcConfVal(conf: Double, n: Int): Double = {
    val stdNormDist = new NormalDistribution(0, 1)
    val pVal = (1 - conf) / 2.0
    stdNormDist.inverseCumulativeProbability(1 - pVal) / Math.sqrt(n)
}
```

```
import org.apache.commons.math3.distribution.NormalDistribution
import com.cloudera.sparkts.models.Autoregression
import org.apache.spark.mllib.linalg._
calcConfVal: (conf: Double, n: Int)Double
```

```
def acf(data: Array[Double], maxLag: Int, conf: Double = 0.95) = {
    // calculate correlations and confidence bound
    val autoCorrs = UnivariateTimeSeries.autocorr(data, maxLag)
    val confVal = calcConfVal(conf, data.length)
}
```

```
def pacf(data: Array[Double], maxLag: Int, conf: Double = 0.95) = {
    // create AR(maxLag) model, retrieve coefficients and calculate
    confidence bound
    val model = Autoregression.fitModel(new DenseVector(data), maxLag)
    val pCorrs = model.coefficients // partial autocorrelations are the
    coefficients in AR(n) model
    val confVal = calcConfVal(conf, data.length)
}
```

```
acf: (data: Array[Double], maxLag: Int, conf: Double)Unit
pacf: (data: Array[Double], maxLag: Int, conf: Double)Unit
```

```
//calculating acf
val autoC = UnivariateTimeSeries.autocorr(cc, 20)
```

```
autoC: Array[Double] = Array(0.15985960653767617, 0.07822934497499003, 0.051
04178272023124, 0.03185898579582731, 0.02940081553604699, 0.0191147184851530
9, 0.014325336877323201, 0.01350030016098633, 0.014950189714590315, 0.016887
683052156863, 0.014020513417277041, 0.0088403512962757, 0.00833189049362899
5, 0.005490817537416041, 8.82023584502792E-4, -0.0014000519138274822, -0.006
05184528400493, -0.006115838711134724, -0.006609667118626515, -0.00497244817
8312112)
```

```

//calculating confident interval value for 5%
val confVal2 = calcConfVal(0.95, cc.length)

confVal2: Double = 0.006128269705725016

//case class for reconverting Array[Double] to Dataframe for visualisation
case class acfclass(x:Double, corr:Double, conf:Double) // x is lag value,
corr is autocorrelation, conf is confidence interval value

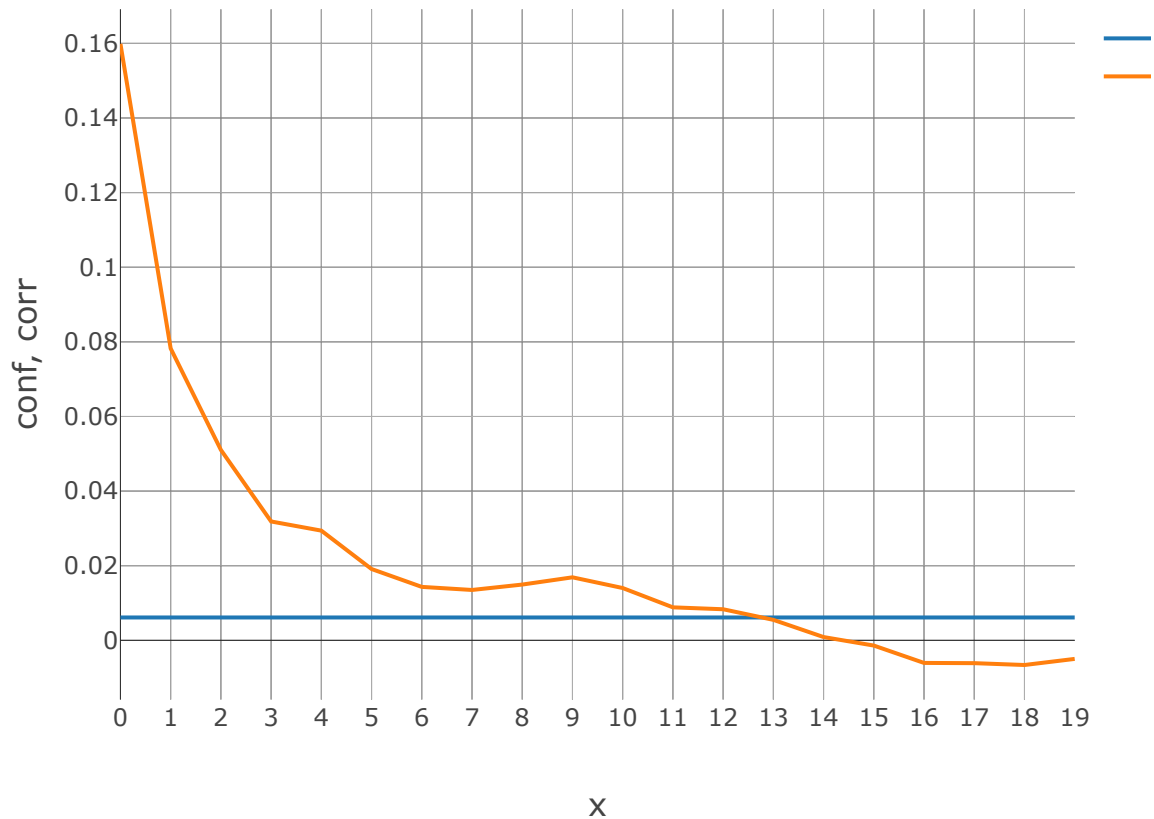
defined class acfclass

//collection of acfclass objects
val f = for(i <- 0 to 19)yield{
  acfclass(i, autoC(i) ,confVal2 )
}

f: scala.collection.immutable.IndexedSeq[acfclass] = Vector(acfclass(0.0,0.15985960653767617,0.006128269705725016), acfclass(1.0,0.07822934497499003,0.006128269705725016), acfclass(2.0,0.05104178272023124,0.006128269705725016), acfclass(3.0,0.03185898579582731,0.006128269705725016), acfclass(4.0,0.02940081553604699,0.006128269705725016), acfclass(5.0,0.01911471848515309,0.006128269705725016), acfclass(6.0,0.014325336877323201,0.006128269705725016), acfclass(7.0,0.01350030016098633,0.006128269705725016), acfclass(8.0,0.014950189714590315,0.006128269705725016), acfclass(9.0,0.016887683052156863,0.006128269705725016), acfclass(10.0,0.014020513417277041,0.006128269705725016), acfclass(11.0,0.0088403512962757,0.006128269705725016), acfclass(12.0,0.008331890493628995,0.006128269705725016), acfclass(13.0,0.005490817537416041,0.006128269705725016), acfclass(14.0,8.82023584502792E-4,0.006128269705725016), acfclass(15.0,-0.0014000519138274822,0.006128269705725016), acfclass(16.0,-0.00605184528400493,0.006128269705725016), acfclass(17.0,-0.006115838711134724,0.006128269705725016), acfclass(18.0,-0.006609667118626515,0.006128269705725016), acfclass(19.0,-0.004972448178312112,0.006128269705725016))

//plot acf graph
display(f.toSeq.toDF)

```



//acf graph crosses the confident line for the first time at lag value x=13, therefore q=13

```
//calculating pacf
// create AR(maxLag) model, retrieve coefficients and calculate confidence bound
val model = Autoregression.fitModel(new DenseVector(cc), 20)
    val pCorrs = model.coefficients // partial autocorrelations are the coefficients in AR(n) model
```

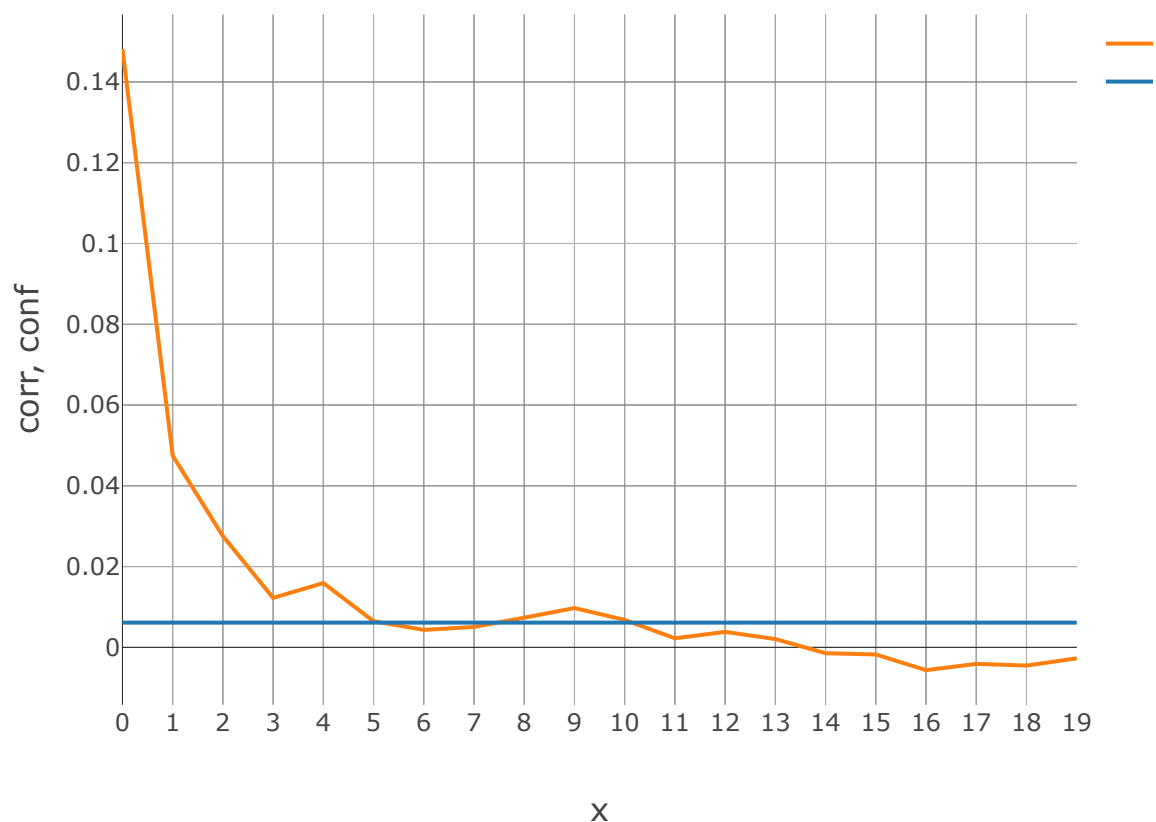
```
model: com.cloudera.sparkts.models.ARModel = com.cloudera.sparkts.models.ARModel@3d8e1ceb
pCorrs: Array[Double] = Array(0.14814005189294893, 0.04748073410040342, 0.027557210554358398, 0.012252914228101056, 0.015928687733959314, 0.006466256757204596, 0.004326543518545098, 0.005051619760605817, 0.007353556735416871, 0.00973015466197282, 0.006802798298257134, 0.0022449303174158753, 0.0038286787543913565, 0.002053598790637832, -0.001450916900002485, -0.00175555176488986, -0.005649625633282044, -0.004087619613910831, -0.004504395672759216, -0.002715647009149274)
```



```
val f2 = for(i <- 0 to 19)yield{
  acfclass(i, pCorrs(i) ,confVal2 )
}
```

```
f: scala.collection.immutable.IndexedSeq[acfclass] = Vector(acfclass(0.0,0.14814005189294893,0.006128269705725016), acfclass(1.0,0.04748073410040342,0.006128269705725016), acfclass(2.0,0.027557210554358398,0.006128269705725016), acfclass(3.0,0.012252914228101056,0.006128269705725016), acfclass(4.0,0.015928687733959314,0.006128269705725016), acfclass(5.0,0.006466256757204596,0.006128269705725016), acfclass(6.0,0.004326543518545098,0.006128269705725016), acfclass(7.0,0.005051619760605817,0.006128269705725016), acfclass(8.0,0.007353556735416871,0.006128269705725016), acfclass(9.0,0.00973015466197282,0.006128269705725016), acfclass(10.0,0.006802798298257134,0.006128269705725016), acfclass(11.0,0.0022449303174158753,0.006128269705725016), acfclass(12.0,0.0038286787543913565,0.006128269705725016), acfclass(13.0,0.002053598790637832,0.006128269705725016), acfclass(14.0,-0.001450916900002485,0.006128269705725016), acfclass(15.0,-0.00175555176488986,0.006128269705725016), acfclass(16.0,-0.005649625633282044,0.006128269705725016), acfclass(17.0,-0.004087619613910831,0.006128269705725016), acfclass(18.0,-0.004504395672759216,0.006128269705725016), acfclass(19.0,-0.002715647009149274,0.006128269705725016))
```

```
display(f2.toSeq.toDF)
```



```
//pacf graph crosses the confident line for the first time at lag value x=
5, therefore p = 5
```

```
//Now lets use p=5, q=13, d=0 as parameters of ARIMA models and predict
```

```
//In scala, to apply ARIMA model we need vector therefore we convert column data to vector
```

```
import org.apache.spark.mllib.linalg.Vector
import com.cloudera.sparkts.stats.TimeSeriesStatisticalTests
import org.apache.spark.mllib.linalg.Vectors
val ts =
Vectors.dense(weather.select("MeanTemp").rdd.collect.map(_.getDouble(0)))
```

[illegible]

```
//import required dependencies
import com.cloudera.sparkts.stats._
import com.cloudera.sparkts.models._
//fitting ARIMA model
val arimaModel = ARIMA.fitModel(5, 0, 13, ts)
```

```
import com.cloudera.sparkts.stats._
import com.cloudera.sparkts.models._
armaModel: com.cloudera.sparkts.models.ARIMAModel = com.cloudera.sparkts.mo
dels.ARIMAModel@5a9e3f1f
```

```
//predicting 50 future values  
arimaModel.forecast(ts, 50)
```

```
res40: org.apache.spark.mllib.linalg.Vector = [0.5437894491217253,0.83386149  
26319519,0.8003718232876662,1.4931783656711775,1.625375177511836,1.441658563  
8942383,1.5712270978965954,2.146600709106111,2.264114703199161,1.96791129358  
83252,2.164053060205302,1.7882432129383803,1.7396980303137395,1.707344597860  
8266,1.6631187669418332,1.648721971220636,1.628127223823239,1.61317940850284  
84,1.5993171513222422,1.5876944736854839,1.5775547399869352,1.56884858581358  
79,1.561325722616133,1.5548417903051786,1.5492476499496728,1.544423145166277  
3,1.5402617191135235,1.5366724695645873,1.5335766453569342,1.530906441171672  
6,1.5286033324926431,1.526616854851082,1.5249034767405831,1.523425653017329  
1,1.5221509996463907,1.5210515849306858,1.5729947622984033,1.52922549967409  
3,1.5481428792490517,1.6394827856928869,1.5980836974432324,1.594806857097427  
4,1.5844918598531164,1.553883029050622,1.5465660277847535,1.542748790947846  
1,1.5385976715252754,1.5353129042880223,1.5323779239194377,1.582772940338674  
3,1.5905477330866533,1.9355958708760326,1.6391159613692743,1.753391264585601  
6,1.7012631197017825,1.6012420009533583,1.623553957818754,1.594166387054367  
4,1.7906078767838771,1.6113017147196391,1.6814145253703832,1.619507126064078  
3,1.5821626421005524,1.5806842193243427,1.6217188696642513,1.572184241817113  
5,1.5848743585605398,2.253080974641941,1.8405909117742394,1.963510998291111  
4,1.837008609358858,1.689437786459794,2.8372860821567403,1.8675556580188077,  
2.3346163809155374,3.028683642960409,2.4256930531100673,2.468096168025685,2.  
2889040460797823,7.339330519689777,11.282884144188024,6.584092125154323,8.53
```