

IGHASC 2024: Indo-German Workshop on Hardware-aware Scientific Computing
Heidelberg, Oct 2024

It is all in the GPUs - How the Hardware Architecture impacted Scientific Software in the US Exascale Computing Project

Hartwig Anzt

Chair of Computational Mathematics, TU Munich
Adjunct Professor, University of Tennessee



The US Exascale Computing Project



Advancing Scientific Discovery



Strengthening National Security



Improving Industrial Competitiveness

Addressing a National Imperative

The Exascale Computing Project is an aggressive research, development, and deployment project focused on delivery of mission-critical applications, an integrated software stack, and exascale hardware technology advances.

Application Development



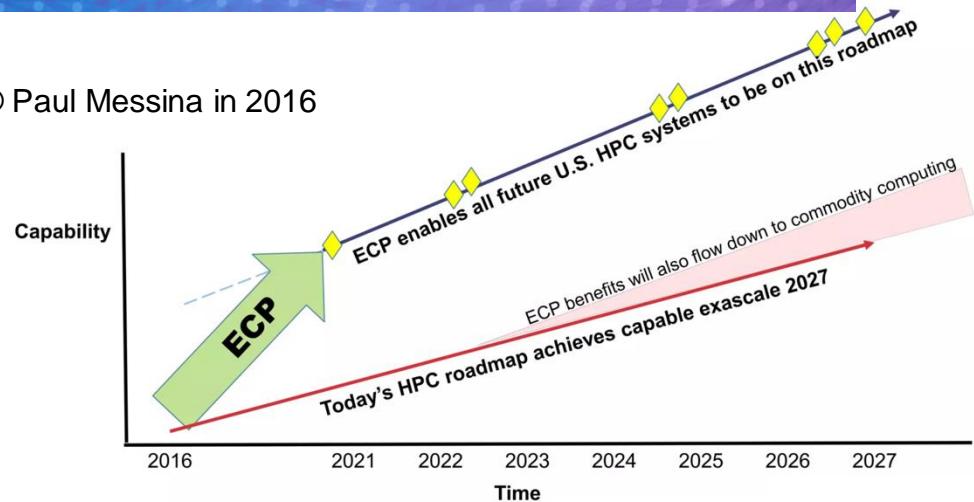
Software Technology



Hardware & Integration



© Paul Messina in 2016



The US Exascale Computing Project

- 3 computers. (~2B)
 - \$600M each
 - \$400M to vendors for Design, Path, Fast - Forward



AMD Based
(Up & running)
20 MW



Intel Based
(Up & running)
40 MW



AMD APU Based
(being commissioned)

The US Exascale Computing Project

- 3 computers. (~2B)
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Rank	System	Cores	Rmax (PFlop/s)	Rpeak (PFlop/s)	Power (kW)
1	Frontier - HPE Cray EX235a, AMD Optimized 3rd Generation EPYC 64C 20Hz, AMD Instinct MI250X, Slingshot-11, HPE DOE/SC/Oak Ridge National Laboratory United States	8,699,904	1,206.00	1,714.81	22,786
2	Aurora - HPE Cray EX - Intel Exascale Compute Blade, Xeon CPU Max 9470 52C 2.4GHz, Intel Data Center GPU Max, Slingshot-11, Intel DOE/SC/Argonne National Laboratory United States	9,264,128	1,012.00	1,980.01	38,698
3	Eagle - Microsoft NDv5, Xeon Platinum 8480C 48C 2GHz, NVIDIA H100, NVIDIA Infiniband NDR, Microsoft Azure Microsoft Azure United States	2,073,600	561.20	846.84	
4	Supercomputer Fugaku - Supercomputer Fugaku, A64FX 48C 2.2GHz, Tofu interconnect D, Fujitsu RIKEN Center for Computational Science Japan	7,630,848	442.01	537.21	29,899
5	LUMI - HPE Cray EX235a, AMD Optimized 3rd Generation EPYC 64C 2GHz, AMD Instinct MI250X, Slingshot-11, HPE EuroHPC/CSC Finland	2,752,704	379.70	531.51	7,107
6	Alps - HPE Cray EX254n, NVIDIA Grace 72C 3.1GHz, NVIDIA GH200 Superchip, Slingshot-11, HPE Swiss National Supercomputing Centre (CSCS) Switzerland	1,305,600	270.00	353.75	5,194

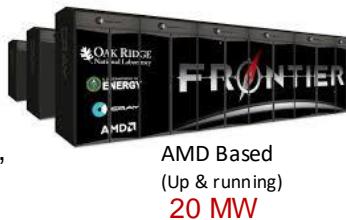
98% of FLOP/s in GPUs
2% of FLOP/s in CPUs

92% of FLOP/s in GPUs
8% of FLOP/s in CPUs

The US Exascale Computing Project



- 3 computers. (~2B)
 - \$600M each
 - \$400M to vendors for Design, Path, Fast - Forward
- Application and Software Development(~2B)



LatticeQCD	NWChemEx	GAMESS	ExaStar	ExaSky	EQSIM
Validate Fundamental Laws of Nature Objective: Validate Fundamental Laws	Tackling Chemical, Materials, and Biomolecular Challenges in Exascale Objective: Tackling Chemical, Materials, and Biomolecular Challenges in Exascale	General Atomic and Molecular Electronic Structure System	Exascale Models of Stellar Explosions Objective: Demystify Origin of Chemical Elements	Computing at the Extreme Scales Objective: Cosmological Probe of the Standard Model of Particle Physics	High-Performance, Multidisciplinary Simulations for Regional-Scale Earthquake Hazard/Risk Assessments
EXAALT	ExaAM	QMCPACK	WDMApp	ExaSMR	WarpX
Molecular Dynamics at Exascale Objective: Tackling Chemical, Materials, and Biomolecular Challenges in Exascale	Transforming Additive Manufacturing through Exascale Simulation Objective: Transforming Additive Manufacturing through Exascale Simulation	Quantum Mechanics at Exascale	High-fidelity Whole Device Modelling of Magnetically Confined Fusion Plasmas	Coupled Monte Carlo Neutrinos and Fluid Flow Simulation of Small Modular Reactors	Exascale Modeling of Advanced Particle Accelerators
ExaSGD	CANDLE	ExaBiome	ExaWind	Combustion-PELE	MFIX-Exa
Optimizing Stochastic Grid Dynamics at Exascale Objective: Optimizing Stochastic Grid Dynamics at Exascale	Exascale Deep Learning-Enabled Precision Medicine for Cancer Objective: Exascale Deep Learning-Enabled Precision Medicine for Cancer	Exascale Solutions for Microbiome Analysis	Exascale Predictive Wind Plant Flow Physics Modeling	High-efficiency, Low-emission Combustion Engine Design	Performance Prediction of Multiphase Energy Conversion Device
Ristra	MAPP	EMPIRE AND SPARC	Subsurface	ESM-MMF	ExaFEL
Multi-physics simulation tools for weapons-relevant applications	Multi-physics simulation tools for High Energy Density Physics (HEDP) and weapons-relevant applications for DOE and DoD	EMPIRE addresses electromagnetic plasma physics, and SPARC addresses reentry aerodynamics	Exascale Subsurface Simulator of Coupled Flow, Transport, Reactions, and Mechanics	Cloud-Resolving Climate Modeling of the Earth's Water Cycle	Data Analytics at Exascale for Free Electron Lasers
			Adaptive Mesh Refinement	Efficient Exascale Discretizations	Online Data Analysis and Reduction at the Exascale
			Particle-Based Applications	Efficient Implementation of Key Graph Algorithms	Exascale Machine Learning Technologies

PMR Core (17)	Compilers and Support (7)	Tools and Technology (11)	xSDK (16)	Visualization Analysis and Reduction (9)	Data mgmt, I/O Services, Checkpoint restart (12)	Ecosystem/E4S at-large (12)
QUO	openarc	TAU	hypre	ParaView	SCR	mpfileUtils
Papyrus	Kitsune	HPCToolkit	FleCSI	Catalyst	FAODEL	TriBITS
SICM	LLVM	Dyninst Binary Tools	MFEM	VTK-m	ROMIO	MarFS
Legion	CHILL autotuning comp	Gotocha	Kokkoskernels	SZ	Mercury (Mochi suite)	GUFI
Kokkos (support)	LLVM openMP comp	Caliper	Trilinos	zip	HD5	Intel GEOPM
RAJA	OpenMP V & V	PAPI	SUNDIALS	Visit	BEE	Parallel netCDF
CHAI	Flang LLVM Fortran comp	Program Database Toolkit	PETSc/TAO	ASCENT	ADIOS	FSEFI
PaRSEC*		Search (random forests)	libEnsemble	Cinema	Darshan	Kitten Lightweight Kernel
DARMA	Siboka	STRUMPACK	ROVER		UnifyCR	COOLR
GASNet-EX		SuperLU			VeloC	NRM
Cthreads	C2C				IOSS	ArgoContainers
BOLT	Sonar	ForTrilinos			HXHM	Spack
UPC++		SLATE			PMR	
MPICH		MAGMA			Tools	
Open MPI		DTK			Math Libraries	
Umpire		Tasmanian			Data and Vis	
AML		Ginkgo			Ecosystems and delivery	

A few words about myself

- Born and raised in Karlsruhe
- PhD in Numerical Mathematics from KIT in 2012
- Focus on computational linear algebra and high performance computing (HPC)
- Linear solvers, preconditioners, ...
- During my PostDoc at the University of Tennessee, I developed MAGMA sparse



MAGMA-sparse as a “child” of MAGMA explores the development of sparse linear algebra functionality for NVIDIA GPUs.

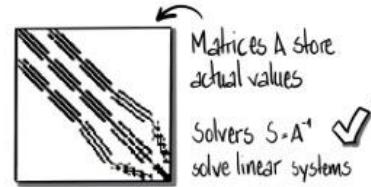


Limitations:

- *C code with hand-written build system*
- *Sparse unit testing*
- *Focus on NVIDIA GPUs*
- *Design-specific limitations (flexibility/extensibility)*

Designing a math toolset for ECP applications

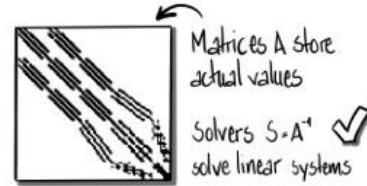
Ginkgo - A sparse linear algebra library for HPC



Designing a math toolset for ECP applications

written in C++

Ginkgo - A sparse linear algebra library for HPC



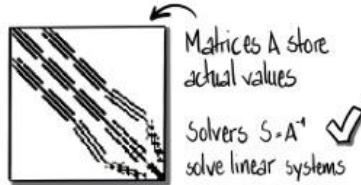
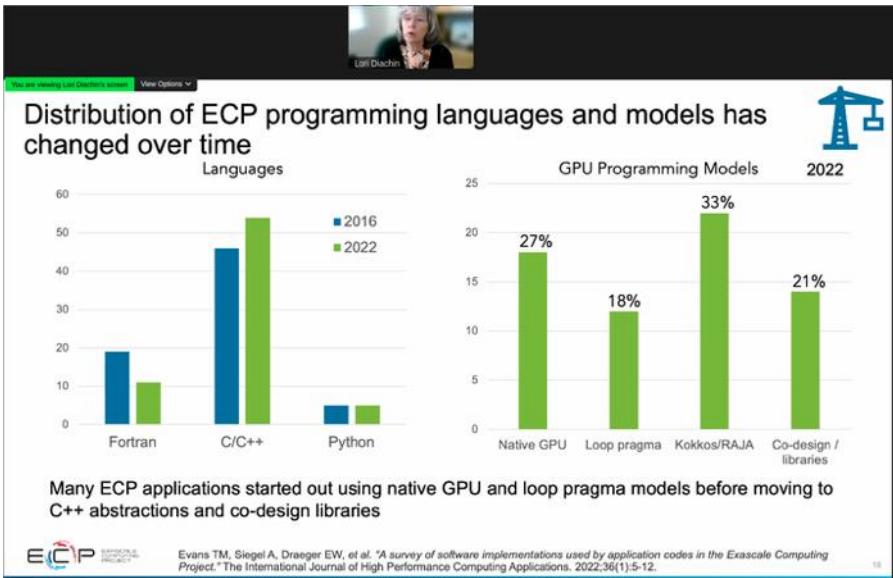
Matrices A store
actual values

Solvers $S = A^{-1}$ ✓
solve linear systems

Designing a math toolset for ECP applications

written in C++

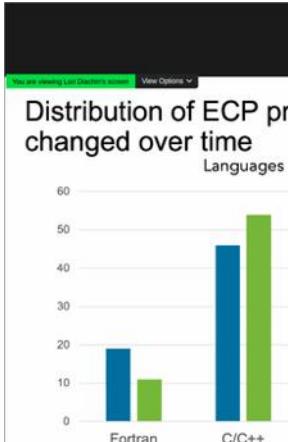
Ginkgo - A sparse linear algebra library for HPC



written in C++ Ginkgo - A sparse linear algebra library for HPC

BACK TO THE BUILDING BLOCKS:

A PATH TOWARD SECURE AND MEASURABLE SOFTWARE



Many ECP applications start with FEBRUARY 2024
C++ abstractions and co-designed libraries



Evans TM, Siegel A, Draeger EW, et al. "A survey of software implementations used by application Project." The International Journal of High Performance Computing Applications. 2022;36(1):5-12.

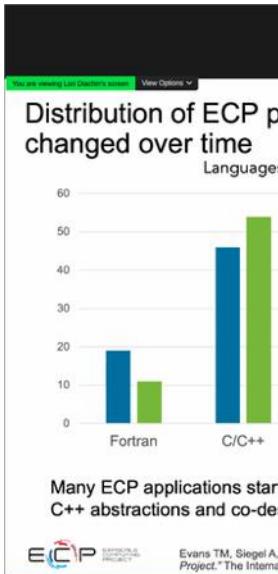


Memory safety vulnerabilities are a class of vulnerability affecting how memory can be accessed, written, allocated, or deallocated in unintended ways.ⁱⁱⁱ Experts have identified a few programming languages that both lack traits associated with memory safety and also have high proliferation across critical systems, such as C and C++.^{iv} Choosing to use memory safe programming languages at the outset, as recommended by the Cybersecurity and Infrastructure Security Agency's (CISA) Open-Source Software Security Roadmap is one example of developing software in a secure-by-design manner.^v

Designing a math toolset for ECP applications

written in C++ → Ginkgo - A sparse linear algebra library for HPC

Translating All C TO Rust (TRACTOR)



ACTIVE

Contract Opportunity

Notice ID
DARPA-SN-24-89

Related Notice

Department/Ind. Agency
DEPT OF DEFENSE

Sub-tier
DEFENSE ADVANCED RESEARCH PROJECTS AGENCY (DARPA)

Office
DEF ADVANCED RESEARCH PROJ

General Information

Contract Opportunity Type: Special Notice

All Dates/Times are: (UTC-04:00) EASTERN

Original Published Date: Jul 29, 2024 02:

Original Response Date: Aug 19, 2024 11:

Inactive Policy: Manual

Original Inactive Date: Aug 27, 2024

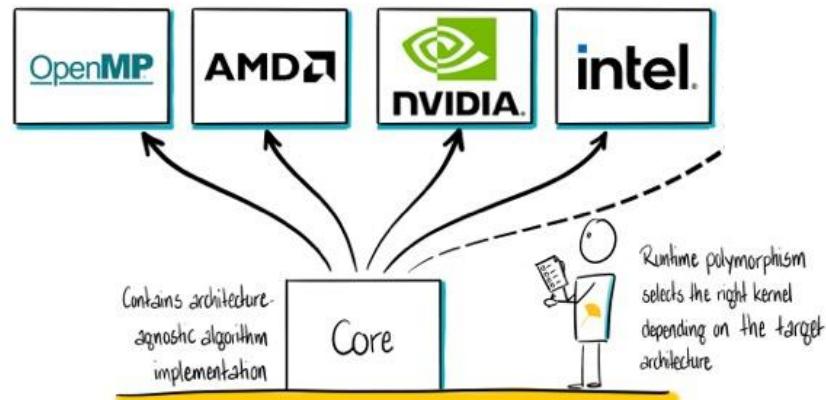
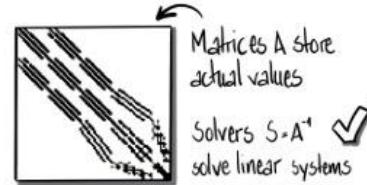


Description

The TRACTOR program aims to achieve a high degree of automation towards translating legacy C to Rust, with the same quality and style that a skilled Rust developer would employ, thereby permanently eliminating the entire class of memory safety security vulnerabilities present in C programs. Performers might employ novel combinations of software analysis (e.g., static analysis and dynamic analysis), and machine learning techniques (e.g., large language models). The draft solicitation will be posted shortly.

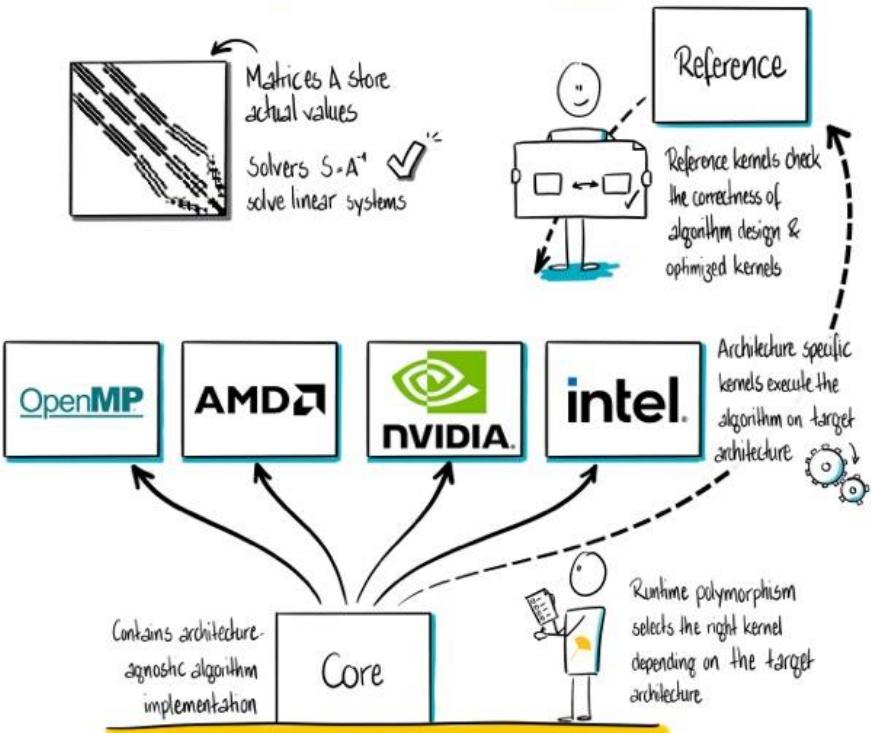
Designing a math toolset for ECP applications

written in C++ ↗ Ginkgo - A sparse linear algebra library for HPC



Designing a math toolset for ECP applications

written in C++ Ginkgo - A sparse linear algebra library for HPC



Designing a math toolset for ECP applications

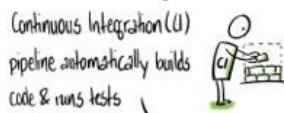
build	code_quality
build/amd/nompi/clang/rocm45/debu...	clang-tidy
build/amd/nompi/clang/rocm45/relea...	iwvu
build/amd/nompi/clang/rocm514/rele...	subdir-build
build/amd/nompi/qcc/rocm45/relea...	warnings
build/amd/nompi/qcc/rocm514/debu...	
build/amd/nompi/qcc/rocm514_w...	
build/cuda10/nompi/clang/cuda/rele...	
build/cuda10/nompi/clang/cuda/rele...	
build/cuda11/nompi/qcc/cuda/debu...	
build/cuda11/nompi/qcc/cuda/debu...	
build/icpx20231/qcpu/release/shared	
build/icpx/qcpu/release/static	
build/nocuda-nomixed/nompi/clang...	
build/nocuda-nomixed/nompi/clang...	
build/nocuda-nomixed/openmpi/qcc...	
build/nocuda/nompi/clang/core/rele...	
build/nocuda/nompi/qcc/core/debu...	
build/nocuda/nompi/qcc/core/debu...	
build/nocuda/nompi/qcc/omp/relea...	
build/nocuda/nompi/qcc/omp/relea...	
build/nocuda/openmpi/clang/omp/d...	
build/nocuda/openmpi/clang/omp/q...	
build/nvhpc227/cuda117/nompi/nvc...	
build/nvhpc233/cuda120/nompi/nvc...	
build/windows-cuda/release/shared	
build/windows/release/shared	

written in C++ Ginkgo - A sparse linear algebra library for HPC

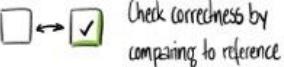
Development process



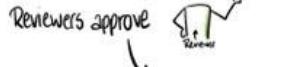
Developers push new code to the repository



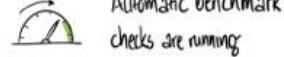
Continuous Integration (CI) pipeline automatically builds code & runs tests



Check correctness by comparing to reference



Reviewers approve



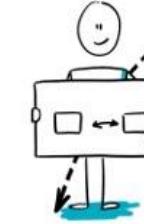
Automatic benchmark checks are running

Ginkgo



Matrices A store actual values

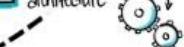
Solvers S = A⁻¹ solve linear systems



Reference

Reference kernels check the correctness of algorithm design & optimized kernels

Architecture specific kernels execute the algorithm on target architecture



Contains architecture-agnostic algorithm implementation

Core



Runtime polymorphism selects the right kernel depending on the target architecture

Designing a math toolset for ECP applications

Building Trusted Scientific Software

Software Verification

PUBLISHED JUN 11, 2015 AUTHOR ARASHI TOSHI TOPICS BETTER RELIABILITY TESTS

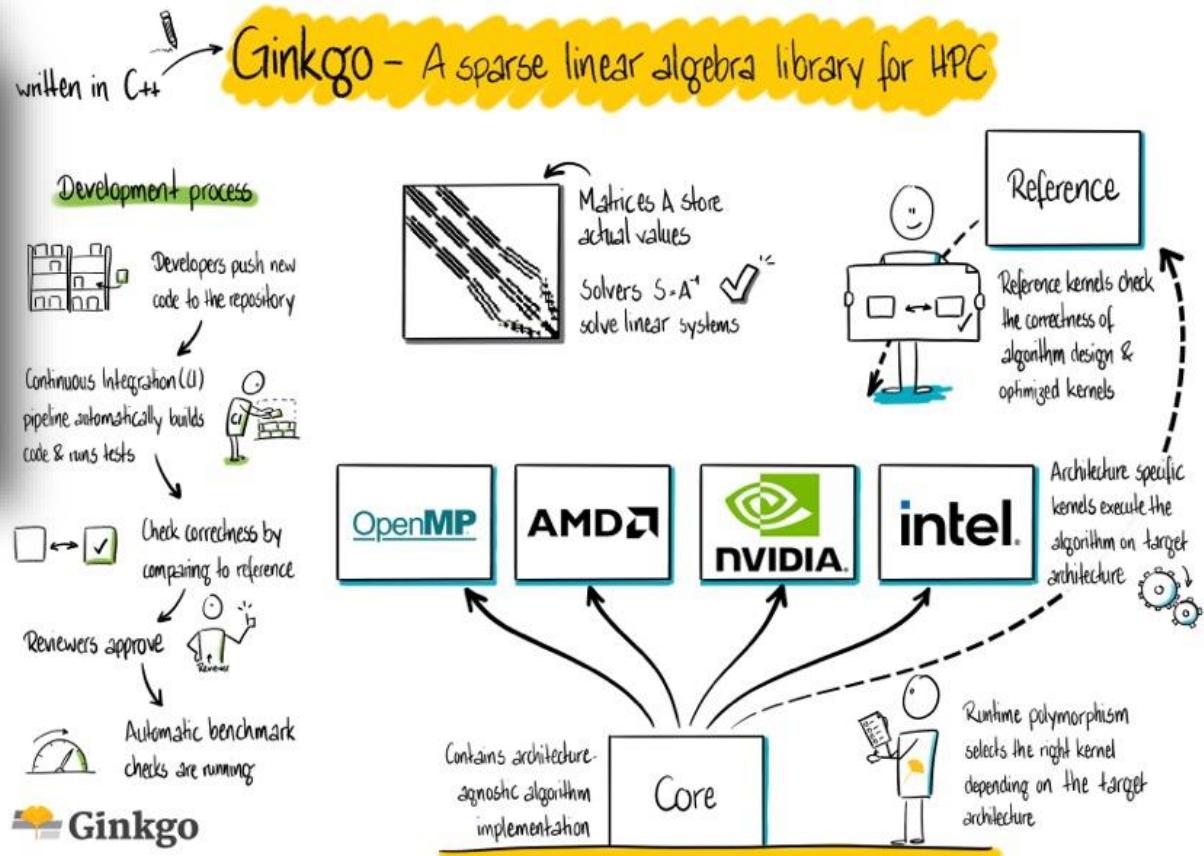
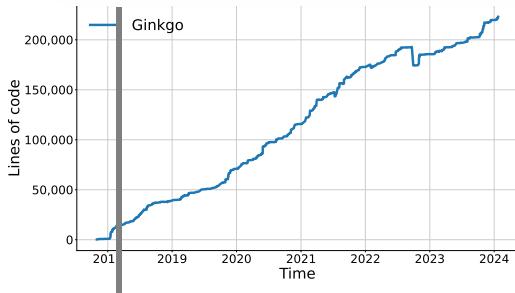
In the realm of software, verification is often erroneously a proper subset of verification for gaining confidence in the holistic process by which the developers convince that the method was designed to do. In scientific software this could mean numerical stability, and efficacy of the method in the expected results. Note that verification is limited to a model specification, not that the model itself matches validation process.

I have worked on the phrase "Verified" to mean

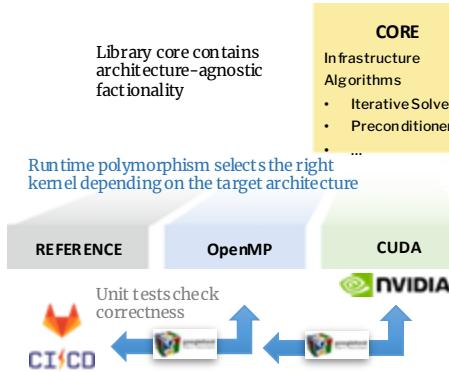
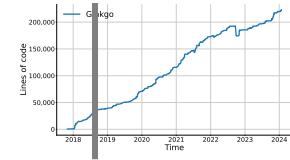
Pairing internal verification for

IDEAS productivity

better scientific software



Starting with the CUDA backend



	OMP	CUDA
Basic		
SpMV	✓	✓
SpMM	✓	✓
SpGeMM	✓	✓
BICG	✓	✓
BICGSTAB	✓	✓
CG	✓	✓
CGS	✓	✓
GMRES	✓	✓
IDR	✓	✓
(Block-)Jacobi	✓	✓
ILU/IC		✓
Parallel ILU/IC	✓	✓
Parallel ILUT/ICT	✓	✓
Sparse Approximate Inverse	✓	✓
Krylov solvers		

Linear Operator Interface

We express everything as Linear Operator.

- Internally, we leverage C++ class inheritance.
- Applications can apply any functionality as a linear operator.



Matrix-Vector Product

Preconditioner (for matrix A)

Solver (for system $Ax = b$)

$$x := A \cdot b$$

$$x := M^{-1} \cdot b$$

$$x := S \cdot b$$

$$M^{-1} \approx A^{-1}$$

$$S \approx A^{-1}$$

$$M^{-1} = \Pi(A)$$

$$S = \Sigma(A)$$

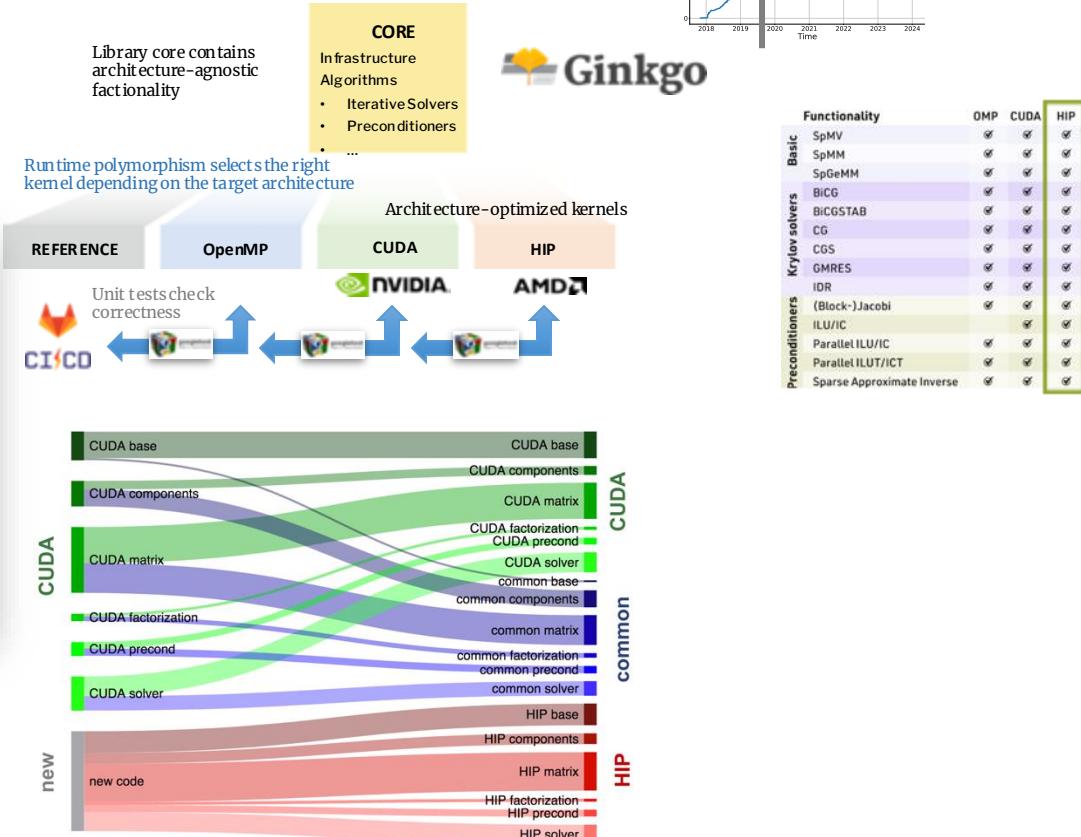
All of them can be expressed as

Application of a linear operator* (LinOp) $L : \mathbb{F}^m \rightarrow \mathbb{F}^m$

Extending to AMD GPUs

~2 months

The screenshot shows a GitHub repository page for the Ginkgo library. The header includes the logo for "better scientific software". The navigation bar has links for "Resources", "Blog", "Events", and "About". Below the header, the breadcrumb navigation shows "HOME > BLOG > Porting the Ginkgo Package to AMD's HIP Ecosystem". The main content title is "Porting the Ginkgo Package to AMD's HIP Ecosystem". The author is "HARTWIG ANZT" and the date is "PUBLISHED JUN 25, 2020". The topics listed are "BETTER RELIABILITY", "TESTING", "BETTER PLANNING", and "DESIGN". The blog post discusses the experience of porting CUDA code to AMD's Heterogeneous-compute Interface for Portability (HIP). The content area contains several paragraphs of text and a conclusion.

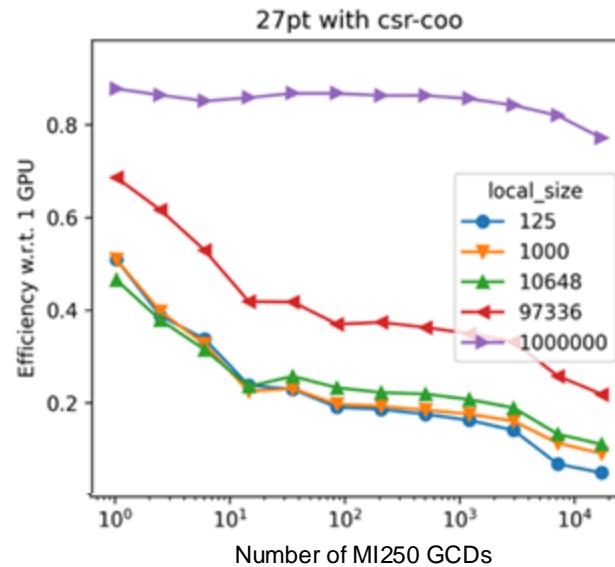
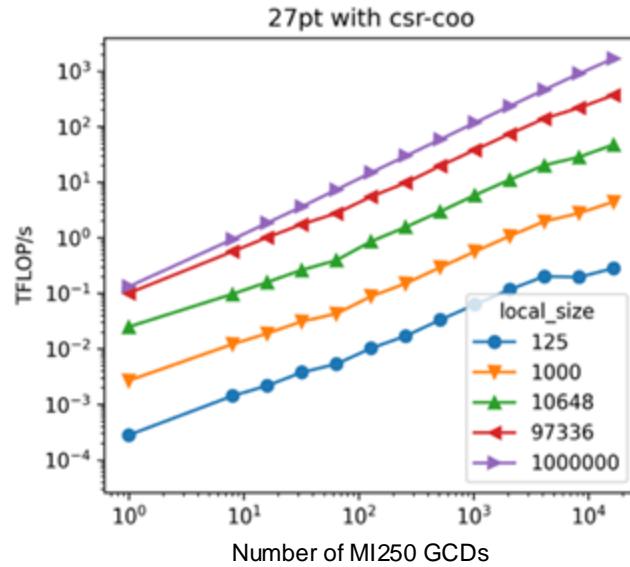


Weak and strong Scalability

Frontier (#1 TOP500)

SpMV Weak scaling: problem size increases with parallel resources

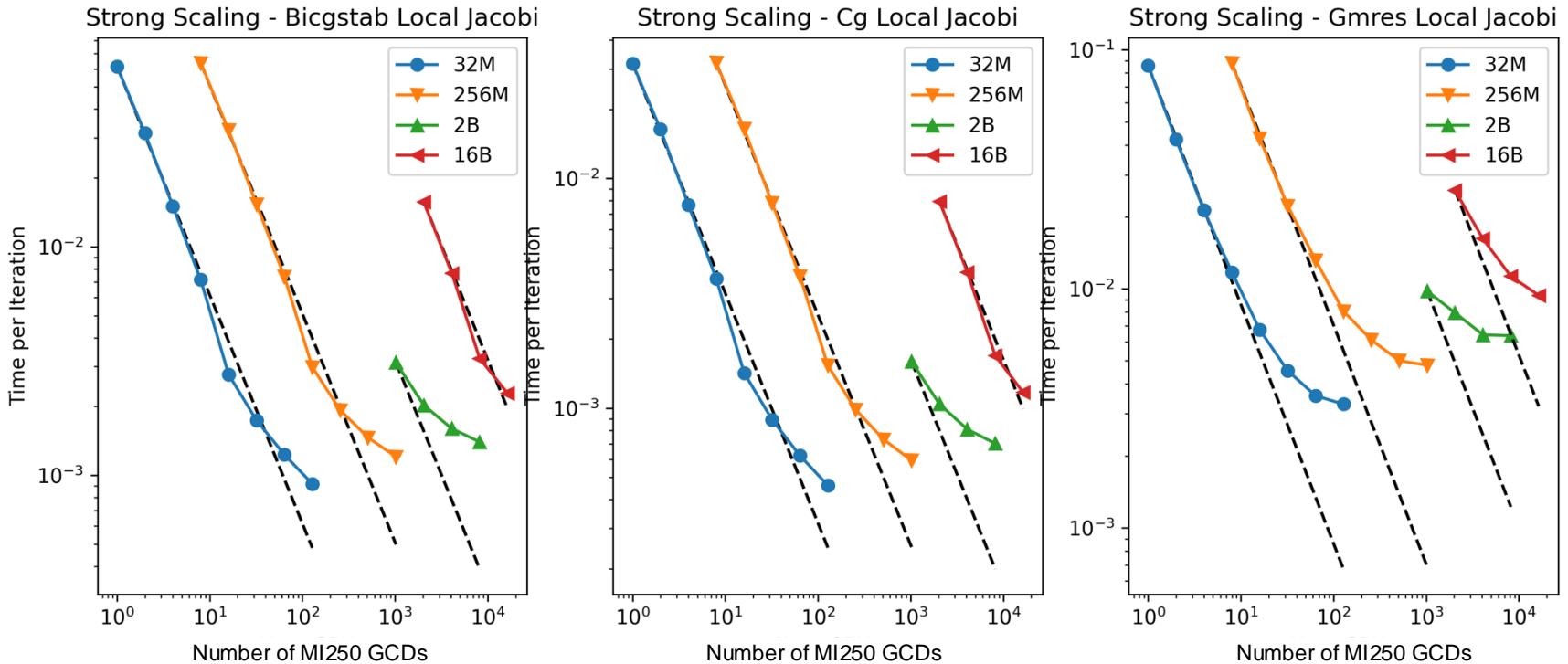
Weak scaling up to 8k AMD MI250 GPUs (16k GCDs)



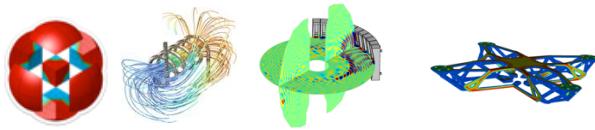
Weak and strong Scalability

Strong scaling: problem size constant, parallel resources increase

Frontier (#1 TOP500)



We “forgot” the customer on the way...



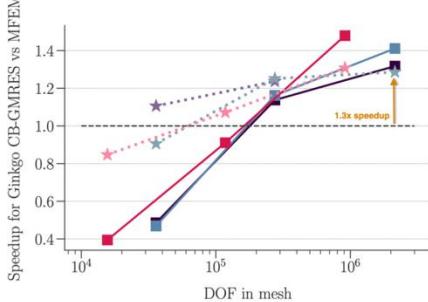
MFEM is a *free, lightweight, scalable C++ library* for finite element methods.

Speeding up MFEM’s “example 22” on GPUs

Example 22 of the MFEM finite element library solves harmonic oscillation problems, with a forced oscillation imposed at the boundary. In this test, we use variant 1:

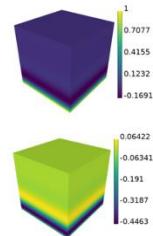
$$-\nabla \cdot (a \nabla u) - \omega^2 b u + i \omega c u = 0$$

with $a = 1$, $b = 1$, $\omega = 10$, $c = 20$



- p = 1 (V100)
- ★·· p = 1 (MI50)
- p = 2 (V100)
- ★·· p = 2 (MI50)
- p = 3 (V100)
- ★·· p = 3 (MI50)

Real part of solution (top),
imaginary part of solution



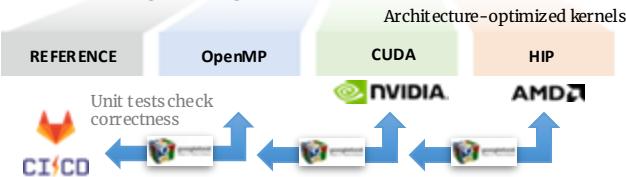
Speedup of Ginkgo’s Compressed Basis-GMRES solver vs MFEM’s GMRES solver for three different orders of basis functions (p), using MFEM matrix-free operators and the Ginkgo-MFEM integration wrappers in MFEM. CUDA 10.1/V100 and ROCm 4.0/MI50.

Library core contains architecture-agnostic functionality

CORE

Infrastructure
Algorithms
• Iterative Solvers
• Preconditioners
• ...

Run time polymorphism selects the right kernel depending on the target architecture



Natalie Beams



Tzanio Kolev

Functionality	OMP	CUDA	HIP
SpMV	✓	✓	✓
SpMM	✓	✓	✓
SpGeMM	✓	✓	✓
BICG	✓	✓	✓
BICGSTAB	✓	✓	✓
CG	✓	✓	✓
CGS	✓	✓	✓
GMRES	✓	✓	✓
IDR	✓	✓	✓
(Block-)Jacobi	✓	✓	✓
ILU/IC		✓	✓
Parallel ILU/IC	✓	✓	✓
Parallel ILUT/ICT	✓	✓	✓
Sparse Approximate Inverse	✓	✓	✓

Krylov solvers

Preconditioners

Utilities	On-Device Matrix Assembly	MC64/RCM reordering	Wrapping user data	Logging	PAPI counters
	✓	✓	✓		
	✓	✓		✓	
			✓	✓	
				✓	✓

Contribute and benefit from community



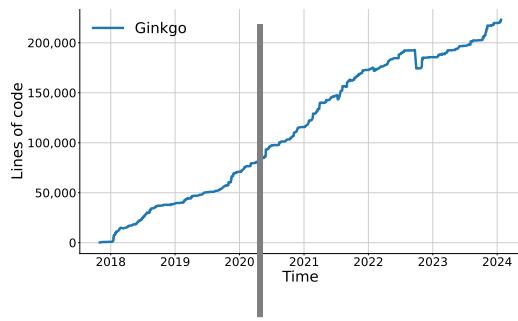
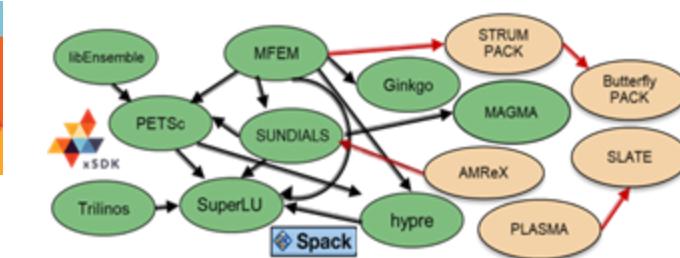
The xSDK provides infrastructure for and interoperability of a **collection of related and complementary software elements**—developed by diverse, independent teams throughout the high-performance computing (HPC) community—that provide the building blocks, tools, models, processes, and related artifacts for rapid and efficient development of high-quality applications.

November 2022

- 26 math libraries
- 2 domain components
- 16 mandatory xSDK community policies
- Spack xSDK installer

xSDK community policies:

- 16 mandatory policies,
- 8 recommended policies,
- 4 Spack variant guidelines
- Available on Github
<https://xsdk.info/policies/>



	Functionality	OMP	CUDA	HIP
Basic				
SpMV	✓	✓		
SpMM	✓	✓		
SpGeMM	✓	✓		
BICG	✓	✓		
BICGSTAB	✓	✓		
CG	✓	✓		
CGS	✓	✓		
GMRES	✓	✓		
IDR	✓	✓		
(Block-)Jacobi	✓	✓		
ILU/IC		✓		
Parallel ILU/IC	✓	✓		
Parallel ILUT/ICT	✓	✓		
Sparse Approximate Inverse	✓	✓		
Krylov solvers				
Trilinos				
PETSc				
MFEM				
SUNDIALS				
Ginkgo				
MAGMA				
AMReX				
PLASMA				
hypre				
SLATE				
ButterflyPACK				
Preconditioners				
Spack				
hysrc				
SuperLU				
SUNDIALS				
PETSc				
MFEM				
libEnsemble				
Utilities				
On-Device Matrix Assembly	✓	✓		
MC64/RCM reordering	✓			
Wrapping user data		✓		
Logging		✓		
PAPI counters		✓		

Extending to Intel GPUs

~18 months

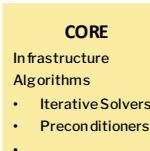


Since 1987 - Covering the Fastest Computers in the World and the People Who Run Them

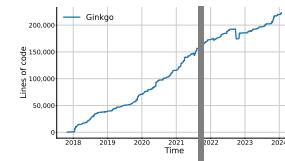
- Home
- Technologies
- Sectors
- COVID-19
- AI/ML/DL

Preparing for the Arrival of Intel's Discrete High-Performance GPUs
By Harwig Anzt
March 23, 2021

Library core contains architecture-agnostic functionality



Runtime polymorphism selects the right kernel depending on the target architecture



Functionality	OMP	CUDA	HIP	DPC++
SpMV	✓	✓	✓	✓
SpMM	✓	✓	✓	✓
SpGeMM	✓	✓	✓	✓
BICG	✓	✓	✓	✓
BICGSTAB	✓	✓	✓	✓
CG	✓	✓	✓	✓
CGS	✓	✓	✓	✓
GMRES	✓	✓	✓	✓
IDR	✓	✓	✓	✓
(Block-)Jacobi	✓	✓	✓	✓
ILU/IIC	✓	✓	✓	✓
Parallel ILU/IIC	✓	✓	✓	✓
Parallel ILUT/ICT	✓	✓	✓	✓
Sparse Approximate Inverse	✓	✓	✓	✓



Mike Tsai

tid % subgroup size >= 4 gives wrong division

(double) 1/a gives wrong result when the tid % subgroup size >= 4
For example, when a = 1.07338829563753890
1/a should be 0.931629125853232
if (local_id == assign_id) { a = double(1)/a; }
when assign_id < 4, Gen9 GPU still give the correct result
when assign_id >= 4, Gen9 GPU gives wrong 0.9316293597221375 the product is 1.0000000506
CPU has more worse result

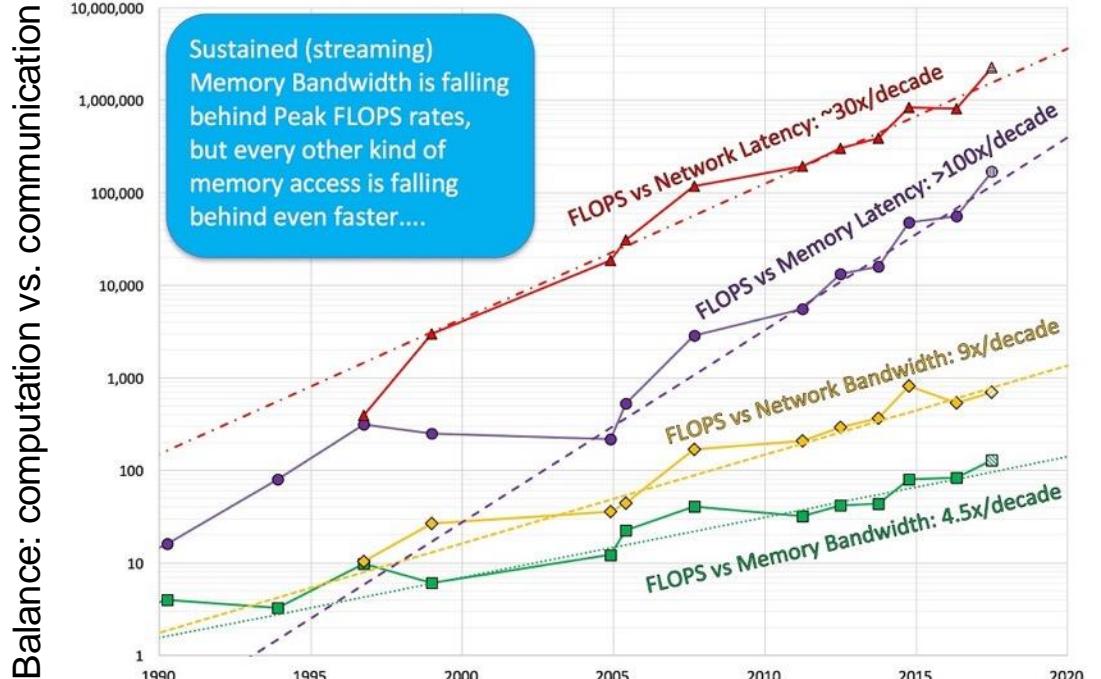
It is connected to optimizations (not reproducible with O0). Regular floating point options, fma, fp-speculation=off do not impr. Ticket number: XDEPS-4031

Devcloud node issue

- sycl-ls/clinfo does not give any output s001-n225, s011-n006
- no gpu on the nodes s001-n232, s001-n233, s011-n008
- github.com is not accessible on login-2

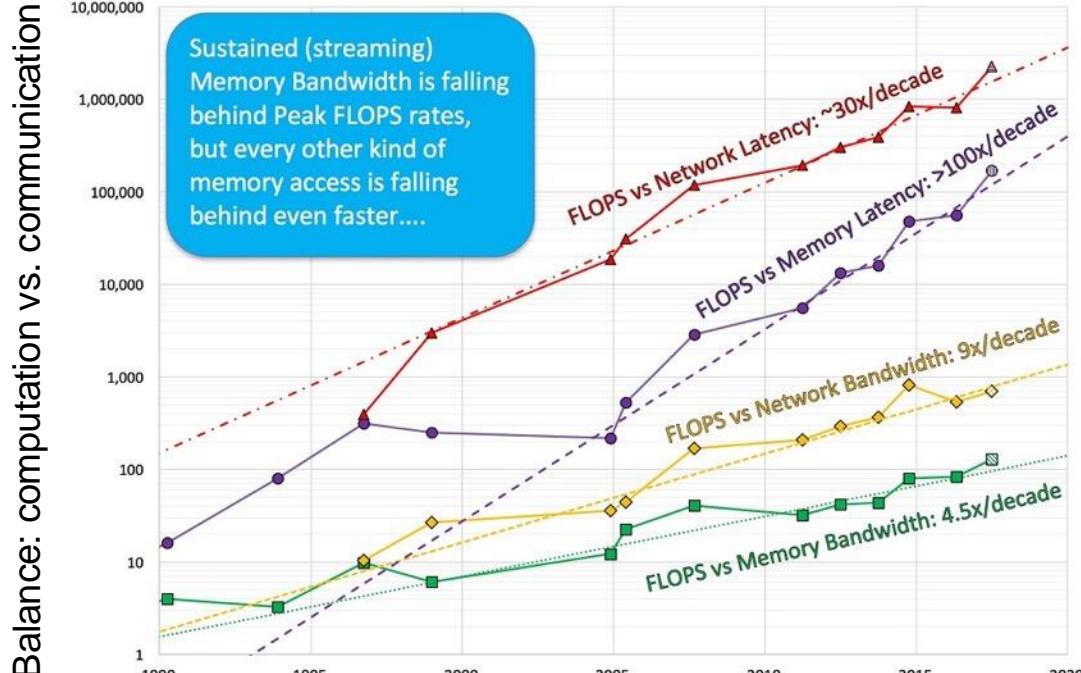
Utilities	On-Device Matrix Assembly	MC64/RCM reordering	Wrapping user data	Logging	PAPI counters
	✓	✓	✓	✓	✓

Hardware Trends – ECP Mixed Precision Focus Effort



Trends in the relative performance of floating-point arithmetic and several classes of data access for select HPC servers over the past 25 years. Source: John McCalpin

Hardware Trends – ECP Mixed Precision Focus Effort



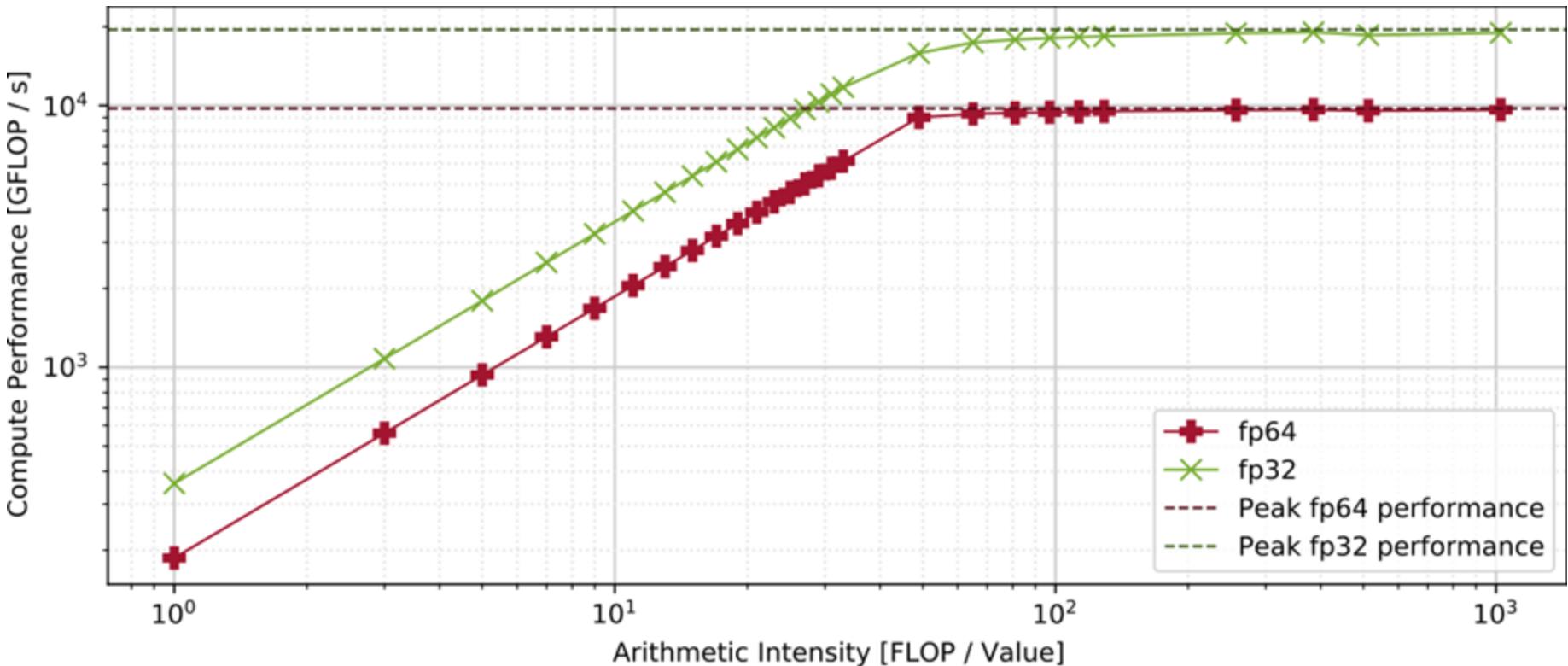
Trends in the relative performance of floating-point arithmetic and several classes of data access for select HPC servers over the past 25 years. Source: John McCalpin

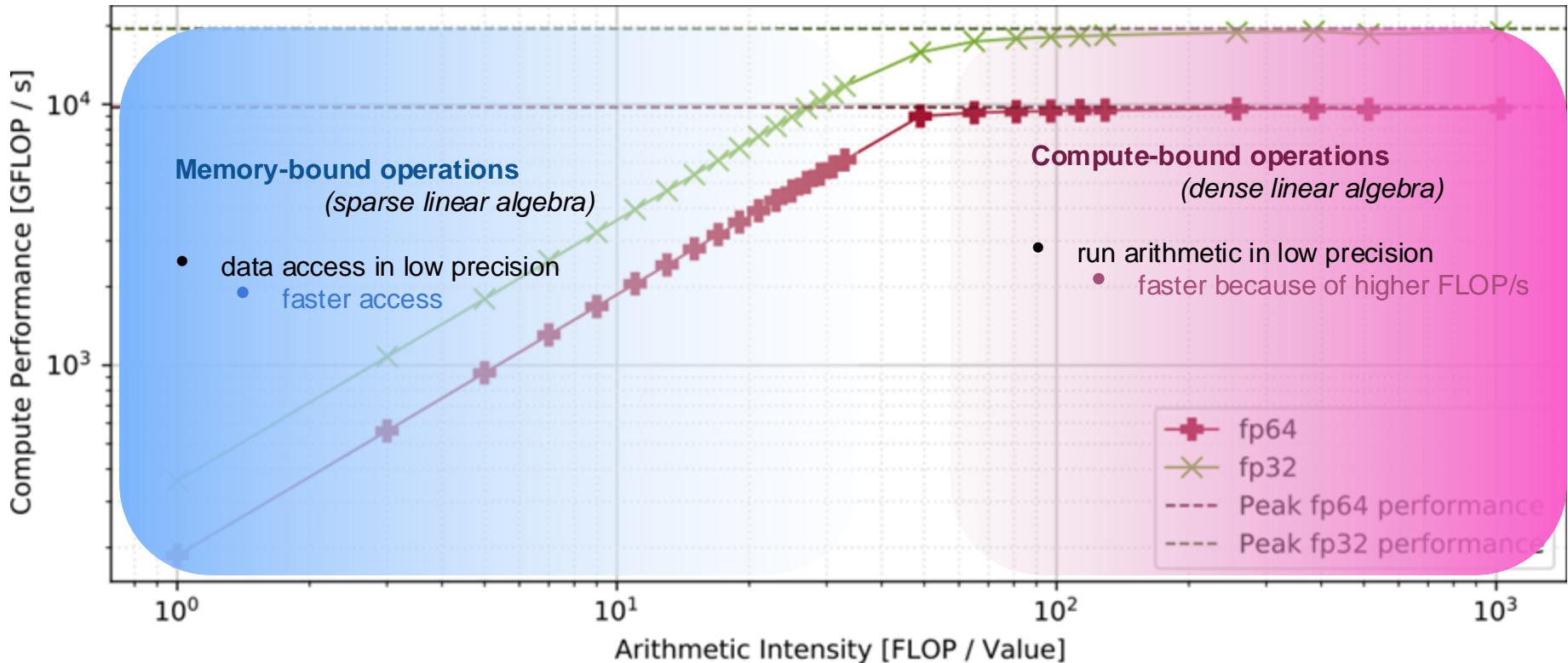
NVIDIA

Form Factor	H100 SXM
FP64	34 teraFLOPS
FP64 Tensor Core	67 teraFLOPS
FP32	67 teraFLOPS
TF32 Tensor Core	989 teraFLOPS ^z
BFLOAT16 Tensor Core	1,979 teraFLOPS ^z
FP16 Tensor Core	1,979 teraFLOPS ^z
FP8 Tensor Core	3,958 teraFLOPS ^z
INT8 Tensor Core	3,958 TOPS ^z

- (Dense) Matrix Performance > Vector Performance
- Low Precision Perf > High Precision Performance

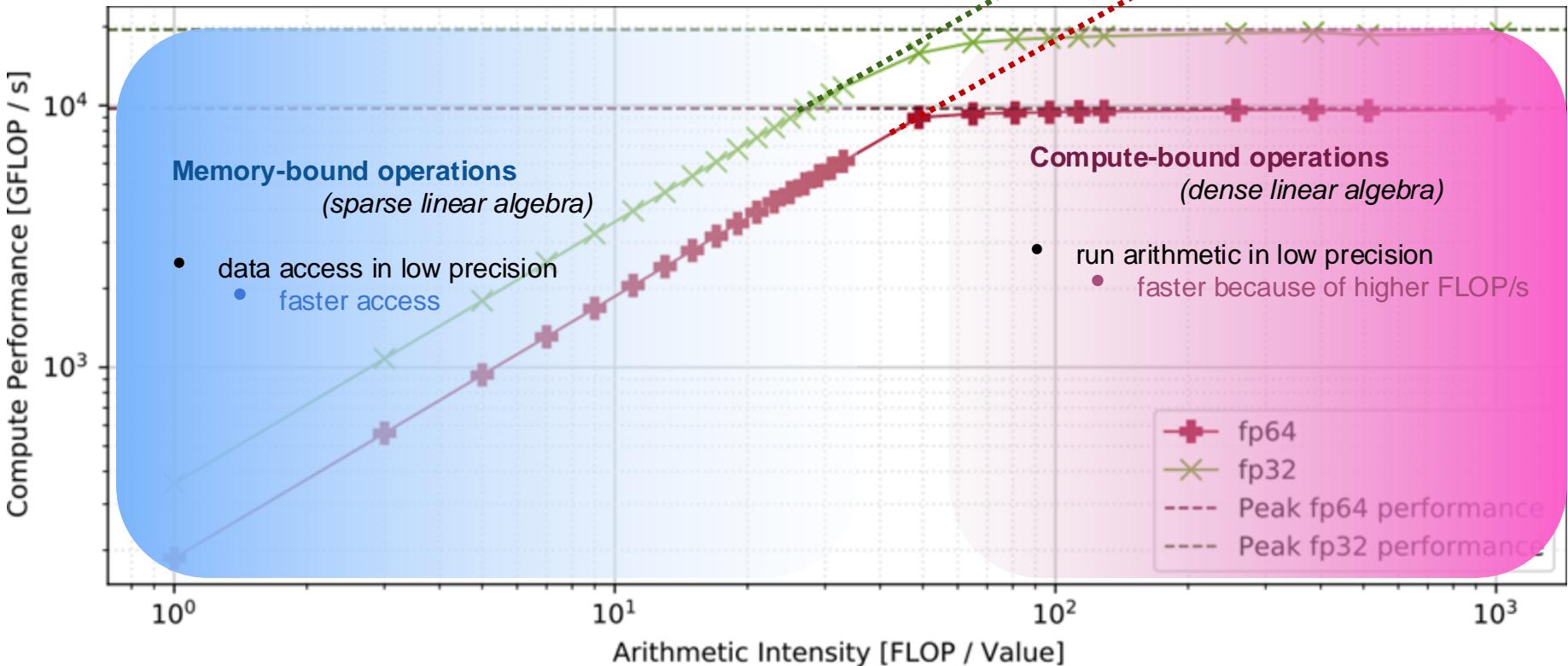
NVIDIA A100





Matrix fp32

Matrix fp64



Linear System $Ax=b$ with $\text{cond}(A) \approx 10^7$
 (apache2 from SuiteSparse) NVIDIA V100 GPU

Double precision GMRES

Initial residual norm
 $\sqrt{r^T r} : 9670.36$
 Final residual norm
 $\sqrt{r^T r} : 9.6639e-09$
 GMRES iteration count: 23271
 GMRES execution time: 43801 ms

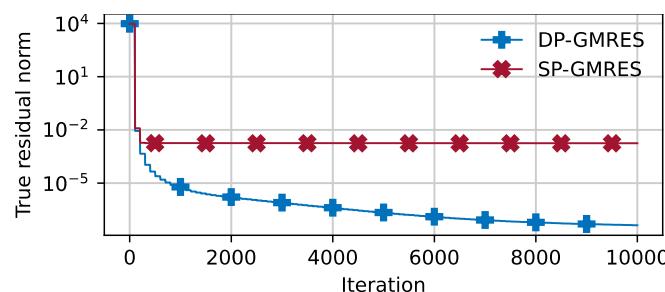
Relative residual $\sim 10^{-12}$

Single precision GMRES

Initial residual norm
 $\sqrt{r^T r} : 9670.36$
 Final residual norm
 $\sqrt{r^T r} : 0.00175464$
 GMRES iteration count: 25000
 GMRES execution time: 27376 ms

Relative residual $\sim 10^{-7}$

$\sim 2x$ faster!

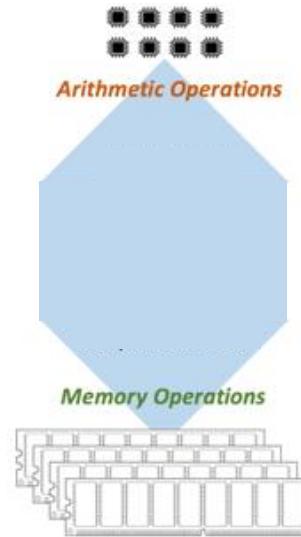


forward error \approx (unit round-off) * (linear system's condition number)

N. Higham: Accuracy and stability of numerical algorithms. SIAM, 2002.

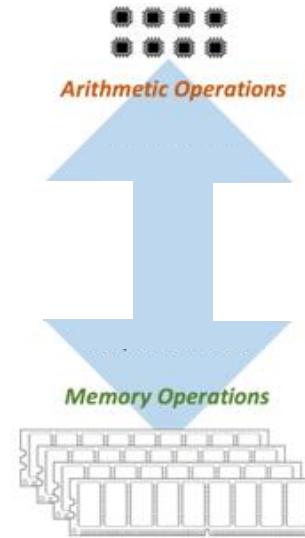
ECP Focus Effort Mixed Precision

- Traditionally, we use a strong coupling between the precision formats used for arithmetic operations the precision format handling data in main memory.



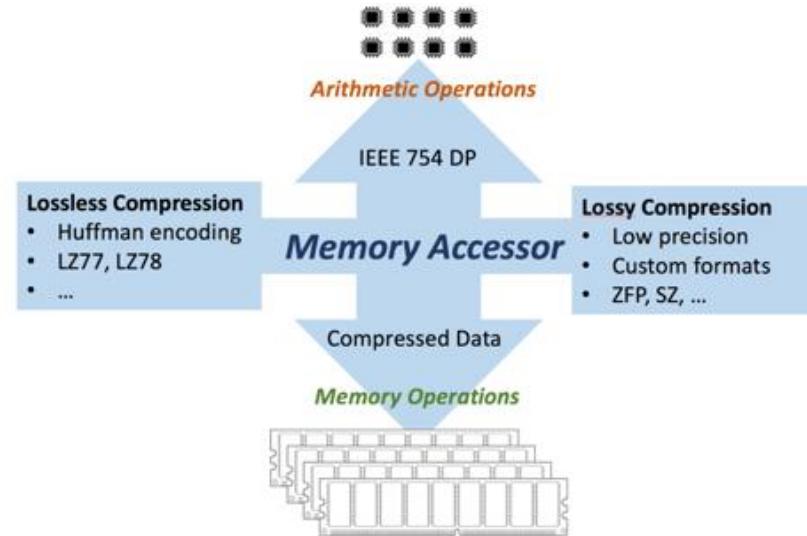
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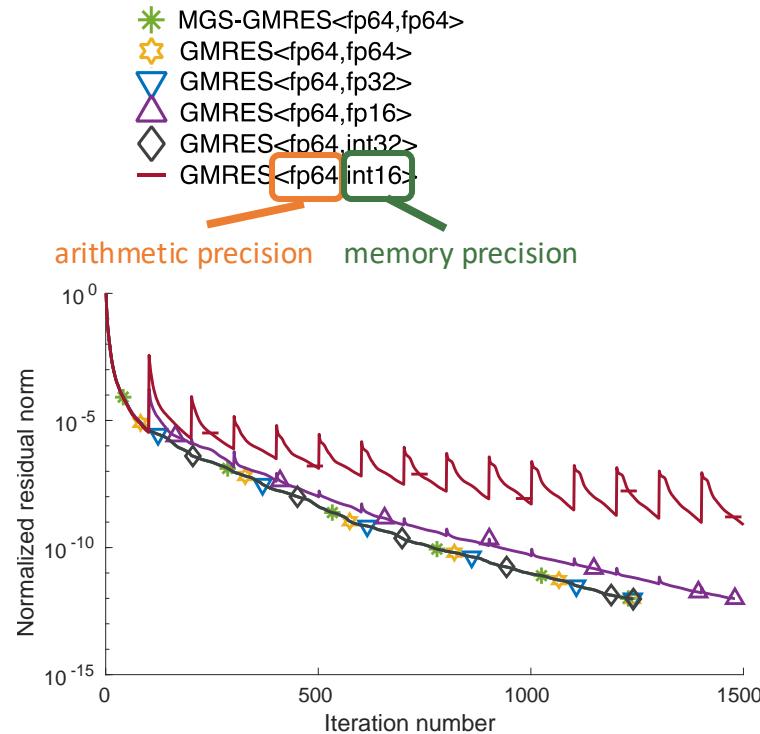
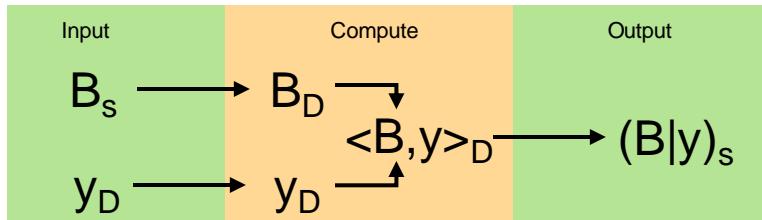
ECP Focus Effort Mixed Precision

- Traditionally, we use a strong coupling between the precision formats used for arithmetic operations the precision format handling data in main memory.
- *We should compute in fp64*
- *Data should be compressed for main memory access (low precision/compression)*
- *Compression / Conversion needs to happen on-the-fly*



Compressed Basis (CB-) GMRES

- Use double precision in all arithmetic operations;
- Store Krylov basis vectors \mathbf{B} in lower precision;
 - Search directions are no longer DP-orthogonal;
 - Hessenberg system maps solution to “perturbed” Krylov subspace;
 - Additional iterations may be needed;
 - As long as the loss-of-orthogonality is moderate, we should see moderate convergence degradation;



Linear System $Ax=b$ with $\text{cond}(A) \approx 10^7$
 (apache2 from SuiteSparse) NVIDIA V100 GPU

Double precision GMRES

Initial residual norm

$\sqrt{r^T r} : 9670.36$

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$\sqrt{r^T r} : 9.6639e-09$

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Final residual norm

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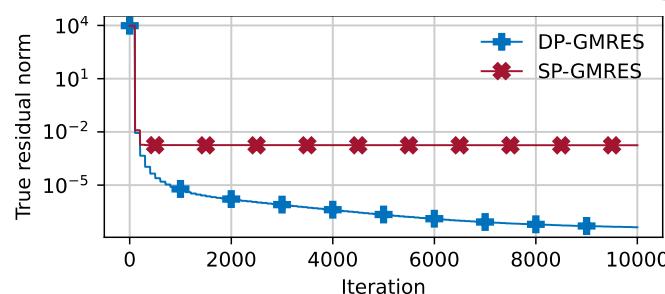
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Relative residual $\sim 10^{-7}$



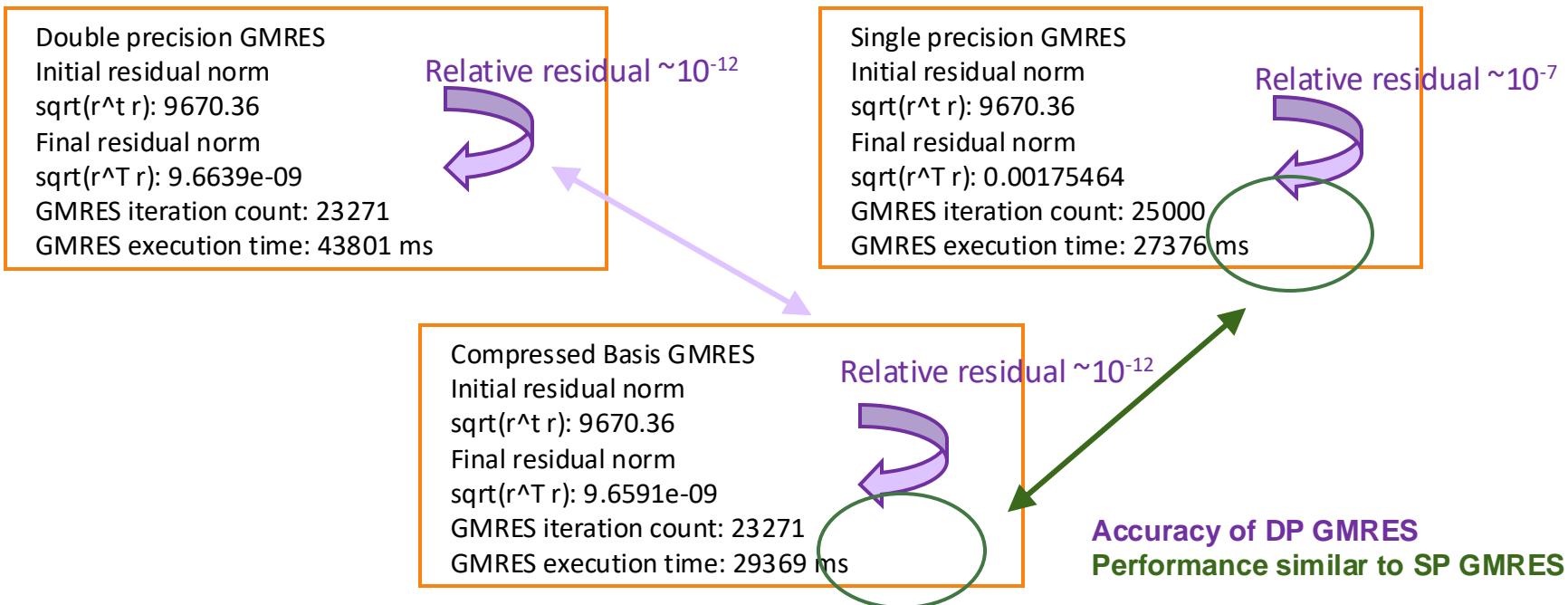
$\sim 2x$ faster!

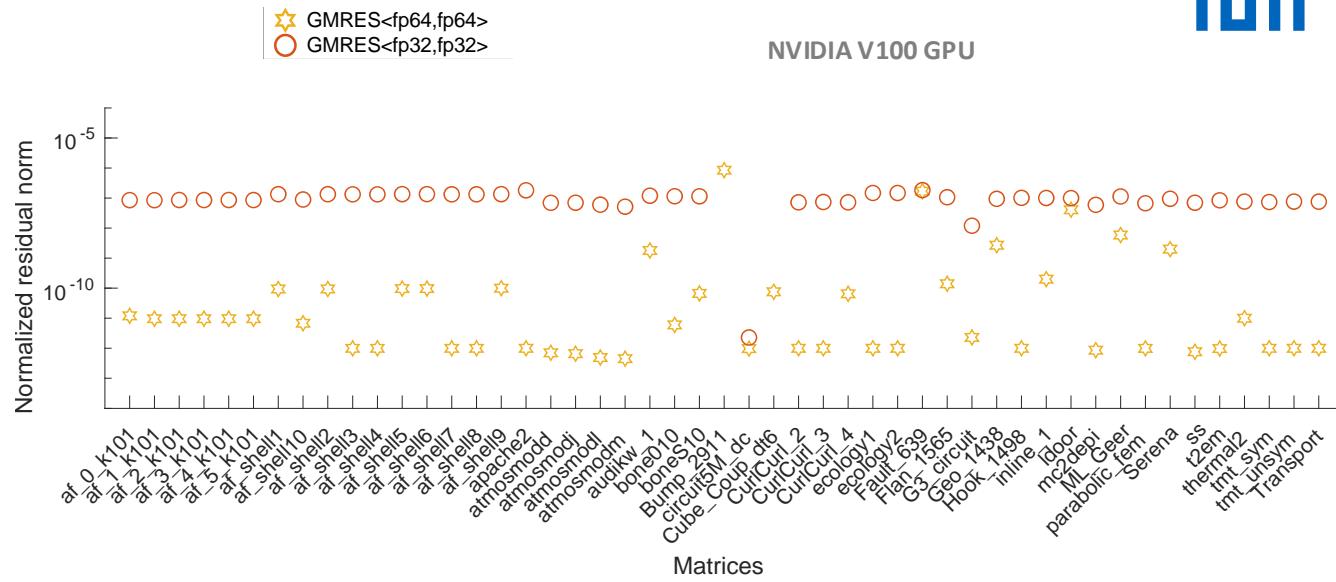


forward error \approx (unit round-off) * (linear system's condition number)

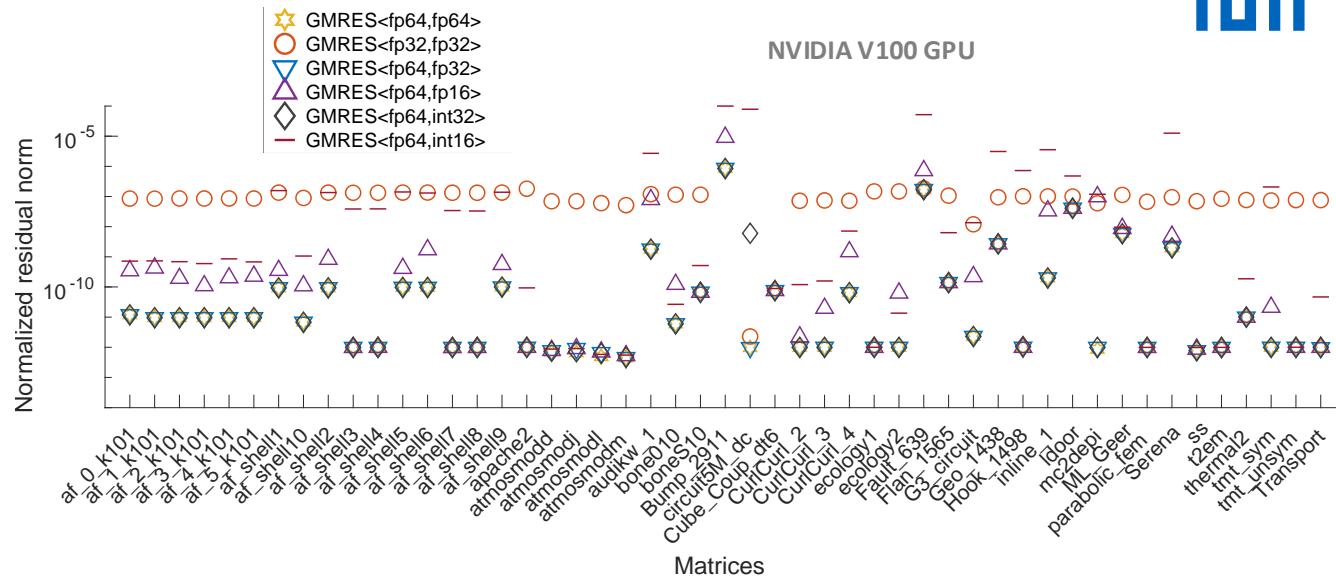
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Linear System $Ax=b$ with $\text{cond}(A) \approx 10^7$
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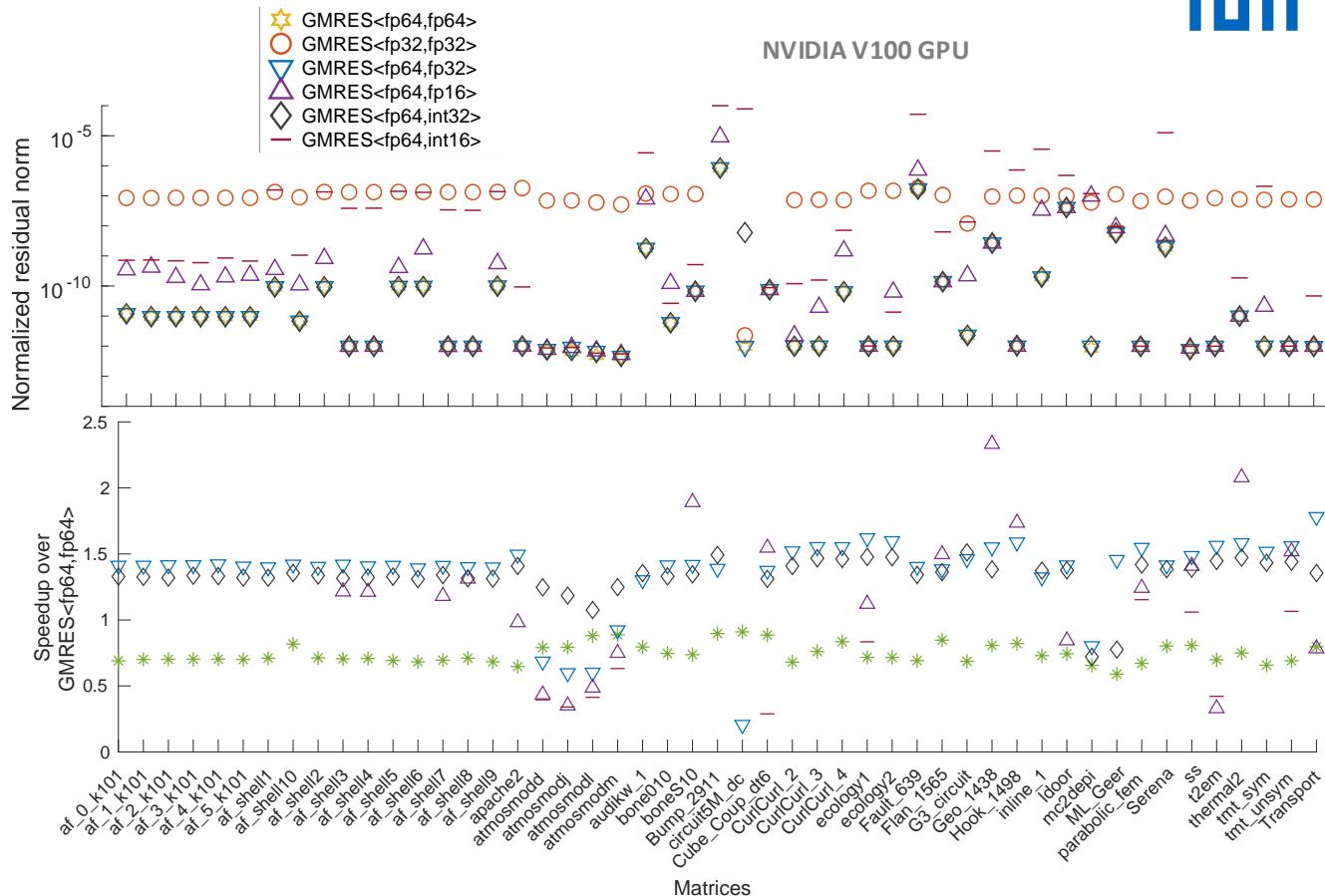
- CB-GMRES using 32-bit storage preserves DP accuracy
(SP-GMRES does not)



- CB-GMRES using 32-bit storage preserves DP accuracy (SP-GMRES does not)
- Speedups problem-dependent
- Speedup $\varnothing 1.4x$ (for restart 100)
- 16-bit storage mostly inefficient



Aliaga JI, Anzt H, Grützmacher T, Quintana-Ortí ES, Tomás AE. Compressed basis GMRES on high-performance graphics processing units. *The International Journal of High Performance Computing Applications*. 2022;0(0). doi:[10.1177/10943420221115140](https://doi.org/10.1177/10943420221115140)

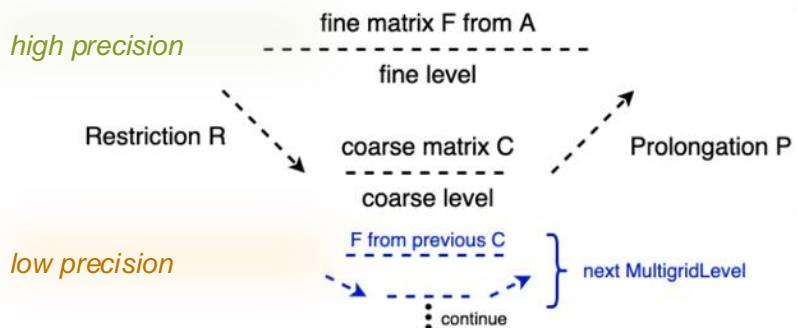


- Preconditioning iterative solvers

- Idea: Approximate inverse of system matrix to make the system “easier to solve”:

$$\text{and solve } Ax = b \Leftrightarrow P^{-1}Ax = P^{-1}b \Leftrightarrow \tilde{A}x = \tilde{b}$$

- Mixed Precision Multigrid Preconditioner



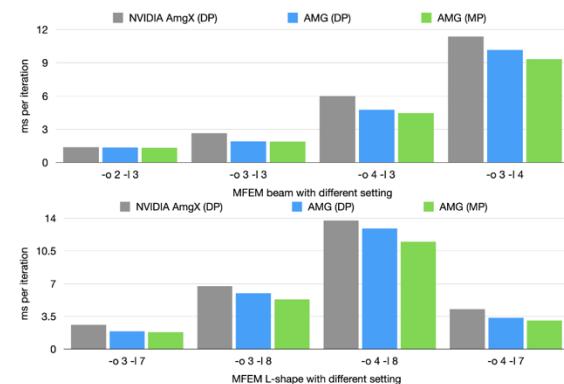
```

1 multigrid::build()
2   .with_max_levels(10u) // equal to NVIDIA/AMGX 11 max levels
3   .with_min_coarse_row(64u)
4   .with_pre_smoothes(sm, sm_f)
5   .with_mg_level(pgm, pgm_f)
6   .with_level_selector(
7     [](const size_type level, const LinOp*) -> size_type {
8       // Only the first level is generated by MultigridLevel(double).
9       // The subsequent levels are generated by MultigridLevel(float)
10      return level >= 1 ? 1 : 0;
11    })
12   .with_coarsest_solver(coarsest_solver_f)

```



Mike Tsai

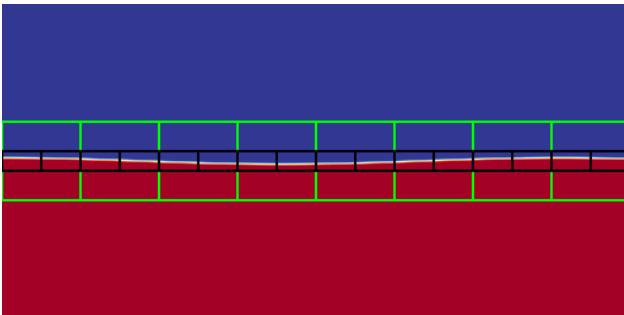


Application Needs – ECP Batched Focus Effort

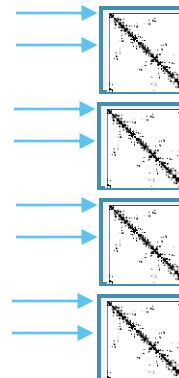
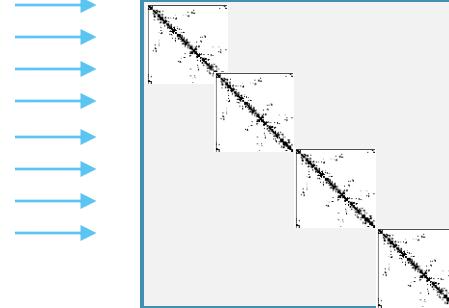
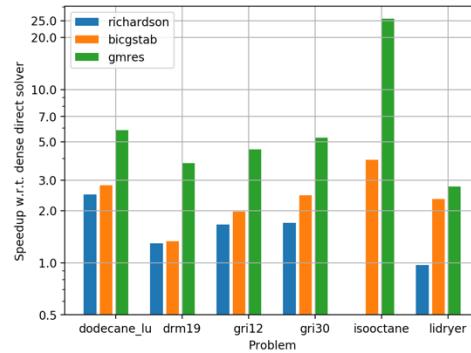
Batched iterative solvers for SUNDIALS / PeleLM

PeleLM is a parallel, adaptive mesh refinement (AMR) code that solves the reacting Navier-Stokes equations in the low Mach number regime. The core libraries for managing the subcycling AMR grids and communication are found in the [AMReX source code](#).

<https://amrex-combustion.github.io/PeleLM/overview.html>



Problem	Size	Non-zeros (A)	Non-zeros (L+U)
dodecane_lu	54	2,332 (80%)	2,754 (94%)
drm19	22	438 (90%)	442 (91%)
gri12	33	978 (90%)	1,018 (93%)
gri30	54	2,560 (88%)	2,860 (98%)
isoctane	144	6,135 (30%)	20,307 (98%)
lidryer	10	91 (91%)	91 (91%)



Batched Sparse Iterative Solvers for Computational Chemistry Simulations on GPUs

Publisher: IEEE

Cite This

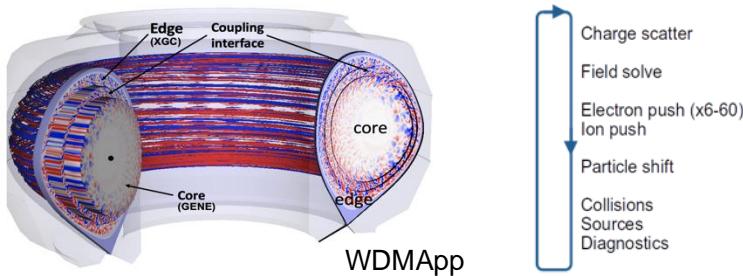
PDF

Isha Aggarwal ; Aditya Kashi ; Pratik Nayak ; Cody J. Balos ; Carol S. Woodward ; Hartwig Anzt All Authors

Batched Functionality for the Collision Operator

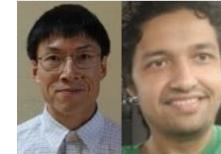
XGC is a gyrokinetic particle-in-cell code, which specializes in the simulation of the edge region of magnetically confined thermonuclear fusion plasma. The simulation domain can include the magnetic separatrix, magnetic axis and the biased material wall. XGC can run in total-delta-f, and conventional delta-f mode. The ion species are always gyrokinetic except for ETG simulation. Electrons can be adiabatic, massless fluid, driftkinetic, or gyrokinetic.

Source: https://xgc.pppl.gov/html/general_info.html

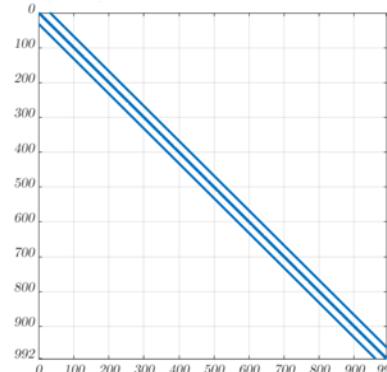


XGC collision operator: fully nonlinear multi-species Fokker-Planck-Landau
For each mesh vertex:

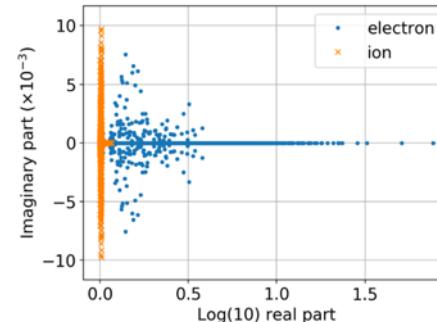
- Outer nonlinear solver: Picard method with inner linear solves
- Linear solve: discretize velocity space with approx 35x35 velocity grid
- direct solve on CPU using LAPACK banded solver **dgbsv**
- After GPU porting of XGC, this is the remaining CPU intensive kernel for collision operator



Paul Lin Dhruva Kulkarni

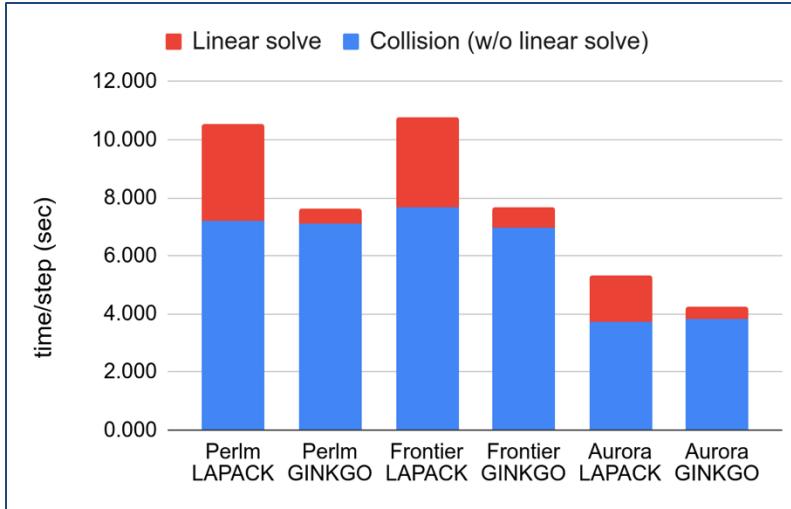


- Two species
- Ions easy to solve
- Electrons hard to solve
- Banded matrix structure
- Non-symmetric, need BiCGSTAB
- $n = \sim 1,000$
- $nz = \sim 9,000$



Batched Functionality for the Collision Operator

- XGC DIII-D National Fusion Facility tokamak electromagnetic (EM) test case
- 8 nodes of NERSC Perlmutter: 32 A100s, 1 MPI per GPU; single socket 64-core AMD EPYC
- 8 nodes OLCF Frontier: 32 MI250X, 64 GCDs, 1 MPI per GCD; single socket 64-core AMD EPYC
- 8 nodes ALCF Aurora: 48 Intel Data Center Max 1550, 96 tiles, 1 MPI per tile; dual socket 52-core Intel CPU Max 9470C SPR



Aditya Kashi, Pratik Nayak, Dhruva Kulkarni, Aaron Scheinberg, Paul Lin, and Hartwig Anzt. **Batched sparse iterative solvers on gpu for the collision operator for fusion plasma simulations**. In *2022 IEEE International Parallel and Distributed Processing Symposium (IPDPS)*, pages 157–167. IEEE, 2022.

Mathematical Formulation of the ExaSGD Core Challenge Security constrained multiperiod AC optimal power flow analysis

Posed as an optimization problem:

Find

$$\min_{x_t, y_{tsk}} (\sum_t F_t(x_t) + \sum_{tsk} G_{tsk}(x_t + y_{tsk}))$$

generator fuel cost

wind curtailment,
load shedding,
power imbalance, etc.

flow definitions,
power balance

bounds: generator power,
voltage, branch flow

generator ramping limit

Subject to:

$$H_{tsk}(x_t, y_{tsk}) = 0$$

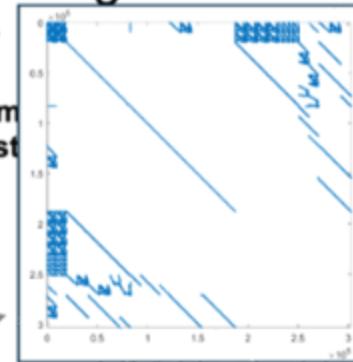
$$Q_{tsk}(x_t, y_{tsk}) \leq 0$$

$$R_t(x_t, x_{t+1}) \leq 0$$



The optimization problem
the underlying linear system

$$\left[\begin{array}{c|ccccc|c|c} K_1 & & & & & & & \\ K_2 & & & & & & & \\ K_3 & & & & & & & \\ \hline & \cdots & & \cdots & & \cdots & & \cdots \\ B_1^T & B_2^T & B_3^T & \cdots & B_N^T & K_0 & | & x \\ & & & & & & | & r_0 \end{array} \right]$$



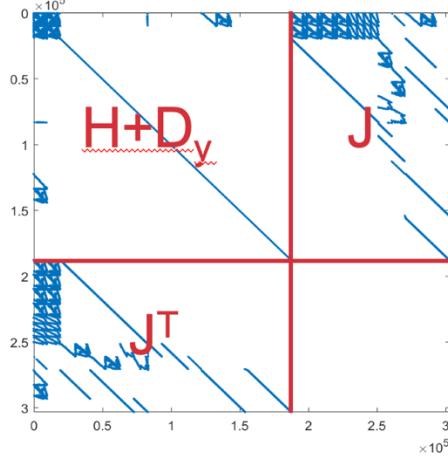
EXASGD



© Slaven Peles

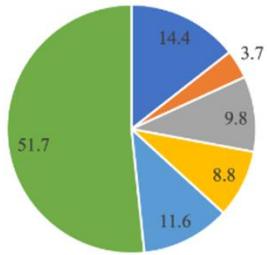
- The characteristic block-arrow coupling structure can be exploited to decompose the optimization problem, nevertheless there is no solver that can tackle this on a GPU-based architecture.

Sparse Direct Solvers

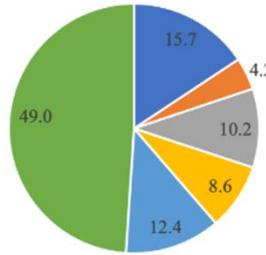


Grid	Buses	Generators	Lines	$N(K_k)$	$\text{nnz}(K_k)$
Northeastern US	25 K	4.8 K	32.3 K	108 K	1.19 M
Eastern US	70 K	10.4 K	88.2 K	296 K	3.20 M
Western and Eastern US	82 K	13.4 K	104.1 K	340 K	3.73 M

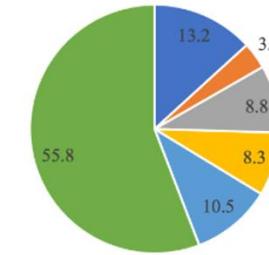
■ Hessian ■ Constraints ■ Constraint Jacobian ■ Other ■ Solve ■ Factorize



(a) Northeast U.S. grid



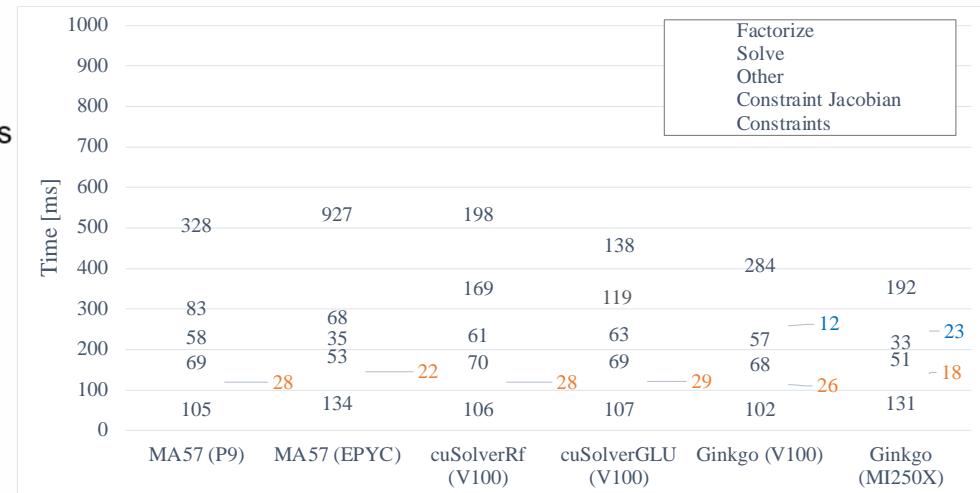
(b) Eastern U.S. grid



(c) Eastern and Western U.S. grids

Liner Solver Performance within Optimization Algorithm Average per iteration times (including first iteration on CPU)

- Each GPU solution outperforms all CPU baselines.
- Ginkgo performance improves on a better GPU.
- Iterative refinement configuration affects linear solver performance and optimization solver convergence.
- Ginkgo is the first GPU-resident sparse direct linear solver.



Multiple promising GPU-resident sparse linear solvers

29

After 6 years of development

Library core contains architecture-agnostic functionality

CORE
Infrastructure
Algorithms

- Iterative Solvers
- Preconditioners
- ...

Runtime polymorphism selects the right kernel depending on the target architecture



Unit tests check correctness



	FUNCTIONALITY	OMP	CUDA	HIP	DPC++
Basic	SpMV	✓	✓	✓	✓
	SpMM	✓	✓	✓	✓
	SpGeMM	✓	✓	✓	✓
	BICG	✓	✓	✓	✓
	BICGSTAB	✓	✓	✓	✓
	CG	✓	✓	✓	✓
	CGS	✓	✓	✓	✓
	GCR	✓	✓	✓	✓
	GMRES	✓	✓	✓	✓
	FCG	✓	✓	✓	✓
	FGMRES	✓	✓	✓	✓
	IR	✓	✓	✓	✓
	IDR	✓	✓	✓	✓
	Block-Jacobi	✓	✓	✓	✓
	ILU/IC	✓	✓	✓	✓
	Parallel ILU/IC	✓	✓	✓	✓
	Parallel ILUT/ICT	✓	✓	✓	✓
	ISAI	✓	✓	✓	✓
Batched	Batched BICGSTAB	✓	✓	✓	✓
	Batched CG	✓	✓	✓	✓
	Batched GMRES	✓	✓	✓	✓
	Batched ILU	✓	✓	✓	✓
	Batched ISAI	✓	✓	✓	✓
	Batched Block-Jacobi	✓	✓	✓	✓
AMG	AMG preconditioner	✓	✓	✓	✓
	AMG solver	✓	✓	✓	✓
	Parallel Graph Match	✓	✓	✓	✓
	Symbolic Cholesky	✓	✓	✓	✓
	Numeric Cholesky	✓	✓	✓	✓
	Symbolic LU	✓	✓	✓	✓
	Numeric LU	✓	✓	✓	✓
	Sparse TRSV	✓	✓	✓	✓
Sparse direct	On-Device Matrix Assembly	✓	✓	✓	✓
	MC64/RCM reordering	✓			
	Wrapping user data	✓	✓	✓	✓
	Logging	✓	✓	✓	✓
	PAPI counters	✓	✓	✓	✓

✓ MPI Support

✓ Single-GPU Support

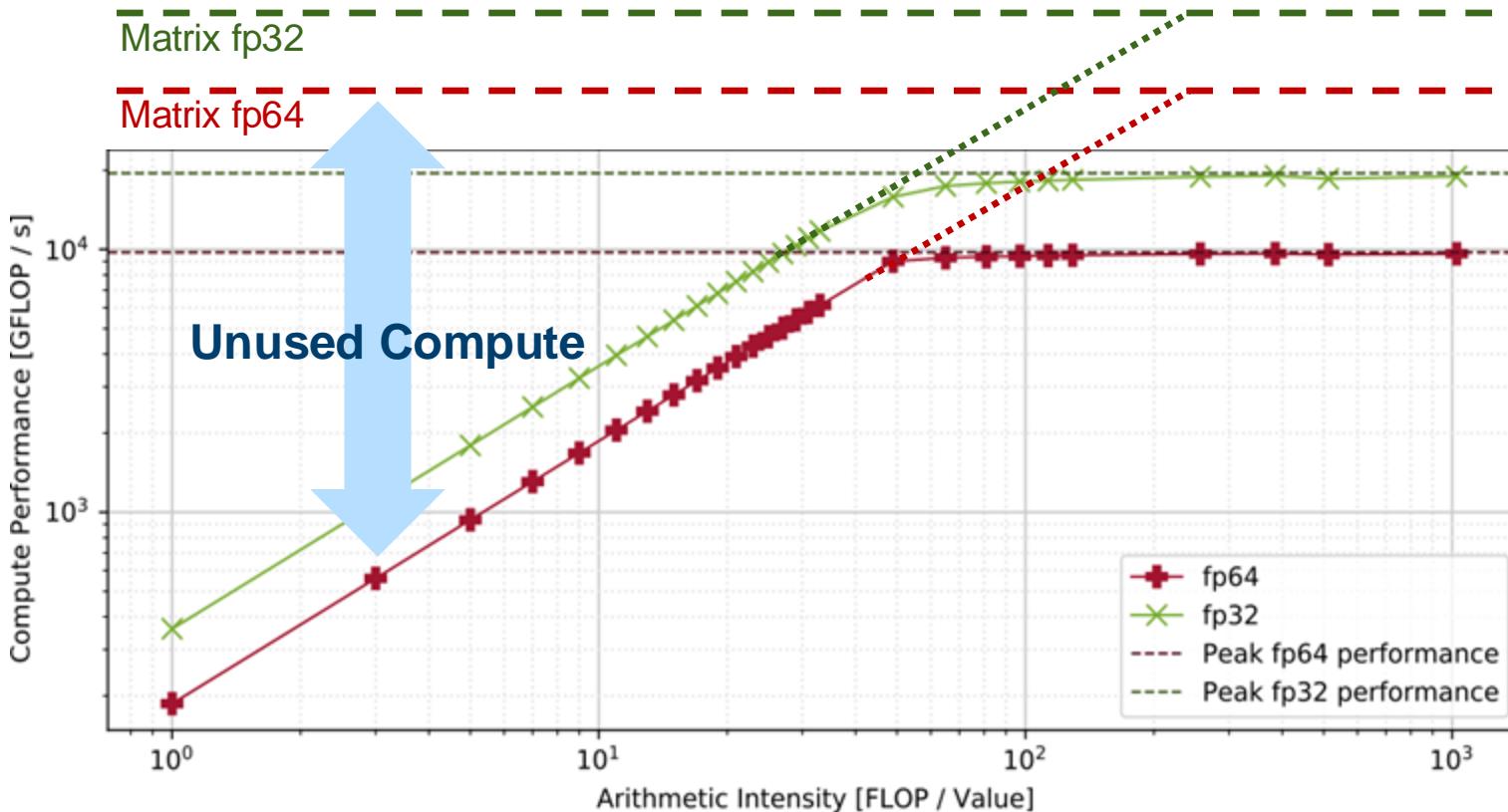
Lessons learnt

- ECP earmarking roughly half the budget to Software & App development is a game changer.
 - Central component for the success of ECP.
 - This concept needs to – and does become - the blueprint for other nations, companies, and projects.
- Workforce recruitment and workforce retention are the key to success in software development.
 - Money does not write software. RSEs do. We need to create attractive career plans.
 - We need to make research software development attractive to students. Academic recognition. Industry career paths.
- Anticipating the future in hardware development accelerates the porting process.
 - Blueprints and early access systems both useful.
 - Interaction with industry is mutually beneficial.
- Strategic initiatives, interaction and collegial behavior are important.
 - Strategic focus groups, conferences, and meetings bring experts together and create collaboration.
 - Listen to the application needs. Value input and acknowledge collaborators.

Lessons learnt

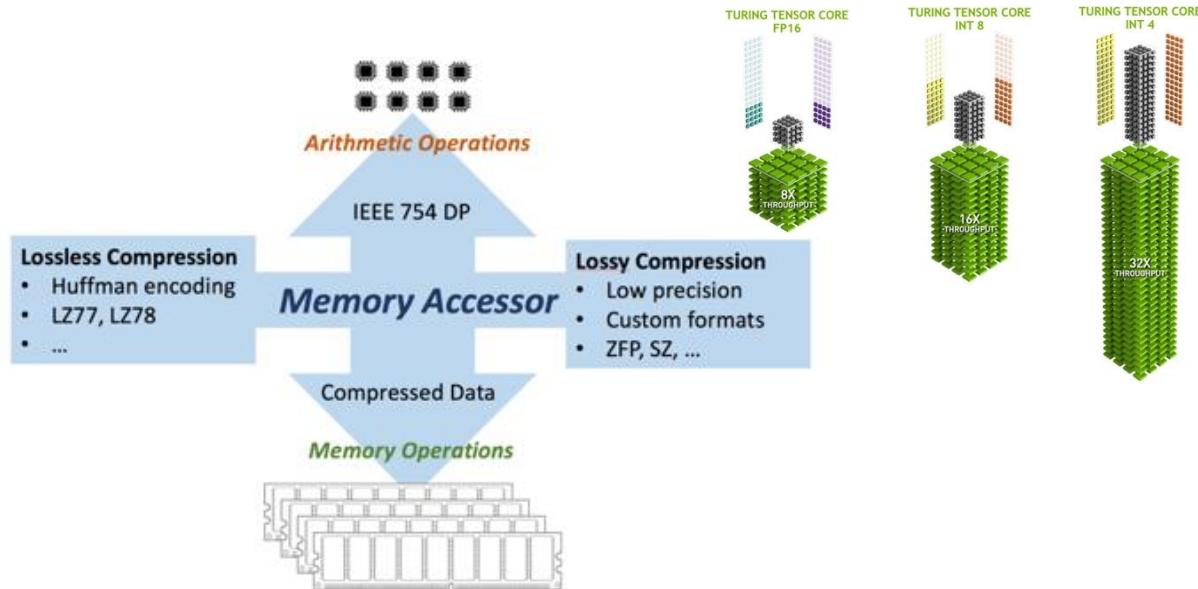
- **AI is dominating the hardware market.**
 - **Low precision will become the major format supported by hardware** (16 bit? 8bit?).
 - We need likely have to **emulate higher precision** if we require it in applications.
- **Bandwidth and Latency can not keep up with growth in compute power.**
 - **We need use compression on all levels** – likely hierarchically combined.
 - Optimizations need to focus on replacing communication with repetitive computation.
- **Resilience has become more a “secret discussion” than a showstopper.**
 - We know that MTF rates are in the hours for some machines.
 - Often, the topic is silenced for political reason.
- **AI is here to stay.**
 - **AI is an alternative to classical simulations and can enhance classical simulations.**
 - Like classical simulations, AI needs highly optimized matrix and vector operations, communication, and algorithms.

Activities going forward: There's plenty of room at the Top



Activities going forward

Using the Tensor cores for better in-register compression



Activities going forward

Sparse BLAS working group

- On the path to defining a standard for sparse BLAS operations

Interface for Sparse Linear Algebra Operations

September 19, 2024

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1st Sparse BLAS workshop, 2023



2nd Sparse BLAS workshop, 2024

Intel, NVIDIA, AMD, IBM, EVIDEN, Arm, MathWorks, LLNL, LBNL, SNL, MIT, UC Berkeley, UTK, KIT, TUM

Working Toward an Interface for Sparse BLAS

Description: While sparse matrix computations are at the heart of many scientific and engineering applications, there exists no widely adopted interface standard. A reason for this may be the plethora of optimization options relevant to today's accelerator architectures. At the same time, many vendors already provide support for sparse matrix computations in proprietary libraries, but due to diverging architectural constraints, these libraries have different execution models, APIs, and formats supported. We started a cross-institutional effort involving academia and industry to define an API for sparse linear algebra operations. In the BoF, we present a blueprint and discuss considerations motivating design choices.

Event Type: Birds of a Feather

[+ Add to Schedule](#)

Time:
Thursday, 21 November 2024
12:15pm - 1:15pm EST

Location: B207

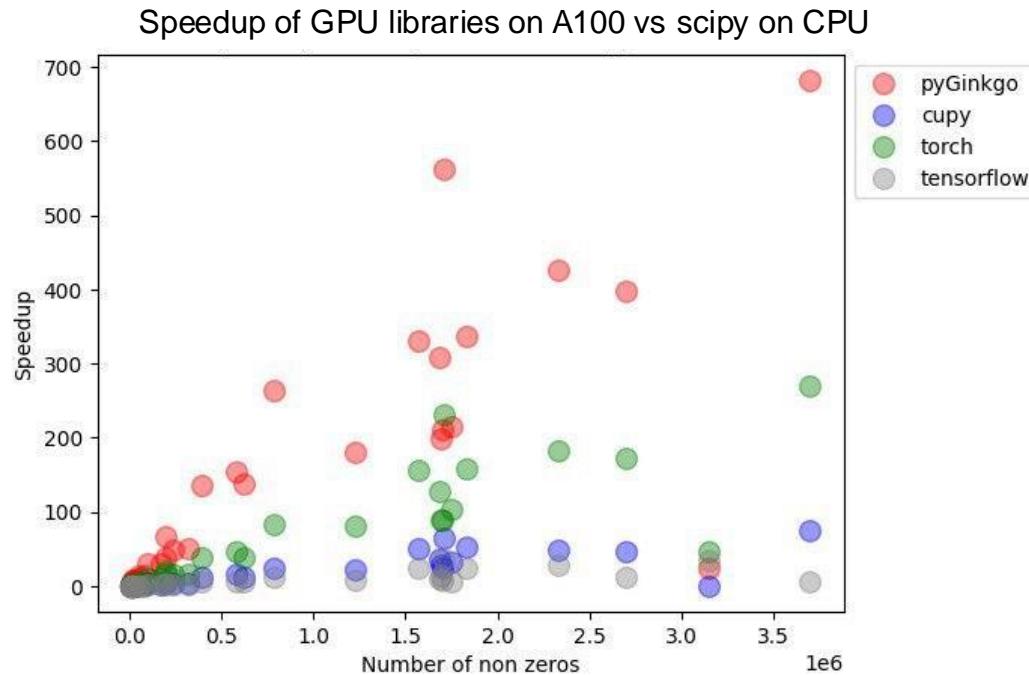
Registration Categories:

TP XOXIX

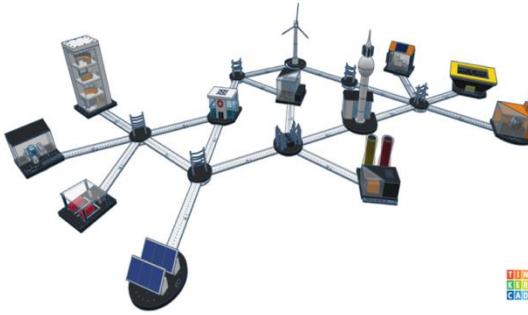
Links:
[Website](#)

Activities going forward

Linear algebra functionality for AI software stacks

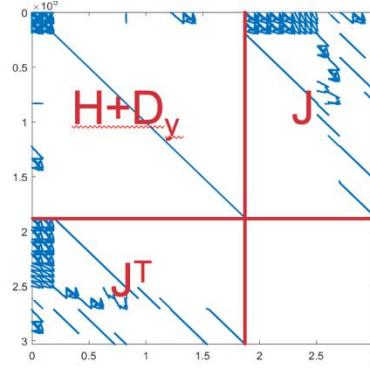


Activities going forward

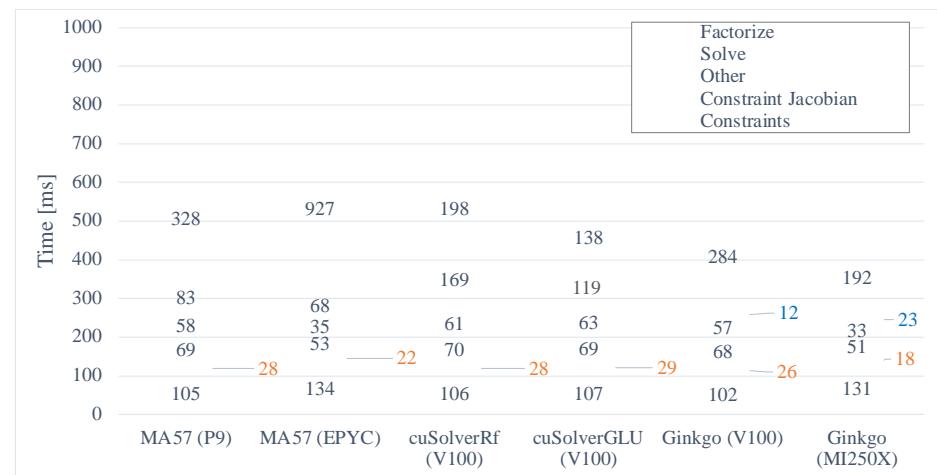
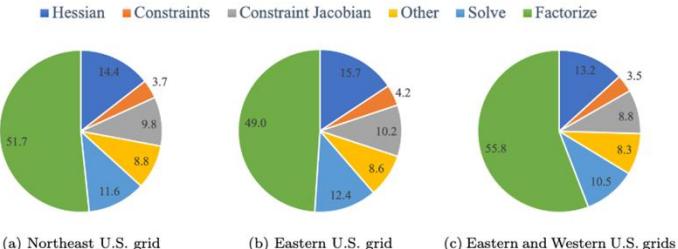


$$\begin{bmatrix} K_k \\ H + D_y & J \\ J^T & 0 \end{bmatrix} \begin{bmatrix} \Delta x_k \\ \Delta y \\ \Delta \lambda \end{bmatrix} = \begin{bmatrix} r_k \\ r_y \\ r_\lambda \end{bmatrix},$$

- J – sparse constraints Jacobian,
- H – sparse Hessian,
- D_y – arises from log-barrier function

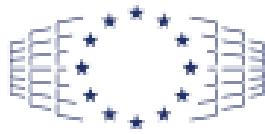
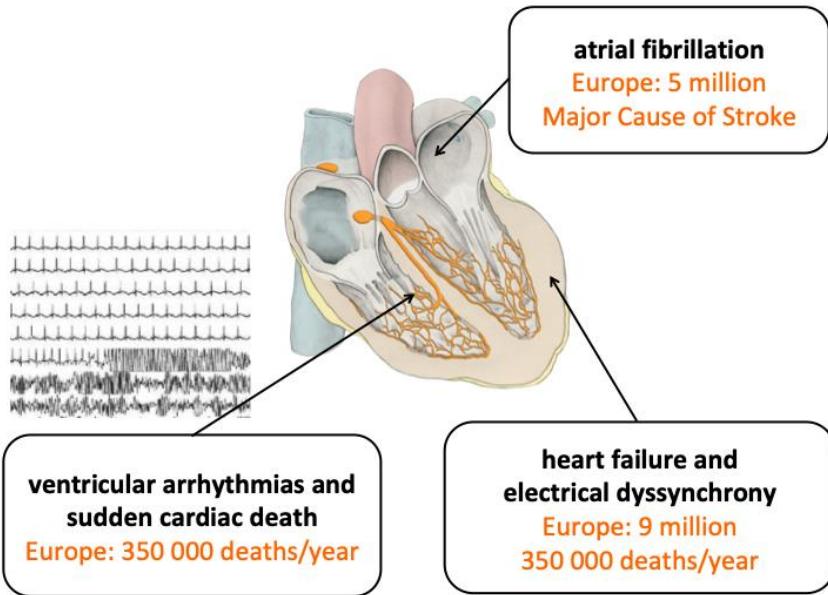


Grid	Buses	Generators	Lines	$N(K_k)$	nnz(K_k)
Northeastern US	25 K	4.8 K	32.3 K	108 K	1.19 M
Eastern US	70 K	10.4 K	88.2 K	296 K	3.20 M
Western and Eastern US	82 K	13.4 K	104.1 K	340 K	3.73 M



Activities going forward

- Cardiac disease is the #1 cause of death in Europe and half of these deaths are caused by electrical malfunctions.
- Structural muscle damage is crucial in most of these.



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