

Topic: Elastic and Inelastic Collisions

A - Aim

To understand the **difference between elastic and inelastic collisions**, and how **momentum and energy** are conserved or lost in different types of collisions.

C - Concept

- A **collision** occurs when two bodies exert forces on each other over a short time.
 - **Elastic Collision**: Both **momentum and kinetic energy are conserved**.
 - **Inelastic Collision**: **Momentum is conserved**, but **kinetic energy is not**.
 - **Perfectly inelastic collision**: Objects stick together after collision.
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H - How it works

- Use **momentum conservation** in all types of collisions.
 - Use **kinetic energy conservation** only for **elastic** collisions.
 - In inelastic collisions, part of the kinetic energy is converted into other forms (heat, sound, deformation).
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E - Equations/Formulas

1. **Momentum Conservation** (all collisions):
$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$

2. **Kinetic Energy Conservation** (elastic only):

$$\frac{1}{2}m_1u_1^2 + \frac{1}{2}m_2u_2^2 = \frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2$$
$$m_1u_1^2 + m_2u_2^2 = m_1v_1^2 + m_2v_2^2$$

3. **Final Velocity (perfectly inelastic):**

$$v = \frac{m_1u_1 + m_2u_2}{m_1 + m_2}$$

4. **Coefficient of restitution (e):**

$$e = \frac{v_2 - v_1}{u_1 - u_2}$$

- $e = 1$: perfectly elastic
- $0 < e < 1$: inelastic
- $e = 0$: perfectly inelastic

S - Steps to solve problems

1. Write down the **mass and velocities** before and after collision.
2. Use **momentum conservation equation**.
3. If elastic, also apply **kinetic energy conservation**.
4. Solve the system of equations.
5. For perfectly inelastic, use combined mass formula.

E - Example

Q: A 1 kg ball moving at 4 m/s collides with a 2 kg stationary ball. If the collision is perfectly inelastic, find their final velocity.

Sol:

- Use: $v = \frac{m_1u_1 + m_2u_2}{m_1 + m_2}$

