

Accelerating Fusion Plasma Collision Operator Solves with Portable, Batched Iterative Solvers on GPUs

How to make Research Software Faster Better Harder Stronger - Lessons learnt from the US Exascale Computing Project

Hartwig Anzt



The US Exascale Computing Project



Advancing Scientific Discovery

The ECP aims to ensure availability of the exascale computing ecosystem necessary for developing clean energy systems, improving the resilience of our infrastructure, designing new materials that can perform in extreme environments, adapting to changes in the water cycle, developing smaller and more powerful accelerators for use in medicine and industry, and much more. Several projects focus on data-intensive problems to enable effective use of the data streams from powerful scientific facilities, complex environmental genomes, and cancer research (patient genetics, tumor genomes, molecular simulations, and clinical data).



Strengthening National Security

The ECP teams are also developing new applications for supporting the NNSA Stockpile Stewardship Program, which is responsible for maintaining the readiness and reliability of our nuclear weapons systems—without underground testing. Assessing the performance of weapons systems subject to hostile environments and potential threat scenarios exceeds the capabilities of current HPC systems and codes. NNSA application projects are focused on providing the sophisticated modeling and analysis tools needed to sustain the U.S. nuclear deterrence.



Improving Industrial Competitiveness

Exascale systems will be used to accelerate research that leads to innovative products and speeds commercialization, creating jobs and driving US competitiveness across industrial sectors, such as the emerging energy economy. To ensure alignment with US industry needs, the ECP is engaging senior technology decision makers from among the country's most prominent private sector companies.

The US Exascale Computing Project

Addressing a National Imperative

The Exascale Computing Project is an aggressive research, development, and deployment project focused on delivery of mission-critical applications, an integrated software stack, and exascale hardware technology advances.

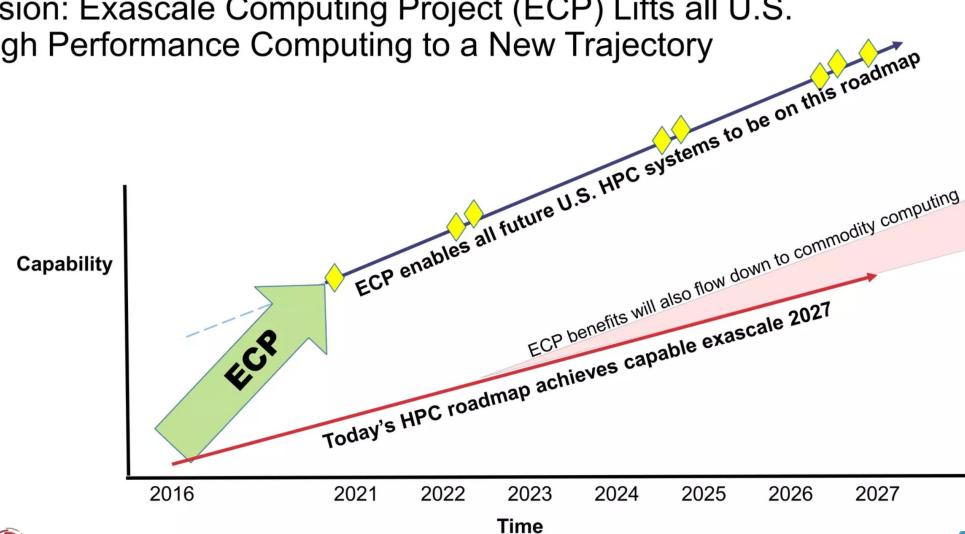
Application Development 

Software Technology 

Hardware & Integration 

© Paul Messina in 2016

Vision: Exascale Computing Project (ECP) Lifts all U.S. High Performance Computing to a New Trajectory



The US Exascale Computing Project

- 3 computers. (~2B)
 - \$600M each
 - \$400M to vendors for Design, Path, Fast - Forward
 - Application and Software Development(~2B)



Rank	System	Cores	Rmax [PFlop/s]	Rpeak [PFlop/s]	Power (kW)
1	Frontier - HPE Cray EX235a, AMD Optimized 3rd Generation EPYC 64C 2GHz, AMD Instinct MI250X, Slingshot-11, HPE DOE/SC/Oak Ridge National Laboratory United States	8,699,904	1,206.00	1,714.81	22,786
2	Aurora - HPE Cray EX - Intel Exascale Compute Blade, Xeon CPU Max 9470 82C 2.4GHz, Intel Data Center GPU Max, Slingshot-11, Intel DOE/SC/Argonne National Laboratory United States	9,264,128	1,012.00	1,980.01	38,698
3	Eagle - Microsoft NDv5, Xeon Platinum 8480C 48C 2GHz, NVIDIA H100, NVIDIA Infiniband NDR, Microsoft Azure Microsoft Azure United States	2,073,600	561.20	846.84	
4	Supercomputer Fugaku - Supercomputer Fugaku, A64FX 48C 2.2GHz, Tofu interconnect D. Fujitsu RIKEN Center for Computational Science Japan	7,630,848	442.01	537.21	29,899
5	LUMI - HPE Cray EX235a, AMD Optimized 3rd Generation EPYC 64C 2GHz, AMD Instinct MI250X, Slingshot-11, HPE EuroHPC/CSC Finland	2,752,704	379.70	531.51	7,107
6	Alps - HPE Cray EX254n, NVIDIA Grace 72C 3.1GHz, NVIDIA GH200 Superchip, Slingshot-11, HPE Swiss National Supercomputing Centre (CSCS) Switzerland	1,305,600	270.00	353.75	5,199

The US Exascale Computing Project



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LatticeQCD	NWChemEx	GAMESS	ExaStar	ExaSky	EQSIM
Validate Fundamental Laws of Nature Objective: Validate Fundamental Laws	Tackling Chemical, Materials, and Biomolecular Challenges in Exascale	General Atomic and Molecular Electronic Structure System	Exascale Models of Stellar Explosions Objective: Demystify Origin of Chemical Elements	Computing at the Extreme Scales Objective: Cosmological Probe of the Standard Model of Particle Physics	High-Performance, Multidisciplinary Simulations for Regional-Scale Earthquake Hazard/Risk Assessments
EXAALT	ExaAM	QMCPACK	WDMApp	ExaSMR	WarpX
Molecular Dynamics at Exascale Objective: Tackling Chemical, Materials, and Biomolecular Challenges in Exascale	Transforming Additive Manufacturing through Exascale Simulation	Quantum Mechanics at Exascale	High-fidelity Whole Device Modelling of Magnetically Confined Fusion Plasmas	Coupled Monte Carlo Neutrinos and Fluid Flow Simulation of Small Modular Reactors	Exascale Modeling of Advanced Particle Accelerators
ExaSGD	CANDLE	ExaBiome	ExaWind	Combustion-PELE	MFIX-Exa
Optimizing Stochastic Grid Dynamics at Exascale Objective: Optimizing Stochastic Grid Dynamics at Exascale	Exascale Deep Learning-Enabled Precision Medicine for Cancer	Exascale Solutions for Microbiome Analysis	Exascale Predictive Wind Plant Flow Physics Modeling	High-efficiency, Low-emission Combustion Engine Design	Performance Prediction of Multiphase Energy Conversion Device
Ristra	MAPP	EMPIRE and SPARC	Subsurface	ExaMMF	ExaFEL
Multi-physics simulation tools for weapons-relevant applications	Multi-physics simulation tools for High Energy Density Physics (HEDP) and weapons-relevant applications for DOE and DOD	EMPIRE addresses electromagnetic plasma physics, and SPARC addresses reentry aerodynamics	Exascale Subsurface Simulator of Coupled Flow, Transport, Reactions, and Mechanics	Cloud-Resolving Climate Modeling of the Earth's Water Cycle	Data Analytics at Exascale for Free Electron Lasers
			Adaptive Mesh Refinement	Efficient Exascale Discretizations	Online Data Analysis and Reduction at the Exascale
			Particle-Based Applications	Efficient Implementation of Key Graph Algorithms	Exascale Machine Learning Technologies

Sustainable software development

PMR Core (17)	Compilers and Support (7)	Tools and Technology (11)	xSDK (16)	Visualization Analysis and Reduction (9)	Data mgmt, I/O Services, Checkpoint restart (12)	Ecosystem/E4S at-large (12)
QUO	openarc	TAU	hypre	ParaView	SCR	mpfileUtils
Papyrus	Kitsune	HPCToolkit	FleSci	Catalyst	FAODEL	TriBITS
SICM	LLVM	Dyninst Binary Tools	MFEML	VTK-m	ROMIO	MarFS
Legion	CHILL autotuning comp	Gotcha	Kokkoskernels	SZ	Mercury (Mochi suite)	GUFI
Kokkos (support)	LLVM openMP comp	Caliper	Trilinos	zip	HDF5	Intel GEOPM
RAJA	OpenMP V & V	PAPI	SUNDIALS	VisIt	Parallel netCDF	BEE
CHAI	Flang/LLVM Fortran comp	Program Database Toolkit	PETSc/TAO	ASCENT	ADIOS	FSEFI
PaRSEC*		Search (random forests)	libEnsemble	Cinema	Darshan	Kitten Lightweight Kernel
DARMA	Siboka	STRUMPACK	ROVER		UnityCR	COOLR
GASNet-EX		SuperLU			VeloC	NRM
Qthreads	C2C				IOSS	ArgoContainers
BOLT	Sonar	ForTrilinos			HXHM	Spack
UPC++		SLATE			PMR	
MPICH		MAGMA			Tools	
Open MPI		DTK			Math Libraries	
Umpire		Tasmanian			Data and Vis	
AML		Ginkgo			Ecosystems and delivery	

Legend:

- PMR
- Tools
- Math Libraries
- Data and Vis
- Ecosystems and delivery

A few words about myself

- Born and raised in Karlsruhe
- PhD in Numerical Mathematics from KIT
- Focus on computational linear algebra and high performance computing (HPC)
- Linear solvers, preconditioners, ...
- During my PostDoc at the University of Tennessee, I developed MAGMA sparse



MAGMA-sparse as a “child” of MAGMA explores the development of sparse linear algebra functionality for NVIDIA GPUs.



Limitations:

- *C code with hand-written build system*
- *Sparse unit testing*
- *Focus on NVIDIA GPUs*
- *Design-specific limitations (flexibility/extensibility)*

Learn from your peers...



Building Trusted Scientific Software



PUBLISHED JUN 28, 2018 AUTHOR MIKE HER

Software Verification



PUBLISHED AUG 15, 2018 AUTHOR ANSHU I

Think Locally, Act Globally: Outreach for Better Scientific Software



I have worked in the scientific software field for more! phrase "Verification is doing things right, and validation phrase to memory in order to avoid confusion when the

Pairing internal and external concerns
Verification focuses on internal concerns of a good sol

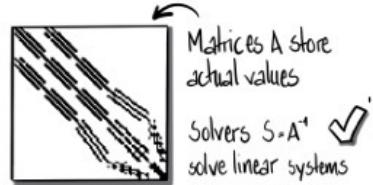
In the realm of software, verification is often erroneo proper subset of verification for gaining confidence in the holistic process by which the developers convinc it was designed to do. In scientific software this coul numerical stability, and efficacy of the method in the expected results. Note that verification is limited to e model specification, not that the model itself matche validation process.

An ambitious goal
The ECP needs to deliver a software environment and applications ready to run on exascale computers, which are scheduled to be deployed starting in 2021. Achieving this goal entails a major, large-scale software development effort. Recognizing the challenges development teams will face, the ECP is supporting the IDEAS Productivity project to help scientific researchers improve their development practices.

PUBLISHED JUL 17, 2018 AUTHOR DAVID BERNHOLDT TOPICS BETTER SKILLS PERSONAL PRODUCTIVITY AND SUSTAINABILITY

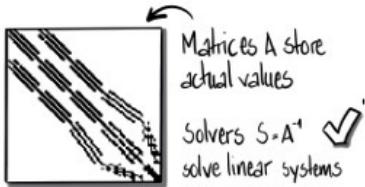
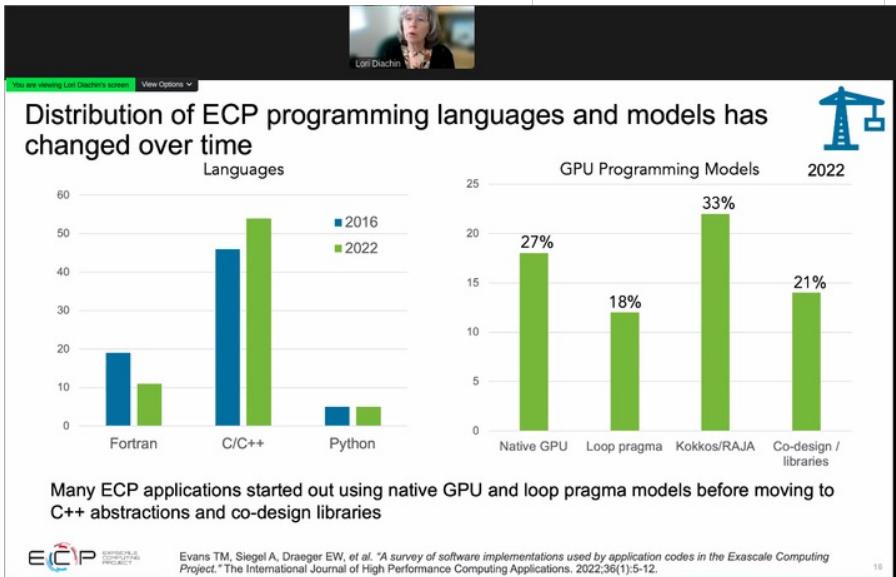
Designing a math toolset for ECP applications

Ginkgo - A sparse linear algebra library for HPC



Designing a math toolset for ECP applications

written in C++ → Ginkgo - A sparse linear algebra library for HPC



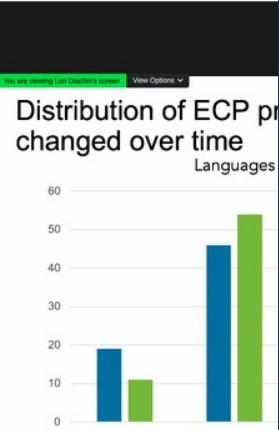
Solvers $S = A^{-1}$ ✓
solve linear systems

Designing a math toolset for ECP applications

written in C++ → Ginkgo - A sparse linear algebra library for HPC

BACK TO THE BUILDING BLOCKS:

A PATH TOWARD SECURE AND MEASURABLE SOFTWARE



Many ECP applications start with FEBRUARY 2024
C++ abstractions and co-design libraries



Evans TM, Siegel A, Draeger EW, et al. "A survey of software implementations used by application Project." The International Journal of High Performance Computing Applications. 2022;36(1):5-12.



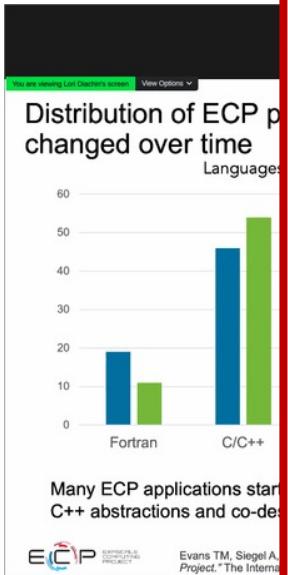
THE WHITE HOUSE
WASHINGTON

Memory safety vulnerabilities are a class of vulnerability affecting how memory can be accessed, written, allocated, or deallocated in unintended ways.ⁱⁱⁱ Experts have identified a few programming languages that both lack traits associated with memory safety and also have high proliferation across critical systems, such as C and C++.^{iv} Choosing to use memory safe programming languages at the outset, as recommended by the Cybersecurity and Infrastructure Security Agency's (CISA) Open-Source Software Security Roadmap is one example of developing software in a secure-by-design manner.^v

Designing a math toolset for ECP applications

written in C++ → Ginkgo - A sparse linear algebra library for HPC

Translating All C TO Rust (TRACTOR)



ACTIVE

Contract Opportunity

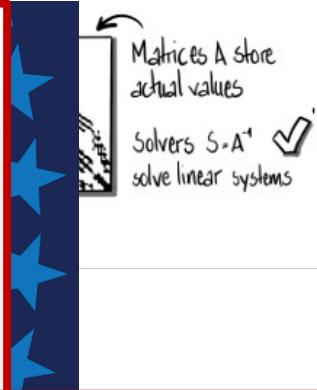
Notice ID
DARPA-SN-24-89

Related Notice

Department/Ind. Agency
DEPT OF DEFENSE

Sub-tier
DEFENSE ADVANCED RESEARCH PROJECTS AGENCY (DARPA)

Office
DEF ADVANCED RESEARCH PROJ



General Information

Contract Opportunity Type: Special Notice

All Dates/Times are: (UTC-04:00) EASTERN

Original Published Date: Jul 29, 2024 02:00:00

Original Response Date: Aug 19, 2024 11:59:59

Inactive Policy: Manual

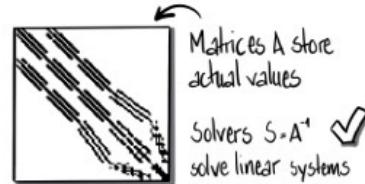
Original Inactive Date: Aug 27, 2024

Description

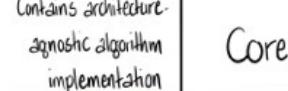
The TRACTOR program aims to achieve a high degree of automation towards translating legacy C to Rust, with the same quality and style that a skilled Rust developer would employ, thereby permanently eliminating the entire class of memory safety security vulnerabilities present in C programs. Performers might employ novel combinations of software analysis (e.g., static analysis and dynamic analysis), and machine learning techniques (e.g., large language models). The draft solicitation will be posted shortly.

Designing a math toolset for ECP applications

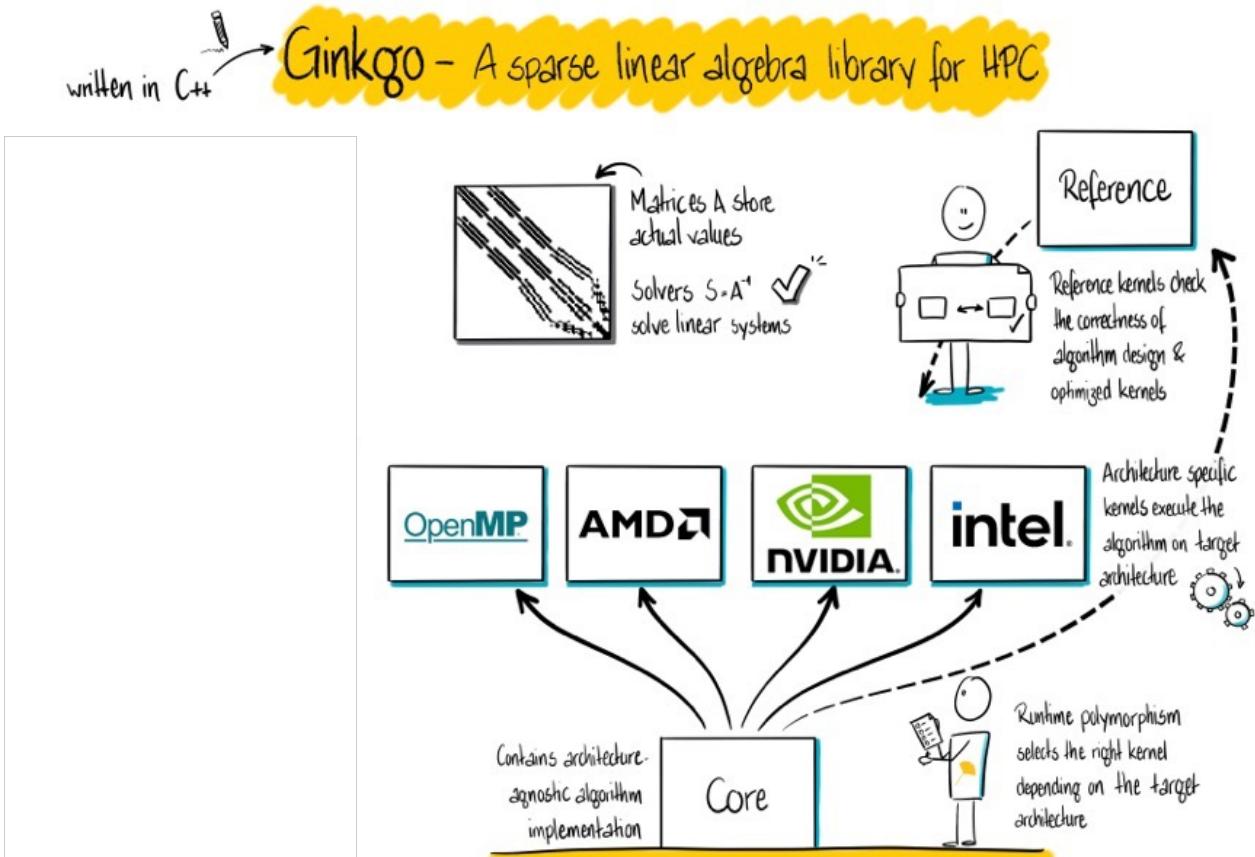
written in C++ → Ginkgo - A sparse linear algebra library for HPC



Contains architecture-agnostic algorithm implementation

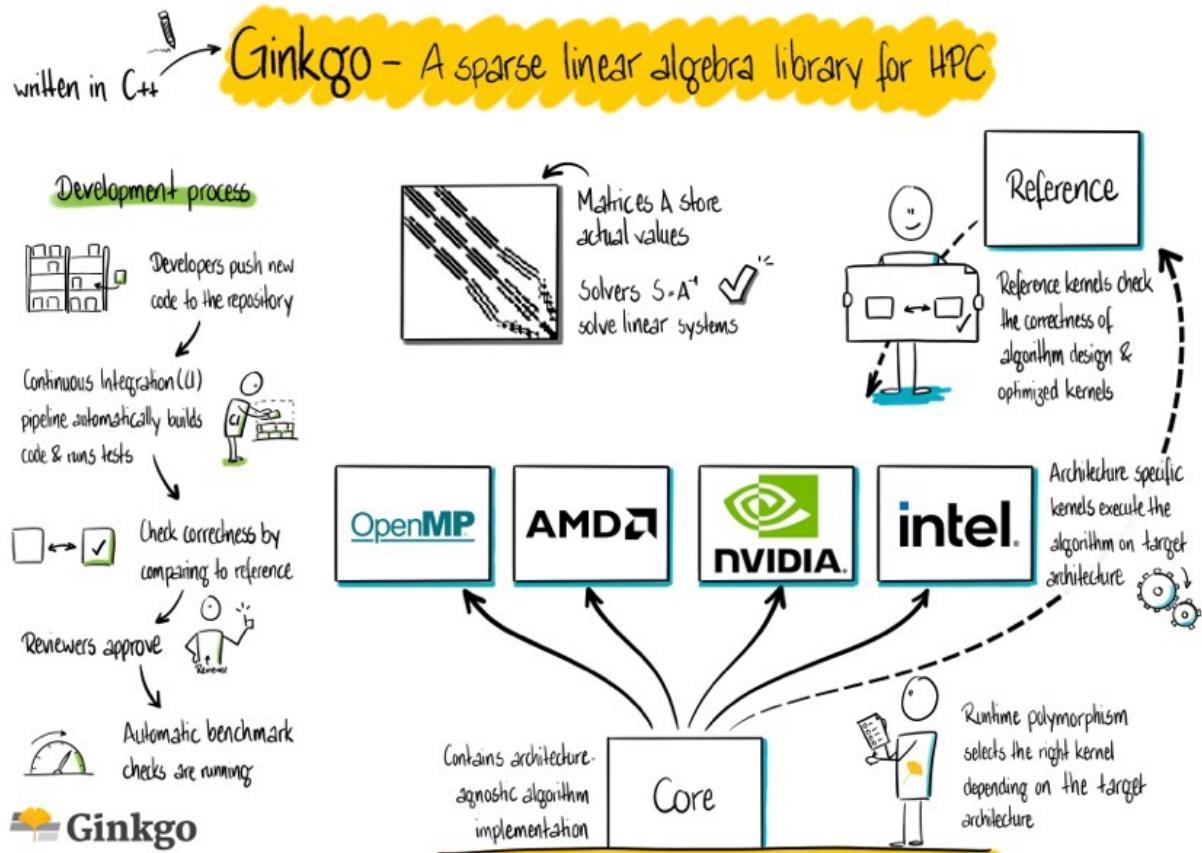


Designing a math toolset for ECP applications

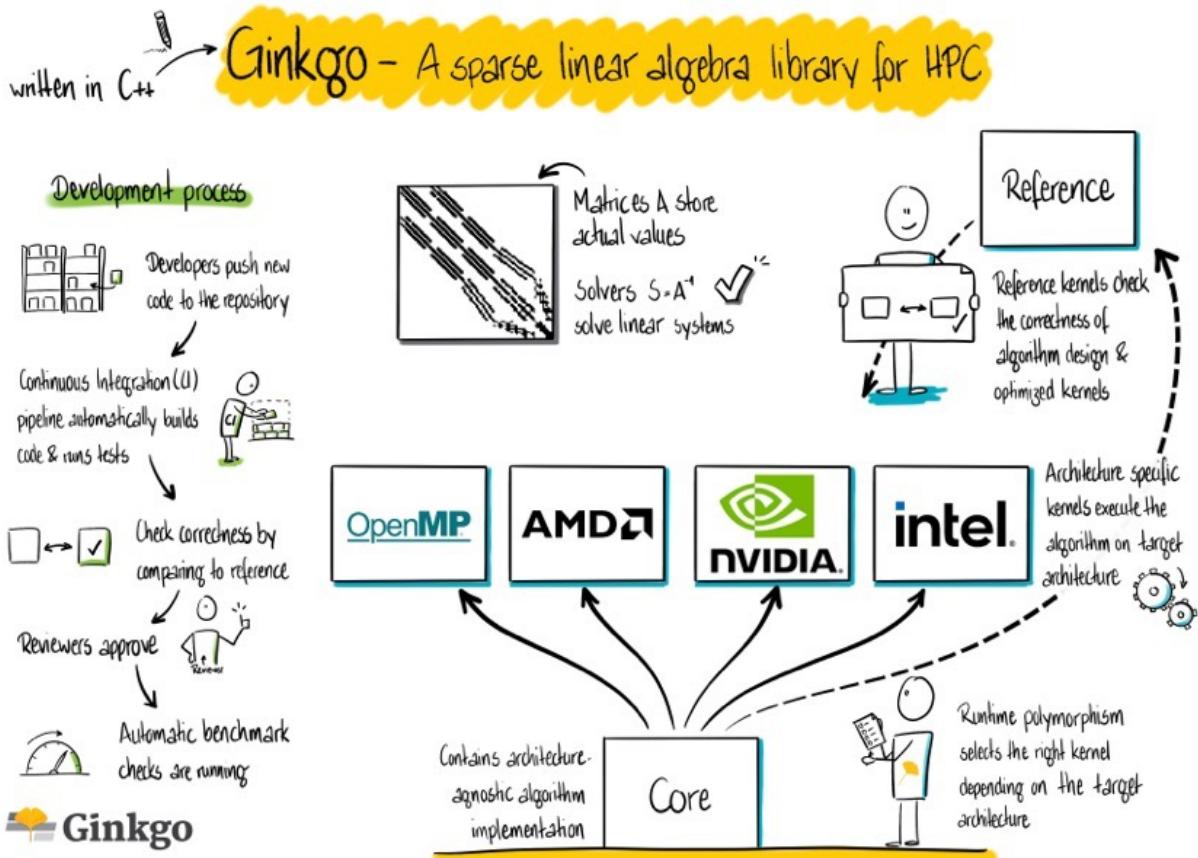
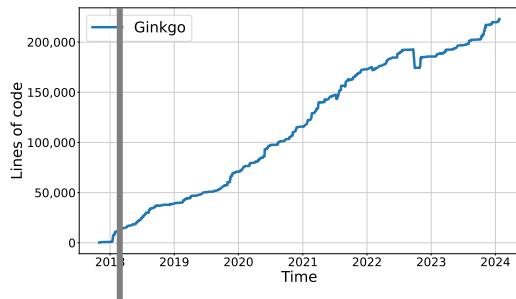


Designing a math toolset for ECP applications

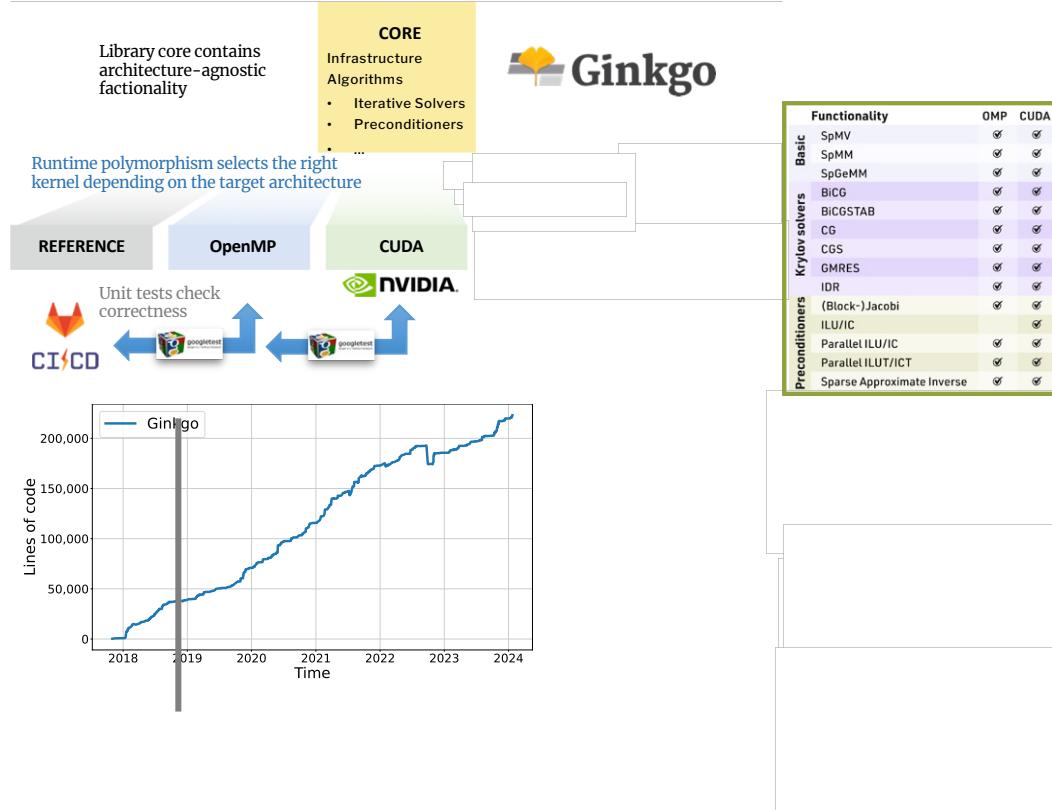
build	code_quality
● build/amd/nompi/clang/rocm45/deb...	● clang-tidy
● build/amd/nompi/clang/rocm45/rele...	● iwyu
● build/amd/nompi/clang/rocm514/rele...	● subdir-build
● build/amd/nompi/qcc/rocm45/relea...	● warnings
● build/amd/nompi/qcc/rocm514/debu...	
● build/amd/nompi/qcc/rocm514_w...	
● build/cuda10/mvapich2/qcc/cuda/re...	
● build/cuda10/nompi/clang/cuda/rele...	
● build/cuda10/nompi/clang/cuda/rel...	
● build/cuda11/nompi/qcc/cuda/debu...	
● build/cpx20231/lgpu/release/shared	
● build/cpx/lgpu/release/static	
● build/nocuda-nomixed/nompi/clang/...	
● build/nocuda-nomixed/nompi/clang/...	
● build/nocuda-nomixed/openmpi/qcc...	
● build/nocuda/nompi/clang/core/rele...	
● build/nocuda/nompi/qcc/core/debu...	
● build/nocuda/nompi/qcc/omp/relea...	
● build/nocuda/nompi/qcc/omp/relea...	
● build/nocuda/openmpi/clang/omp/d...	
● build/nocuda/openmpi/clang/omp/ql...	
● build/nvhpc227/cuda117/nompi/nvc...	
● build/nvhpc233/cuda120/nompi/nvc...	
● build/windows-cuda/release/shared	
● build/windows/release/shared	



Designing a math toolset for ECP applications



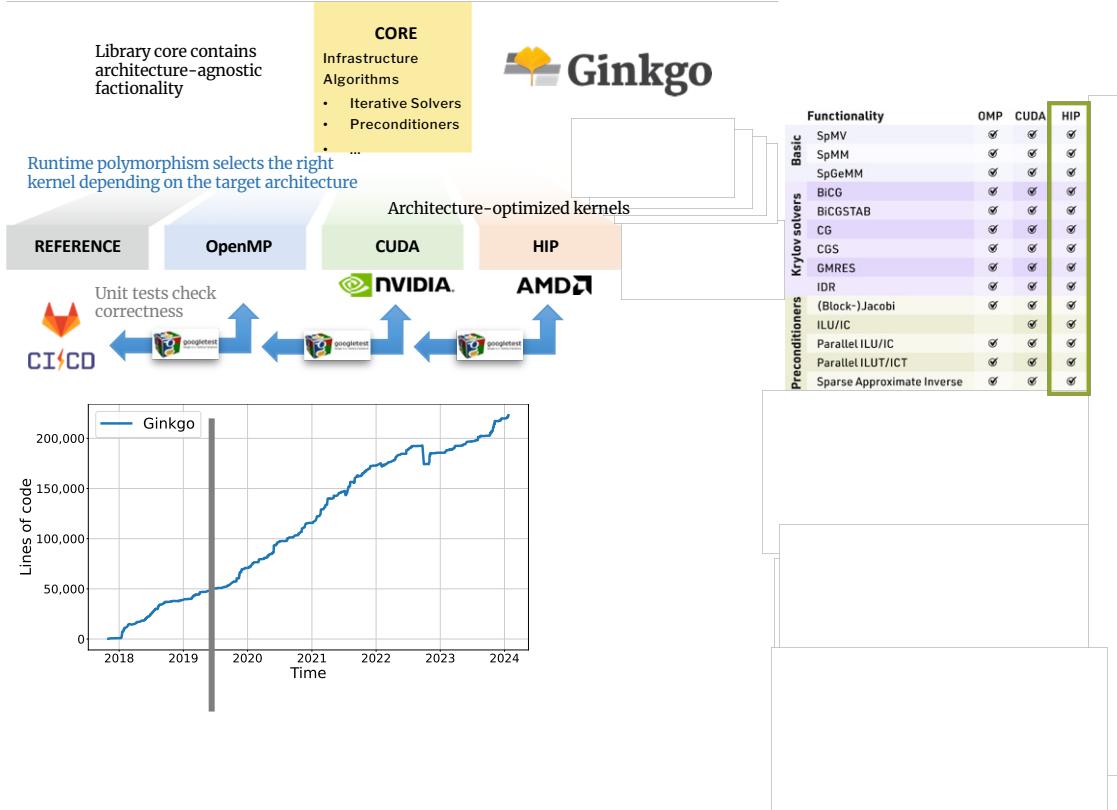
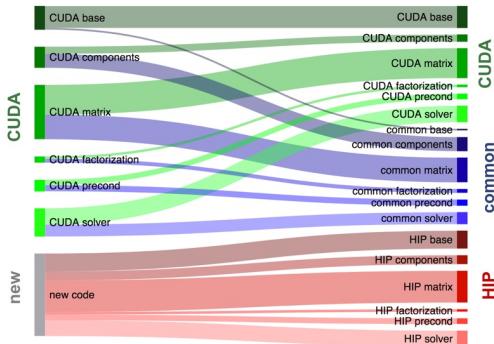
Starting with the CUDA backend



Extending to AMD GPUs

~2 months

The screenshot shows a blog post titled "Porting the Ginkgo Package to AMD's HIP Ecosystem". The post discusses the experience of porting CUDA code to AMD's Heterogeneous-compute Interface for Portability (HIP). It includes sections on CUDA base, CUDA components, CUDA matrix, CUDA factorization, CUDA preconditioner, CUDA solver, common base, common components, common matrix, common factorization, common preconditioner, common solver, HIP base, HIP components, new code, HIP matrix, HIP factorization, HIP preconditioner, and HIP solver. The post is published on June 25, 2020, by Hartwig Anzt.

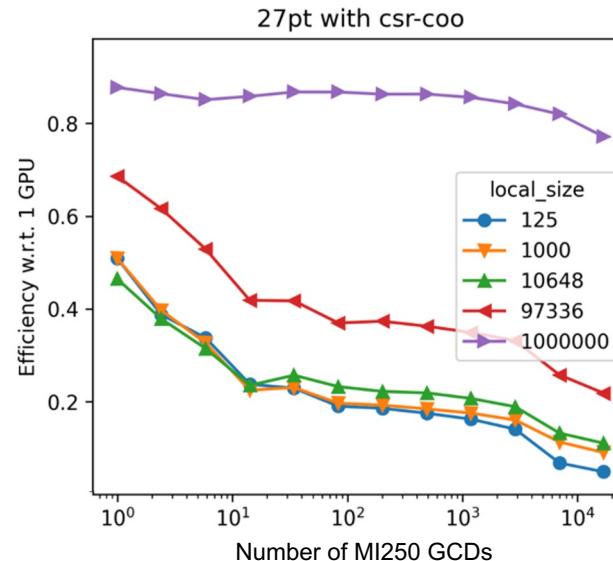
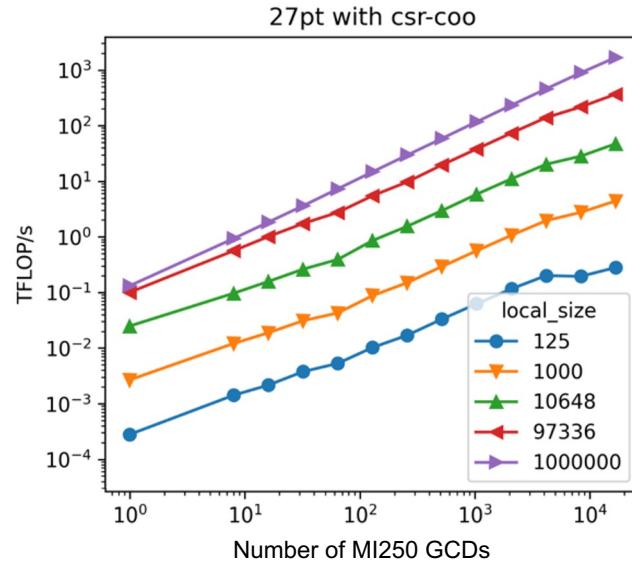


Weak and strong Scalability

Frontier (#1 TOP500)

SpMV Weak scaling: problem size increases with parallel resources

Weak scaling up to 8k AMD MI250 GPUs (16k GCDs)

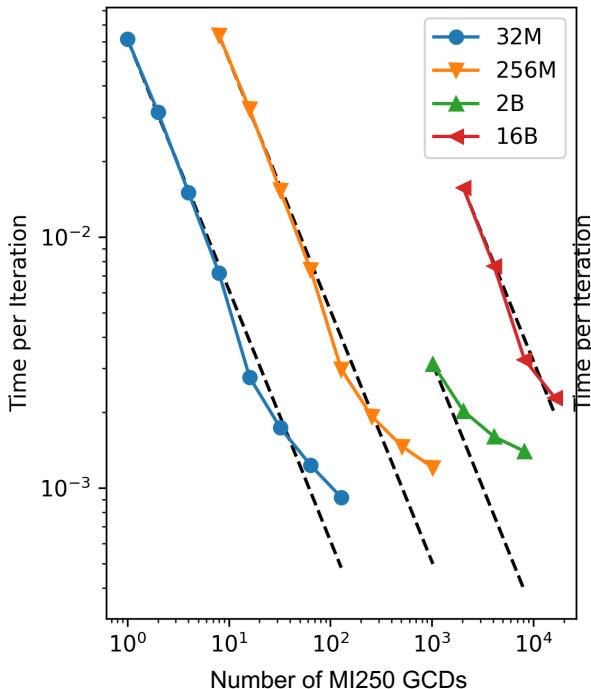


Weak and strong Scalability

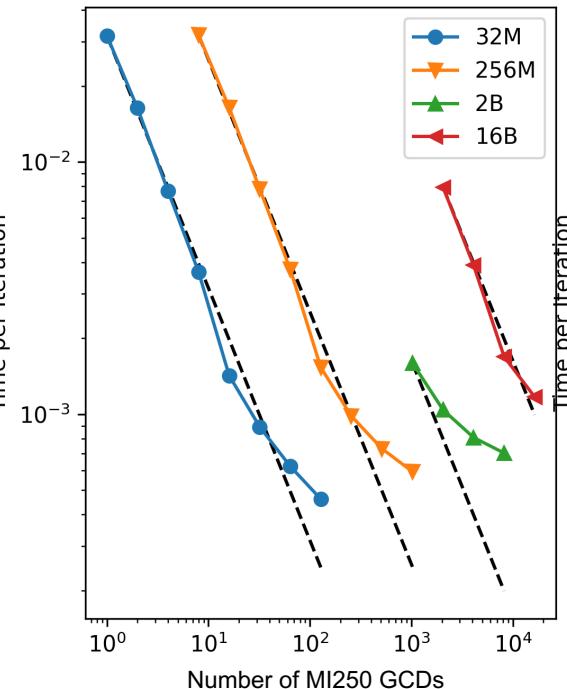
Strong scaling: problem size constant, parallel resources increase

Frontier (#1 TOP500)

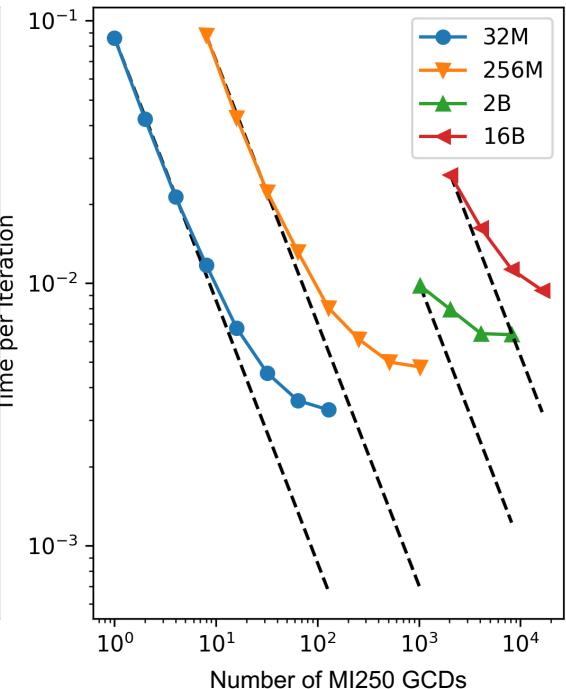
Strong Scaling - Bicgstab Local Jacobi



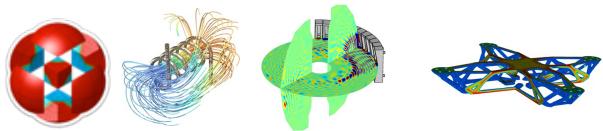
Strong Scaling - Cg Local Jacobi



Strong Scaling - Gmres Local Jacobi



We “forgot” the customer on the way...



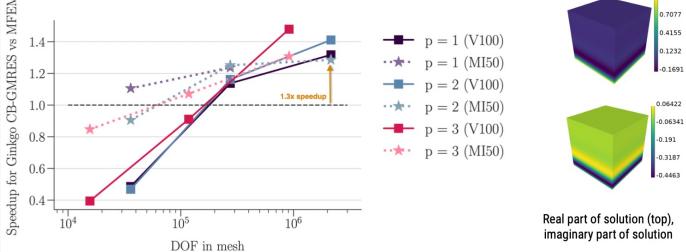
MFEM is a *free, lightweight, scalable C++ library* for finite element methods.

Speeding up MFEM’s “example 22” on GPUs

Example 22 of the MFEM finite element library solves harmonic oscillation problems, with a forced oscillation imposed at the boundary. In this test, we use variant 1:

$$-\nabla \cdot (a \nabla u) - \omega^2 bu + i\omega cu = 0$$

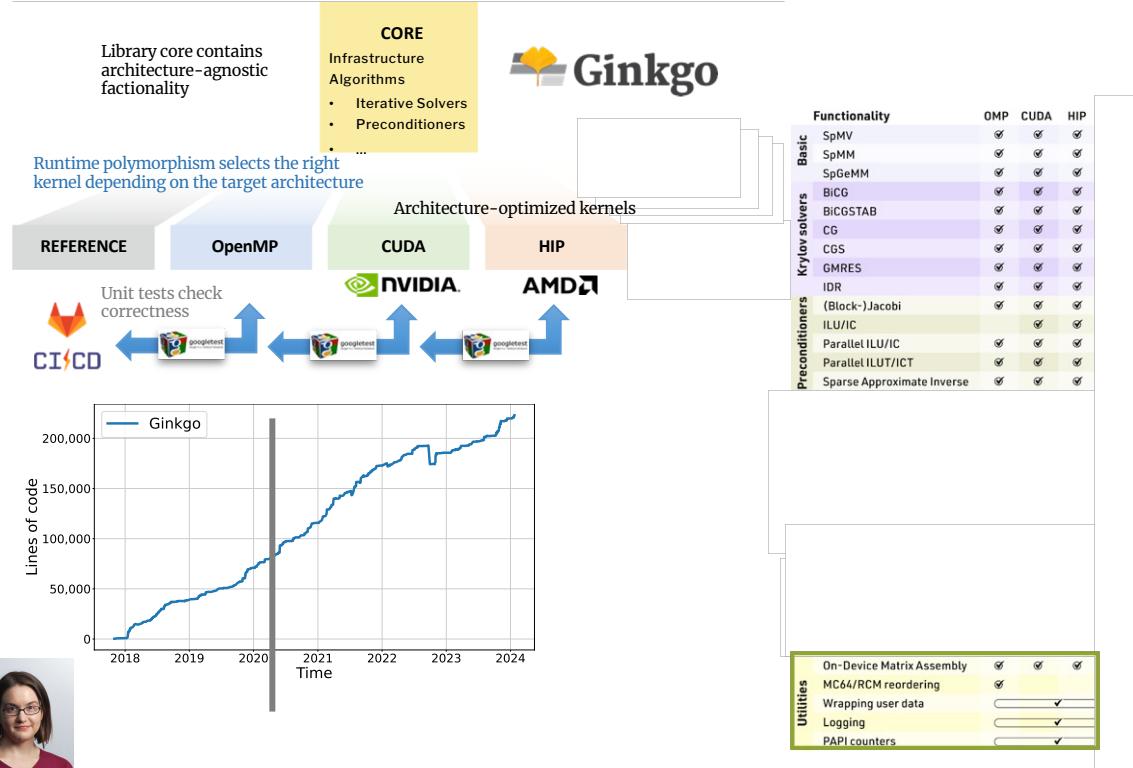
with $a = 1$, $b = 1$, $\omega = 10$, $c = 20$



Speedup of Ginkgo’s Compressed Basis-GMRES solver vs MFEM’s GMRES solver for three different orders of basis functions (p), using MFEM matrix-free operators and the Ginkgo-MFEM integration wrappers in MFEM. CUDA 10.1/V100 and ROCm 4.0/MI50.



Natalie Beams



Extending to Intel GPUs

~18 months



Since 1987 - Covering the Fastest Computers in the World and the People Who Run Them

- Home
- Technologies
- Sectors
- COVID-19
- AI/ML/DL



March 23, 2021

[yhmtsai / try_oneapi](https://github.com/yhmtsa1/try_oneapi) Private

Code Issues Pull requests Actions Projects Security Insights

1 master · 1 branch · 0 tags

Go to file Add file Code About

yhmtsai format update 69d2173 on Aug 7, 2022 70 commits

No description, website, or topics provided.

arg_struct WIP 2 years ago

atomic atomic and get_in_template 2 years ago

check_uninit some checker last year

classical_csr cpu barrier issue in classical csr spmv last year

clinfo clinfo 2 years ago

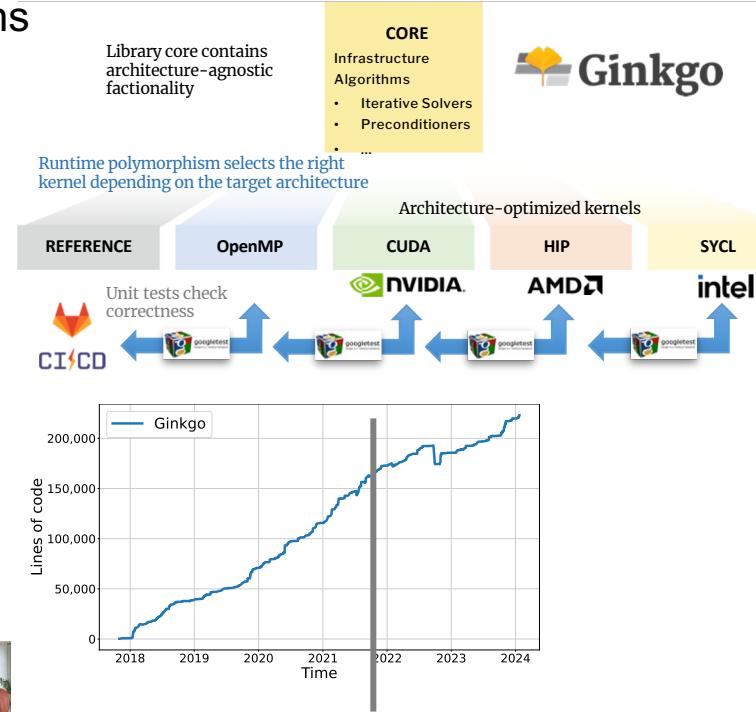
coop_cuda keep some history but I do not check them detail last year

coop_draft keep some history but I do not check them detail last year

Releases No releases published Create a new release



Mike Tsai



Functionality	OMP	CUDA	HIP	DPC++
SpMV	✓	✓	✓	✓
SpMM	✓	✓	✓	✓
SpGeMM	✓	✓	✓	✓
BICG	✓	✓	✓	✓
BICGSTAB	✓	✓	✓	✓
CG	✓	✓	✓	✓
CGS	✓	✓	✓	✓
GMRES	✓	✓	✓	✓
IDR	✓	✓	✓	✓
(Block-)Jacobi	✓	✓	✓	✓
ILU/IC		✓	✓	✓
Parallel ILU/IC	✓	✓	✓	✓
Parallel ILUT/ICT	✓	✓	✓	✓
Sparse Approximate Inverse	✓	✓	✓	✓

Basic

Krylov solvers

Utilities

Extending to Intel GPUs

- Bi-Weekly technical meetings with Intel
- Long list of bug reports, feature requests, performance data discussions, documentation improvements ...

cuBLAS backend (and potentially other domains) fails with latest LLVM builds #223

Summary

As first observed in #219 many tests in cuBLAS backend is failing with latest LLVM builds.

Version

I have tried LLVM commit: 66361038b63caee566fc9648fda50b7422b83 and got the below tests failing (showing only a few of them)

```

1 - BLAS/RT/NrmTestSuite/NrmTests.RealSinglePrecision/Column_Major_TITAN RTX (Failed)
3 - BLAS/RT/NrmTestSuite/NrmTests.ComplexDoublePrecision/Column_Major_TITAN RTX (Failed)
5 - BLAS/RT/NrmTestSuite/NrmTests.ComplexDoublePrecision/Row_Major_TITAN RTX (Failed)
7 - BLAS/RT/NrmTestSuite/NrmTests.ComplexDoublePrecision/Column_Major_TITAN RTX (Failed)
19 - BLAS/RT/ImaxTestSuite/ImaxTests.RealDoublePrecision/Column_Major_TITAN RTX (Failed)
23 - BLAS/RT/ImaxTestSuite/ImaxTests.ComplexDoublePrecision/Column_Major_TITAN RTX (Failed)
35 - BLAS/RT/DotcTestSuite/DotcTests.ComplexSinglePrecision/Column_Major_TITAN RTX (Failed)
36 - BLAS/RT/DotcTestSuite/DotcTests.ComplexSinglePrecision/Row_Major_TITAN RTX (Failed)
47 - BLAS/RT/AusmTestSuite/AusmTests.ComplexSinglePrecision/Column_Major_TITAN RTX (Failed)
48 - BLAS/RT/AusmTestSuite/AusmTests.ComplexSinglePrecision/Row_Major_TITAN RTX (Failed)
85 - BLAS/RT/DoubleTestSuite/DoubleTests.ComplexSinglePrecision/Column_Major_TITAN RTX (Failed)

```

From [DPC++ AoT documentation](#), not clear:

- The options are also required at linking time? Unused in files without kernels?
- Any example of other projects integrating AoT in a CMake setup?

Intel Compiler (Fortran/C/C++/L0) - Intel Discrete GPU Accelerator - Joint Laboratory for System Evaluation (enl.gov)
[hang_atomic_on_local](#)
 Ticket number: CMPLRLLVM-36572 (works in PVC, but still fails on ATS node)
 related to driver not compiler self

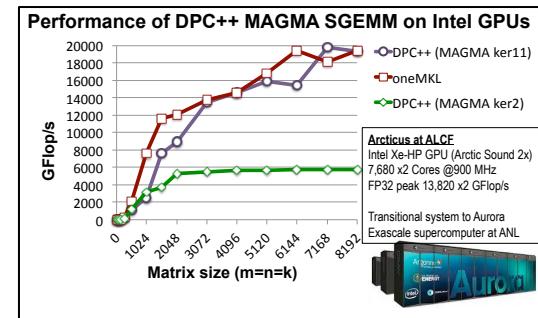
tid % subgroup size >= 4 gives wrong division

(double) 1/a gives wrong result when the tid % subgroup size >= 4. For example, when a = 1.0733829563753890 1/a should be 0.931629312583232 if (local_id == assign_id) { a = double(1)/a; } when assign_id >= 4, Gen9 GPU still give the correct result when assign_id >= 4, Gen9 GPU gives wrong 0.931629312583232 CPU has more worse result

It is connected to optimizations (not reproducible with O0). f-speculation=off do not improve results. Ticket number: XDEPS-4031 ()

Jevcloud node issue

- sycl-ls/clinfo does not give any of s001-n225, s011-n006
- no gpu on the nodes s001-n232, s001-n233, s011-n008
- github.com is not accessible on Jevcloud



... but also docker image contributions and bug fixes!

ginkgohub/oneapi:cuda11.6

DIGEST: sha256:8bc4c18d79e75b183ac1leafcd0753365c6e1a94edc3046d9a0eb8ba2d7bd934
 OS/ARCH: linux/amd64
 COMPRESSED SIZE: 6.63 GB
 LAST PUSHED: 22 days ago by [yhmtsai](#)

fix cuda/nip backend location #219

Description

From Intel/lm64#607, it moves almost all headers from CL/sycl to sycl I followed #219 way to fix it. make the header can use syscl.h if they exist and allow the old intel lvm. I also update the CL/sycl.hpp which are not changed before.

All Submissions

Do all unit tests pass locally? Attach a log. A: It is a compiling issue.
 ✓ Have you formatted the code using clang-format?

Bug fixes

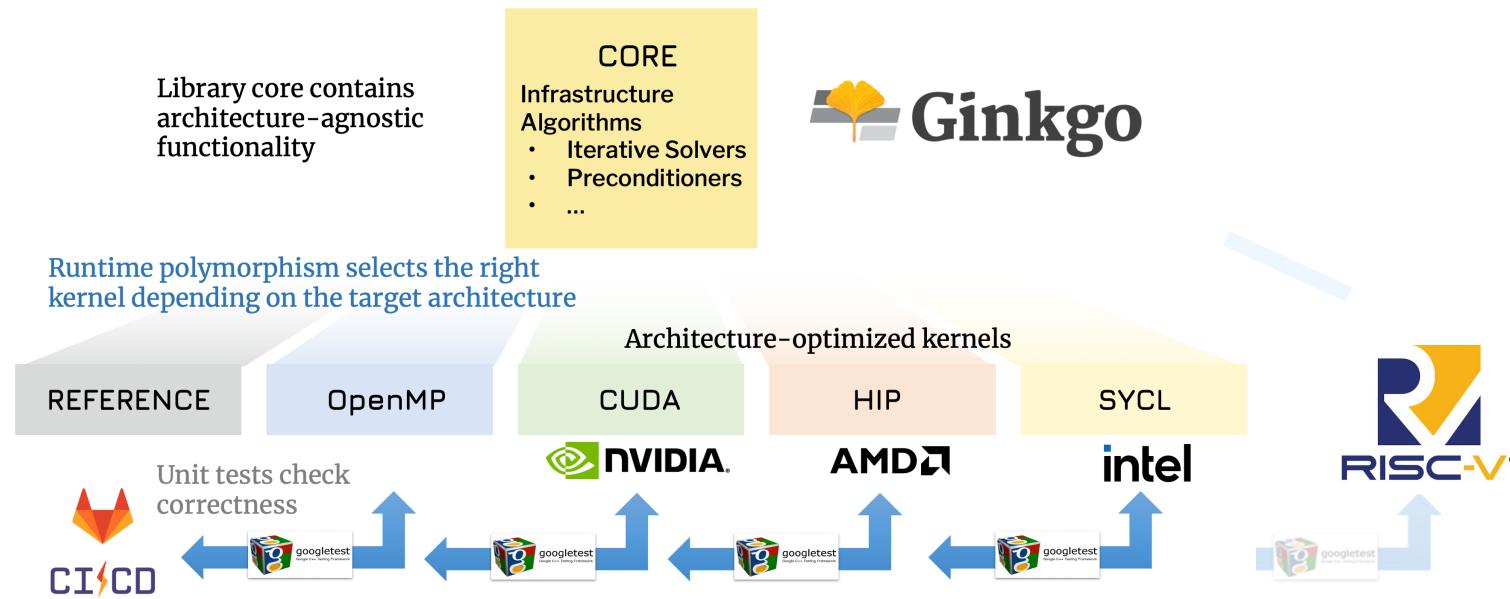
Have you added relevant regression tests? A: It is a compiling issue.
 ✓ Have you included information on how to reproduce the issue (either in a GitHub issue or in this PR)?
 Reproduce:
 compile the latest intel lvm and this repo, it will not be able to compile due to missing headers.

Comments

yhmtsai added 2 commits 2 months ago
 use the correct syscl path after Intel/lm64#607
 Fix the missing syscl/sycl.h

mometerel commented on Aug 1
 Thanks for the PR. Is the description from syscl.h to CL correct? My understanding is all header files moved

Portability and Extendibility as Central Design Principle

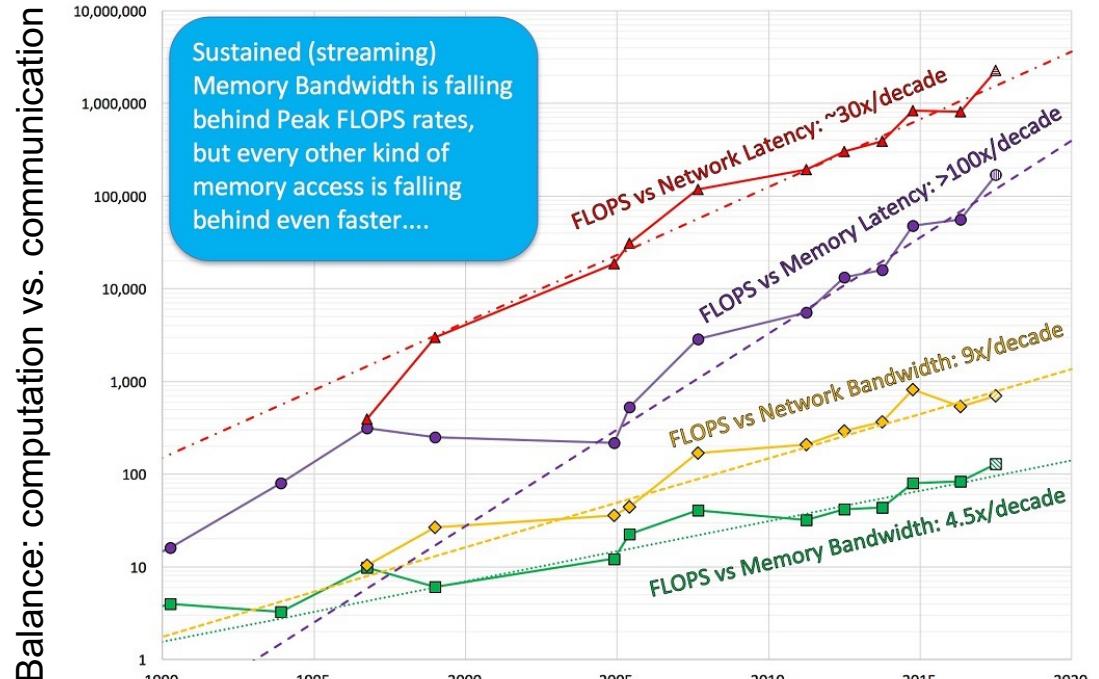


This software design gives portability, performance, and sustainability.

Hardware Trends



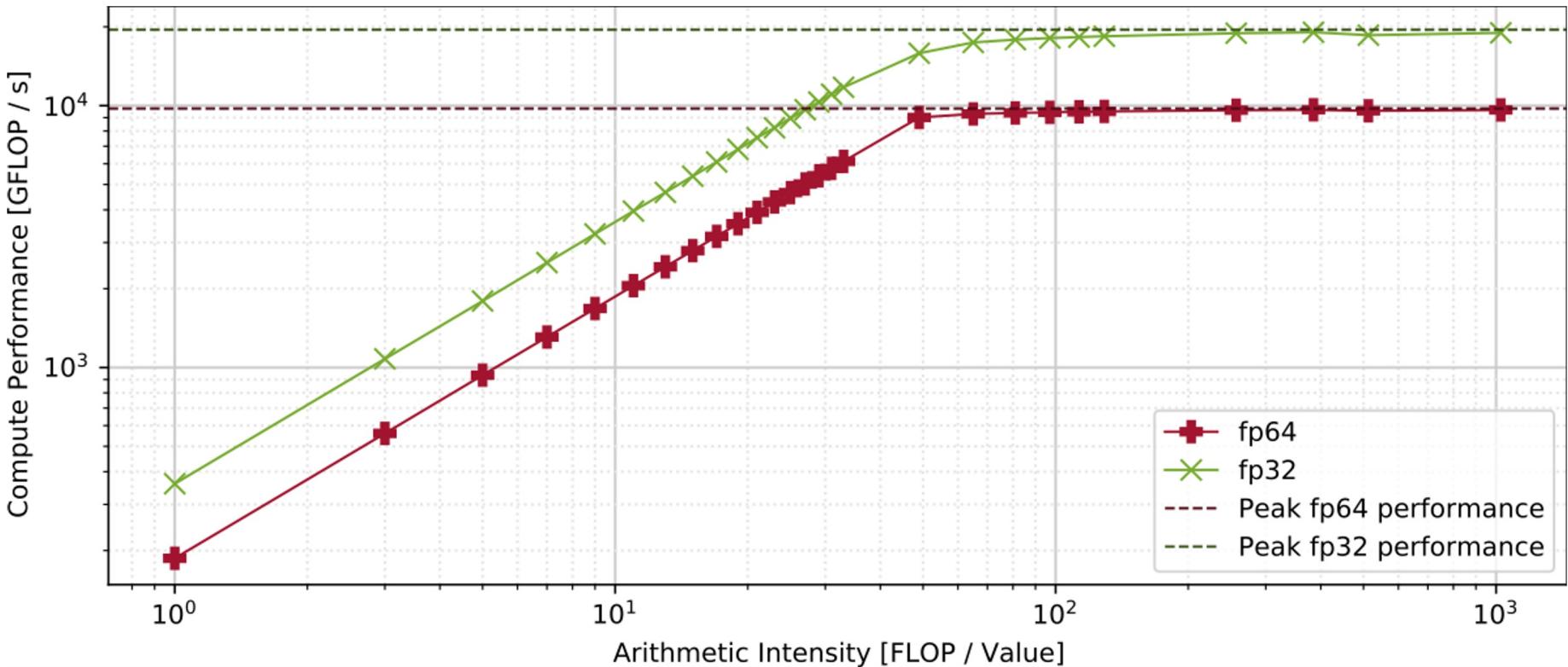
Form Factor	H100 SXM
FP64	34 teraFLOPS
FP64 Tensor Core	67 teraFLOPS
FP32	67 teraFLOPS
TF32 Tensor Core	989 teraFLOPS ^z
BFLOAT16 Tensor Core	1,979 teraFLOPS ^z
FP16 Tensor Core	1,979 teraFLOPS ^z
FP8 Tensor Core	3,958 teraFLOPS ^z
INT8 Tensor Core	3,958 TOPS ^z
GPU memory	80GB
GPU memory bandwidth	3.35TB/s

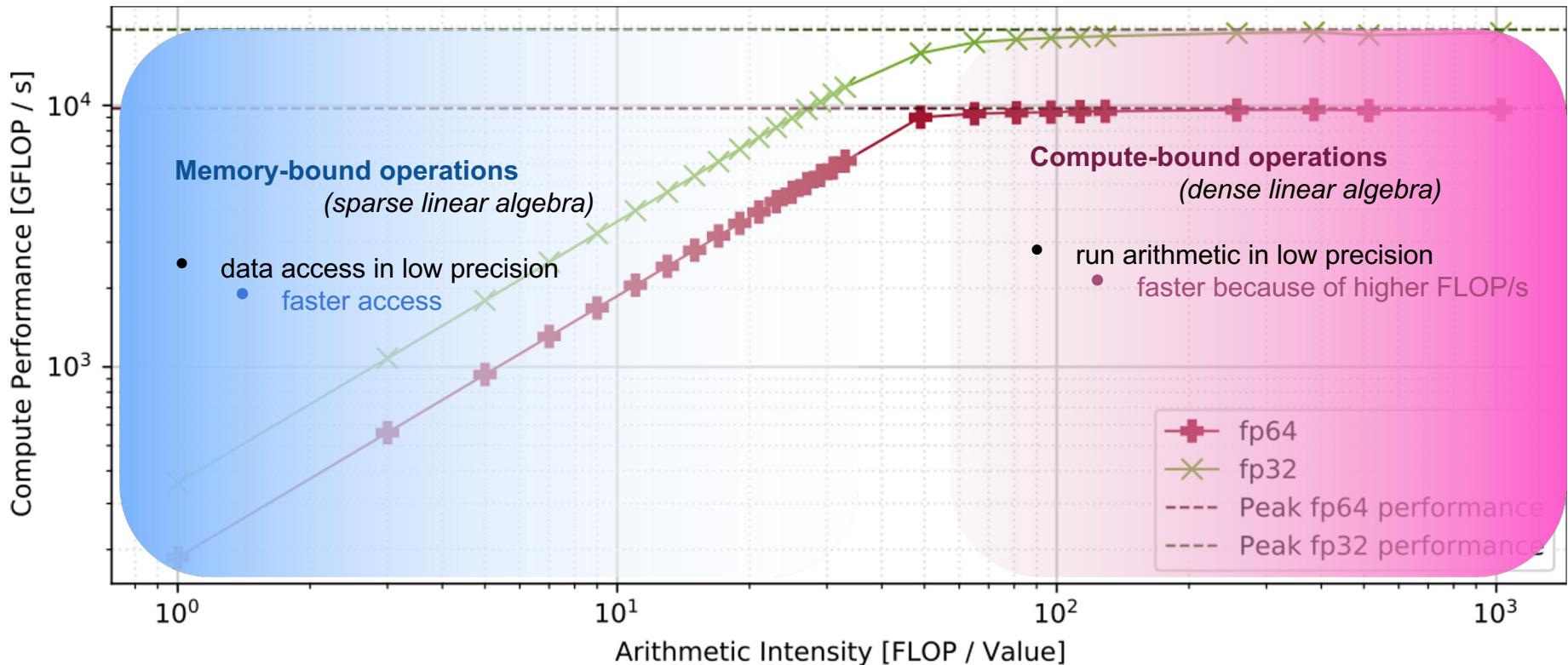


- (Dense) Matrix Performance > Vector Performance
- Low Precision Perf > High Precision Performance

Trends in the relative performance of floating-point arithmetic and several classes of data access for select HPC servers over the past 25 years. Source: John McCalpin

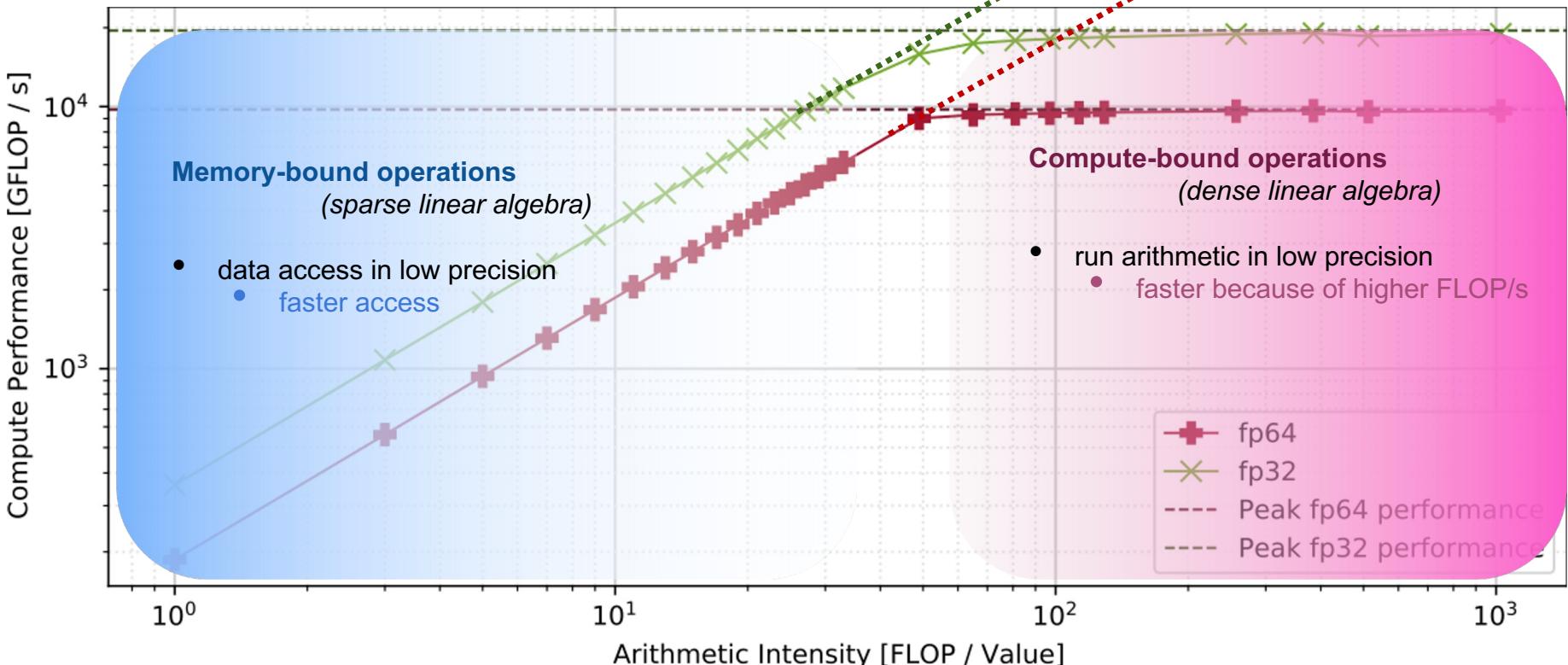
NVIDIA A100





Matrix fp32

Matrix fp64



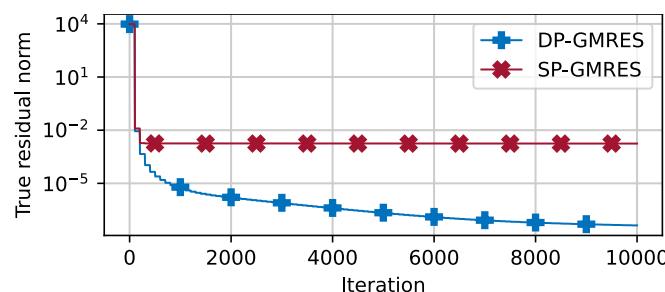
Linear System $Ax=b$ with $\text{cond}(A) \approx 10^7$
 (apache2 from SuiteSparse) NVIDIA V100 GPU

Double precision GMRES

Initial residual norm $\text{sqrt}(r^T r)$: 9670.36
 Final residual norm $\text{sqrt}(r^T r)$: $9.6639e-09$
 GMRES iteration count: 23271
 GMRES execution time: 43801 ms

Single precision GMRES

Initial residual norm $\text{sqrt}(r^T r)$: 9670.36
 Final residual norm $\text{sqrt}(r^T r)$: 0.00175464
 GMRES iteration count: 25000
 GMRES execution time: 27376 ms



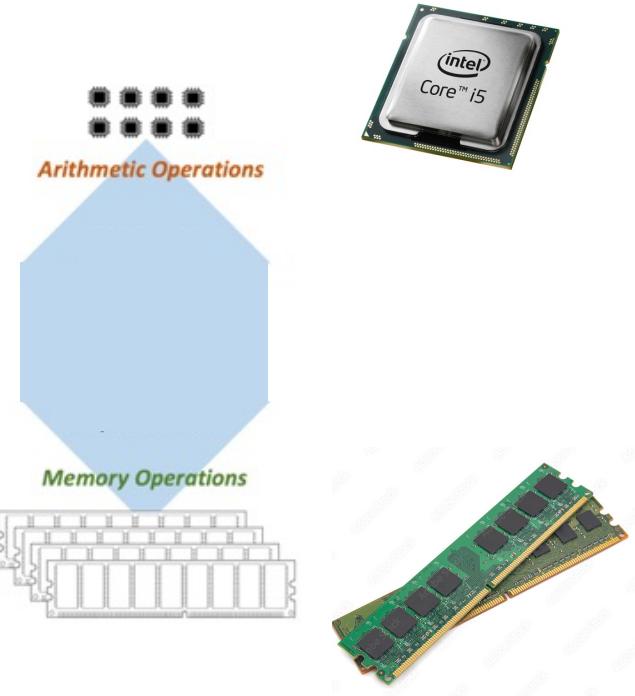
~2x faster!

forward error \approx (unit round-off) * (linear system's condition number)

N. Higham: Accuracy and stability of numerical algorithms. SIAM, 2002.

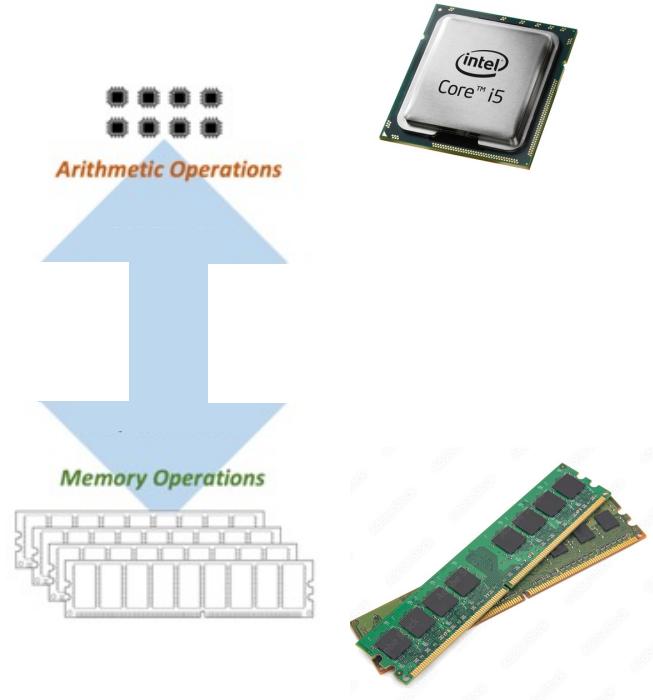
ECP Focus Effort Mixed Precision

- Traditionally, we use a strong coupling between the precision formats used for arithmetic operations the precision format handling data in main memory.
- *We should compute in fp64*
- *Data should be compressed for main memory access (low precision/compression)*
- *Compression / Conversion needs to happen on-the-fly*



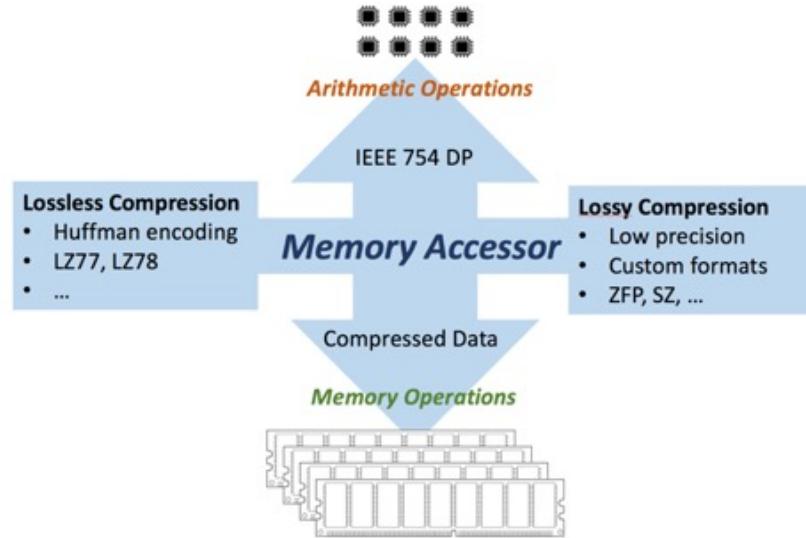
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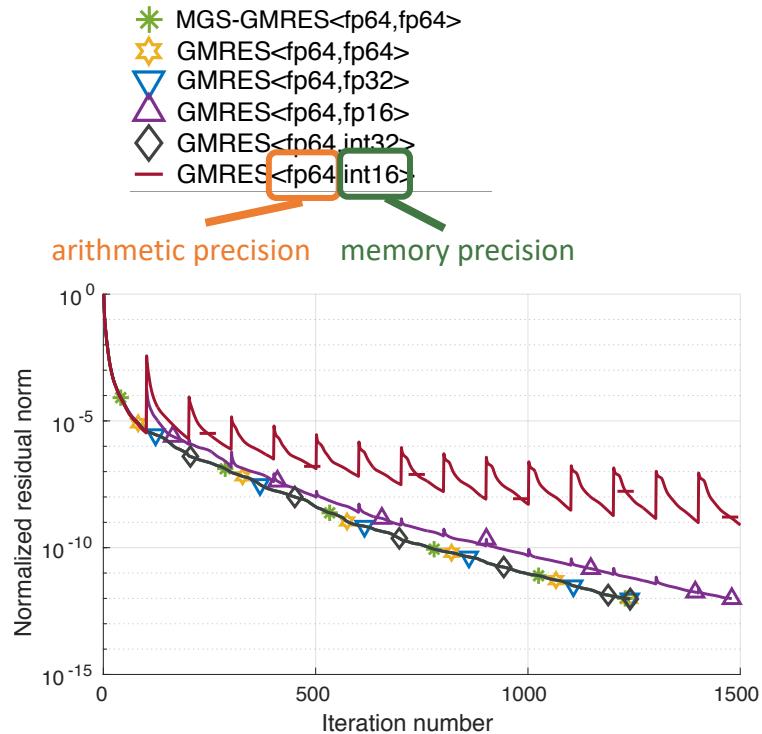
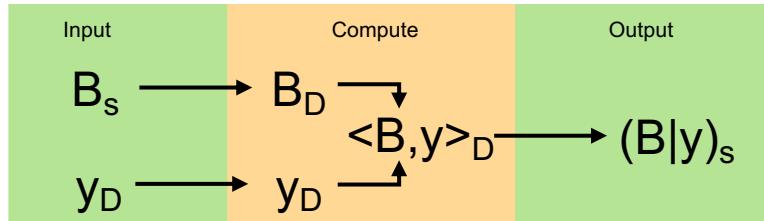
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Compressed Basis (CB-) GMRES

- Use double precision in all arithmetic operations;
- Store Krylov basis vectors \mathbf{B} in lower precision;
 - Search directions are no longer DP-orthogonal;
 - Hessenberg system maps solution to “perturbed” Krylov subspace;
 - Additional iterations may be needed;
 - As long as the loss-of-orthogonality is moderate, we should see moderate convergence degradation;

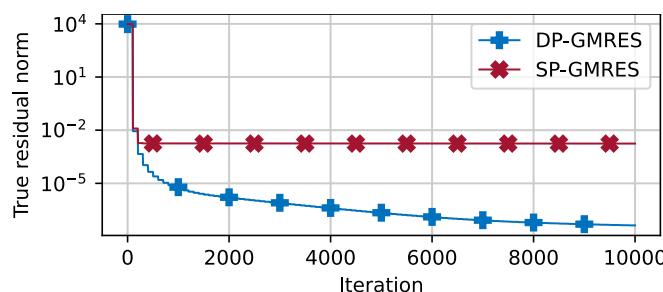


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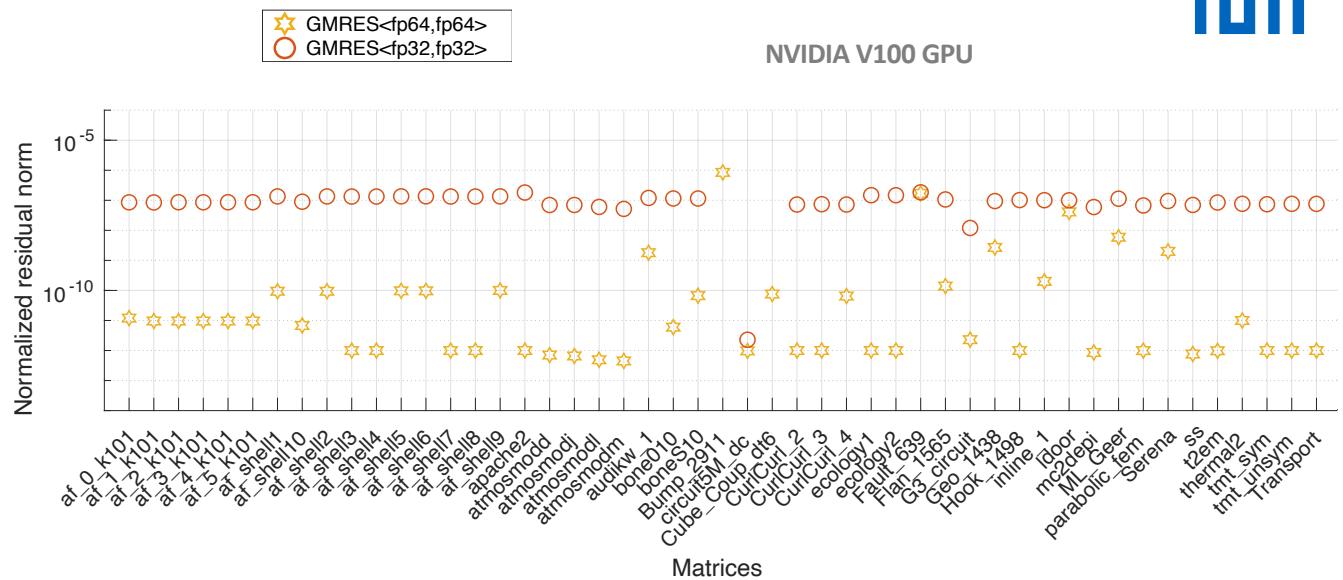
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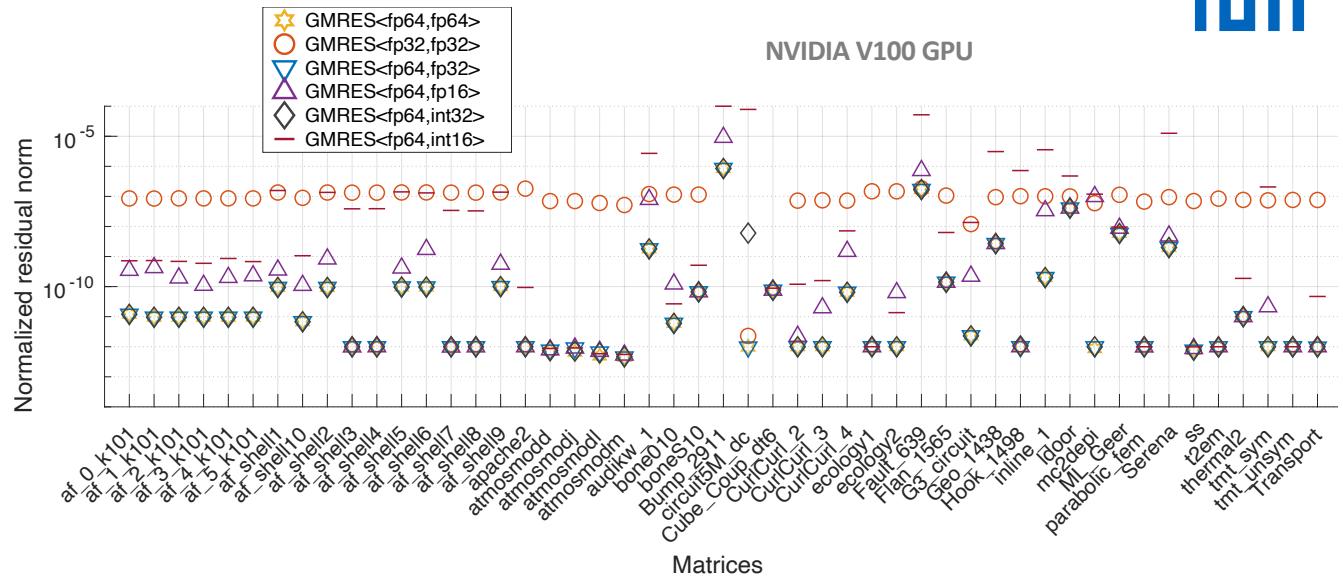
Initial residual norm **Relative residual $\sim 10^{-12}$**
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Final residual norm
 $\sqrt{r^T r}$: 9.6591e-09
GMRES iteration count: 23271
GMRES execution time: 29369 ms

Accuracy of DP GMRES
Performance similar to SP GMRES

NVIDIA V100 GPU



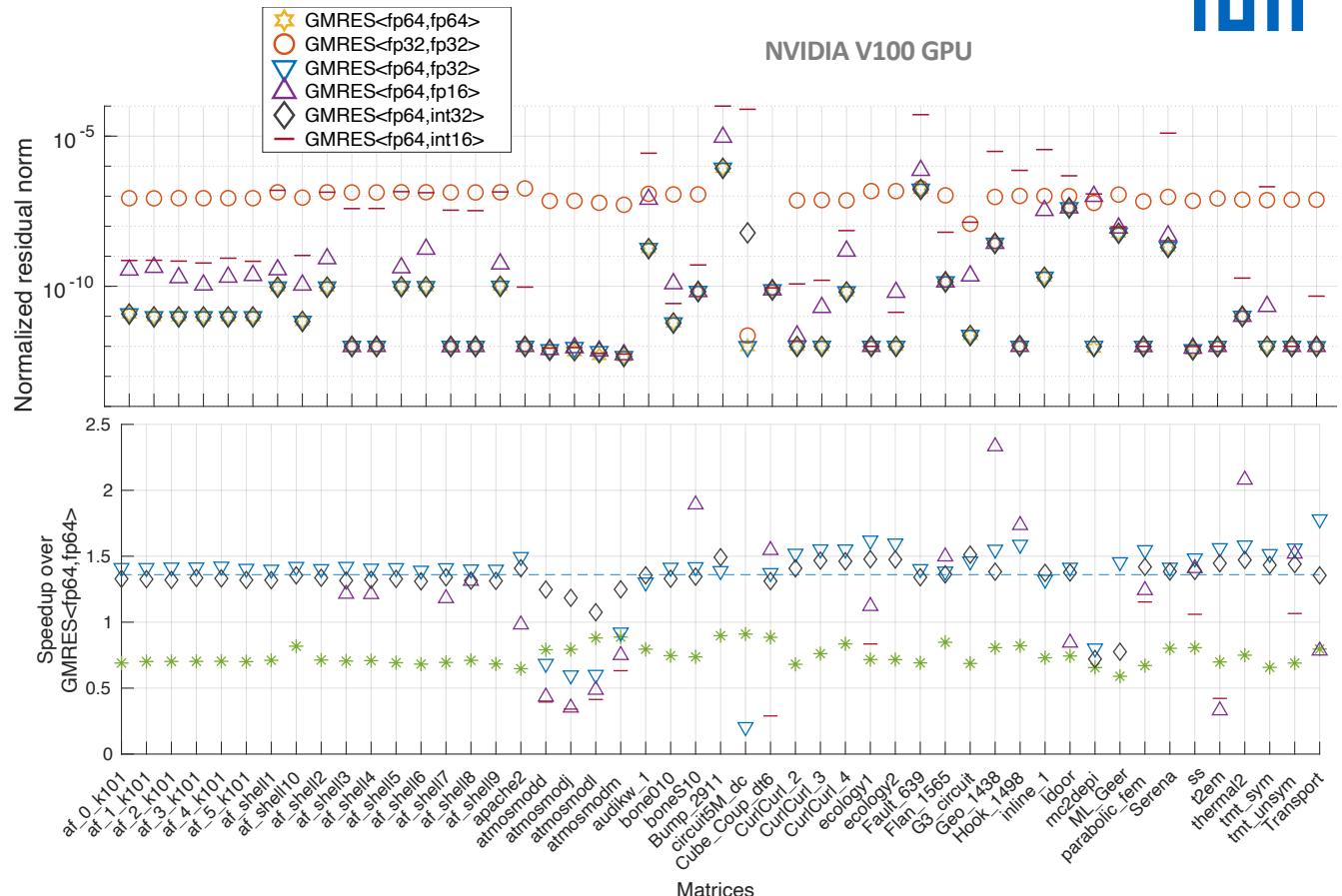
- CB-GMRES using 32-bit storage preserves DP accuracy (SP-GMRES does not)



- CB-GMRES using 32-bit storage preserves DP accuracy (SP-GMRES does not)
- Speedups problem-dependent
- Speedup $\varnothing 1.4x$ (for restart 100)
- 16-bit storage mostly inefficient



Aliaga JI, Anzt H, Grützmacher T, Quintana-Ortí ES, Tomás AE. Compressed basis GMRES on high-performance graphics processing units. *The International Journal of High Performance Computing Applications*. 2022;0(0). doi:[10.1177/10943420221115140](https://doi.org/10.1177/10943420221115140)



ECP Focus Effort Mixed Precision



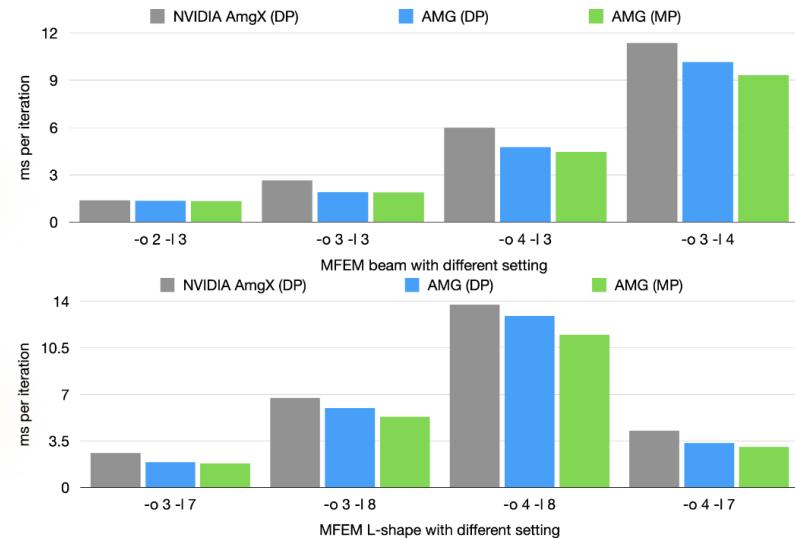
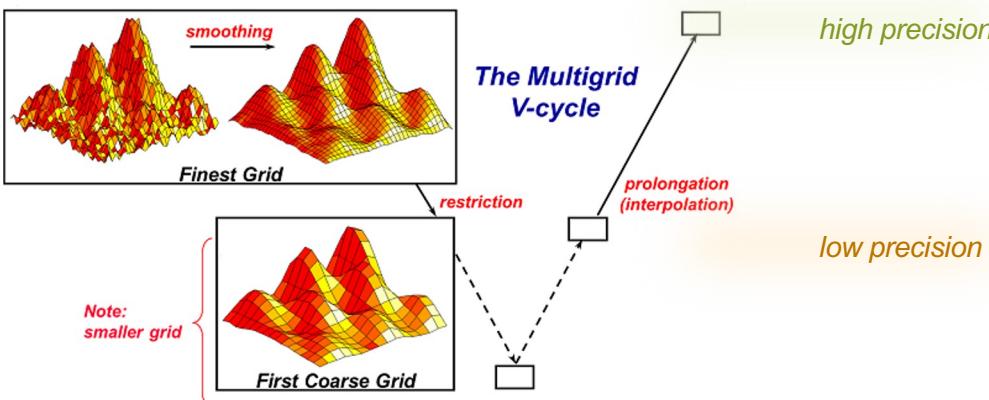
Mike Tsai

- Preconditioning iterative solvers

- Idea: Approximate inverse of system matrix to make the system “easier to solve”: $P^{-1} \approx A^{-1}$
and solve $Ax = b \Leftrightarrow P^{-1}Ax = P^{-1}b \Leftrightarrow \tilde{A}x = \tilde{b}$

- Mixed Precision Multigrid Preconditioner

Stephen F. McCormick, Joseph Benzaken, Rasmus Tamstorf: Algebraic error analysis for mixed-precision multigrid solvers, <https://arxiv.org/abs/2007.06614>

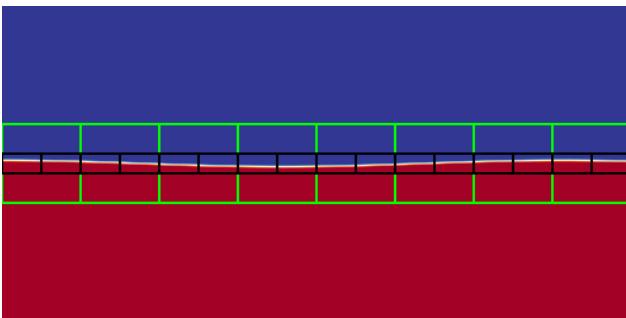


Batched Focus Effort

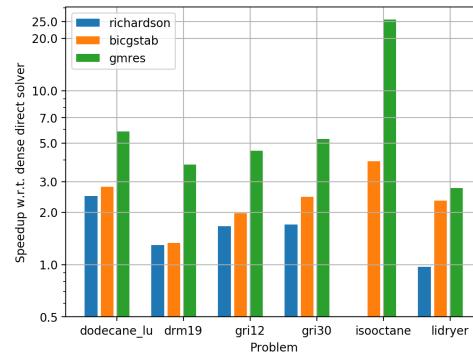
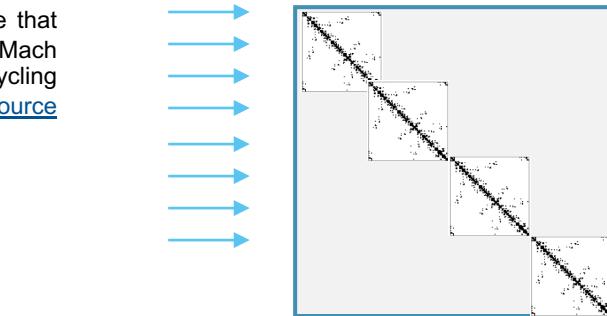
Batched iterative solvers for SUNDIALS / PeleLM

PeleLM is a parallel, adaptive mesh refinement (AMR) code that solves the reacting Navier-Stokes equations in the low Mach number regime. The core libraries for managing the subcycling AMR grids and communication are found in the [AMReX source code](#).

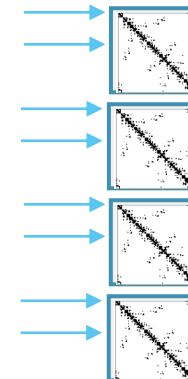
<https://amrex-combustion.github.io/PeleLM/overview.html>



Problem	Size	Non-zeros (\mathbf{A})	Non-zeros ($\mathbf{L+U}$)
dodecane_lu	54	2,332 (80%)	2,754 (94%)
drm19	22	438 (90%)	442 (91%)
gr12	33	978 (90%)	1,018 (93%)
gr30	54	2,560 (88%)	2,860 (98%)
isoctane	144	6,135 (30%)	20,307 (98%)
lidryer	10	91 (91%)	91 (91%)



Carol Woodward Cody Balos



Batched Sparse Iterative Solvers for Computational Chemistry Simulations on GPUs

Publisher: IEEE

Cite This

PDF

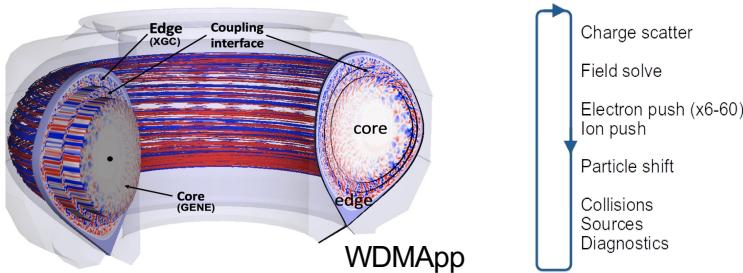
Isha Aggarwal ; Aditya Kashi ; Pratik Nayak ; Cody J. Balos ; Carol S. Woodward ; Hartwig Anzt All Authors



Batched Functionality for the Collision Operator

XGC is a gyrokinetic particle-in-cell code, which specializes in the simulation of the edge region of magnetically confined thermonuclear fusion plasma. The simulation domain can include the magnetic separatrix, magnetic axis and the biased material wall. XGC can run in total-delta-f, and conventional delta-f mode. The ion species are always gyrokinetic except for ETG simulation. Electrons can be adiabatic, massless fluid, driftkinetic, or gyrokinetic.

Source: https://xgc.pppl.gov/html/general_info.html



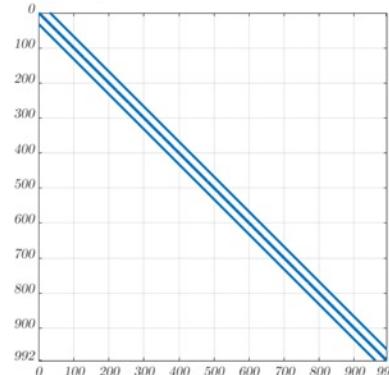
XGC collision operator: fully nonlinear multi-species Fokker-Planck-Landau

For each mesh vertex:

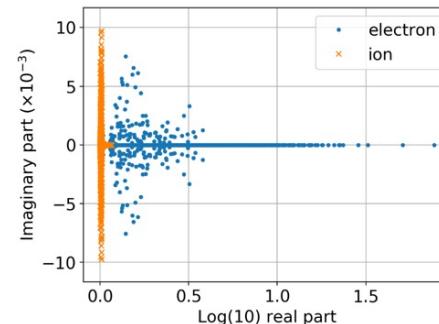
- Outer nonlinear solver: Picard method with inner linear solves
- Linear solve: discretize velocity space with approx 35x35 velocity grid
- direct solve on CPU using LAPACK banded solver **dgbsv**
- After GPU porting of XGC, this is the remaining CPU intensive kernel for collision operator



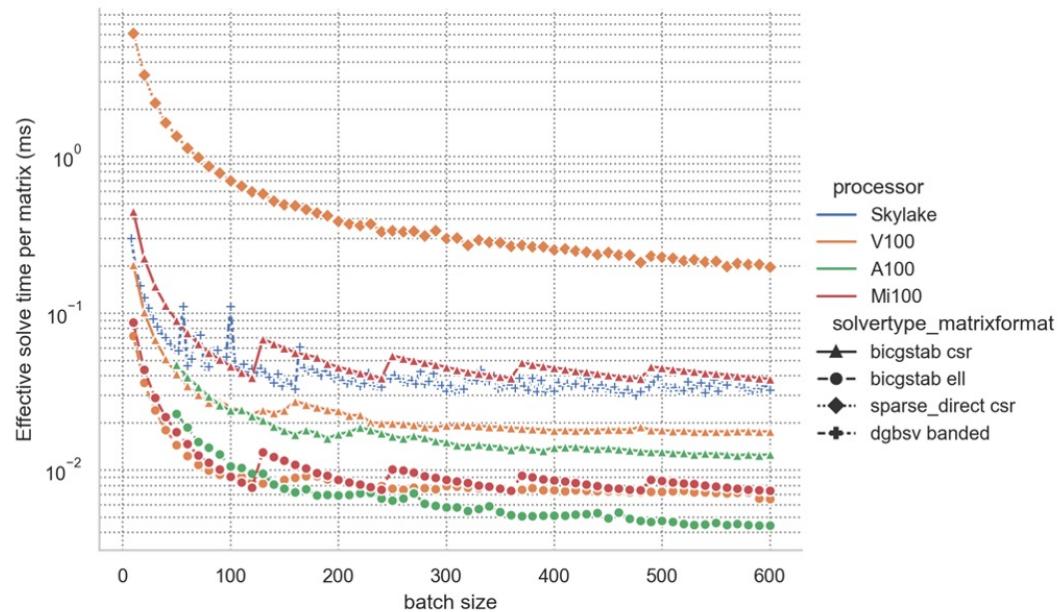
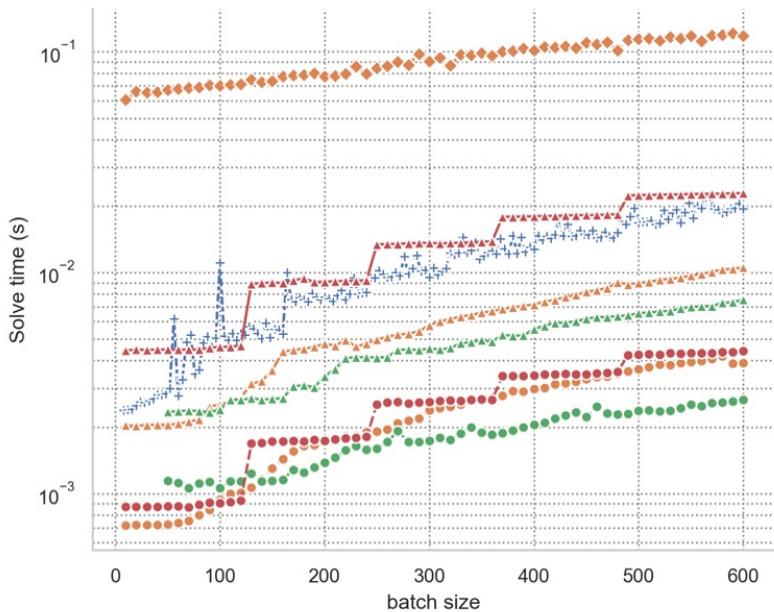
Paul Lin Dhruva Kulkarni



- Two species
- Ions easy to solve
- Electrons hard to solve
- Banded matrix structure
- Non-symmetric, need BiCGSTAB
- $n = \sim 1,000$
- $nz = \sim 9,000$

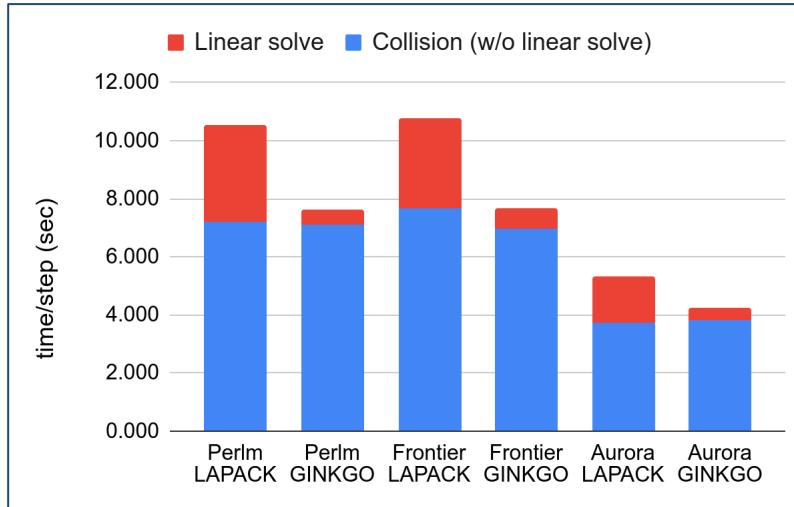


Batched Functionality for the Collision Operator



Batched Functionality for the Collision Operator

- XGC DIII-D National Fusion Facility tokamak electromagnetic (EM) test case
- 8 nodes of NERSC Perlmutter: 32 A100s, 1 MPI per GPU; single socket 64-core AMD EPYC
- 8 nodes OLCF Frontier: 32 MI250X, 64 GCDs, 1 MPI per GCD; single socket 64-core AMD EPYC
- 8 nodes ALCF Aurora: 48 Intel Data Center Max 1550, 96 tiles, 1 MPI per tile; dual socket 52-core Intel CPU Max 9470C SPR



Aditya Kashi, Pratik Nayak, Dhruva Kulkarni, Aaron Scheinberg, Paul Lin, and Hartwig Anzt. **Batched sparse iterative solvers on gpu for the collision operator for fusion plasma simulations**. In *2022 IEEE International Parallel and Distributed Processing Symposium (IPDPS)*, pages 157–167. IEEE, 2022.

Mathematical Formulation of the ExaSGD Core Challenge

Security constrained multiperiod AC optimal power flow analysis

Posed as an optimization problem:

Find

$$\min_{x_t, y_{tsk}} (\sum_t F_t(x_t) + \sum_{tsk} G_{tsk}(x_t + y_{tsk}))$$

generator fuel cost

wind curtailment,
load shedding,
power imbalance, etc.

flow definitions,
power balance

bounds: generator power,
voltage, branch flow

generator ramping limit

Subject to:

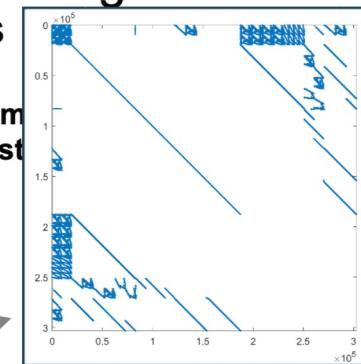
$$H_{tsk}(x_t, y_{tsk}) = 0$$

$$Q_{tsk}(x_t, y_{tsk}) \leq 0$$

$$R_t(x_t, x_{t+1}) \leq 0$$

The optimization problem
the underlying linear system

$$\left[\begin{array}{c|ccccc|c} K_1 & & & & & & \\ \hline K_2 & & & & & & \\ K_3 & & & & & & \\ \hline & \dots & \dots & \dots & \dots & \dots & \dots \\ B_1^T & B_2^T & B_3^T & \dots & B_N^T & B_0 & | & y_N \\ & & & & & x & | & r_N \\ & & & & & & & r_0 \end{array} \right]$$



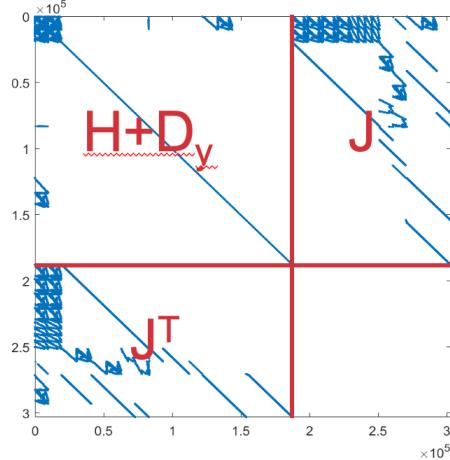
EXASGD



© Slaven Peles

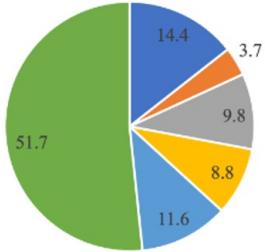
- The characteristic block-arrow coupling structure can be exploited to decompose the optimization problem, nevertheless there is no solver that can tackle this on a GPU-based architecture.

Sparse Direct Solvers

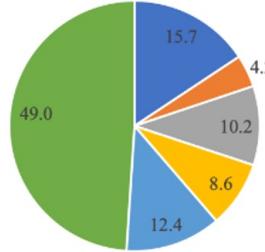


Grid	Buses	Generators	Lines	$N(K_k)$	$\text{nnz}(K_k)$
Northeastern US	25 K	4.8 K	32.3 K	108 K	1.19 M
Eastern US	70 K	10.4 K	88.2 K	296 K	3.20 M
Western and Eastern US	82 K	13.4 K	104.1 K	340 K	3.73 M

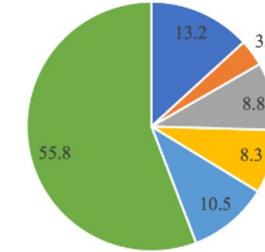
■ Hessian ■ Constraints ■ Constraint Jacobian ■ Other ■ Solve ■ Factorize



(a) Northeast U.S. grid



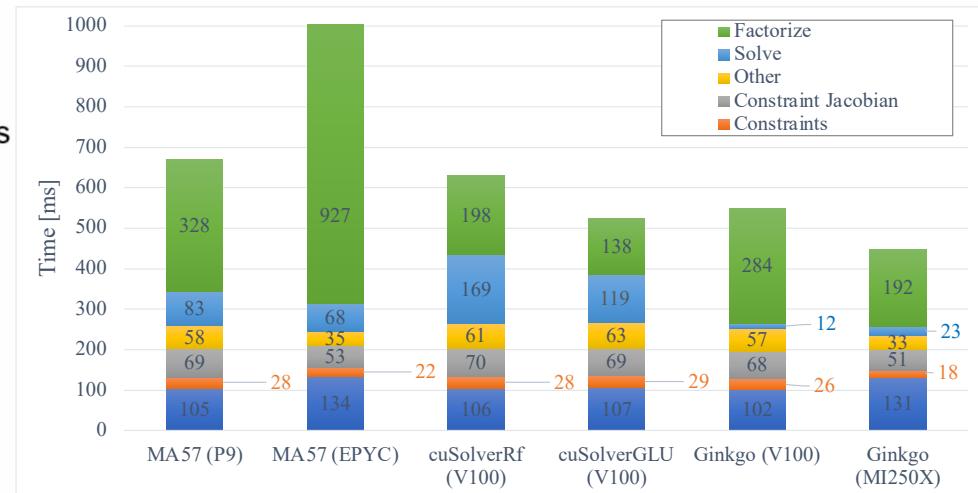
(b) Eastern U.S. grid



(c) Eastern and Western U.S. grids

Liner Solver Performance within Optimization Algorithm Average per iteration times (including first iteration on CPU)

- Each GPU solution outperforms all CPU baselines.
- Ginkgo performance improves on a better GPU.
- Iterative refinement configuration affects linear solver performance and optimization solver convergence.
- Ginkgo is the first GPU-resident sparse direct linear solver.

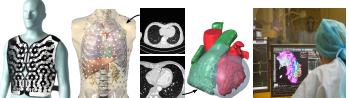


Multiple promising GPU-resident sparse linear solvers

29

After 6 years of development

- EuroHPC Project MICROCARD uses Ginkgo



<https://www.microcard.eu>

- DoE SciDAC-5 : Development of High-Fidelity Simulation Capabilities for ELM-free Design Optimization



- BMBF PDExa and ExaSIM projects use Ginkgo



The Open Source CFD Toolbox

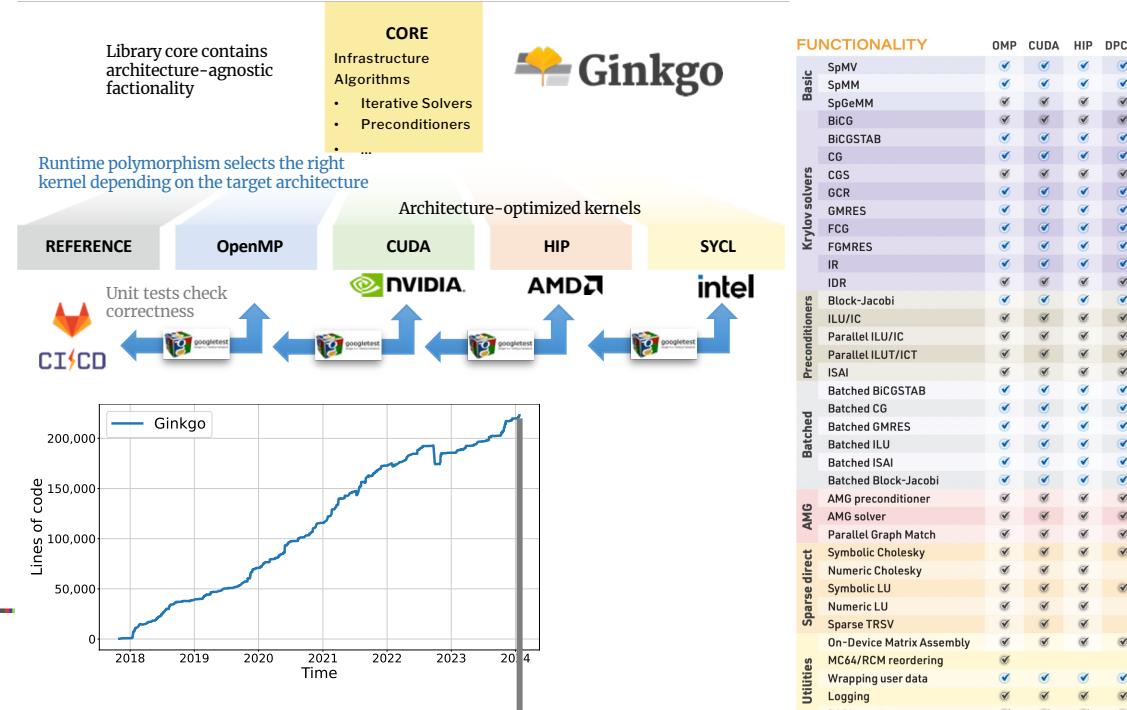


CEED/NekRS

Minor of NekRS - GPU-oriented version of Nek5000. Please use the official repository: <https://github.com/Nek5000/nekrs>, to create issues and pull requests.



- Companies are evaluating Ginkgo



Lessons learnt over the years

- ECP earmarking roughly half the budget to Software & App development is a game changer.
 - Central component for the success of ECP.
 - This concept needs to – and does become - the blueprint for other nations, companies, and projects.
- Workforce recruitment and workforce retention are the key to success in software development.
 - Money does not write software. RSEs do. We need to create attractive career plans.
 - We need to make research software development attractive to students. Academic recognition. Industry career paths.
- Anticipating the future in hardware development accelerates the porting process.
 - Blueprints and early access systems both useful.
 - Interaction with industry is mutually beneficial.
- Strategic initiatives, interaction and collegial behavior are important.
 - Strategic focus groups, conferences, and meetings bring experts together and create collaboration.
 - Listen to the application needs. Value input and acknowledge collaborators.

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