

Part - B

g_{cm} (cascade)

$$\beta = (20) \quad V_A = \infty.$$

$$r_{01} = \frac{V_A}{I_{CO}} = \infty$$

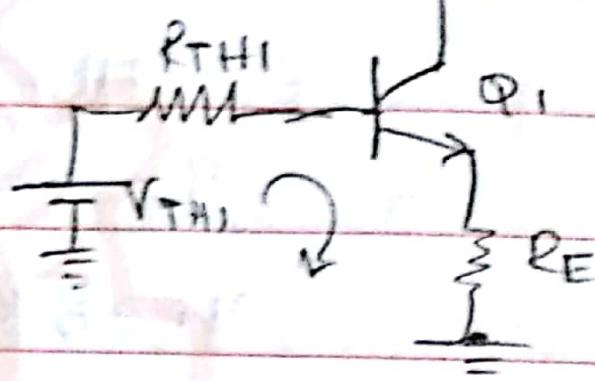
$$r_{B2} = \frac{V_A}{I_{CO}} = \infty.$$

of O.C capacitors
↓
DC Analysis.

$$V_{CC} = 12V$$

$$R_A = 10k\Omega$$

$$V_{TH1} = \frac{12 \times 12.7k}{12.7k + 67.3k}$$



$$V_{TH1} = 1.905V$$

$$R_{TH1} = 10.68k\Omega \Rightarrow (R_1 || R_2)$$

i/p KV1,

$$V_{TH1} = I_{B1}R_{TH1} + V_{BE1} + I_{B1}(1+\beta)R_{E1}$$

$$I_{B1} = \frac{V_{TH1} - V_{BE1}}{R_{TH1} + (1+\beta)R_{E1}} = \frac{1.905 - 0.7}{10.68k + (12)(6k)}$$

$$I_{B1} = 4.768mA$$

$$I_{C1} = \beta I_{B1} = 120 \times 4.768mA$$

$$I_{C1} = 0.572mA$$

$$g_{m1} = \frac{I_{C1}}{V_T} = \frac{0.572mA}{26mV}$$

$$g_{m1} = 0.022 A/V$$

$$r_{H1} = \frac{\beta V_T}{I_{CQ1}} = \frac{120 \times 26mV}{0.572mA}$$

$$r_{H1} = 5.454k\Omega$$

DC Analysis

$$V_{TH2} = \frac{12 \times 45k}{(45 + 15)k}$$

$$\boxed{V_{TH2} = 9V}$$

$$R_{TH2} = 45k \parallel 15k \Rightarrow (R_3 \parallel R_4)$$

$$\boxed{R_{TH2} = 11.25k\Omega}$$

i_{IP} kVRL

$$I_{B2} = \frac{V_{TH2} - V_{BE2}}{R_{TH2} + (1+\beta)R_E2}$$

$$= \frac{9 - 0.7}{11.25k + (12)(1.6)k}$$

(O-C capacitor)

$$\boxed{I_{B2} = 0.0405 \text{ mA}}$$

$$I_{C2} = \beta I_{B2} = 120 \times 0.0405 \text{ mA}$$

$$\boxed{I_{C2} = 4.86 \text{ mA}}$$

$$g_{m2} = \frac{I_{C2}}{V_T} = \frac{4.86}{26} \text{ m}$$

$$\boxed{g_{m2} = 0.1869 \text{ A/V}}$$

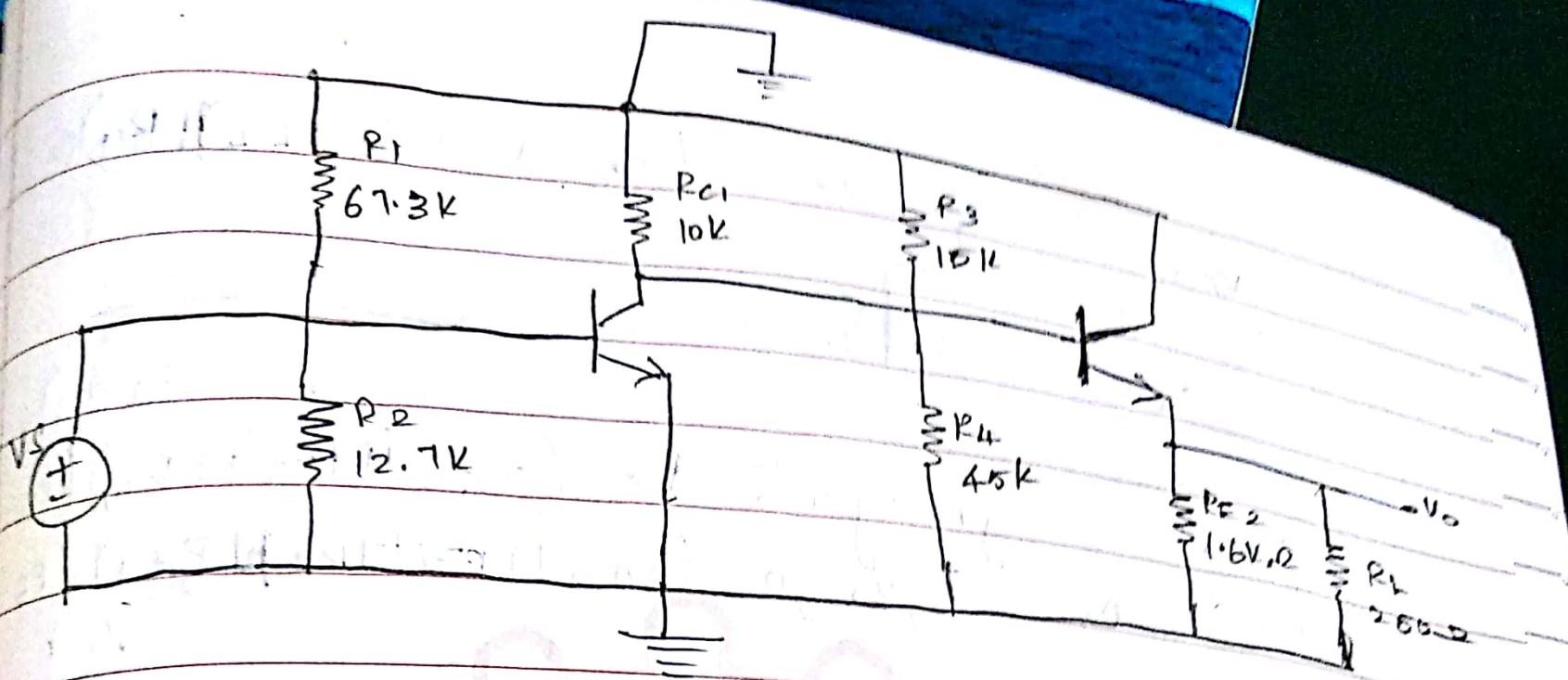
$$\gamma_{\pi2} = \frac{\beta V_T}{I_{C2}} = \frac{120 \times 26}{4.86} \text{ m}$$

$$\boxed{\gamma_{\pi2} = 0.642 \text{ k}\Omega}$$

(b) overall gain, $A_v = \frac{V_o}{V_s}$

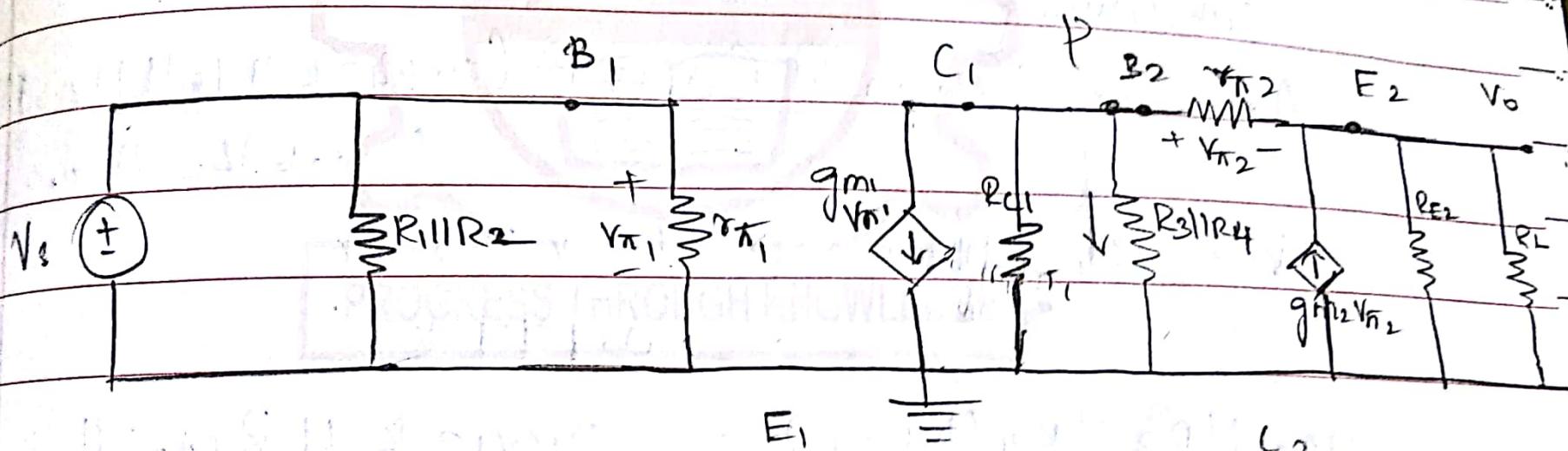
small signal analysis,

S.C. all capacitors and dc sources,



hybrid pi-model

$$r_{o1} = r_{o2} = \infty$$



$$N_o = g_{m2} V_{pi2} (R_E2 \parallel R_L) \quad \text{--- (1)}$$

At P_E , KCl ,

$$g_{m1} V_{pi1} + \frac{V_{pi2}}{R_{pi2}} + \frac{V_{pi2}}{R_3 \parallel R_4} + \frac{V_{pi2}}{R_{cl}} = 0$$

$$V_{pi1} = V_s$$

$$g_{m1} V_s = - V_{pi2} \left(\frac{1}{r_{pi2}} + \frac{1}{R_3 \parallel R_4 \parallel R_{cl}} \right)$$

$$\frac{V_{pi2}}{1 + \frac{g_{m1} V_s}{r_{pi2}}} = \frac{\frac{1}{R_{pi2}} + \frac{1}{R_3 \parallel R_4 \parallel R_{cl}}}{\left(\frac{1}{r_{pi2}} + \frac{1}{R_3 \parallel R_4} \right) \frac{1}{R_{cl}}} \quad \frac{1}{R_P} = \frac{1}{R_1 \parallel R_2}$$

$$R_P = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}}$$

$$V_{D2} = -g_{m1} V_S \left(r_{T2} \| R_3 \| R_4 \| R_{C1} \right) \quad (2)$$

Sub (2) in (1)

$$V_o = -g_{m1} g_{m2} V_S \left(r_{T2} \| R_3 \| R_{C1} \right) \left(R_E \| R_L \right)$$

$$V_o = A_v = -g_{m1} g_{m2} \left(r_{T2} \| R_3 \| R_4 \right) \left(R_{C1} \right) \left(R_E \| R_L \right)$$

No

$$\therefore \text{gain, } A_v = -g_{m1} g_{m2} \left(r_{T2} \| R_3 \| R_4 \| R_{C1} \right) \left(R_E \| R_L \right)$$

Substituting

$$A_v = - \frac{(0.022)(0.187)}{(0.642K \| 15K \| 45K \| 10K)} \frac{(0.642K \| 15K \| 45K \| 10K)}{(1.6K \| 0.2K)}$$

$$A_v \approx R_E \| R_L \Rightarrow 1.6K \| 0.2K \\ = 0.177 K$$

$$(r_{T2} \| R_3 \| R_4 \| R_{C1}) = 0.642K \| R_{T2} \| 10K \\ = 0.642K \| 11.25K \| 10K \\ = 0.572K$$

$$\text{Now, } A_v = -6.022(0.187)(0.177)(0.572)$$

$$A_v = 416.5$$

$\times 10^6$

c) swing in o/p voltage,

$$I_{C2} = 40.66 \text{ mA}$$

$$o = V_{CE2} + (R_E \| R_L) i_{C2}$$

$$i_{C2} = -\frac{1}{R_E2 \parallel R_L} V_{CE2}$$

$$\text{slope} = -\frac{1}{R_E2 \parallel R_L} = \frac{-1}{1.6K \parallel 0.2K}$$

$$\text{slope} = -\frac{1}{0.177K}$$

$$i_{C2} = -\frac{1}{0.177K} V_{CE2}$$

$$|V_{CE2}|_{\max} = 0.177K \times i_{C2}$$

$$(V_{CE})_{\max} = 0.86V$$

$$2 \times V_{CE} = 1.72V$$

\therefore Maximum output voltage swing is $1.72V$ peak-to-peak.

$$(f) CM = ? \quad AV = ? \quad f_H = ?$$

$$\text{given: } K_p = 2 \text{ m A/V}^2 \quad V_{TP} = -2V$$

$$\lambda = 0.01 \text{ V}^{-1} \quad g_s = 10 \mu F \quad g_{dS} = 1 \mu F$$

DC analysis,

O.C. capacitance:

$$V_g = 0V \quad V_{DS} = 9 - V_S = I_{DRS}$$

$$V_S = 9 - I_{DRS}$$

$$V_{sg} = V_s - V_g \quad \rightarrow ①$$

$$V_{sg} = q - I_D R_S$$

$$I_D = K_p (V_{sg} + V_{TP})^2 \quad (\text{sub } ①)$$

$$I_D = 2m (q - I_D R_S - 2)^2$$

$$I_D = 2m (7 - 1.2 K I_D)^2$$

$$I_D = 2m (49 + 1.44 K^2 I_D^2 - 16.8 K I_D)$$

$$I_D = 98m + 2.88 K I_D^2 - 33.6 I_D$$

$$2.88 K I_D^2 - 34.6 I_D + 98m = 0$$

$$I_D = 7.4 m$$

$$I_D = 1.5 mA$$

$$V_{sg} = q - 1.5 (1.2)$$

$$V_{sg} = 3.6 V$$

$$V_{ds} > V_{sg} + V_{TP}$$

Op ~~at~~ KRL,

$$18 = T_D R_S + V_{DS} + I_D R_D$$

$$V_{DS} = 18 - I_D (R_S + R_D)$$

$$V_{DS} \approx 18 - 1.5 m (2.2) \quad (3)$$

$$(V_{DS} = 8.1 V)$$

$$g_m = 2 \sqrt{K_p I_D} = 2 \sqrt{2m \times 4.8}$$

$$g_m = 6 m$$

Miller capacitance,

$$C_M = C_{gd} (1 + g_m (R_D || R_L))$$

$$C_M = 1 pF (1 + 6m (1 k))$$

$$C_M = 7 \text{ pF}$$

3 dB upper frequency

$$f_H = \frac{1}{2\pi R_{eq} C_{eq}}$$

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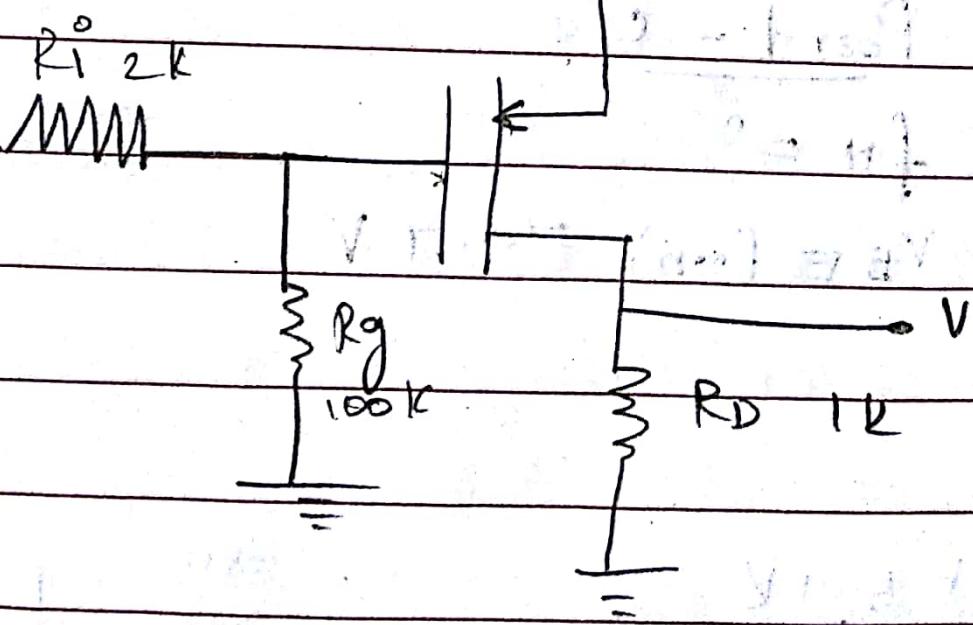
$$2\pi (R_g || R_{si}) (C_{gs} + C_M)$$

$$f_H = \frac{1}{2\pi (2k || 100k) (10 \text{ pF} + 7 \text{ pF})}$$

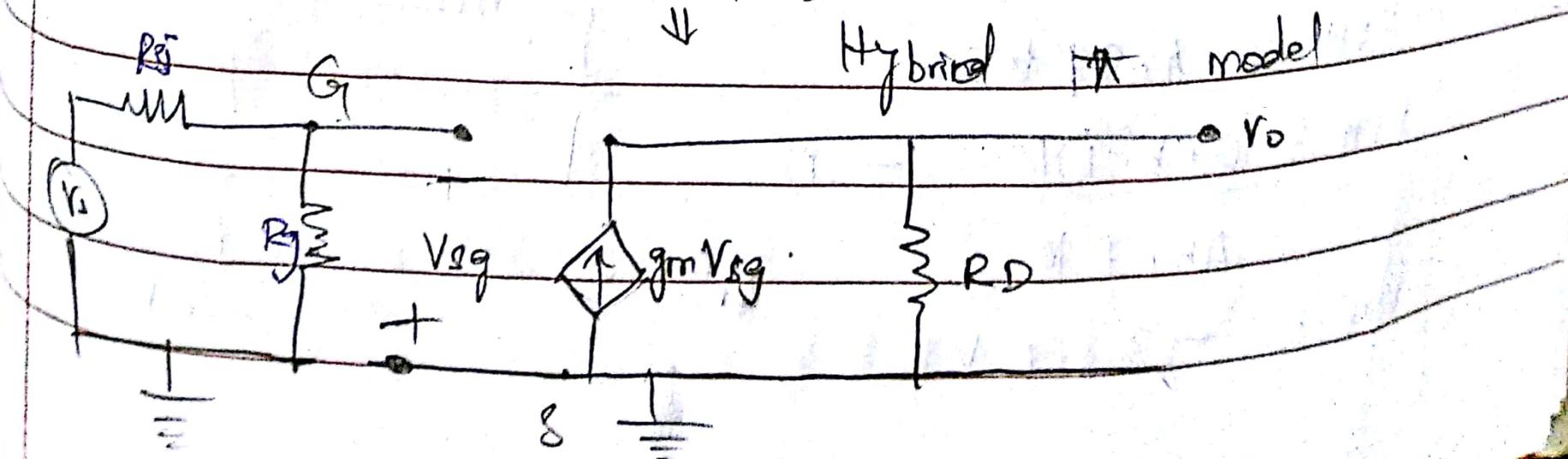
$$f_H = \frac{1}{2\pi (1.96)(17) \times 10^{-9}} = 4.77 \text{ MHz}$$

Small signal analysis

S.C cap & dc sources



Hybrid pi model



$$V_o = -g_m V_{sg} R_D$$

$$-V_{sg} = \frac{V_s R_g}{R_g + R_{si}}$$

$$\therefore V_o = -g_m V_s R_D \frac{R_g}{R_g + R_{si}}$$

$$A_v = \frac{V_o}{V_s} = -g_m R_D \frac{R_g}{R_g + R_{si}}$$

$$\therefore A_v = -6 \times 1K \frac{100K}{102K}$$

$$= -6 \times \frac{100}{102}$$

$$A_v = -5.88$$

PROGRESS THROUGH KNOWLEDGE

Part - c.

9) $A_v = ?$ $f_H = ?$

$$\beta = 100 \quad V_{BE(on)} = 0.7V$$

$$V_A = \infty$$

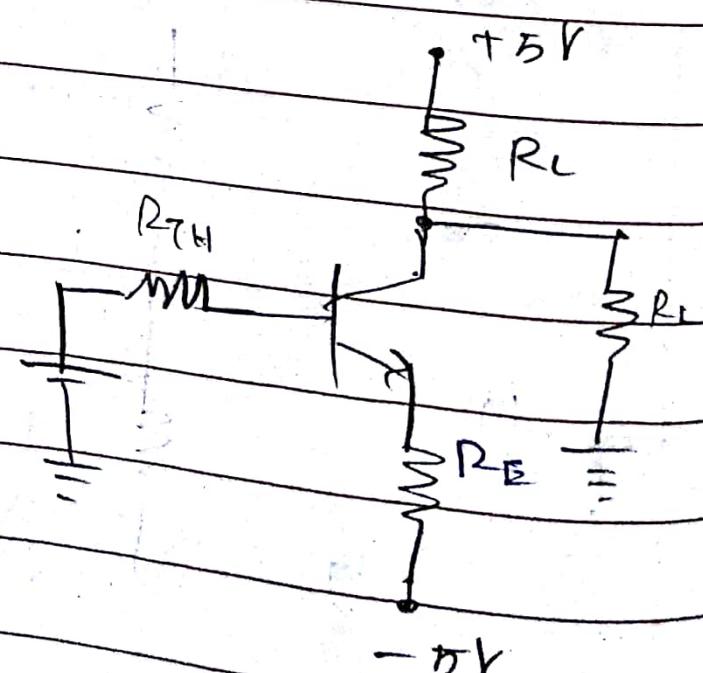
DC analysis,

$$R_{TH} = 40K \parallel 5.7K$$

$$R_{TH} = 1.99K \Omega$$

$$V_{TH} = \frac{10(5.7)K}{45.7K} - 5$$

$$V_{TH} = -3.89V$$



$$V_{TH} = I_B D_{TH} + V_{BE} - (1 + \beta) R_E I_B - 5$$

$$-3.89 + 5 - 0.7 = I_B (R_{TH} + (1 + \beta) R_E)$$

$$\frac{0.41}{4.99k\Omega + (0.1)(0.5k\Omega)} = I_{BQ}$$

$$I_{BQ} = 7.38 \text{ mA}$$

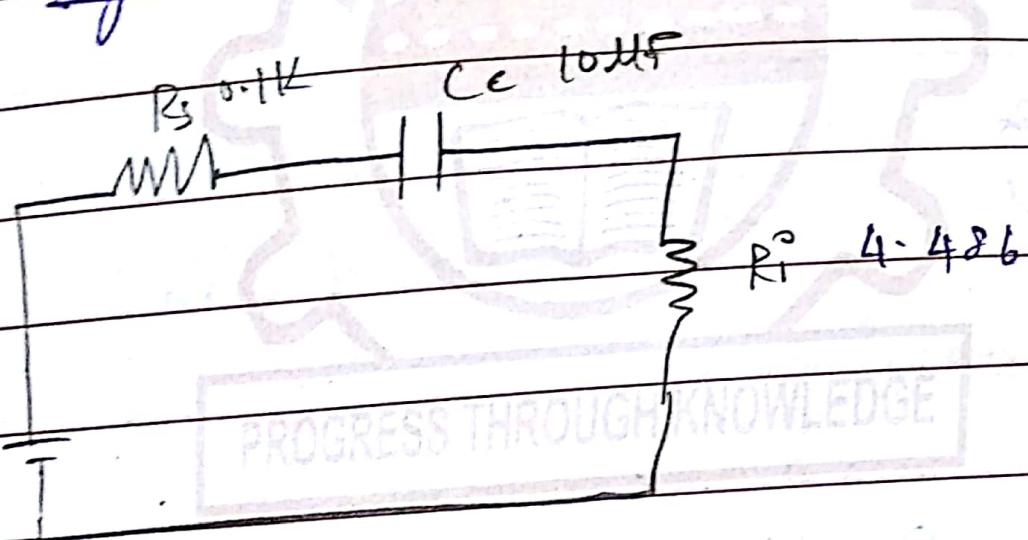
$$I_{CQ} = 0.738 \text{ mA}$$

$$g_m = \frac{I_{CQ}}{V_T} = \frac{0.738}{26}$$

$$r_\pi = \frac{V_T \times R_E}{I_{CQ}}$$

$$g_m = 0.0284$$

$$r_\pi = 3.523 \text{ k}\Omega$$



$$R_i = R_1 \parallel R_2 \parallel R_{ib}$$

$$R_{ib} = r_\pi + (1 + \beta) R_E$$

$$R_{ib} = 3.523 \text{ k}\Omega + (0.1)(0.5 \text{ k}\Omega)$$

$$R_{ib} = 54.023 \text{ k}\Omega$$

$$R_i = R_{TH} \parallel R_{ib}$$

$$= 4.99 \text{ k}\Omega \parallel 54.023 \text{ k}\Omega$$

$$R_i = 4.486 \text{ k}\Omega$$

Series C equivalent ckt.

$$\therefore T_s = (R_s + R_p) \parallel C_s$$

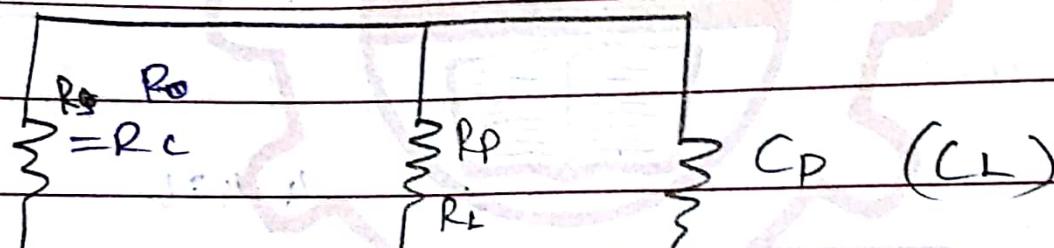
$$\text{Here, } T_s = \frac{(R_s + R_i) C_o}{(0.1 k + 4.486 k) 10 \mu}$$

$$T_s = 4.586 \times 10^{-3} \text{ s}$$

$$[T_s = 4.586 \text{ ms}]$$

$$f_L = \frac{1}{2\pi T_s} = \frac{1000}{2\pi \times 4.586}$$

$$f_L = 3.47 \text{ Hz}$$



$$R_o = R_c || r_o$$

$$R_o = R_c || r_o$$

$$T_p = (R_s || R_p) C_p$$

$$\text{here, } T_p = (R_c || R_L) C_L$$

$$= (5k || 10k) 15 \mu$$

$$= 3.33 \times 15 \times 10^{-9}$$

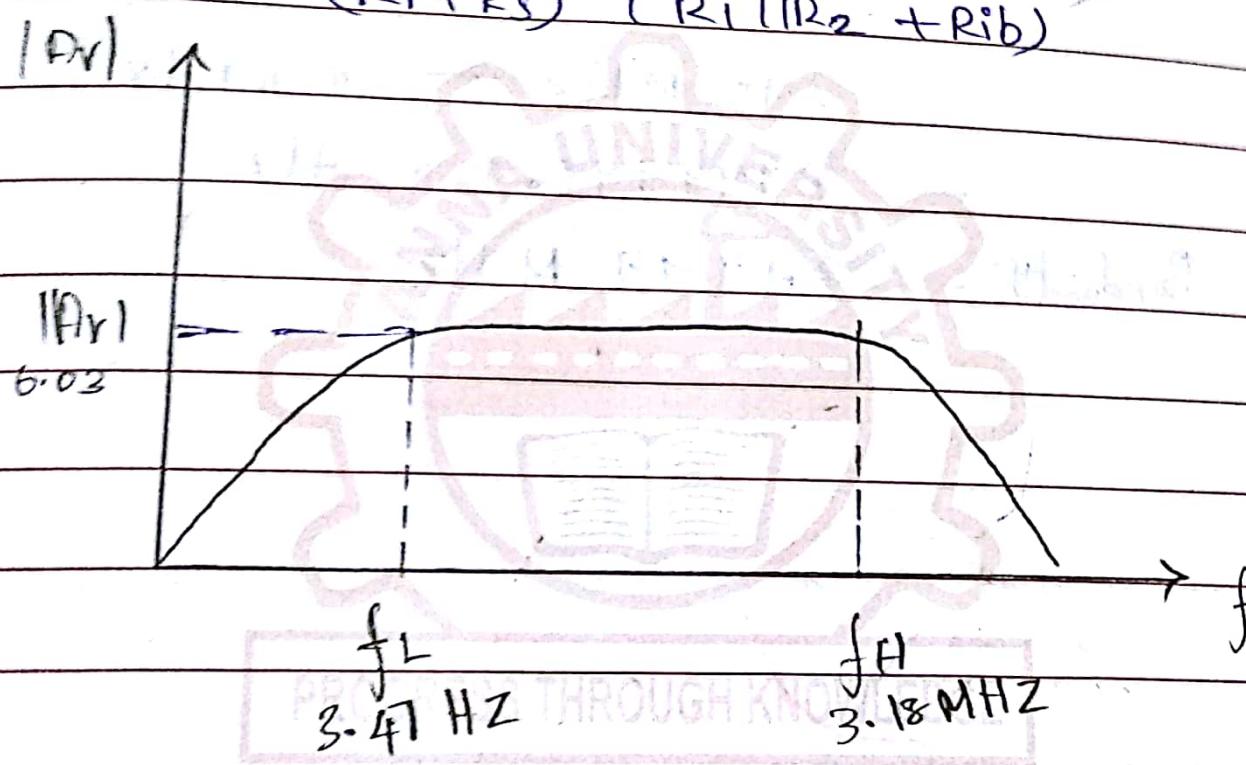
$$T_p = 50 \times 10^{-9} \text{ s}$$

$$f_H = \frac{1}{2\pi T_p} = \frac{10^9}{2\pi \times 50} (49.99) \text{ (approx)}$$

$$f_H = 3.18 \text{ MHz}$$

For maximum gain,
 S.C. coupling capacitor
 O.C. load capacitor

$$A_v = \frac{-g_m (R_c || R_L) (R_1 || R_2)}{(R_i + R_s) (R_1 || R_2 + R_{ib})}$$



Given, CE amplifier, with R_E

$$\therefore A_v = -\frac{\beta (R_c || R_L) \left(\frac{R_i}{R_i + R_s} \right)}{r_\pi + (1 + \beta) R_E}$$

$$R_i = 4.486 k\Omega \quad r_\pi = 3.523 k\Omega$$

$$\begin{aligned}
 \therefore |A_v| &= \frac{\beta (R_c || R_L) \left(\frac{R_i}{R_i + R_s} \right)}{r_\pi + (1 + \beta) R_E} = \frac{100 (\beta || 10) k}{(3.523 k) + (1 + \beta) R_E} \\
 &= \frac{100 \times 3.33 k}{54.023 k} \left(\frac{4.486 k}{4.486 k + 0.1 k} \right)
 \end{aligned}$$

$$|D_V| = 6.03$$

∴ mid band gain = 6.03

$$\text{Bandwidth} = f_H - f_L$$

$$= 3.18 \text{ MHz} - 3.47 \text{ Hz}$$

$$= 3179996.53 \text{ Hz}$$

$$\text{Bandwidth} = 3.1799 \text{ MHz}$$