

03-07-18

Chapter - 1

Number System .

1. Binary Number system
2. Decimal " "
3. Octal " "
4. Hexadecimal " "
(Hex)

2. Decimal $\Rightarrow 0, 1, 2, \dots, 9$

$$\begin{aligned}356 &= 3 \times 100 + 5 \times 10 + 6 \times 1 \\&= 3 \times 10^2 + 5 \times 10^1 + 6 \times 10^0\end{aligned}$$

Weights

Base or radix of decimal no. system = 10

1. Binary $\Rightarrow 0$ and 1

Base of no. is 2.

3. Octal $\Rightarrow 0, 1, 2, 3, 4, 5, 6, 7$

Base of system is 8

4. Hexadecimal $\Rightarrow 0, 1, 2, \dots, 10, 11, 12, 13, 14, 15$.

A B C D E F

Base of system is 16.

Conversion

1. of decimal base 10

Binary
(repeated division by 2)

$$\begin{array}{r} 2 | 356 \\ 2 | 178 - 0 \\ 2 | 89 - 0 \\ 2 | 44 - 1 \\ 2 | 22 - 0 \\ 2 | 11 - 0 \\ 2 | 5 - 1 \\ 2 | 2 - 1 \\ \hline 1 - 0 \end{array}$$

Octal
(repeated div by 8)

$$\begin{array}{r} 8 | 356 \\ 8 | 44 - 4 \\ 8 | 5 - 4 \\ \hline (544)_8 \end{array}$$

Hex.
(repeated \div 16)

$$\begin{array}{r} 16 | 356 \\ 16 | 22 - 4 \\ 16 | 1 - 6 \\ \hline (164)_{16} \end{array}$$

To octal

0.87

0.96

0.68

0.87

0.87

0.92

0.72

0.52

To hex

0.87

CONVERSI

(11011

Resultant

Binary value $\Rightarrow (101100100)_2$

Octal value $\Rightarrow (544)_8$

Hex value $\Rightarrow (164)_{16}$

2. 356.87

.87

To binary :-

$$0.87 \times 2 = 1.74$$

$$0.74 \times 2 = 1.48$$

$$0.48 \times 2 = 0.96$$

$$0.96 \times 2 = 1.92$$

$$0.92 \times 2 = 1.84$$

$$0.84 \times 2 = 1.68$$

1. Take only decimal value repeatedly

2. Take the integer value from top to bottom

$356.87 \Rightarrow$ binary $\Rightarrow (101100100.110111)_2$

To octal

.87

$$\begin{array}{r}
 0.87 \times 8 = 6.96 \\
 0.96 \times 8 = 7.68 \\
 0.68 \times 8 = 5.44
 \end{array}
 \text{upto } 5 \text{ values.}$$

$$\Rightarrow (544.675)_8$$

To hex

.87

$$\begin{array}{r}
 0.87 \times 16 = 13.92 \Rightarrow D.92 \\
 0.92 \times 16 = 14.72 \Rightarrow E.72 \\
 0.72 \times 16 = 11.52 \Rightarrow B.52 \\
 0.52 \times 16 = 8.32 \Rightarrow 8.32
 \end{array}$$

$$\Rightarrow (164.DEB8)_{16}$$

CONVERSION OF BINARY TO DECIMAL.

$$(110110)_2 \Rightarrow (54)_{10} \text{ [decimal]}$$

$$\begin{array}{r}
 0 \times 2^0 = 0 \\
 + \\
 1 \times 2^1 = 2 \\
 + \\
 1 \times 2^2 = 4 \\
 + \\
 0 \times 2^3 = 0 \\
 + \\
 1 \times 2^4 = 16 \\
 + \\
 1 \times 2^5 = 32 \\
 \hline
 54
 \end{array}$$

CONVERSION OF BINARY TO OCTAL.

$$1.9) \underline{(110110)_2} = (66)_8$$

↓ MSB ↓ LSB

OCTAL IN BINARY :-

0 - 000
1 - 001
2 - 010
3 - 011
4 - 100
5 - 101
6 - <u>110</u>
7 - 111

① Start from least significant bit
[last value]

(or) LS B
↓
bit

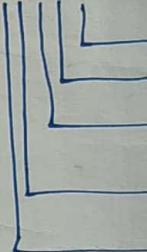
MSB \Rightarrow Most significant bit

② Group it in terms of 3 from right (LSB)

I. convert

1. 10110...
2. (16.5),
3. (26.24)
4. (DADA)

1. 10110-0



$$2.9) \underline{(001101111101)_2} = (1575)_8$$

CONVERSION OF BINARY TO HEXA DECIMAL.

0 - 0000	8 4 2 1 \rightarrow weight of binary
1 - 0001	
2 - 0010	
3 - 0011	
4 - 0100	
5 - 0101	
6 - 0110	
7 - 0111	
8 - 1000	
9 - 1001	
A - 1010	
B - 1011	
C - 1100	
D - 1101	
E - 1110	
F - 1111	

Group into 4

0.0
↓
0x2

2. (16.5)₁₆



0.5x

\Rightarrow

$$18) \underline{0110110}_2 = (36)_{16}$$

$$20) \underline{0110111101}_2 = (37D)_{16}$$

least
bit
value]

LSB
Bit

significant

terms
sign
(SB)

I convert the following numbers to DECIMAL

$$1. 10110.0101$$

$$2. (16.5)_{16}$$

$$3. (26.24)_8$$

$$4. (DADA.B)_{16}$$

$$1. 10110.0101$$

$$\begin{array}{r} | \\ 10110.0101 \\ | \quad | \\ 0 \times 2^0 \longrightarrow 0 \\ 1 \times 2^1 \longrightarrow 2 \\ 1 \times 2^2 \longrightarrow 4 \\ 0 \times 2^3 \longrightarrow 0 \\ 1 \times 2^4 \longrightarrow 16 \\ \hline 22 \end{array}$$

$$\begin{array}{r} 0101 \\ | \quad | \quad | \\ 0 \quad 1 \quad 0 \quad 1 \\ | \quad | \quad | \quad | \\ 2^0 \quad 2^1 \quad 2^2 \quad 2^3 \\ \frac{1}{2} + \frac{1}{4} \\ 22.3125 \end{array}$$

$$\begin{array}{r} 0.0101 \\ | \\ 0 \times 2^{-1} \quad | \quad | \\ 0 \times 2^{-3} \quad | \\ 1 \times 2^{-4} = \frac{1}{16} \\ 0 \times 2^{-2} \quad | \\ 1 \times 2^{-1} = \frac{1}{4} \end{array}$$

$$22 + \frac{1}{16} + \frac{1}{4} = (22.3125)_{10}$$

$$2. (16.5)_{16} \text{ to decimal}$$

$$\begin{array}{r} | \\ 6 \times 16^0 = 6 \\ | \\ 1 \times 16^1 = 16 \end{array}$$

$$0.5 \times 16^{-1} = 5/16$$

$$\Rightarrow 6 + 16 + 5/16 = (22.3125)_{10}$$

$$3. (26.24)_8$$

$$\begin{array}{r} \boxed{ } \\ \rightarrow 6 \times 8^0 \rightarrow 6 \\ \rightarrow 2 \times 8^1 \rightarrow 16 \end{array}$$

$$0.24$$

$$\begin{array}{r} \boxed{ } \\ \rightarrow 2 \times 8^{-1} = 2/8 \\ \rightarrow 4 \times 8^{-2} = 4/64 \end{array}$$

$$\Rightarrow 6 + 16 + 2/8 + 4/64 = \\ = 22 + 20/64 = 22 + 5/16 = (22.3125)_{10}$$

$$4. (DADA.B)_{16}$$

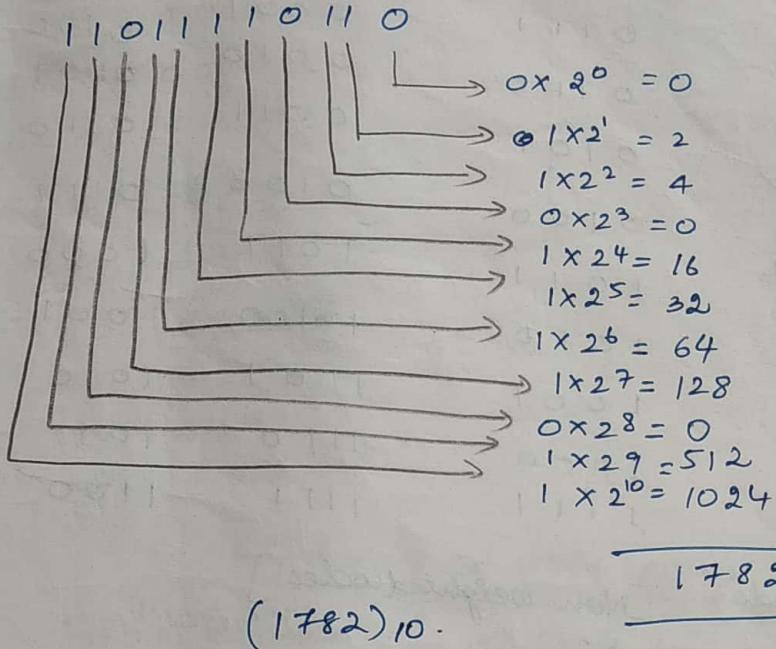
$$\begin{array}{c} D A D A . B \\ | | | | \downarrow \quad \downarrow \\ 13 \times 16^1 \quad 10 \times 16^0 \quad 11 \times 16^{-1} \\ | \quad | \quad | \\ 10 \times 16^2 \\ | \\ 13 \times 16^3 \end{array}$$

$$\Rightarrow 53248 + 2560 + 208 + 10 + 0.6875 \\ = (56026.6875)_{10}$$

6.7.18

1. 011011110110

to decimal.



TO hexa decimal $\rightarrow (6F6)_{16}$, TO octal $(3366)_8$



3. 011011110110
 $(6F6)_{16}$



$(3366)_8$

BINARY CODES

ASCII \rightarrow American Standard Code for Information Interchange

$\boxed{8421} \rightarrow$ Binary code $\Rightarrow 0 \text{ to } 15 \rightarrow$ Hexadecimal

84-2-1

$\checkmark 8421$

$\checkmark BCD$

$\checkmark Gray$

$\checkmark Biunary$

Exclss-3

Binary coded Decimal

8421

• BCD

8421

0 0000

1 0001

2 0010

3 0011

4 0100

5 0101

6 0110

7 0111

8 1000

9 1001

WEIGHTED CODES

84-2-1

0 0000

1 0001

2 0010

3 0101

4 0100

5 1011

6 1010

7 1001

8 1000

9 1111

Binary coded decimal

BCD

2421

84-2-1

0 0000

1 0001

2 0010

3 0011

4 0100

5 0101

6 0110

7 0111

8 1000

9 1100

(Non Weighted)

Excess 3

+3 to BCD

0 0041

1 0100

2 0101

3 0110

4 0111

5 1000

6 1001

7 1010

8 1011

9 1100

Bi quinary

Bi

50

0 01

1 01

2 01

3 01

4 01

5 10

6 10

7 10

8 10

9 10

• Gray code [Non weighted codes]

Reflected code (or) Unit distance code (or) cyclic

(0 to 15)

Excess-3

0011

0100

1011

1100

1101

1110

1111

010

110

110

sign

magn

f

+13 sign

-13 no.

0 0000
 1 0001
 2 0011
 3 0010
 4 0110
 5 0111
 6 0101
 7 0100
 8 1100
 9 1101
 10 1111
 11 1110
 12 1010
 13 1011
 14 1001
 15 1000

13 000

+13 000

-13 100

✓

MSB

38
 Non Weighted
 Excess 3
~~+3 to BCD~~

Biquinary (Weighted)

Bi quinary

0001	50	43210
0100	0	010001
0101	1	0100010
0110	2	0100100
0111	3	01000
1000	4	010000
1001	5	100001
1010	6	100010
1011	7	100100
1100	8	100100
1101	9	100000

Finding of ones parity.

01011000 → no of 1's is 3
 odd parity

11011000 → no of 1's is 4
 even parity.

Signed Numbers / Integers.

Sign magnitude form
 +13 (0)
 -13 (1)
 signed nos

One's complement
 (Diminished Radix Comp)
 + → same
 - → take complement
 1 → 0, 0 → 1

Decimal
 9's 10's
 (Diminished Radix)
 (Radix)
 → take complement
 1 → 0, 0 → 1
 add 1.

$$\begin{array}{r} 11110010 \\ + 1 \\ \hline 11110011 \end{array}$$

13	00001101	00001101
+13	00001101	00001101
-13	10001101	11110010

MSB add(1)

[Can be of 8 (or) 5 bit]

[In computers
 Subtraction is done
 in 2's complement]

BINARY ADDITION

A	B	CY	Truth Table
0	0	00	
0	1	00	
1	0	00	
1	1	10	

1011 = 11

$$\begin{array}{r} \text{19) } \quad \begin{array}{r} 1 \\ 0 \\ 1 \\ 1 \\ \hline 11010 \end{array} \\ \hline \end{array}$$

summation is more than
the required bit
it is called as
CARRY

$$\begin{array}{r} \text{29) } \quad \begin{array}{r} 1 \\ 1 \\ 0 \\ 1 \\ 1 \\ 0 \\ 1 \\ \hline 100111 \end{array} \\ \hline \end{array}$$

$$\begin{array}{r} 2 | 25 \\ 2 | 12 - 1 \\ 2 | 6 - 0 \\ 2 | 3 - 0 \\ \hline 1 - 1 \end{array}$$

$$\begin{array}{lll} \text{1-8) } & \begin{array}{l} \text{sign Mag.} \\ \hline \end{array} & \begin{array}{l} 1's \text{ comp} \\ \hline \end{array} & \begin{array}{l} 2's \text{ comp} \\ \hline \end{array} \\ & \begin{array}{l} 25 \\ 00011001 \\ +25 \\ 00011001 \\ -25 \\ 10011001 \end{array} & \begin{array}{l} 00011001 \\ 00011001 \\ 00011001 \\ 11100110 \\ \hline \end{array} & \begin{array}{l} 00011001 \\ 00011001 \\ 00011001 \\ 11100110 \\ \hline \end{array} \\ & & \begin{array}{l} +1 \\ \hline \end{array} & \begin{array}{l} 11100111 \\ \hline \end{array} \end{array}$$

BINARY SUBTRACTION

$$\begin{array}{r} 1011 \\ (-) \quad 1101 \\ \hline 1101 \end{array}$$

0
1
10
11
100

By 2's comp method.

$$\begin{array}{r} 13 \rightarrow 1101 \rightarrow 1101 \\ 11 - 1011 \qquad \qquad 0101 \\ \hline \end{array}$$

$$\underbrace{10010}_{\text{1's comp}}$$

$$\begin{array}{r} 11 \quad 1011 \quad 1011 \\ - 13 \quad 1101 \quad 0011 \\ \hline 11010 \rightarrow 2^{\text{'}} \end{array}$$

- Steps
1. first no. take as it is
 2. 2nd no. take 2's comp
 3. add both 1's comp

$$\begin{array}{r} 0100 \\ + \quad 1 \\ \hline 0101 \end{array}$$

2's comp

$$\begin{array}{r} 0010 \\ 0001 \\ + \quad 1 \\ \hline 0010 \end{array}$$

LOGIC GATES

AND

$$Y = A \cdot B$$

OR

$$Y = A + B \quad [\text{diff from binary addition}]$$

NOT

$$Y = \bar{A}$$

{ NAND

$$Y = \overline{A \cdot B} \quad \text{NOT + AND}$$

} basic gates

NOR

$$Y = \overline{A + B} \quad \text{NOT + OR}$$

} universal gates

XOR

$$Y = A \oplus B \Rightarrow \overline{AB} + B\overline{A}$$

Both are complements of each other.

X NOR

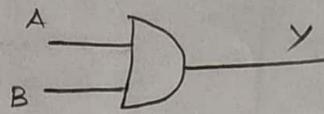
$$Y = A \odot B \Rightarrow AB + \overline{A}\overline{B}$$

$$\begin{aligned} \overline{A \oplus B} &= A \odot B \\ \overline{A \odot B} &= A \oplus B \end{aligned}$$

Symbols

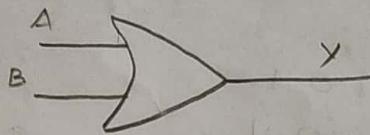
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AND

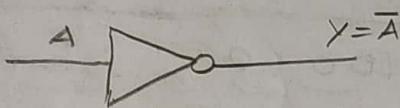


$$\text{AND} = Y$$

OR



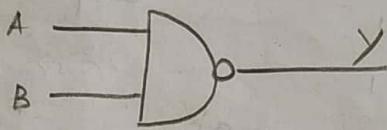
NOT



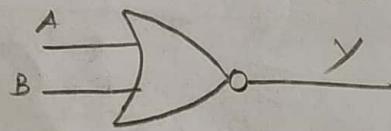
OR

A
0
0
1
1

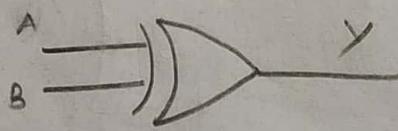
NAND



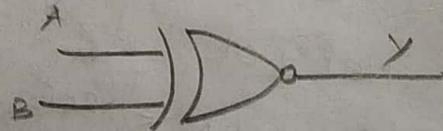
NOR



XOR



XNOR



Inver

A
0
1

N

A
0
0
1
1

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Logic gates

$$\text{AND} = Y = A \cdot B$$

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

XOR

A	B	Y = A \oplus B
0	0	0
0	1	1
1	0	1
1	1	0

OR

A	B	Y = A + B
0	0	0
0	1	1
1	0	1
1	1	1

XNOR

A	B	Y = A \odot B
0	0	1
0	1	0
1	0	0
1	1	1

Inverter (NOT)

A	B	Y = \bar{A}
0		1
1		0

NAND

A	B	Y = $\overline{A \cdot B}$
0	0	1
0	1	1
1	0	1
1	1	0

NOR

A	B	Y = $\overline{A + B}$
0	0	1
0	1	0
1	0	0
1	1	0

AND laws:-

$$A \cdot 0 = 0$$

$$A \cdot 1 = A$$

$$A \cdot A = A$$

$$A \cdot \bar{A} = 0$$

OR laws:-

$$A + 0 = A$$

$$A + 1 = 1$$

$$A + A = A$$

$$A + \bar{A} = 1$$

Double Inversion law:-

$$(A')' = \bar{\bar{A}} = A$$

Commutative laws:-

$$AB = BA$$

$$A+B = B+A$$

Associative laws:-

$$A(BC) = (AB)C$$

$$A+(B+C) = (A+B)+C$$

Distributive laws:-

$$A(B+C) = AB+AC$$

$$A+BC = (A+B)(A+C)$$

Absorption

$$A(A+B) = A$$

$$A+A = A$$

De Morgan

$$(A+B)' = \bar{A}\bar{B}$$

$$(AB)' = \bar{A}+\bar{B}$$

Boolean

$$Y = f(X)$$

Reduction

I. Use

$$1. \quad ?$$

$$2. \quad \alpha$$

$$3. \quad \beta$$

Answer

$$1. \quad x$$

$$2. \quad ?$$

$$= ?$$

$$= ?$$

Absorption law:

$$A(A+B) = A$$

$$A+AB = A$$

$$\begin{aligned} & \rightarrow A \cdot A + A \cdot B \\ &= A + A \cdot B \\ &= A(1+B) \\ &= A \end{aligned}$$

De Morgan's law:

$$(A+B)' = A'B'$$

$$(AB)' = A'B'$$

Boolean expression.

$$Y = A'B + B'CD$$

individuals are called as literals

Reduction of Boolean Expression.

1. Boolean laws (simple)
2. Karnaugh map. (complicated)
3. Tabulation method. (v. complicated)

I. Use Boolean laws & reduce the expression.

1. $xy + xy'$
2. $xyz + x'y + xy'z'$
3. $(a+b+c')(a'b'+c)$

Answers.

$$\begin{aligned} 1. \quad & xy + xy' \\ & x(y+y') = x \cdot 1 \\ & = x \end{aligned}$$

$$\begin{aligned} 2. \quad & xyz + x'y + xy'z' \\ & = xy(z+z') + x'y \\ & = xy + x'y \\ & = y(x+x') \\ & = y \cdot 1 = y \end{aligned}$$

$$3. (a+b+c')(a'b'+c)$$

$$\begin{aligned} &= aa'b' + a'b'b + a'b'c + ac + bc + \cancel{c'c} \\ &= 0 + 0 + a'b'c' + ac + bc \\ &= a'b'c' + ac + bc \quad // \end{aligned}$$

$$4. (BC' + A'D)(AB' + C'D')$$

$$\begin{aligned} &= \cancel{\underline{AB'}}\cancel{\underline{BC'}} + \cancel{\underline{BC'}}\cancel{\underline{CD'}} + \cancel{\underline{AA'}}\cancel{\underline{DB'}} + \cancel{\underline{A'DC'D'}} \\ &= 0 \end{aligned}$$

$$5. A'B(D' + c'D) + B(A + A'cD)$$

$$= A'BD' + \underline{A'BC'D} + BA + B\underline{A'C}\underline{D}$$

$$= \cancel{A'D}\cancel{BC'} +$$

$$= A'BD(C' + c') + A'BD' + BA$$

$$= A'BD + A'BD' + BA$$

$$= A'B(D + D') + BA$$

$$= A'B + BA$$

$$= B(A + A')$$

$$= B$$

$$6. (A' + c)(A' + c')(A + B + c'D) = A'(B + c'D)$$

$$= (A'A' + A'c' + cA' + \cancel{cc'}) (A + B + c'D)$$

$$= A'(A' + c' + c)(A + B + c'D)$$

$$= A'(\cancel{A'A} + A'B + A'c'D + c'A + c'B + c'c'D + AC + CB + \cancel{Cc'D})$$

$$= A'(\cancel{A'B} + \cancel{A'c'D} + \cancel{c'A} + \cancel{c'B} + \cancel{c'c'D} + \cancel{Ac} + \cancel{CB})$$

$$= A' [B(c + c') + A(c + c') + c'c'D + A'c'D + A'B]$$

$$= A' [B + A + c'c'D + A'c'D + A'B]$$

$$\begin{aligned} & (A' + c'c') \\ &= A'(A + c) \\ &= A'(B + c) \end{aligned}$$

Implementation

$$y = \underline{xy}$$

x —

y —

x —

y →

NAND

$$y = \overline{\overline{y}} =$$

x —

y —

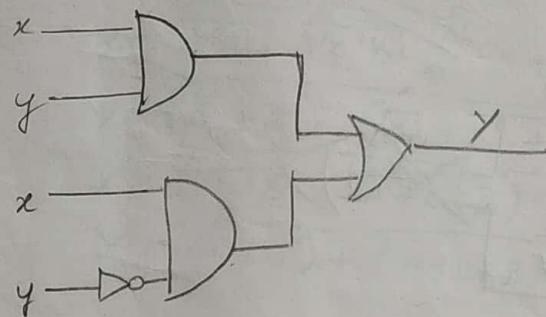
x —

y —

$$\begin{aligned}
 & (A' + cC') (A + B + C'D) \\
 &= A' (A + B + C'D) = A'A + A'B + A'C'D \\
 &= A'(B + C'D)
 \end{aligned}$$

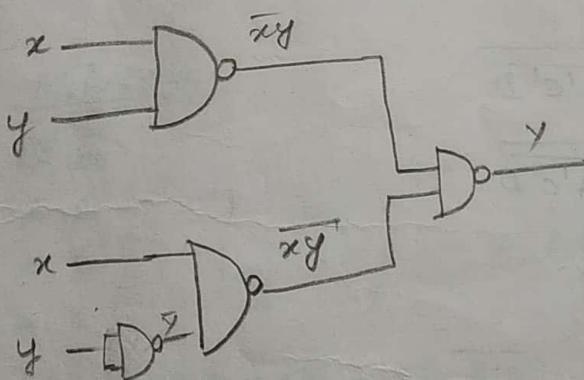
Implementation using Logic gates.

$$Y = \underline{xy} + \underline{x}y'$$



NAND

$$\begin{aligned}
 Y &= \overline{\overline{xy}} = \overline{\overline{xy} + \overline{x}y'} \\
 &= \overline{\overline{xy}} = \overline{\overline{xy} \cdot \overline{xy'}} \quad \text{NAND} \Leftrightarrow \text{NOR}
 \end{aligned}$$

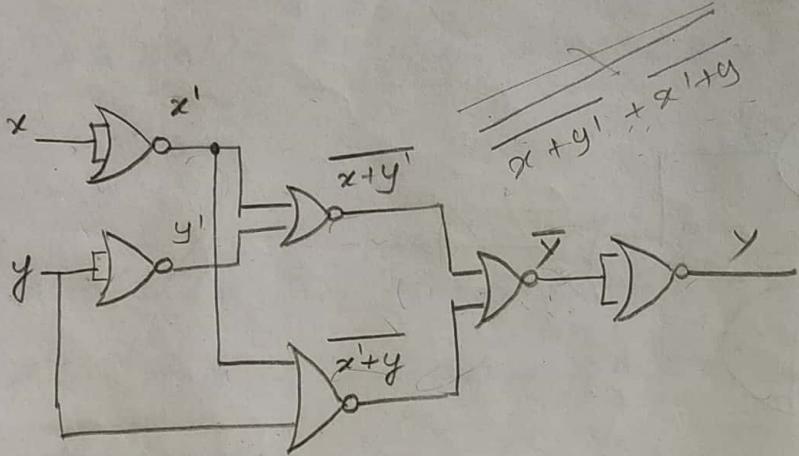


NOR.

$$\begin{aligned}
 y &= \overline{\overline{xy} \cdot \overline{x'y'}} \\
 &= \overline{(x'+y') (x'y)} \\
 &= \overline{(x'+y')} + \overline{(x'y)}
 \end{aligned}$$

($x' + y'$) [Avoid multiplication]

only NOR



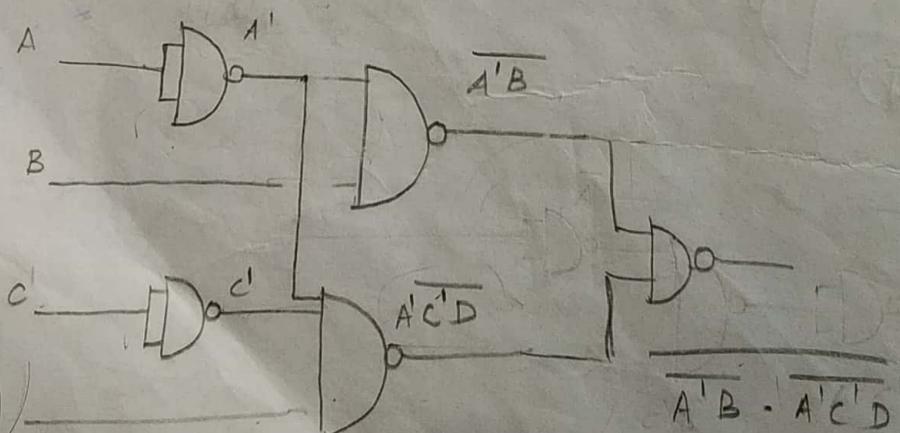
$$A'(B+C'D)$$

only NAND and only NOR.

\Rightarrow only NAND

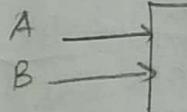
$$y = A'B + A'C'D$$

$$\begin{aligned}
 Y = \overline{\overline{y}} &= \overline{A'B + A'C'D} \\
 &= \overline{A'B} \cdot \overline{A'C'D}
 \end{aligned}$$



07.18

Ma



Min

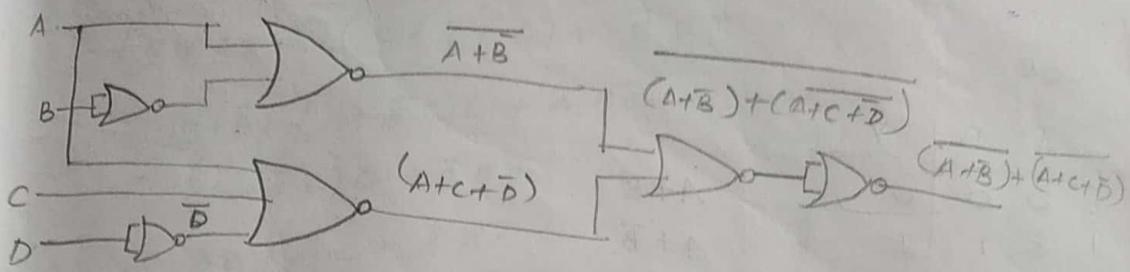
$\bar{A} \bar{B}$

$\bar{A} B$

$A \bar{B}$

$A B$

only NOR



$$Y = \overline{A'B}, \overline{A'C'D}$$

$$Y = (\bar{A} + \bar{B}) \cdot (\bar{A}' + \bar{C}' + \bar{D})$$

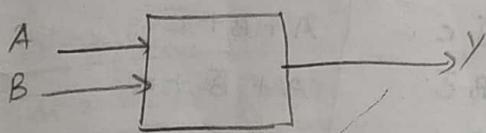
$$Y = (A + B) \cdot (A + C + \bar{D})$$

$$Y = (\bar{A} + \bar{B}) + (A + C + \bar{D})$$

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Maxterms and Minterms

OR



A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

Minterm:

$$\bar{A}\bar{B}$$

$$\bar{A}B$$

$$A\bar{B}$$

$$AB$$

0 → complemented

$$Y \bar{A} \text{ or } \bar{B}$$

canonical form → A (or) B

$$Y = \bar{A}B + A\bar{B} + AB \quad (\text{sum of pdts})$$

$$= B(\bar{A} + A) + A\bar{B}$$

$$= B + A\bar{B}$$

$$= (B + A)(\bar{B} + \bar{B})$$

$$= A + B \rightarrow \text{standard form}$$

→ consider only ones.

Max terms:

Sum of literals/variables

OR

A	B	y
0	0	0
1	0	1
2	1	1
3	1	1

$$A+B$$

$$A+\bar{B}$$

$$\bar{A}+B$$

$$\bar{A}+\bar{B}$$

0 → A un complemented
1 → A complemented
(or) B

Max:

$$(A+B+C)$$

$$= (B+\bar{A})$$

$$= (B+A)$$

$$= B$$

$$=$$

$$=$$

$$Y = A+B$$

(plot of sum)

→ consider zeros.

Q)

A	B	C	y	Min	Max
0	0	0	0	$\bar{A}\bar{B}\bar{C}$	$A+B+C$
1	0	0	1	$\bar{A}\bar{B}C$	$A+B+\bar{C}$
2	0	1	0	$\bar{A}B\bar{C}$	$A+\bar{B}+C$
3	0	1	1	$\bar{A}BC$	$A+\bar{B}+\bar{C}$
4	1	0	0	$A\bar{B}\bar{C}$	$\bar{A}+B+C$
5	1	0	0	$A\bar{B}C$	$\bar{A}+B+\bar{C}$
6	1	1	0	$AB\bar{C}$	$\bar{A}+B+\bar{C}$
7	1	1	1	ABC	$\bar{A}+\bar{B}+\bar{C}$

Max:

$$(A+B+C)$$

1. canonical

2. standard

sum
product

$$\begin{aligned}
 Y &= \bar{A}\bar{B}\bar{C} + \underline{\bar{A}\bar{B}\bar{C}} + \underline{\bar{A}B\bar{C}} + \underline{ABC} \\
 &= BC(\bar{A}+A) + \bar{A}\bar{B}C + \bar{A}B\bar{C} \\
 &= BC + \cancel{\bar{A}\bar{B}C} + \cancel{\bar{A}B\bar{C}} \\
 &= BC + \bar{A}(BC) \\
 &= \bar{A}B(C+\bar{C}) + C(\bar{A}\bar{B} + AB) \\
 &= \bar{A}B + C \\
 &= BC(\bar{A}+A) + \bar{A}\bar{B}C + \bar{A}B\bar{C} \\
 &= BC + \bar{A}\bar{B}C + \bar{A}B\bar{C}
 \end{aligned}$$

$$y = (A$$

$$= A$$

$$=$$

$\rightarrow A$ complemented
 $\rightarrow \bar{A}$ complemented
 (or) B

Max:

$$\begin{aligned}
 & (A+B+C)(\bar{A}+\bar{B}+C)(\bar{A}+\bar{B}+\bar{C})(\bar{A}+\bar{B}+C) \\
 & = (B+\bar{A}\bar{B}C)(C+\bar{A}\bar{B}C) + \bar{A}B\bar{C} \\
 & = (B+\bar{B})(B+\bar{A}C)C + \bar{A}B\bar{C} \\
 & = (B+\bar{A}C)C + \bar{A}B\bar{C} \\
 & = BC + \bar{A}(C+\bar{C})(C+B) \\
 & = BC + \bar{A}(B+C) \\
 & = BC + \bar{A}B + \bar{A}C
 \end{aligned}$$

std form
sum of pdt

Max:

$$(A+B+C)(\bar{A}+\bar{B}+C)(\bar{A}+\bar{B}+\bar{C})(\bar{A}+\bar{B}+C)$$

[pdts of max terms] canonical

1. canonical form:
2. standard form

sum of Minterms. [all the variables are present]

Product of max terms.

sum of products

product of sums.

Q.

$$y = (A+A\bar{B}) \rightarrow \text{sum of pdt [std form]}$$

$$= A(B+\bar{B}) + A\bar{B}$$

$$= AB + A\bar{B} + A\bar{B}$$

$$= AB + A\bar{B} \rightarrow \text{sum of min terms [canonical form]}$$

$$= \Sigma(2, 3)$$

$A+B$	$A+\bar{B}$
0 0	0 1
0	1

missing terms B means $B + \bar{B}$ takes

$B + \bar{B}$

takes

$$\begin{aligned}
 2. \quad y &= BC + \bar{A}B + \bar{A}C \rightarrow \text{sum of pdt} \\
 &= BC(A + \bar{A}) + \bar{A}B(C + \bar{C}) + \bar{A}C(B + \bar{B}) \\
 &= \underline{\underline{BCA}} + \underline{\underline{BC\bar{A}}} + \underline{\underline{\bar{A}BC}} + \underline{\underline{\bar{A}\bar{B}\bar{C}}} + \underline{\underline{\bar{A}CB}} + \underline{\underline{\bar{A}C\bar{B}}}
 \end{aligned}$$

$$\begin{aligned}
 &= ABC + \bar{A}BC + \bar{A}B\bar{C} + \bar{A}C\bar{B} \\
 &= \sum_m (1, 2, 3, 7)
 \end{aligned}$$

$$T_m = [(A+0+0)(\bar{A}+B+C)(\bar{A}+B+\bar{C})(\bar{A}+C+\bar{B})]$$

$$3. \quad y = (\bar{A} + \bar{B})(\bar{A} + B + \bar{C})(\bar{B} + C) \rightarrow \text{pdः of sum}$$

missing variable

$$\begin{aligned}
 &= (\bar{A} + \bar{B} + C\bar{C})(A + B + \bar{C})(A\bar{A} + \bar{B} + C) \rightarrow C\bar{C} \Rightarrow 0 \\
 &= (\bar{A} + \bar{B} + C)(\bar{A} + \bar{B} + \bar{C}) \not\in A + B + \bar{C} (A + \bar{B} + C) \\
 &\quad (A + \bar{B} + C) \\
 &= \prod_m (1, 2, 6, 7)
 \end{aligned}$$

$$Q. 4. \quad y = (c' + d)(b + c')$$

$$5. \quad y = (b + cd)(c + bd)$$

$\sum (3)$

6. convert

$$4. \quad y = (c' + d)(b + c')$$

$\Rightarrow \cancel{b\bar{c} + c}$

$$= (\bar{c} + d + b\bar{c})(b + \bar{c} + d\bar{d})$$

$$= (\bar{c} + d + b)(\bar{c} + d + \bar{b})(b + \bar{c} + d)(b + \bar{c} + \bar{d})$$

$$= \underbrace{(b + \bar{c} + d)}_2 (\underbrace{\bar{b} + \bar{c} + d}_6) (\underbrace{b + \bar{c} + d}_{\cancel{3}}) (\underbrace{b + \bar{c} + \bar{d}}_{\cancel{3}}) \quad (if) F(A, B, C, D)$$

$$= \prod_m (2, 3, 6)$$

$$= \sum_m (0, 1, 4, 5, 7)$$

6. convert
i) $f(x, y, z)$

$$\begin{aligned}
 \text{So } y &= (b+c\bar{d})(c+b\bar{d}) \\
 y &= \cancel{(b(c+\bar{c})(d+\bar{d}) + c\bar{d}(b+\bar{b}))} \\
 &\quad \cancel{(b+\bar{b})c(d+\bar{d}) + (c+\bar{c})b\bar{d}} \\
 &= (b+c)(b+d)(c+b)(c+d) \\
 &= (b+c+d\bar{d}) \{ b\bar{d} + d + c\bar{c} \} (c+b+d\bar{d}) \{ c+d + b\bar{b} \} \\
 &= \cancel{(b+c+d)} \cancel{(b+c+\bar{d})} \cancel{(b+c+d)} \cancel{(b+\bar{c}+\bar{d})} \\
 &\quad \cancel{(b+c+d)} \cancel{(b+c+\bar{d})} \cancel{(b+c+d)} \cancel{(b+\bar{c}+\bar{d})} \\
 &= \pi(0, 1, 2, 4)
 \end{aligned}$$

$$= \Sigma(3, 5, 6, 7) = \pi(0, 1, 2, 4)$$

6. convert

6. convert to other canonical form. 0 - 8

$$\begin{aligned}
 \text{(i) } f(x, y, z) &= \Sigma(1, 3, 5) \rightarrow \pi(0, 2, 4, 6, 7, \cancel{8}) \\
 f(xyz) &= (\cancel{x}\cancel{y}z + \cancel{x}yz + x\cancel{y}z) \\
 &\quad \cancel{8} \quad \cancel{3} \quad \cancel{5}
 \end{aligned}$$

$$\begin{aligned}
 \text{(ii) } F(A, B, C, D) &= \pi(3, 5, 8, 11) \\
 &= \Sigma(0, 1, 2, 4, 6, 7, 9, 10, 12, 13, 14, 15)
 \end{aligned}$$

$\pi \Leftarrow \Sigma$

complemental to each other

$$F(A, B, C, D) = \prod (3, 5, 8, 11)$$

Karnaugh Map (K-Map)

Variables -

Q)

	2	1	B	$\bar{B}(0)$	$B(1)$
	A	\bar{A}	$\bar{A}\bar{B}$	$\bar{A}B$	AB
0	\bar{A}	0	0	1	
1	A	1	\bar{A}	AB	1

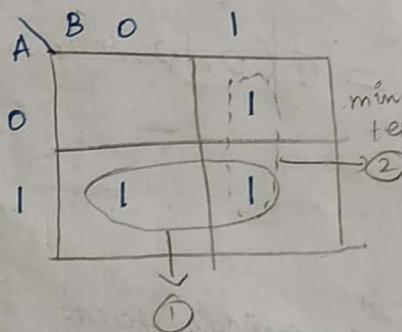
$A \rightarrow \text{MSB}$

$B \rightarrow \text{LSB}$

$\Rightarrow 2$ variable
K-map

Truth table:

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1



STEPS:

[consider

adjacent ones]

\Rightarrow only in vertical (or)
horizontal way.

\Rightarrow consider in
powers of 2
(ie) 1, 2, 4, 8, 16...

\Rightarrow group the higher
no. of adjacent
ones.

① $\rightarrow A$

② $\rightarrow B$

$$Y = A + B$$

1			1
1		1	1

due to folding & combinations
are possible

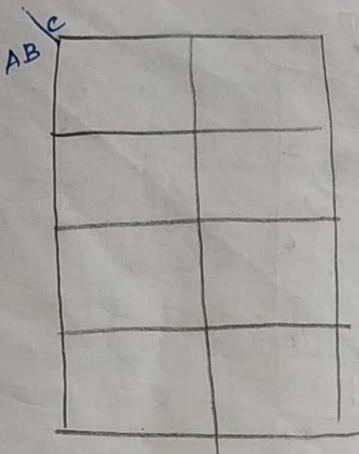
$$F = \bar{C} + AB$$

A	BC
\bar{A}	O
A	1

$$Y = B$$

3 Variable form

[adjacent box \rightarrow 1 bit variation]



		A\BC	00	01	101	10
		0	$\bar{A}\bar{B}C$	$\bar{A}\bar{B}C$	$\bar{A}B\bar{C}$	$\bar{A}B\bar{C}$
		1	$A\bar{B}\bar{C}$	$A\bar{B}C$	ABC	$A\bar{B}C$
(or)	A	0	0	1	3	2
		1	4	5	7	6

Q)

	A	B	C	Y
0	0	0	0	0
1	0	0	1	1
2	0	1	0	1
3	0	1	1	1
4	1	0	0	0
5	1	0	1	0
6	1	1	0	1
7	1	1	1	1

		BC\B̄C	00	01	101	10
		0	1	1	1	1
		1	0	1	1	1
	A	0	0	1	1	1
		1	4	5	7	6

$$Y = \bar{A}C + \bar{A}B + BC$$

1. $F(x, y, z) = \Sigma(3, 4, 5, 7)$

		BC\B̄C	00	01	11	10
		0	0	1	1	1
		1	1	1	1	1
	A	0	0	1	1	1
		1	4	5	7	6

$$Y = BC + \cancel{\bar{A}C} + \bar{A}\bar{B} + \cancel{\bar{A}C}$$

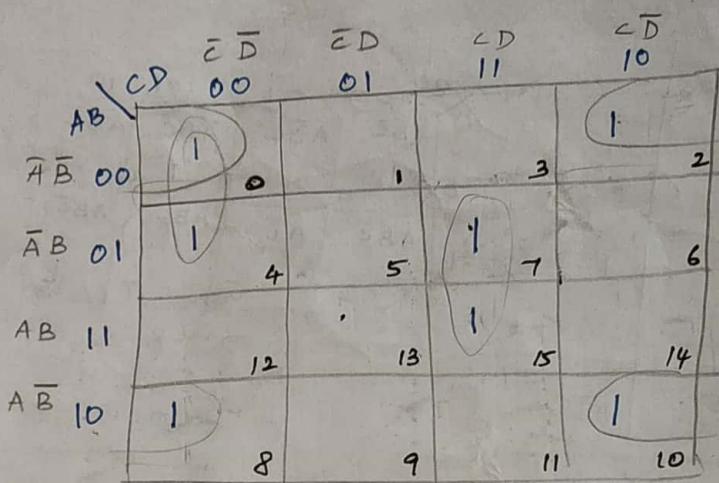
including
or excluding
give the same
value

$\boxed{1 \ 5 \ 7}$
redundant term

[not necessary]

4 Variable Map

- 16 square boxes.

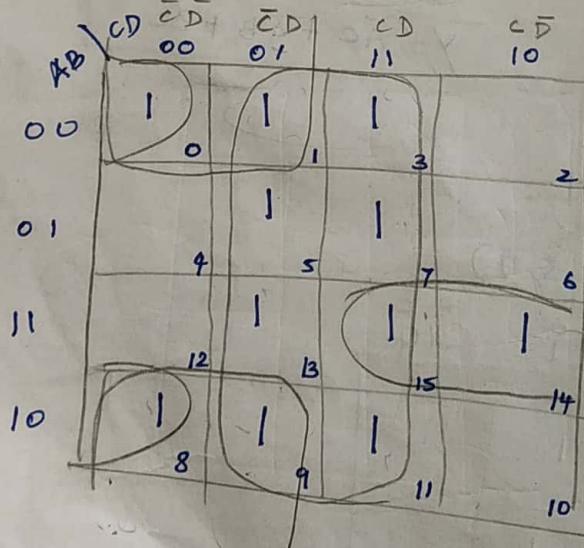


$$Y = \overline{B} \overline{D} + \overline{A} \overline{C} \overline{D} + B \overline{C} D$$

17.07.18

Reduce the boolean expression using k-map.

1. $F(A, B, C, D) = \sum(0, 1, 3, 5, 7, 8, 9, 11, 13, 14, 15)$



$$Y = \overline{B} \overline{C} \overline{D} + \overline{D} + ABC$$

2. $F(A, B, C, D)$

$$\begin{array}{cccc} 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{array}$$

$$\begin{array}{cccc} AB & CD & 0 & 0 \\ AB & CD & 0 & 1 \\ AB & CD & 1 & 0 \\ AB & CD & 1 & 1 \end{array}$$

3. $F(w, x, y)$

$$\begin{array}{cccc} w & x & y & z \\ \overline{w} \overline{x} & 00 & & \\ \cancel{w} \cancel{x} & 01 & & \\ w \cancel{x} & 11 & & \\ \overline{w} x & 10 & & \end{array}$$

$$= w \bar{x} y (z)$$

$$= \cancel{w} w \bar{x}$$

$$(x w -$$

$$= \cancel{w} \cancel{x} y z$$

$$x w y \bar{z}$$

$$\overline{w} \bar{x} x$$

$$2. F(A, B, C, D) = \prod (5, 6, 7, 9, 10, 11, 13, 15) \\ = \sum (0, 1, 2, 3, 4, 8, 12, 14)$$

0 0 1 1 A B
1 0 1 A B
1 0 0 A B
0 1 1 A B

		CD			
		00	01	11	10
AB	00	1	1	1	1
	01	1	0	0	0
11	00	1	0	0	1
	10	1	0	0	0

$$= \bar{A}\bar{B} + \bar{C}\bar{D} + A\bar{B}\bar{D}$$

$$= (\bar{B}+\bar{D})(\bar{A}+\bar{D})(\bar{A}+\bar{B}+\bar{C})(\bar{A}+\bar{B}+\bar{C})$$

$$3. F(w, x, y, z) = w\bar{x}y + \bar{x}\bar{y}\bar{z} + y\bar{z} + \bar{w}\bar{z}$$

		yz			
		00	01	11	10
wx	00	1	0	1	2
	01	1	4	5	6
wx	11	12	13	15	14
	10	1	8	9	11

~~wxyz~~

~~y = w~~

$$y = y\bar{z} + \bar{w}\bar{z} +$$

$$w\bar{x}y$$

$$y = y\bar{z} + w\bar{x}y + \bar{w}\bar{z} + \bar{x}\bar{z}$$

$$= w\bar{x}y(z+\bar{z}) + \bar{x}\bar{y}\bar{z}(w+\bar{w}) + (x+\bar{x})(w+\bar{w})y\bar{z} + \bar{w}\bar{z}(x+\bar{x})(y+\bar{y})$$

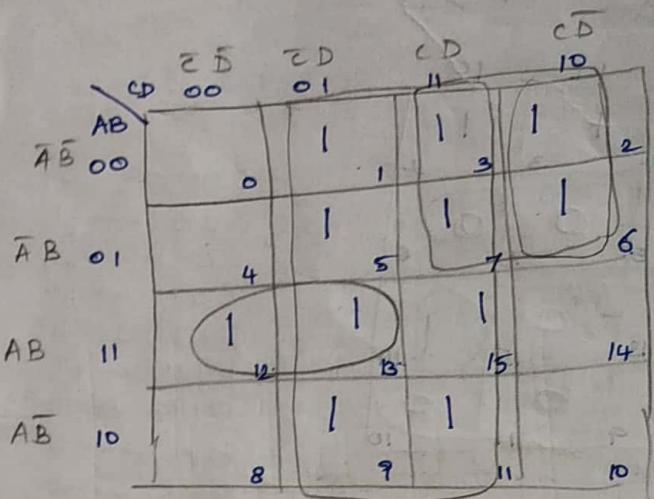
$$= w\bar{x}yz + w\bar{x}y\bar{z} + \bar{x}\bar{y}\bar{z}w + \bar{x}\bar{y}\bar{z}\bar{w} + (xw+x\bar{w}+\bar{x}w+\bar{x}\bar{w})y\bar{z} + \bar{w}\bar{z}(xy+x\bar{y}+\bar{x}y+\bar{x}\bar{y})$$

$$= \cancel{w\bar{x}yz} + w\bar{x}y\bar{z} + \bar{x}\bar{y}\bar{z}w + \bar{x}\bar{y}\bar{z}\bar{w} + xw\bar{y}\bar{z} + x\bar{w}y\bar{z} + \bar{x}wy\bar{z} + \bar{x}\bar{w}y\bar{z} + \bar{w}\bar{z}xy + \bar{w}\bar{z}x\bar{y} + \bar{w}\bar{z}\bar{x}y + \bar{w}\bar{z}\bar{x}\bar{y}$$

$$(11, 15, 8, 0, 14, 6, 10, 2, 5, 4, 2, 0)$$

$$(0, 1, 2, 4, 8, 6, 8, 10, 11, 14)$$

$$4. F = \sum (1, 2, 3, 5, 6, 7, 9, 11, 12, 13, 15)$$



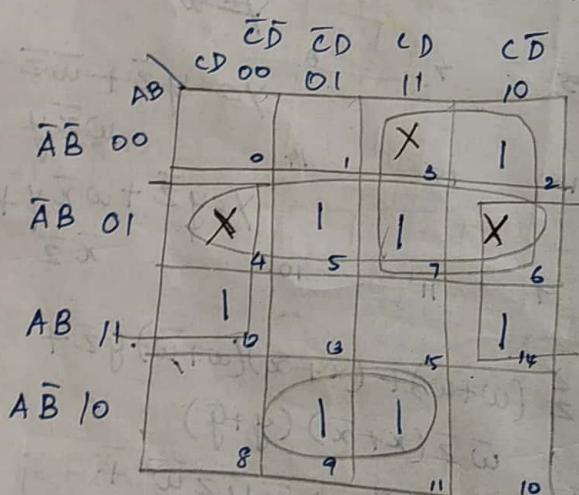
$$Y = D + \bar{A}C + ABC$$

20/07/18

K-map with don't care. 'X'.

$$1. F () = \sum_m (2, 5, 7, 9, 11, 12, 14) + \sum_d (3, 4, 6)$$

↙
don't care. 'X'



$$F = \bar{A}B + \bar{A}C + B\bar{D} + A\bar{B}D$$

28)

$$F = \bar{B}\bar{C}Y$$

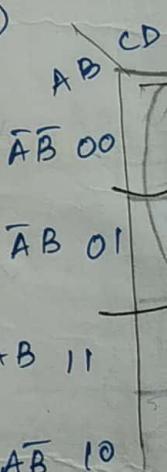
$$30. F(ABCD)$$

$$29. F = \bar{x}$$

$$x_0$$

$$x_1$$

30)



$$Y = \bar{A}$$

$$Y = A$$

28)

$$F = \bar{x}\bar{y}z + x\bar{y}\bar{z} + x\bar{y}z$$

38. $F(ABCD) = \sum (0, 6, 8, 13, 14) -$
 $D(ABCD) = \sum (2, 4, 10)$

29). $F = \bar{x}yz + x\bar{y}\bar{z} + x\bar{y}z$

	$\bar{y}\bar{z}$ 00	$\bar{y}z$ 01	$y\bar{z}$ 11	yz 10
$\bar{x}0$	0	3	1	2
$x1$	1	1	5	7
	4		7	6

$$Y = x\bar{y} + \bar{x}yz$$

39)

	$\bar{C}\bar{D}$ 00	$\bar{C}D$ 01	CD 11	$C\bar{D}$ 10
$\bar{A}\bar{B}00$	1	0	3	2
$\bar{A}\bar{B}01$	X	4	5	6
$A\bar{B}11$	12	13	15	14
$A\bar{B}10$	8	9	11	10

No need to map all x.

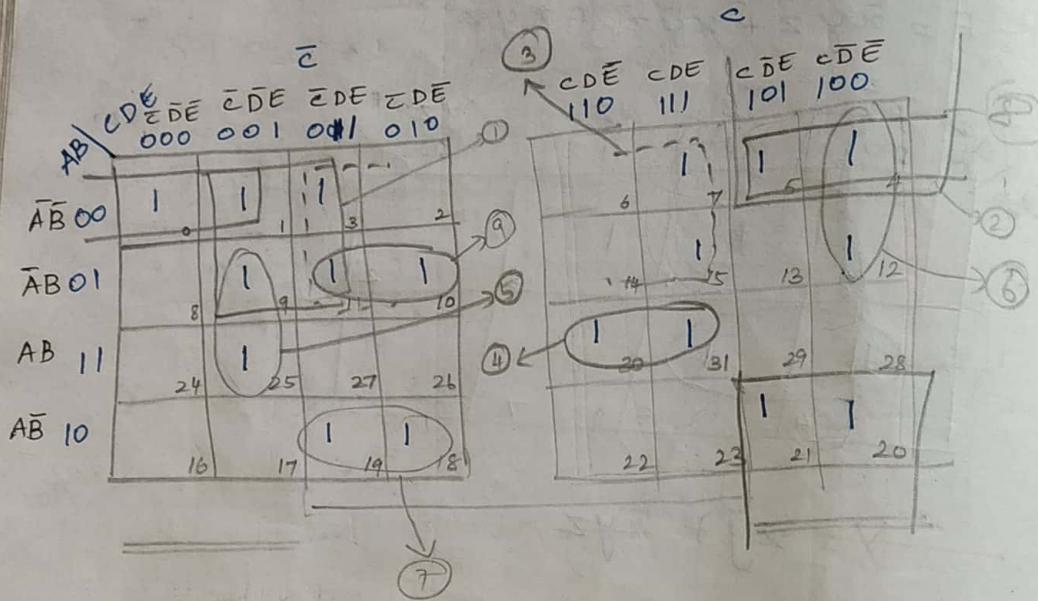
~~$$Y = \bar{A}\bar{C}\bar{D} + A.B\bar{C}D + \bar{B}\bar{C}\bar{D} \quad \bar{B}\bar{D} + \bar{A}\bar{D} + C\bar{D}$$~~

~~$$Y = ABCD + \bar{B}\bar{D} + \bar{A}\bar{D} + C\bar{D}$$~~

5 VARIABLE MAP. (0-31)

Q. $F = \sum (0, 1, 3, 5, 7, 9, 10, 11, 12, 15, 18, 19, 20, 21, 25, 30, 31)$

$F = \overline{CDE} + A$

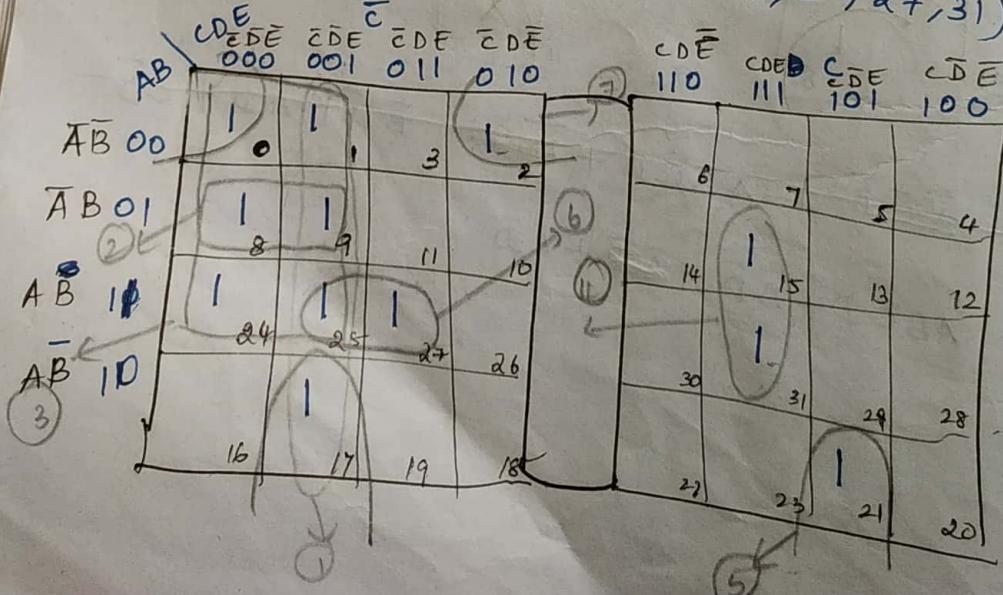


$$F = \overline{ACE} + \overline{AB}\overline{D} + \overline{ADE} + ABCD + B\overline{CDE} + \overline{A}\overline{CDE} + \\ A\overline{B}\overline{CD} + \overline{B}\overline{C}\overline{D} + \overline{ABC}\overline{D}$$

TABULATION METHOD

5 Variable (Quine McHaleky Method)

Q. $F = \sum (0, 1, 2, 8, 9, 15, 17, 21, 24, 25, 27, 31)$



(Q.M.H.)

Q. Total
6 groups

0
1
2
8
9
17
24
21
25
15
27
31

Iteration

$$F = \cancel{E\bar{D}C} + \bar{A}\bar{C}\bar{D} + B\bar{C}\bar{D} + BCDE + A\bar{B}\bar{D}E + A\bar{B}\bar{C}E + \\ \bar{A}\bar{B}\bar{C}\bar{E}$$

TABULATION METHOD

(Quine McCluskey Method)

[consider the highest number]

→ convert into binary

→ group with no of ones

(-) → don't care symbol.

Iteration - 1

Q.

Total
6 groups

	A	B	C	D	E	
0	0	0	0	0	0	✓
1	0	0	0	0	1	✓
2	0	0	0	1	0	✓
8	0	1	0	0	0	✓
9	0	1	0	0	1	✓
17	1	0	0	0	1	✓
24	1	1	0	0	0	✓
21	1	0	1	0	1	
25	1	1	0	0	1	✓
15	0	1	1	1	1	✓
27	1	1	0	1	1	✓
31	1	1	1	1	1	✓

Iteration - 2

Iteration - 1

(0, 1)	0000 - ✓
(0, 2)	000 - 0
(0, 8)	0 - 000 ✓
(1, 9)	0 - 001 ✓
(1, 17)	- 0001 ✓
(8, 9)	0100 - ✓
(8, 24)	- 1000
(9, 25)	- 1001 ✓
(17, 21)	10 - 01
(17, 25)	1 - 001 ✓
(24, 25)	1100 -
(25, 27)	110 - 1
(15, 31)	- 111 1
(27, 31)	11 - 11

Iteration 2

(0, 1, 8, 9)	0 - 00 -
(0, 8, 17, 25)	0 - 00 -
(1, 9, 17, 25)	-- 001
(1, 17, 9, 25)	- 001
(8, 9, 24, 25)	- 100 -
(8, 24, 9, 25)	100 -

steps

1. Single
entry from
each column

Prime Implicants

(0, 2)	$\bar{A} \bar{B} \bar{C} \bar{E}$
(17, 21)	$A \bar{B} \bar{D} E$
(28, 27)	$A \bar{B} \bar{C} E$
(15, 31)	$B C D E$
(27, 31)	$A B D E$
(0, 1, 8, 9)	$\bar{A} \bar{C} \bar{D}$
(1, 9, 17, 25)	$\bar{C} \bar{D} E$
(8, 9, 24, 25)	$B \bar{C} \bar{D}$

nts	Minterm	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	
(0, 2)	0	✓	?	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31

P. Implicants	Minterm	0	1	2	8	9	15	17	21	24	25	27	31	steps
$\bar{A}\bar{B}\bar{C}\bar{E}$	(0, 2) \odot	x	*	(x)										1. Single entry from each column should be selected as essential P.I
$A\bar{B}\bar{D}E$	(17, 21) \odot				x	(x)								2. They have to be marked & put a tick mark
$\bar{A}\bar{B}\bar{C}E$	(25, 27)						x		x					3. their min terms are selected and ticked [on the top]
$B\bar{C}DE$	(15, 31) \odot									x				4. The left over values are denoted as (?)
$\bar{A}BDE$	(27, 31)									x				(i.e) 1, 27
$\bar{A}\bar{C}\bar{D}$	(0, 1, 8, 9)	x	x	x	x	x	x	x	x	x	x	x		
$\bar{C}\bar{D}E$	(1, 9, 17, 25)	x	x	x	x	x	x	x	x	x	x	x		
$B\bar{C}\bar{D}$	(8, 9, 24, 25)													

$$P =$$

$$\bar{A}\bar{B}\bar{C}\bar{E} + A\bar{B}\bar{D}E + BCDE + A\bar{C}\bar{D} + B\bar{C}\bar{D}$$

$$2. F = \{1, 3, 4, 5, 10, 11, 12, 13, 14, 15\}$$

	A	B	C	D
1	0	0	0	1
3	0	0	1	1
4	0	1	0	0
5	0	1	0	1
10	1	0	1	0
11	1	0	1	1
12	1	1	0	0
13	1	1	0	1
14	1	1	1	0
15	1	1	1	1

[separate according to
no. of 1's]

PRIME impl.

(4, 5, 12, 1)

(10, 11, 14,

(12, 13, 14

(1, 3) -

(1, 5) -

(3, 11)

P.I	Mint
$\bar{A}\bar{B}D$	(1
$\bar{A}C\bar{D}$	(1
$\bar{B}C\bar{D}$	(1
$B\bar{C}$	(1
AC	(1
AB	(1

	A	B	C	D	Iteration-I	Iteration-II
					ABC'D	ABC'D
✓1	0	0	0	1	(1, 3) 00-1	(4, 5, 12, 13) -10-
✓4	0	1	0	0	(1, 5) 0-01	(4, 12, 5, 13) -10-
✓3	0	0	1	1	(4, 5) 010- ✓	(10, 11, 14, 15) 1-1-
✓5	0	1	0	1	(4, 12) -100 ✓	(10, 14, 11, 15) 1-1-
✓10	1	0	1	0	(3, 11) -011	(12, 13, 14, 15) 11--
✓12	1	1	0	0	(5, 13) -101 ✓	(12, 14, 13, 15) 11--
✓11	1	0	1	1	(10, 14) 1-10 ✓	
✓13	1	1	0	1	(12, 13) 110- ✓	
✓4	1	1	1	0	(12, 14) 11-0 ✓	
✓5	1	1	1	1	(1, 15) 1-11 ✓	
✓15	1	1	1	1	(13, 15) 11-1 ✓	
					(14, 15) 111- ✓	

PRIME implicants:-

$$(4, 5, 12, 13) \rightarrow B\bar{C}$$

$$(10, 11, 14, 15) \rightarrow AC$$

$$(12, 13, 14, 15) \rightarrow AB$$

$$(1, 3) \longrightarrow \bar{A}\bar{B}D$$

$$(1, 5) \longrightarrow \bar{A}\bar{C}D$$

$$(3, 11) \longrightarrow \bar{B}CD$$

1
3
4
5
10
11
12
13
14
15

P.I	Minterm	1	3	4	5	10	11	12	13	14	15
$\bar{A}\bar{B}D$	(1, 3)	x	x								
$\bar{A}\bar{C}D$	(1, 5)	x		x							
$\bar{B}CD$	(3, 11)		x			x					
$B\bar{C}$	(4, 5, 12, 13)			x	x			x	x		
AC	(10, 11, 14, 15)				x	x			x	x	
AB	(12, 13, 14, 15)						x	x	x	x	

$$\Rightarrow \bar{A}\bar{B}D + B\bar{C} + AC$$

27.7.18

HW

$$Q. F = (A, B, C, D) = \Sigma_m (0, 6, 8, 13, 14)$$

$$d (A, B, C, D) = \Sigma_d (2, 4, 10)$$

Follow the same procedure for both Σ
Exclude don't care in PI table.

		Iteration - I	Iteration - II
0	0000	(0, 2) 00-0✓	(0, 2, 4, 6) 0--0
1	0010	(0, 4) 0-00✓	(0, 2, 8, 10) -0-0
4	0100	(0, 8) -000✓	(0, 4, 2, 6) 0- -0
8	1000	(2, 6) 0-10✓	(2, 8, 2, 10) -0-0
6	0110	(4, 6) 01-0✓	(2, 6, 10, 14) - -10
10	1010	(6, 14) -110✓	(2, 10, 6, 14) - -10
13	1101	(10, 14) 1-10✓	
14	1110		

(Neglect the don't care terms in the table)

P.I

$$(0, 2, 4, 6) \rightarrow \bar{A}\bar{D}$$

$$(0, 2, 8, 10) \rightarrow \bar{B}\bar{D}$$

$$(2, 6, 10, 14) \rightarrow \bar{C}\bar{D}$$

$$0, 2, 4, 6, 8, /10, 14$$

P.I	Minterms	0	6	8	14	13
$\bar{A}\bar{D}$	(0, 2, 4, 6)	X	X			
$\bar{B}\bar{D}$	(0, 2, 8, 10)	X		X		
$\bar{C}\bar{D}$	(2, 6, 10, 14)		X		X	
$A\bar{B}\bar{C}\bar{D}$	13					X

$$ABC\bar{D} + \bar{A}\bar{D} + \bar{B}\bar{D} + C\bar{D}$$

7.7.18

Tutorial on Unit -1.

-

1. Do the following conversion:

- convert $(27.315)_{10}$ to binary
- $\leftrightarrow (C3DF)_{16}$ to binary
- $(26.24)_8$ to decimal
- $(DADA.B)_{16}$ to decimal

2. Obtain 1's and 2's complement of the number.

- 11011010
- 1010.1101

3. e. Perform subtraction using 2's complement of the subtrahend

- $1001 - 110101$
- $101000 - 10101$

4. Convert Perform the binary equivalent of 49 and 29 (of base 10) using signed 2's complement representation.

Then perform

- $(-29) + (+49)$
- $(-29) + (-49)$

convert the answer back to decimal and verify the result.

5. Convert the binary 1101110 to gray code.

6. Reduce the Boolean expression using boolean law.

A] $(A' + C)(A' + C')(A + B + C'D)$

for the reduced ^{eqn} draw circuit using universal gates.

7. Express the function

$(cd + b'c + bd')$ (b+d) sum of min terms &
pdt of max terms (canonical form)

8. Express convert A.F(x,y,z) = $\sum(1,3,5)$
to other canonical form.

B. $F(A,B,C,D) = \Pi(3,5,8,11)$

9. Convert:

A. $(u+xw)(x+u'v)$ into sum of pdt
and pdt of Scem (standard form)

10. Reduce using k-map

A. $F(w,x,y,z) = \sum(2,3,12,13,14,15)$

B. $F = w'z + xz + x'y + wz'$

c.

11. Using Tabulation method find the
reduced expression

A. $F = \sum(1,3,4,5,10,11,12,13,14,15)$

B. $F = \sum(5,6,7,12,14,15)$

$d = \sum(3,9,11,15)$

Verify the results using k-map.

A. (27.315)

2	27
2	13
2	6
2	3
	1

.315 X2

.63 X2

.26 X2

.52 X

.04 X

(27.315)

B. (C3D)

12

12

ANSWERS. for Tutorial on Unit -1

I. A. $(27.315)_{10} \rightarrow (11011.0101)_2$

$$\begin{array}{r} 27 \\ 2 | \quad \quad \\ 13 - 1 \\ 2 | \quad \quad \\ 6 - 1 \\ 2 | \quad \quad \\ 3 - 0 \\ 1 - 1 \end{array}$$

$$.315 \times 2 = 0.63$$

$$.63 \times 2 = 1.26$$

$$.26 \times 2 = 0.52$$

$$.52 \times 2 = 1.04$$

$$.04 \times 2 = 0.08$$

$$(27.315)_{10} \Rightarrow (11011.0101)_2$$

B. $(C3DF)_{16}$ to binary.

A	B	C	D	E	F
10	11	12	13	14	15

$$\begin{aligned} 15 \times 16^0 &= 15 \\ 13 \times 16^1 &= 208 \\ 3 \times 16^2 &= 768 \\ 12 \times 16^3 &= 49152 \end{aligned}$$

$$\begin{aligned} 15 \times 16^0 &= 15 \\ 13 \times 16^1 &= 208 \\ 3 \times 16^2 &= 768 \\ 12 \times 16^3 &= 49152 \end{aligned}$$

(or) $\underline{(1100\ 0011\ 1101\ 1111)_2} \quad (50143)_{10}$

C. $(26.24)_8$ to decimal:

$$\begin{array}{r} 26 \\ \times 8 \\ \hline 6 \\ + 2 \times 8^1 = 16 \\ \hline 22 \end{array}$$

$\cdot 24$

$$\begin{array}{r} 4 \times 8^{-1} = 0.5 \\ 2 \times 8^{-2} = 0.03125 \\ \hline 0.53125 \end{array}$$

$$(26.24)_8 = (22.053125)_{10}$$

D. $(DADA.B)_{16}$ to decimal:

$$\begin{array}{r} D A D A \\ | | | | \\ 10 \times 16^0 = 10 \\ 13 \times 16^1 = 208 \\ 10 \times 16^2 = 2560 \\ 13 \times 16^3 = 53,248 \\ \hline 56,027.6875 \end{array}$$

$$(DADA.B)_{16} = (56027.6875)_{10}$$

1's & 2's complement

A. 11011011

1's \rightarrow 0

2's

2's \rightarrow -

B. 1010.110

1's \rightarrow 2's

2's

3. Subtraction

A. 1001

0

(+) 0

0

B. 10100

(+) 0

1

2. 1's & 2's complement.

A. 11011010

$$1's \rightarrow 001\ 00101$$

2's

$$\begin{array}{r} 2's \rightarrow \\ + 1 \\ \hline 00100110 \end{array}$$

B. 1010.1101

$$1's \rightarrow 0101.0010$$

$$\begin{array}{r} + 1 + 1 \\ \hline 0110.0010 \end{array}$$

$$0101.0010$$

$$\begin{array}{r} + 1 \\ \hline 0101.0011 \end{array}$$

3. Subtraction

Answer

$$\begin{array}{r} 1001 - 0110101 \Rightarrow 2's \rightarrow 1001011 \\ \cancel{001001} \quad (+) 0001001 \\ \hline 1010100 \end{array}$$

$$\begin{array}{r} (+) 0010001 \\ \hline 010100 \end{array}$$

$$\begin{array}{r} 0001001 \\ 1001011 \\ \hline 1010100 \\ \cancel{+ 1010101} \\ \hline 010100 \end{array}$$

$$B. 101000 - 10101 = 2's \rightarrow 1010101100$$

$$\begin{array}{r} 101000 \\ (+) 01011 \\ \hline 11111 \end{array}$$

$$\begin{array}{r} 101000 \\ (+) 101011 \\ \hline 100011 \end{array}$$

(without 2's complement)



Note:

1's complement

$$\boxed{r^n - r^m - N}$$

For 2's complement

$$\boxed{r^n - N}$$

Using 2's complement:

$$2^5 \rightarrow \begin{array}{r} 10100 \\ 10101 \\ \hline 1010011 \\ \underbrace{11}_{\text{Carry}} \end{array}$$

$$\begin{array}{r} 01010101 \\ + 10100101 \\ \hline 10000000 \\ \leftarrow \text{Carry} \end{array}$$

$$\begin{array}{r} (-29) + (+49) \\ -29 \rightarrow 111 \\ +49 \rightarrow \cancel{001} \\ \hline 1000 \end{array}$$

$$\begin{array}{r} i) (-29) + (-49) \\ -29 \rightarrow 111 \\ -49 \rightarrow \cancel{111} \\ \hline 111 \end{array}$$

$$(-29) + (+49)$$

4. Binary equivalence of 49 & -29.

$$\begin{array}{r} 49 \\ 2 | 24-1 \\ 2 | 12-0 \\ 2 | 6-0 \\ 2 | 3-0 \\ \hline 1-1 \end{array}$$

$$\begin{array}{r} 29 \\ 2 | 14-1 \\ 2 | 7-0 \\ 2 | 3-1 \\ \hline 1-1 \end{array}$$

$$(49)_{10} \rightarrow (110001)_2$$

$$(-29)_{10} \rightarrow (11101)_2$$

Sign Magnitude Form.

	Sign Mag.	1's	2's
+49	00110001	00110001	00110001
-49	10110001	11001110	11001111
29	00011101		
+29	00011101	00011101	00011101
-29	10011101	11100010	11100011

$$(-29) + (-49)$$

$$64 \leftarrow$$

(Translating 3's complement form)

$$(i) (-29) + (+49)$$

$$\begin{array}{r} -29 \rightarrow 11100011 \\ +49 \rightarrow 00110001 \\ \hline 100010100 \end{array}$$

$$\begin{array}{r} 49 \\ -29 \\ \hline 20 \end{array}$$

$$(ii) (-29) + (-49)$$

$$\begin{array}{r} -29 \rightarrow 11100011 \\ -49 \rightarrow 11001111 \\ \hline 110110010 \end{array}$$

$$110110010$$

$$\begin{array}{r} 25 \\ 25 \\ \hline 01001110 \end{array}$$

$$(-29) + (+49) \Rightarrow 20 \quad [\text{To verify (i)}]$$

$$\begin{array}{r} 00010100 \\ | \quad | \quad | \quad | \quad | \\ 0 \times 2^0 = 0 \\ 0 \times 2^1 = 0 \\ 1 \times 2^2 = 4 \\ 0 \times 2^3 = 0 \\ 1 \times 2^4 = 16 \end{array}$$

$$20 \rightarrow (i) \text{ is verified}$$

$$(-29) + (-49) \Rightarrow 01001110$$

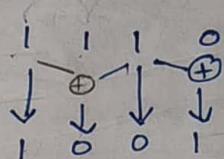
$$\begin{array}{r} 64 \leftarrow 1 \times 2^6 \\ | \quad | \quad | \quad | \quad | \quad | \quad | \\ 0 \times 2^0 \\ 1 \times 2^1 \Rightarrow 2 \\ 2^2 \Rightarrow 4 \\ 2^3 \Rightarrow 8 \\ 0 \times 2^4 \\ 0 \times 2^5 \end{array}$$

$$2 + 4 + 8 + 64 = 78 \rightarrow (ii) \text{ is verified.}$$

Note:

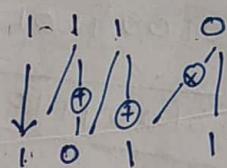
(2m)

BINARY TO GRAY



→ 1st no as it is
→ next nos take X-OR

GRAY TO BINARY



→ next nos ans value
take X-OR.

5. Convert binary $1101110 \Rightarrow$ gray code

1101110

↓

1011001 \Rightarrow gray code.

6. Reduce the boolean expression using Boolean law.

$$A' + C)(A' + C')(A + B + C'D)$$

Using distribution law

$$(A' + C)(A' + C')(A + B + C'D) = (A' + C)(A + B + C'D)$$

$$= A'(A + B + C'D)$$

$$= A'A + A'B + A'C'D$$

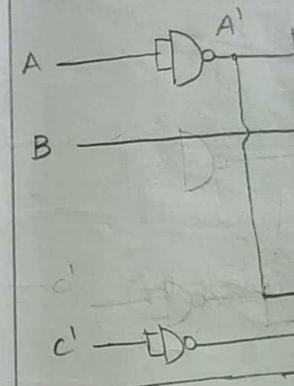
$$= A'B + A'C'D$$

$$= A'(B + C'D)$$

implementation

ONLY US

$$y = A'B + \\ \overline{y} = \overline{\overline{A'B}}$$



\Rightarrow

$$y = A'B$$

$$y = \overline{A'B}$$

$$y = \overline{(\overline{A}\overline{B})}$$

=

=

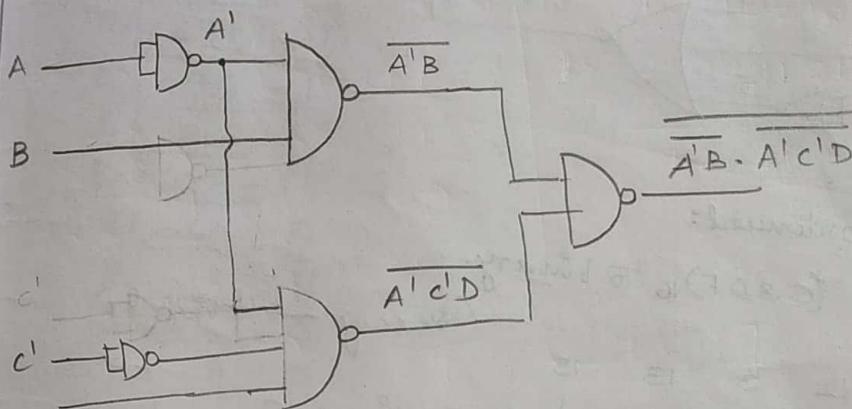
(2m)

implementation using universal logic gates:

ONLY USING NAND AND NOR

$$\text{LHS } Y = A'B + A'C'D$$

$$\bar{Y} = \overline{\overline{A'}B \cdot \overline{A'C'D}} \Rightarrow \text{Only using NAND}$$



\Rightarrow only using NOR

$$Y = A'B + A'C'D$$

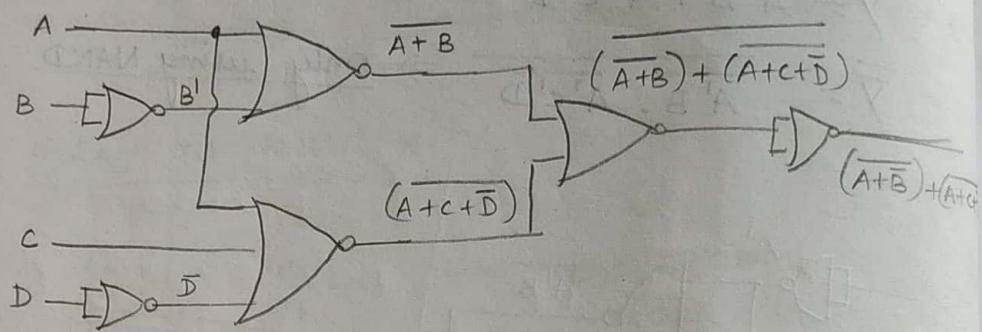
$$Y = \overline{\overline{A'}B \cdot \overline{A'C'D}}$$

$$Y = (\overline{A'} + \overline{B}) \cdot (\overline{A'} + \overline{C} + \overline{D})$$

$$= \overline{(A + B)} \cdot \overline{(A + C + D)}$$

$$= (A + \overline{B}) + \overline{A + C + D}$$

$$Y = \overline{(A+B)} + (\overline{A+C+D})$$



1. (B) continued:

$(CBDF)_{16}$ to binary.

(hexa \rightarrow decimal)

$$\begin{array}{cccc}
 12 & 3 & 13 & 15 \\
 | & | & | & | \\
 \hline
 & & & \rightarrow 15 \times 16^0 = 15 \\
 & & & \rightarrow 13 \times 16^1 = 208 \\
 & & & \rightarrow 3 \times 16^2 = 768 \\
 & & & \rightarrow 12 \times 16^3 = 49,152 \\
 & & & \hline
 & & & (50143)_{10}
 \end{array}$$

(decimal \rightarrow binary)

- Repeated division by 2

$$\underline{2 \mid 50143}$$

$$\text{Ans} \Rightarrow (1100 \ 0011 \ 1101 \ 1111)_2$$

decimal to binary

2	50 143
2	250 71 -1
2	125 35 -1
2	62 67 -1
2	31 33 -1
2	15 66 -1
2	7 83 -0
2	3 91 -1
2	1 95 -1
2	0 97 -1
2	0 48 -1
2	0 24 -0
2	0 12 -0
2	0 6 -0
2	0 3 -0
	1 -01

$$\Rightarrow (110000111101111)_2$$

7. Express the function

$(cd + b'c + bd')(b+d)$ sum of min terms &
pdt of max terms (CANONICAL FORM)

$$\Rightarrow (cd + b'c + bd')(b+d)$$

sum of min terms:-

$$\begin{aligned}
 F &= bcd + b b' c + b d' + cd + b' c d + b d d' \\
 &= bcd + b(c+c')d' + (b+b')cd + b'cd \\
 &= bcd + bcd' + b'c'd' + \cancel{bcd} + \cancel{b'cd} + \cancel{b'cd}
 \end{aligned}$$

111 110 100 011
 7 6 4 3

$$\Sigma_m (3, 4, 6, 7)$$

Pdt of max terms:-

$$\begin{aligned} &= \underline{bcd + bcd' + bc'd' + b'cd} \\ &= cd(b+b') + bd'(c+c') \\ &= cd + bd' \\ &\Rightarrow bd' + cd \quad \text{By distributive law} \\ &= (bd'+c)(bd'+d) \\ &= (b+c)(d'+c)(b+d)(d+d') \\ &= (b+c+dd')(bb'+c+d')(b+cc'+d) \\ &= \cancel{(b+c+d)} \cancel{(b+c+d')} \\ &\quad \cancel{(b+c+d')} \cancel{(b'+c+d')} \\ &\quad \cancel{(b+c+d)} \cancel{(b+c'+d)} \\ &= \cancel{(b+c+d)} \cancel{(b+c+d')} \cancel{(b'+c+d')} \cancel{(b+c'+d)} \\ &= \pi_m(0, 1, 2, 5) \end{aligned}$$

8. Convert

A.) $F(x,y,z) = \sum(1, 3, 5)$
 $= \pi(0, 2, 4, 6, 7)$

B.) $F(A, B, C, D) = \pi(3, 5, 8, 11)$
 $= \sum(0, 1, 2, 4, 6, 7, 9, 10, 12, 13, 14, 15)$
 $= \sum(0, 1, 2, 4, 6, 7, 9, A, C, D, E, F)$

9. Convert:

A. $(u+xw)(x+u'v)$ into sum of pdt and pdt of sum [standard form]

sum of pdt:

$$\begin{aligned} & (u+xw)(x+u'v) \\ &= \cancel{ux + x'} \quad ux + \cancel{u u' v}^{\uparrow 10} + xw x + xw u' v \\ &= ux + xw u' v + xw \leftarrow \text{sum of pdt.} \end{aligned}$$

Pdt of sum:

$$\begin{aligned} & (u+xw)(x+u'v) \quad \text{Using distribution law,} \\ & (u+xw u' v)(x+xw u' v) \\ \Rightarrow & (u+x)(u+w)(u+u') \cancel{(u+v)}^{\uparrow 10} (x+x) \\ & (x+w)(x+u')(x+v) \\ \Rightarrow & (u+x)(u+w)(u+v)(x+w)(x+u')(x+v) \\ \Rightarrow & (u+x)(u+w) \frac{\text{Pdt of sum}}{(x+u')(x+v)} \end{aligned}$$

10. Reduced using k-map.

A. $F(w, x, y, z) = \Sigma(2, 3, 12, 13, 14, 15)$

w	y	z	$\bar{y}\bar{z}$	$\bar{y}z$	yz	$y\bar{z}$
$\bar{w}\bar{x}$	00	00	00	01	11	10
$\bar{w}x$	01	01	01	10	10	11
w	11	11	12	13	15	14
$w\bar{x}$	10	10	01	01	11	10

$$F(w, x, y, z) = w\bar{x} + \bar{w}\bar{x}y$$

B. $F = w'z + xz + x'y + wx'z$

wx	$y_2y_1\bar{y}_0$	\bar{y}_2y_1	$y_2\bar{y}_1$	$y_2\bar{y}_0$
$w\bar{x} \ 00$	0	1	1	1
$wx \ 01$	4	1	1	7
$wx \ 11$	12	1	1	15
$w\bar{x} \ 10$	8	1	1	10
	9		11	14

$x'y_2z$

$$F(w, x, y, z) = z + x'y$$

10. Using tabulation method find the reduced expression:-

A. $F = \sum(1, 3, 4, 5, 10, 11, 12, 13, 14, 15)$

	A	B	C	D
1	0	0	0	1
3	0	0	1	1
4	0	1	0	0
5	0	1	0	1
10	1	0	1	0
11	1	0	1	1
12	1	1	0	0
13	1	1	0	1
14	1	1	1	0
15	1	1	1	1

A
1
4
3
5
10
12
11
13
14
15

Min terms

(1,3)

1,5

3,11

(12,5,1)

10,11,14,1

12,13,14,1

xyz'

	A	B	C	D		Iteration-I		Iteration-II
1	0	0	0	1	✓	(1,3) 00-1°		
4	0	1	0	0	✓	(1,5) 0-01°		
3	0	0	1	1	✓	(4,5) 010- ✓		
5	0	1	0	1	✓	(4,12) -100 ✓		
10	1	0	1	0	✓	(3,11) -011°		
12	1	1	0	0	✓	(5,13) -101°		
11	1	0	1	1	✓	(10,14) 1-10 ✓		
13	1	1	0	1	✓	(12,13) 110- ✓		
14	1	1	1	0	✓	(11,15) 1-11+ ✓		
15	1	1	1	1	✓	(13,15) 11-1 ✓		
						(14,15) 111- ✓		

PRIME IMPlicants:

- (1,3) - $\bar{A}\bar{B}D$
- (1,5) - $\bar{A}\bar{C}D$
- (3,11) - $\bar{B}CD$
- (4,12,5,13) - $B\bar{C}$
- (10,11,14,15) - AC
- (12,13,14,15) - AB

Min terms	P.I	1°	3°	4	5	10	11	12	13	14	15
✓(1,3)	$\bar{A}\bar{B}D$	x	x								
1,5	$\bar{A}\bar{C}D$	x		x							
3,11	$\bar{B}CD$		x			x					
✓(12,5,13)	$B\bar{C}$			x	x		x	x			
✓(10,11,14,15)	AC				x	x			x	x	
✓(12,13,14,15)	AB					x	x	x	x	x	

$$F = \bar{A}\bar{B}D + B\bar{C} + AC.$$

$$F = \bar{A}\bar{B}D + B\bar{C} + AC.$$

Verification using K-map $F = \sum(1, 3, 4, 5, 10, 11, 12, 13, 14, 15)$

$\bar{A}\bar{B}$	CD	$\bar{C}\bar{D}$	$\bar{C}D$	CD	$C\bar{D}$
$\bar{A}B$	00	00	01	11	10
$A\bar{B}$	01	11	11	11	10
AB	11	11	11	11	11
$A\bar{B}$	10	-	-	11	10
	8	9	11	11	10

$$F = A\bar{B}\bar{C} + AC + \bar{A}\bar{B}D$$

Hence verified.

B. $F = \sum(5, 6, 7, 12, 14, 15)$

$d = \sum(3, 9, 11)$

	A	B	C	D
3	0	0	1	1
5	0	1	0	1
6	0	1	1	0
7	0	1	1	1
9	1	0	0	1
11	1	0	1	1
12	1	1	0	0
14	1	1	1	0
15	1	1	1	1

	A	B
3	0	0
5	0	1
6	0	1
9	1	0
12	1	1
7	0	1
11	1	0
14	1	1
15	1	1

Min terms	P.
✓5, 7	\bar{A}
✓9, 11	A
✓12, 14	A
✓3, 7, 11, 15	C
✓6, 7, 14, 15	C

F
$\bar{A}\bar{B}00$
$\bar{A}B01$
$AB11$
$A\bar{B}10$

5, 10, 11, 12, 13, 14, 15

	A	B	C	D	Iteration-1	Iteration-2
3	0	0	1	1	(3, 7) 0-11 ✓	(3, 7, 11, 15) ABC'D --11
5	0	1	0	1	(3, 11) -011 ✓	(3, 11, 7, 15) --11
6	0	1	1	0	(5, 7) 01-10	(6, 7, 14, 15) -11-
9	1	0	0	1	(6, 14) -110 ✓	(6, 14, 7, 15) -11-
12	1	1	0	0	(9, 11) 10-10	
7	0	1	1	1	(12, 14) 11-D 0	(5, 7) A BD
11	1	0	1	1	(7, 15) -111 ✓	(9, 11) A B A B D
14	1	1	1	0	(11, 15) 1-11 ✓	(12, 14) ABD
15	1	1	1	1	(14, 15) 111- ✓	(3, 7, 11, 15) → CD
						(6, 7, 14, 15) → BC

Min terms	P.I	3	5	6	7	9	12	14	15
✓5, 7	$\bar{A}BD$	(X)			X				
✓9, 11	$A\bar{B}D$								
✓12, 14	$A\bar{B}\bar{D}$					(X)		X	
✓3, 7, 11, 15	CD				X				X
✓6, 7, 14, 15	BC		(X)	X			X	X	

$$F = \bar{A}BD + A\bar{B}\bar{D} + BC$$

AB	CD	00	01	11	10	
$\bar{A}\bar{B}$	00	0	1	3	2	verification using k-map.
$\bar{A}B$	01	4	5	1	1	
AB	11	1	X	1	1	Hence Verified.
$A\bar{B}$	10	8	X	X	10	
		9		11		

$$F = BC + \bar{A}BD + A\bar{B}\bar{D}$$

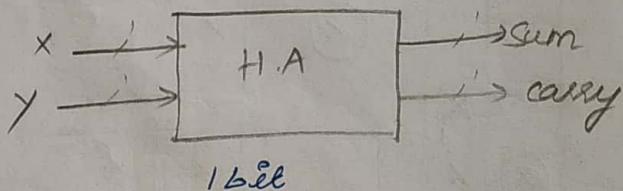
31.07.8

Unit - II combinational circuits

Digital logic circuits

- combinational sequential
 o/p depends upon present i/p (Flip flops)
- Half Adder
 - Full Adder.
 - Ripple carry adder
 - Parallel adder)
 - Mux
 - De Mux
 - Decoder
 - Encoder
 - Comparator
 - Register
 - Counter
 - Shift register
 - ALU
 - Memory
 - Control Unit

Eg:- 1. Half Adder.



x	y	sum	carry
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

$$\text{Sum} = \bar{x}y + x\bar{y} = x \oplus y$$

$$\text{carry} = xy$$

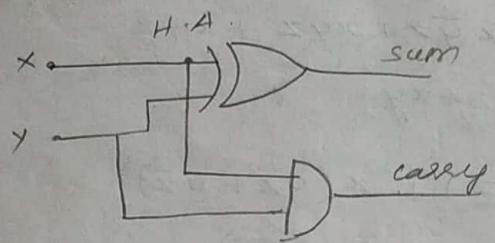
Full Adder

X —
Y —
Cor —
Input —
Carry —

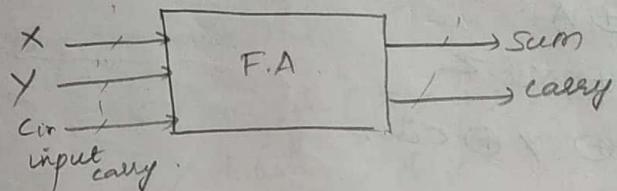
x	y
0	00
1	00
2	01
3	01
4	10
5	10
6	11
7	11

x	y	z
0	00	yz
1	01	00

x	y	z
0	0	0
1	1	1



Full Adder:



x	y	cin	sum	carry
0	0	0	0	0
1	0	1	1	0
2	0	1	1	0
3	0	1	0	1
4	1	0	1	0
5	1	0	0	1
6	1	1	0	1
I	1	1	1	1

		Sum			
		$\bar{y}\bar{z}$	$\bar{y}z$	$y\bar{z}$	yz
		00	01	11	10
\bar{x}	00	0	1	1	2
x	01	1	0	1	6

$$F \Rightarrow \text{sum} \Rightarrow x\bar{y}\bar{z} + \bar{x}\bar{y}z + xy\bar{z} + \bar{x}yz$$

$\bar{y}\bar{z}$	$\bar{y}z$	$y\bar{z}$	yz
0	0	1	3
1	4	5	7
			6

$$\text{carry} \Rightarrow \cancel{yz + xz + xy} \\ \cancel{yz + xz + xy}$$

$$\text{sum: } xy\bar{z} + \bar{x}\bar{y}z + xyz + \bar{x}y\bar{z}$$

$$\text{carry: } yz + xz + xy$$

$$\xrightarrow{\text{sum:}} \bar{x}(\bar{y}z + y\bar{z}) + x(yz + \bar{y}\bar{z}) \\ \bar{x}(\underbrace{y \oplus z}_A) + x(\underbrace{y \odot z}_{\bar{A}})$$

$$= \bar{x}A + x\bar{A}$$

$$= x \oplus A$$

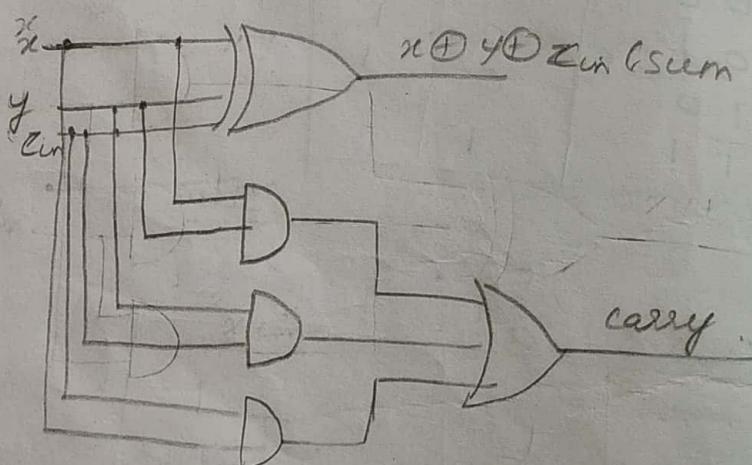
$$= x \oplus y \oplus z$$

$$= x \oplus y \oplus \text{cin.}$$

$$\text{carry: } yz + xz + xy$$

$$\cancel{x(z+y)} + yz$$

$$= xy + y \text{cin} + x \text{cin.}$$



Half Adder

Full Adder

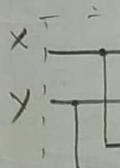
Carry:

=

=

Using

carry
sum



Half

x	0
y	0
sum	0
carry	1

Half Adder..

1. Full Adder using 2 half adder & one OR gate.

carry: $XY + Y_{cin} + X_{cin}$.

$$= XY + (X + \bar{X})Y_{cin} + X(Y + \bar{Y})_{cin}$$

$$= XY + XY_{cin} + \bar{X}Y_{cin} + XY_{cin} + X\bar{Y}_{cin}$$

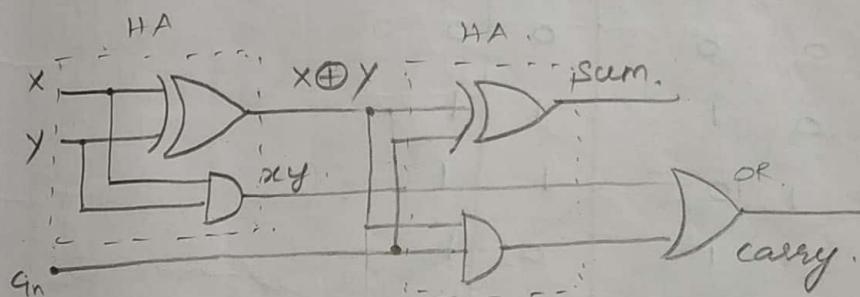
$$= \underbrace{XY}_{\text{sum}} + \underbrace{\bar{X}Y_{cin} + X\bar{Y}_{cin}}_{\text{carry}}$$

Using absorption law: $(A+AB=A)$

$$= XY + \text{cin}(\bar{X}Y + X\bar{Y})$$

$$\underline{\text{carry}} = XY + \text{cin}(X \oplus Y)$$

$$\underline{\text{sum}} = X \oplus Y \oplus \text{cin}$$



2. Half Subtractor.

X	Y	diff (D)	borrow (B)
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

Difference:

$$D = \bar{X}Y + X\bar{Y}$$

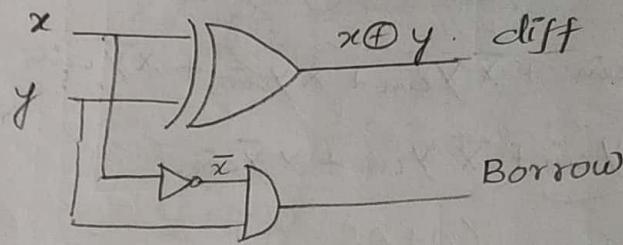
$$= X \oplus Y$$

Borrow

$$B = \bar{X}Y$$

Difference: $x \oplus y$

Borrow: $\bar{x}y$.



FULL SUBTRACTOR:

x	y	c_{in}	D	B
0	0	0	0	0
1	0	0	1	1
2	0	1	0	1
3	0	1	1	1
4	1	0	0	0
5	1	0	1	0
6	1	1	0	0
7	1	1	1	1

$$\begin{array}{r} D \\ 10 \\ - 1 \\ \hline 1 \end{array}$$

x	y	c_{in}	D	B	<u>Difference</u>
0	0	0	0	0	00
1	0	0	1	1	10
2	0	1	0	1	01
3	0	1	1	1	11
4	1	0	0	0	00
5	1	0	1	0	10
6	1	1	0	0	01
7	1	1	1	1	11

$$\text{Difference } D = x\bar{y}\bar{c}_{in} + \bar{x}\bar{y}c_{in} + xyc_{in} + \bar{xy}\bar{c}_{in}$$
$$D = \overline{x \oplus y \oplus c_{in}}$$

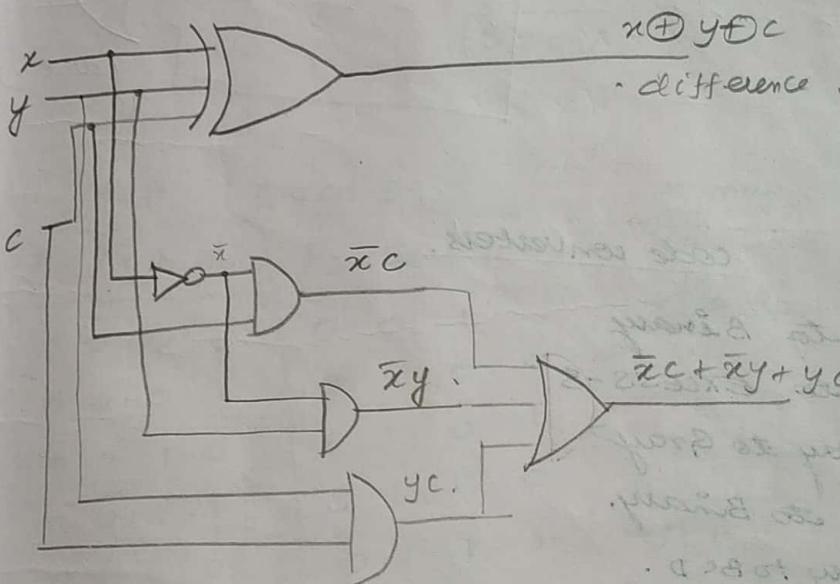
	$y_{in} \bar{y}_c$	\bar{y}_c	y_c	\bar{y}_c
x	0	1	1	1
\bar{x}	0	1	1	1
x	4	5	17	6

$$B = \bar{x}C_{in} + \bar{x}y + yc$$

$$\boxed{B = \bar{x}C + \bar{x}y + yc}$$

= $\bar{x}y + yc$

2 half sub
+ R,



$$B = \bar{x}C + \bar{x}y + yc$$

$$= \bar{x}y + \bar{x}(y + \bar{y})C + (x + \bar{x})yc$$

$$= \underbrace{\bar{x}y}_{\cancel{x}y(1c)} + \underbrace{\bar{x}yc}_{\cancel{x}y + c \oplus xy} + \underbrace{\bar{x}\bar{y}c}_{\cancel{x}\bar{y}c} + \underbrace{xyC}_{\cancel{xyC}} + \underbrace{\bar{x}yc}_{\cancel{\bar{x}yc}}$$

$$= \bar{x}y + c(\bar{x}\bar{y} + xy) + \bar{x}yc$$

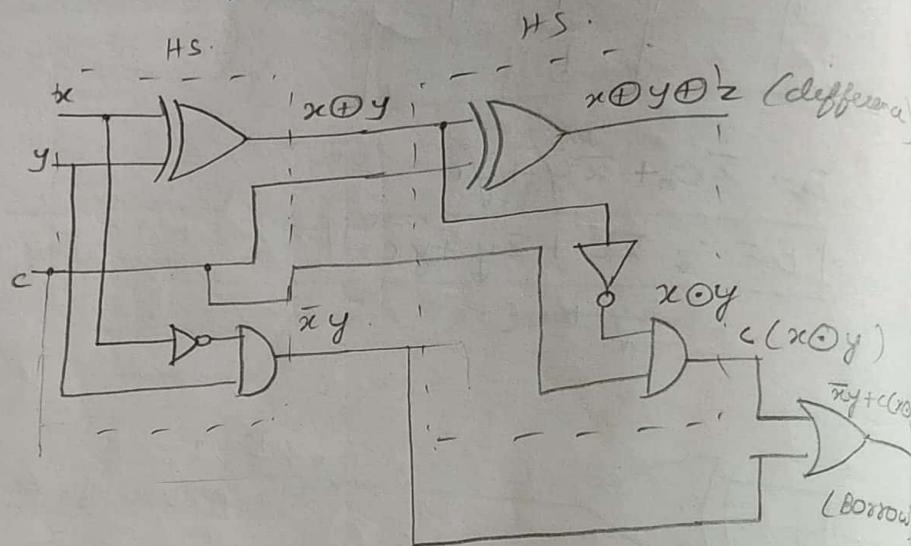
$$= \bar{x}y + c(\bar{x}\bar{y} + xy)$$

$$= \cancel{\bar{x}y + c \oplus \bar{x}y} (x \oplus y)$$

$$B = \bar{x}y + c(x \oplus y)$$

$$B = \bar{x}y + c(x \odot y)$$

$$D = x \oplus y \oplus c.$$



07.08.18

code converters.

1. BCD to Binary
2. BCD to EXCESS-3
3. Binary to Gray
4. Gray to Binary.
5. Binary to BCD.
6. Excess 3 to Binary.

I. BCD

	BCD				BINARY			
	A ₃	A ₂	A ₁	A ₀	B ₃	B ₂	B ₁	B ₀
0	0	0	0	0	0	0	0	0
1	0	0	0	1	0	0	0	0
2	0	0	1	0	0	0	0	1
3	0	0	1	1	0	0	1	0
4	0	1	0	0	0	0	1	1
5	0	1	0	1	0	1	0	0
6	0	1	1	0	0	1	0	1
7	0	1	1	1	0	1	1	0
8	1	0	0	0	1	0	0	0
9	1	0	0	1	1	0	0	1
10	1	0	1	0	1	0	0	1
11	1	0	1	1	1	1	1	1
12	1	0	1	0	Don't care	Don't care	Don't care	Don't care
13	1	1	0	1	Don't care	Don't care	Don't care	Don't care
14	1	1	0	0	Don't care	Don't care	Don't care	Don't care
15	1	1	1	0	1	1	1	0

B	C	D	A
A ₃	A ₂	A ₁	A ₀
0	0	0	0
0	0	0	0
0	0	0	0
0	0	0	0
0	0	0	0
0	1	0	0
0	0	0	1

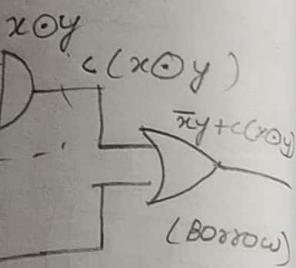
BCD

B	C	D	A
A ₃	A ₂	A ₁	A ₀
0	0	0	0
1	0	0	0
2	0	0	0
3	0	0	0
4	0	1	1
5	0	1	0
6	0	0	1
7	0	0	1
8	1	0	0
9	1	0	0
10	1	0	1
11	1	0	0
12	1	1	0
13	1	1	0
14	1	1	1
15	1	1	1

K map

A ₃ A ₂	A ₃ A ₂ A ₁	A ₃ A ₂ A ₁ A ₀
A ₃ A ₂ 00	0	0
A ₃ A ₂ 01	1	
A ₃ A ₂ 11	X	
A ₃ A ₂ 10	0	

$y \oplus z$ (difference)



BCD		A ₃ A ₂		A ₁ A ₀	
0	0	0	0	0	0
0	0	0	1	0	1
0	0	1	0	1	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	0	0	0	0
0	1	0	0	0	0

BINARY

Draw K maps for B₃ B₂ B₁ B₀

For B₃

A ₃ A ₂		A ₁ A ₀	
00	00	00	00
00	00	01	01
00	01	00	01
00	01	01	00
01	00	00	00
01	00	01	01
01	01	00	00
01	01	01	01

A₃ A₂ 11
A₃ A₂ 10

$$B_3 = A_3$$

$$B_2 = A_2$$

$$B_1 = A_1$$

$$B_0 = A_0$$

BCD Excess 3.

A ₃ A ₂ A ₁ A ₀		E ₃ E ₂ E ₁ E ₀				E ₃
0	0000	00	1	1	X	X
1	0001	01	0	0	X	X
2	0010	01	0	1	X	X
3	0011	01	1	0	X	X
4	0100	01	1	1	11	X
5	0101	10	0	0	10	1
6	0110	10	0	1	1	X
7	0111	10	1	0	X	X
8	1000	10	1	1	X	X
9	1001	11	0	0	X	X

$$E_3 = A_3 + A_2 A_0 + A_2 A_1$$

$$= A_3 + A_2 (A_0 + A_1)$$

$$(A_1 + \bar{A}_1)_{\text{ex3}} = 03$$

K map for E₂.

A ₃ A ₂		A ₁ A ₀		A ₃ A ₂		A ₁ A ₀	
$\bar{A}_3 \bar{A}_2$ 00	00	00	00	00	01	11	10
$\bar{A}_3 \bar{A}_2$ 01	01	01	00	01	00	01	11
$\bar{A}_3 \bar{A}_2$ 11	11	10	11	10	11	11	10
$\bar{A}_3 \bar{A}_2$ 10	10	11	10	11	10	10	10

$$E_2 = A_3 A_0 + \bar{A}_2 A_1 + \bar{A}_3 \bar{A}_2$$

$$A_0 \bar{A}_2 + A_2 \bar{A}_1 \bar{A}_0$$

K map for E_0

		A ₁ A ₀	
		00	01
A ₃ A ₂	00	1 ₀	0 ₁
	01	1 ₄	0 ₅
A ₃ A ₂	11	X ₁₂	X ₁₃
	10	1 ₈	X ₉

$$E_0 = \bar{A}_1\bar{A}_0 + A_1\bar{A}_0$$

$$E_0 = \bar{A}_0(\bar{A}_1 + A_1)$$

K map for E_1

		A ₁ A ₀	
		00	01
A ₃ A ₂	00	1 ₀	0 ₁
	01	1 ₄	0 ₅
A ₃ A ₂	11	X ₁₂	X ₁₃
	10	1 ₈	X ₉

$$E_1 = \bar{A}_1\bar{A}_0 + A_1A_0 = A_1 \oplus A_0$$

$$E_3 = A_3 + A_2(\bar{A}_1 + A_1)$$

$$E_2 = \bar{A}_2(A_1 + A_0) + \bar{A}_1\bar{A}_0A_2$$

$$E_1 = \bar{A}_1\bar{A}_0 + A_1A_0$$

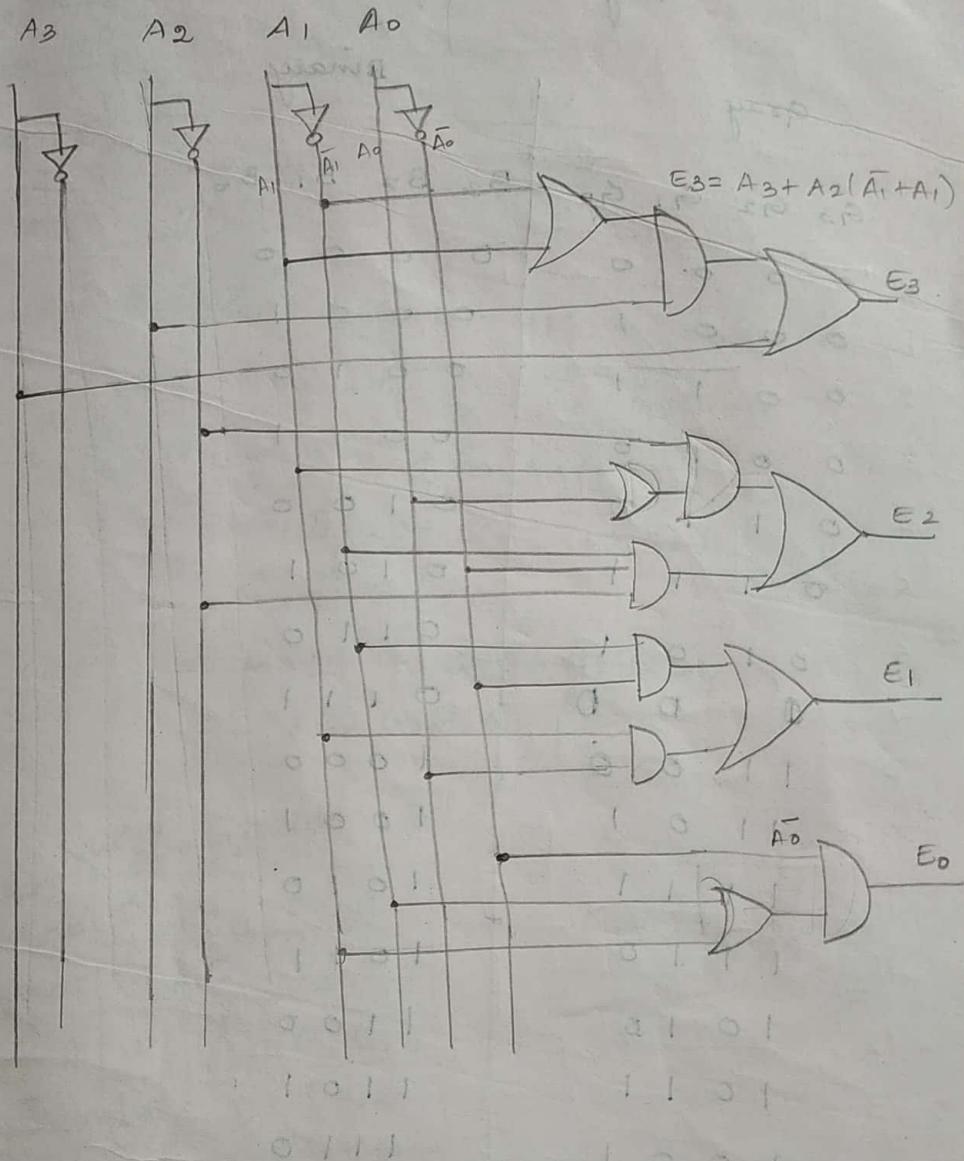
$$E_0 = \bar{A}_0(\bar{A}_1 + A_1)$$

LOGIC

A₃



LOGIC DIAGRAM:



$$E_3 = A_3 + A_2(\bar{A}_1 + A_1)$$

$$E_2 = \bar{A}_2(A_1 + A_0) + \bar{A}_1\bar{A}_0A_2$$

$$E_1 = \bar{A}_1\bar{A}_0 + A_1A_0$$

$$E_0 = \bar{A}_0(\bar{A}_1 + A_1)$$

} Using this logic diagram is shown above

[End - ed]

Deficit Addition

Gray to Binary

Binary

Gray

	G_3	G_2	G_1	G_0	B_3	B_2	B_1	B_0
0	0	0	0	0	0	0	0	0
1	0	0	0	1	0	0	0	1
2	0	0	1	1	0	0	1	0
3	0	0	1	0	0	0	1	1
4	0	1	1	0	0	1	0	0
5	0	1	1	1	0	1	0	1
6	0	1	0	1	0	1	1	0
7	0	1	0	0	0	1	1	1
8	1	1	0	0	1	0	0	0
9	1	1	0	1	1	0	0	1
10	1	1	1	1	1	0	1	0
11	1	1	1	0	1	0	1	1
12	1	0	1	0	1	1	0	0
13	1	0	1	1	1	1	0	1
14	1	0	0	1	1	1	0	0
15	1	0	0	0	1	1	1	1

B_2

$G_3G_2 \backslash G_1G_0$	00	01	11	10
00	0	0	0	0
01	1	1	1	1
11	0	0	0	0
10	1	1	1	1

$$B_3 = G_3$$

$$B_2 = \bar{G}_3 G_2 + G_3 \bar{G}_2$$

$$B_2 = G_3 \oplus G_2$$

<u>B_1</u>	$G_3G_2 \backslash G_1G_0$	$\bar{G}_3G_2 \backslash G_1G_0$	$\bar{G}_3\bar{G}_2 \backslash G_1G_0$	$G_3\bar{G}_2 \backslash G_1G_0$	$\bar{G}_3\bar{G}_2 \backslash G_1G_0$
0	0	0	0	0	0
1	1	1	1	1	1
0	0	0	0	0	0
1	1	1	1	1	1

$$B_1 = G_1$$

=

($G_3 \oplus G_2$)

=

B_0

$G_3G_2 \backslash G_1G_0$	$\bar{G}_3\bar{G}_2 \backslash G_1G_0$
00	00
01	01
11	11
10	10

$$B_0 =$$

= 0

$$= \bar{G}_3 \bar{G}_2$$

$$= (\bar{G}_3 \bar{G}_2)$$

$$= (G_3 G_2)$$

$\bar{G}_3 \bar{G}_2 \bar{G}_1$	$G_1 G_2 \bar{G}_0$	$\bar{G}_1 G_2 G_0$	$G_1 \bar{G}_2 G_0$	$G_1 G_2 \bar{G}_0$
0 0	1 1	0 1	1 1	0 0
1 1	0 0	1 1	0 0	1 1
0 0	1 1	0 0	1 1	0 0
1 1	0 0	1 0	0 1	1 0

$$\begin{aligned}
 B_1 &= G_3 \bar{G}_2 \bar{G}_1 + G_3 G_2 G_1 + \bar{G}_3 \bar{G}_2 G_1 + \bar{G}_3 G_2 \bar{G}_1 \\
 &= G_3 (\bar{G}_2 \bar{G}_1 + G_2 G_1) + \bar{G}_3 (\bar{G}_2 G_1 + G_2 \bar{G}_1) \\
 &= G_3 (G_2 \oplus G_1) + \bar{G}_3 (G_1 \oplus G_2) \\
 &= \bar{G}_3 (G_1 \oplus G_2) + G_3 (\bar{G}_1 \oplus \bar{G}_2) \\
 &= (\bar{G}_3 \oplus G_1 \oplus G_2) \\
 &= G_3 \oplus G_1 \oplus G_2 \\
 &= G_3 \oplus G_2 \oplus G_1
 \end{aligned}$$

$G_3 G_2 \bar{G}_1$	$G_1 G_2 \bar{G}_0$	$\bar{G}_1 G_2 G_0$	$G_1 \bar{G}_2 G_0$	$G_1 G_2 \bar{G}_0$
0 0	1 1	0 0	1 1	0 0
1 1	0 0	1 1	0 0	1 1
0 0	1 1	0 0	1 1	0 0
1 1	0 0	1 0	0 1	1 0

$$\begin{aligned}
 B_0 &= \bar{G}_3 \bar{G}_2 \bar{G}_1 G_0 + \bar{G}_3 \bar{G}_2 G_1 \bar{G}_0 + \\
 &\quad \bar{G}_3 G_2 \bar{G}_1 \bar{G}_0 + \bar{G}_3 G_2 G_1 G_0 + \\
 &\quad G_3 G_2 \bar{G}_1 G_0 + G_3 G_2 G_1 \bar{G}_0 + \\
 &\quad G_3 \bar{G}_2 \bar{G}_1 \bar{G}_0 + G_3 \bar{G}_2 G_1 G_0 \\
 &= \bar{G}_3 \bar{G}_2 (\bar{G}_1 G_0 + G_1 \bar{G}_0) + \bar{G}_3 G_2 (\bar{G}_1 \bar{G}_0 + G_1 G_0) + \\
 &\quad G_3 G_2 (\bar{G}_1 G_0 + G_1 \bar{G}_0) + G_3 \bar{G}_2 (\bar{G}_1 \bar{G}_0 + G_1 G_0) \\
 &= \bar{G}_3 \bar{G}_2 (G_1 \oplus G_0) + \bar{G}_3 G_2 (G_1 \odot G_0) + G_3 G_2 (G_1 \oplus G_0) \\
 &\quad + G_3 \bar{G}_2 (G_1 \odot G_0) \\
 &= (\bar{G}_3 \bar{G}_2 + G_3 G_2)(G_1 \oplus G_0) + (\bar{G}_3 G_2 + \bar{G}_2 G_3)(G_1 \odot G_0) \\
 &= (G_3 \odot G_2)(G_1 \oplus G_0) + G_3 G_2 (G_3 \oplus G_2)(G_1 \odot G_0)
 \end{aligned}$$

$$\begin{aligned}
 &= (G_3 \odot G_2)(G_1 \oplus G_0) + (\overline{G_3 \oplus G_2}) \overline{(G_1 \odot G_0)} \\
 &= (G_3 \odot G_2)(G_1 \oplus G_2) + (\overline{G_3 \odot G_2})(\overline{G_1 \oplus G_0}) \\
 &= \cancel{G_3 \odot G_2 \odot G_1} \\
 &= (G_3 \odot G_2)(G_1 \oplus G_0) + (\overline{G_3 \odot G_2})(\overline{G_0 \oplus G_1})
 \end{aligned}$$

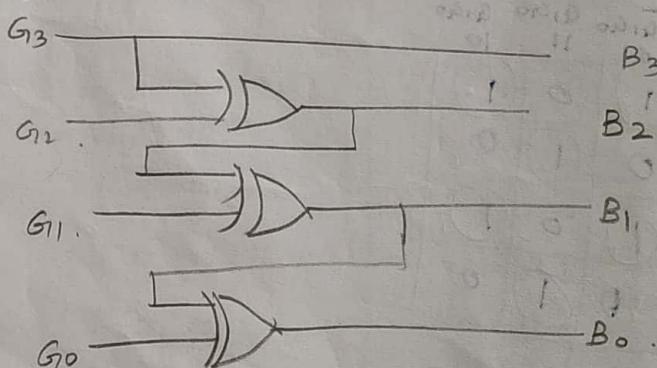
$$(G_3 \odot G_2) \odot G_1 \oplus G_0$$

$$= (\overline{G_3 \oplus G_2})(G_1 \oplus G_0) + (\overline{G_0 \oplus G_1})(G_2 \oplus G_3)$$

$$= G_3 \oplus G_2 \oplus G_1 \oplus G_0$$

$$B_0 = G_0 \oplus B_1 \oplus G_1$$

Design:-



Excess - 3

Excess 3 to Binary

Binary.

E_3	E_2	E_1	E_0	B_3	B_2	B_1	B_0
				0	0	0	0
				0	0	0	1
				0	0	1	0
				0	0	1	1
				0	1	0	0
				0	1	0	1
				0	1	1	0
				0	1	1	1
				1	0	0	0
				1	0	0	1
				1	0	1	0
				1	0	1	1
				1	1	0	0
				1	1	0	1
				1	1	1	0
				1	1	1	1
Don't cares				X			
Don't cares				X			
Don't cares				X			

$$1011 = 0A1A2A4A = A$$

$$1001 = 0A1B2B4B = B$$

at previous steps all needed parts exist
need to numbering with 0 suffix

10.8.18

Binary parallel Adder.

Half adder - 2 bits of each input

Full adder - 3 bits

1. Ripple carry Adder (carry propagate Adder)

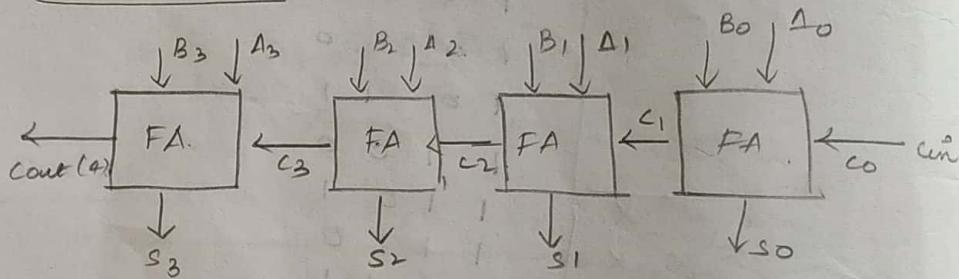
2. carry look ahead adder.

1. Ripple carry Adder :

(made of full adders)

If n bits are required, the n -number of full adders are required.

4-bit RCA.



$$A = A_3 A_2 A_1 A_0 = 1101$$

$$B = B_3 B_2 B_1 B_0 = 1001$$

Initially 2/p carry is zero.

$$A = A_3 A_2 \text{ (A1)} A_0$$

$$B = B_3 B_2 \text{ (B1)} B_0$$

$$\underline{S_3 \quad S_2 \quad S_1 \quad S_0}$$

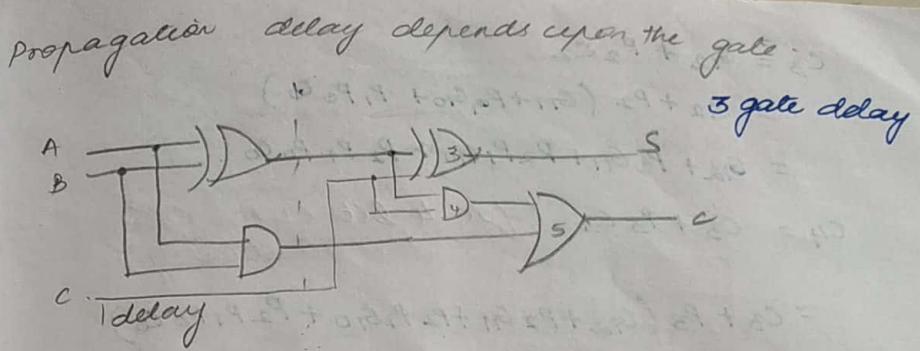
C_4

cout

3 inputs are added

∴ full adders are used

Propagation delay: (Generally in nano second)
Time Delay between the input arrivals to the gate & the generation of carry.

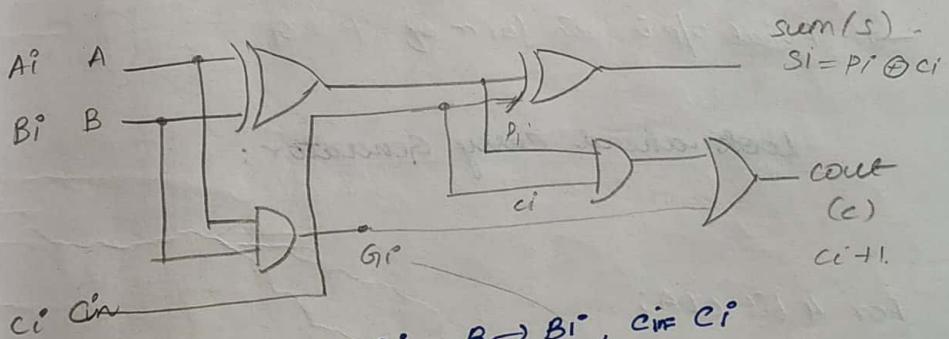


In full adder $\rightarrow 2$ gate delay. (in general)

disadvantage:
longer propagation delay.

2. carry look ahead adder: (high speed parallel adder)
All the carry are generated simultaneously.

We modify based on full adder
[consider it as single bit]



Assume $A \rightarrow A_i$, $B \rightarrow B_i$, $C_i = c_i$

$p_i \rightarrow$ Propagate function $= A_i \oplus B_i$ (for i/p)
 $g_i \rightarrow$ Generate function $= A_i B_i$. (And combination of inputs)

$$c_{i+1} = g_i + p_i c_i$$

apply $i=0$
 $\rightarrow c_1 = g_0 + p_0 c_0$, where $c_0 \rightarrow$ input carry

when $i=2$

$$\rightarrow c_2 = g_1 + p_1 c_1$$

sub c_1 in c_2

$$\begin{aligned} \rightarrow g_2 &= g_1 + p_1 (g_0 + p_0 c_0) \\ &= g_1 + p_1 g_0 + p_1 p_0 c_0 \end{aligned}$$

$$C_3 = G_2 + P_2 C_2$$

$$= G_2 + P_2 (G_1 + P_1 G_0 + P_1 P_0 C_0)$$

$$= G_2 + P_2 G_1 + P_2 P_1 G_0 + P_2 P_1 P_0 C_0.$$

$$C_4 = C_3 + P_3 C_3 \quad (\text{for 4 bit CLA, } C_4 \text{ is the final carry})$$

$$= C_3 + P_3 (G_2 + P_2 G_1 + P_2 P_1 G_0 + P_2 P_1 P_0 C_0)$$

$$= C_3 + P_3 G_2 + P_3 P_2 G_1 + P_3 P_2 P_1 G_0 + P_3 P_2 P_1 P_0 C_0$$

$$C_n = G_{n-1} + P_{n-1} G_{n-2} + P_{n-1} P_{n-2} G_{n-3} + \dots$$

$$\dots + (P_{n-1} P_{n-2} \dots P_1 P_0 C_0)$$

For 8 bit CLA:

$$\begin{aligned} \text{Cout} = C_7 &= G_7 + P_7 G_6 + P_7 P_6 G_5 + P_7 P_6 P_5 G_4 + \\ &P_7 P_6 P_5 P_4 G_3 + P_7 P_6 P_5 P_4 P_3 G_2 + \\ &P_7 P_6 P_5 P_4 P_3 P_2 G_1 + P_7 P_6 P_5 P_4 P_3 P_2 P_1 G_0 + \\ &P_7 P_6 P_5 P_4 P_3 P_2 P_1 P_0 C_0 \quad \text{input carry} \end{aligned}$$

→ Final O/P is in form of P & G

Look ahead carry Generator:



For 4 bit CLA;

we get 4 gate delay (fixed)

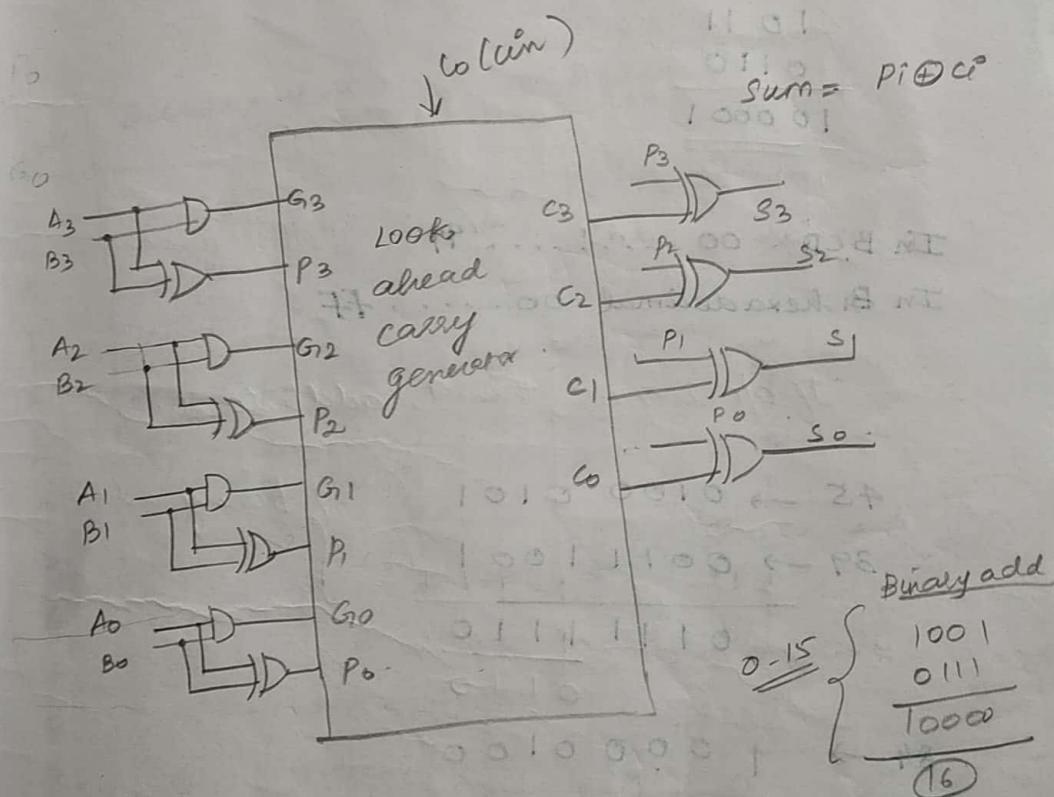
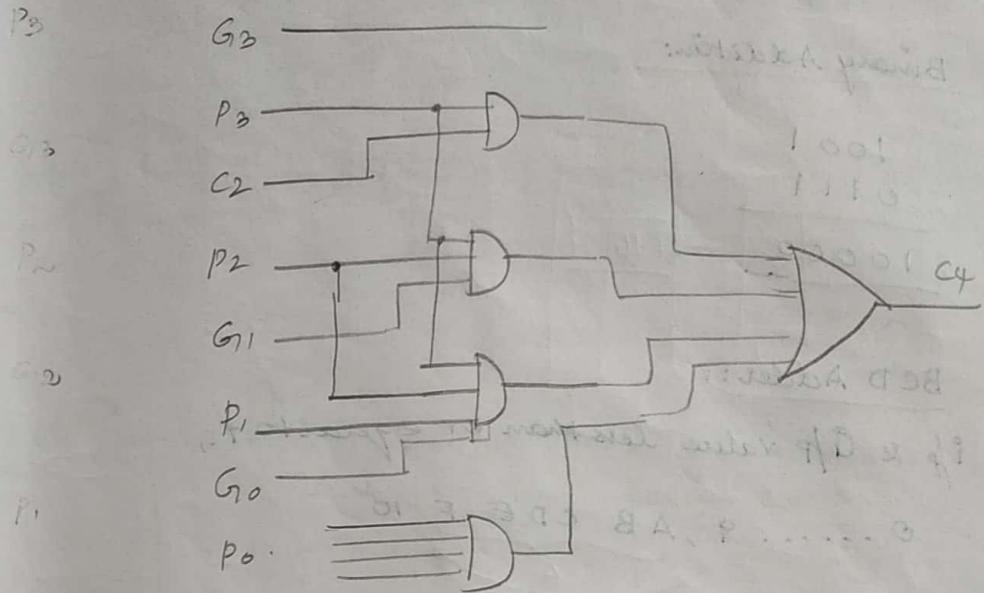
from i/p to output sum.

(Very high speed parallel adder)

to generate $G_1, P \rightarrow 1 \text{ gate}$

to generate sum = 1 gate.

Look ahead carry generator



BCD addition

0 to 9
From 10 it repeats.

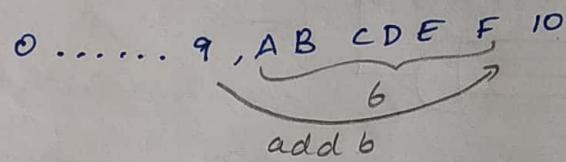
BCD Adder. (4 bit)

Binary Addition:

$$\begin{array}{r}
 1001 \\
 0111 \\
 \hline
 10000
 \end{array} \rightarrow \boxed{16}$$

BCD Adder:

i/p & o/p value less than or equal to 9.



$$\begin{array}{r}
 1011 \\
 0110 \\
 \hline
 100001
 \end{array}$$

In BCD 00 99 highest value
 In Bi hexadecimal 00 FF

If o/p is greater than 9, add 6 do it.

$$45 \rightarrow 0100\ 0101$$

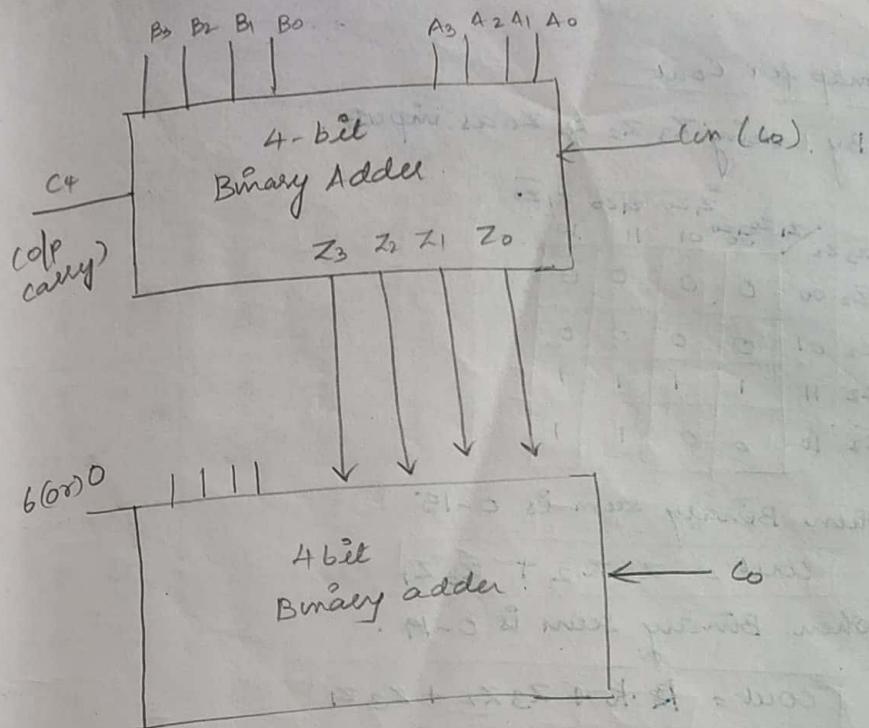
$$39 \rightarrow 0011\ 1001$$

} binary addition

$$\begin{array}{r}
 0111\ 1110 \\
 \hline
 0110
 \end{array}$$

$$84 \rightarrow \underline{1.0000100}$$

0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15



DECIMAL	Binary sum					BCD sum.				
	K	Z_3	Z_2	Z_1	Z_0	Cout	S_3	S_2	S_1	S_0
0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	1	0	0	0	0	1
2	0	0	0	1	0	0	0	0	1	0
3	0	0	0	1	1	0	0	0	1	0
4	0	0	1	0	0	0	0	1	0	1
5	0	0	1	0	1	0	0	1	1	0
6	0	0	1	1	0	0	0	1	1	1
7	0	0	1	1	1	0	0	1	0	0
8	0	1	0	0	0	0	1	0	0	0
9	0	1	0	0	1	0	1	0	0	1
10	0	1	0	1	0	1	0	0	0	0
11	0	1	0	1	1	1	0	0	0	1
12	0	1	1	0	0	1				
13	0	1	1	0	1	1				
14	0	1	1	1	0	1				
15	0	1	1	1	1	1				
.										
19.										

K map for Cout

By taking $Z_3 Z_2 Z_1 Z_0$ as inputs.

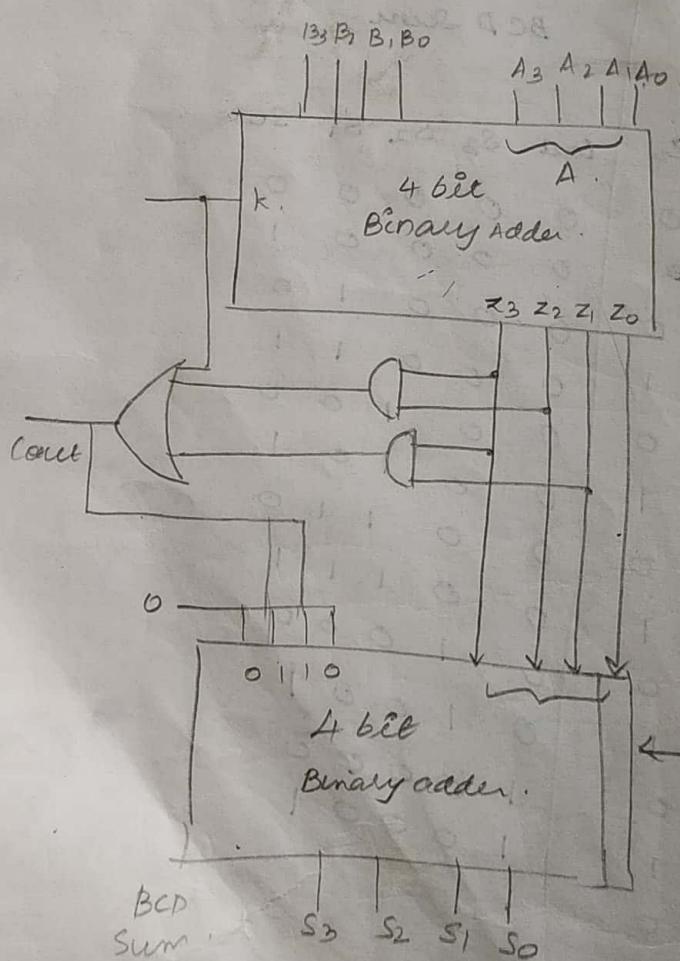
$Z_3 Z_2$	$Z_1 Z_0$	$\bar{Z}_1 \bar{Z}_0$	$Z_1 Z_0$	$\bar{Z}_1 \bar{Z}_0$
$\bar{Z}_3 \bar{Z}_2 00$	0 0	0 0	0 0	0 0
$\bar{Z}_3 Z_2 01$	0 0	0 0	0 0	0 0
$Z_3 Z_2 11$	1 1	1 1	1 1	1 1
$Z_3 \bar{Z}_2 10$	0 0	1 1	1 1	1 1

When Binary sum is 0-15

$$Cout = Z_3 Z_2 + Z_3 Z_1$$

When Binary sum is 0-19.

$$Cout = \bar{Z}_3 \cdot k + Z_3 Z_2 + Z_3 Z_1$$



18

IR

A

A, A0

0 0

0 0

0 0

0 1

0 1

0 0

0 1

1 0

1 0

1 0

1 0

1 0

1 0

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K map

(B)

B1 B0

A1 A0

A1 A0 00

A1 A0 01

A1 A0 11

A1 A0 10

1.10.18

Magnitude comparator

Inputs		Outputs		
A	B	$A > B$	$A = B$	$A < B$
A_1, A_0	B_1, B_0			
0 0	0 0	0	1	0 0
0 0	0 1	0	0	1 1
0 0	1 0	0	0	1 2
0 0	1 1	0	0	1 3
0 1	0 0	1	0	0 4
0 1	0 1	0	1	0 5
0 1	1 0	0	0	1 6
0 1	1 1	0	0	1 7
1 0	0 0	0	0	0 8
1 0	($\bar{B}_1 + 0$)	0	0	9
1 0	1 0	0	1	10
1 0	1 1	0	0	11
1 1	0 0	1	0	12
1 1	0 1	1	0	13
1 1	1 0	1	0	14
1 1	1 1	0	1	15

K map

		A > B			
		$\bar{B}_1 \bar{B}_0$	$\bar{B}_1 B_0$	$B_1 \bar{B}_0$	$B_1 B_0$
		00	01	11	10
$\bar{A}_1 \bar{A}_0$	00	0	0	0	0
$\bar{A}_1 \bar{A}_0$	01	1	0	0	0
$\bar{A}_1 \bar{A}_0$	11	0	0	1	0
$\bar{A}_1 \bar{A}_0$	10	1	1	0	0

A > B

$$= A_0 \bar{B}_1 \bar{B}_0 + \bar{A}_1 A_0 \bar{B}_0 + A_1 \bar{B}_1$$

(ii) $A = B$
 $A = B$

		B ₁ B ₀	00	01	11	10
		A ₁ A ₀	00	01	11	10
		B ₁ B ₀	0	1	3	2
A ₁ A ₀	00	0	1	3	2	
	01	4	5	7	6	
	11	12	13	15	14	
	10	8	9	11	10	

(iii) $A < B$

		B ₁ B ₀				
		A ₁ A ₀	00	01	11	10
		B ₁ B ₀	0	1	1	2
A ₁ A ₀	00	0	1	1	2	
	01	4	5	7	6	
	11	12	13	15	14	
	10	8	9	11	10	

$$\boxed{A=B} = \overline{A_1 A_0} \overline{B_1 B_0} + \overline{A_1} A_0 \overline{B_1} B_0 \\ + A_1 A_0 B_1 B_0 + A_1 \overline{A_0} \overline{B_1} \overline{B_0}$$

$$\boxed{A < B} = \overline{A_1} B_1 + \overline{A_1} \overline{A_0} B_0 + \overline{A_0} B_1 B_0$$

case(i) : $\boxed{A > B}$

$$A > B = A_1 \overline{B_1} + A_0 \overline{B_1} \overline{B_0} + A_1 A_0 \overline{B_0} \\ = A_1 \overline{B_1} + (A_1 + \overline{A_1}) A_0 \overline{B_1} \overline{B_0} + A_1 A_0 (B_1 + \overline{B_1}) \overline{B_0} \\ = A_1 \overline{B_1} + A_1 A_0 \overline{B_1} \overline{B_0} + \overline{A_1} A_0 \overline{B_1} \overline{B_0} + \\ A_1 A_0 B_1 \overline{B_0} + \cancel{A_1 A_0 \overline{B_1} \overline{B_0}} \\ = A_1 \overline{B_1} + A_1 A_0 \overline{B_1} \overline{B_0} + A_0 \overline{B_0} (\overline{A_1} \overline{B_1} + A_1 B_1) \\ = \underbrace{A_1 \overline{B_1} + A_1 A_0 \overline{B_1} \overline{B_0}}_{\text{use adsorption law.}} + (A_1 \odot B_1) A_0 \overline{B_0} \\ = A_1 \overline{B_1} (1 + A_0 \overline{B_0}) + (A_1 \odot B_1) A_0 \overline{B_0}$$

$$\boxed{A > B = A_1 \overline{B_1} + (A_1 \odot B_1) A_0 \overline{B_0}}$$

From (i), (ii) and (iii) cases:-

$$(A = B) = x_1 x_0$$

$$(A > B) = A_1 \overline{B_1} + x_1 A_0 \overline{B_0}$$

$$(A < B) = \overline{A_1} B_1 + x_1 \overline{A_0} B_0$$

case (iii)

A < B

case

while

case (ii) : $A \neq B$

$$\begin{aligned}
 A \neq B &= \overline{A_1} B_1 + \overline{A_1} \overline{A_0} B_0 (B_1 + \overline{B_1}) + \overline{A_0} B_1 B_0 (A_1 + \overline{A_1}) \\
 &= \overline{A_1} B_1 + \overline{\overline{A_1} \overline{A_0} B_0} \overline{B_1} + \overline{\overline{A_1} \overline{A_0} \overline{B_1}} B_0 + \overline{A_1} \overline{\overline{A_0} B_1} B_0 \\
 &\quad + \overline{\overline{A_1} \overline{A_0} B_1} B_0 \\
 &= \overline{A_1} B_1 (1 + \overline{A_0} B_0) + \overline{A_0} B_0 (\overline{A_1} \overline{B_1} + A_1 B_1) \\
 &= \overline{A_1} B_1 + \overline{A_0} B_0 \underbrace{(A_1 \odot B_1)}_{x_1} = \overline{A_1} B_1 + \overline{A_0} B_0 x_1
 \end{aligned}$$

case (ii) $A = B$:-

$$= \overline{A_1} \overline{A_0} \overline{B_1} \overline{B_0} + \overline{A_1} A_0 \overline{B_1} B_0 + A_1 A_0 B_1 B_0 + A_1 \overline{A_0} \overline{B_1}$$

$$\begin{aligned}
 &= \overline{A_1} \overline{B_1} (\overline{A_0} B_0 + A_0 B_0) + A_1 B_1 (A_0 B_0 + \overline{A_0} \overline{B_0}) \\
 &= \overline{A_1} \overline{B_1} (A_0 \odot B_0) + A_1 B_1 (A_0 \odot B_0) \\
 &= (A_0 \odot B_0) (\overline{A_1} \overline{B_1} + A_1 B_1) \\
 &= (A_0 \odot B_0) (A_1 \odot B_1) \\
 &= x_0 x_1 + x_1 x_0
 \end{aligned}$$

Let $x_1 = A_1 \odot B_1$ } $\rightarrow \textcircled{1}$
 $x_0 = A_0 \odot B_0$

similarly $x_1 = A_1 \odot B_1$

While comparing :

LHS \rightarrow RHS

left to Right.

e.g.: $x > y$

$$x = 5 \underline{3} 4 \underline{3} 2 1 7 8$$

$$y = 5 3 4 \underline{2} 1 7 8 7$$

4-bit

$$A = A_3 A_2 A_1 A_0$$

$$B = B_3 B_2 B_1 B_0$$

$$\begin{array}{r} 1101 \\ 1101 \end{array}$$

$$(A > B) = A_3 \bar{B}_3 + X_3 A_2 \bar{B}_2 + X_3 X_2 A_1 \bar{B}_1 + X_3 X_2 X_1 A_0 B_0$$

$$(A < B) = \bar{A}_3 B_3 + X_3 \bar{A}_2 B_2 + X_3 X_2 \bar{A}_1 B_1 + X_3 X_2 X_1 \bar{A}_0 B_0$$

$$(A = B) = X_3 X_2 X_1 X_0$$

21.08.18.

Q. Design a combinational circuit with 3 inputs and 1 output. The output is 1, ~~when~~ when the binary value of input is less than 3. The output is 0 otherwise.

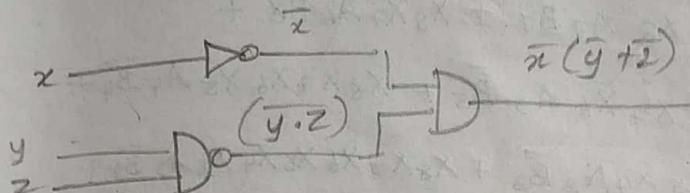
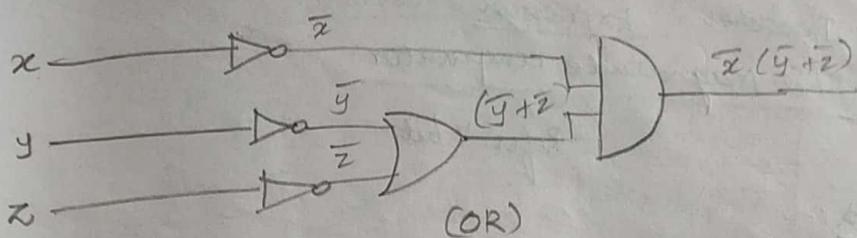
$\Rightarrow x \ y \ z \text{ O/P}$ 2³ \rightarrow 8 combination
Full adder

0	0	0	0	1
1	0	0	1	1
2	0	1	0	1
3	0	1	1	0
4	1	0	0	0
5	1	0	1	0
6	1	1	0	0
7	1	1	1	0

\bar{x}	yz	$\bar{y}\bar{z}$	$\bar{y}z$	$y\bar{z}$	yz
x	00	01	11	10	
x	0	1	1	0	
0	1	1	0	1	
1	0	0	0	0	
	4	5	7	6	

$$= \bar{x} \bar{y} + \bar{x} \bar{z}$$

$$= \bar{x} (\bar{y} + \bar{z})$$

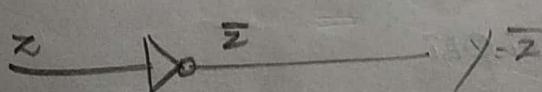


2.Q) Design a combinational circuit with 3 i/p and 1 output. The output is 1 when the binary value of i/p is even no & otherwise 0.

	x	y	z	O/P
0	0	0	0	1
1	0	0	1	0
2	0	1	0	1
3	0	1	1	0
4	1	0	0	1
5	1	0	1	0
6	1	1	0	1
7	1	1	1	0

x	y	z	$y\bar{z}$	$\bar{y}\bar{z}$	$\bar{y}z$	yz	$y\bar{z}$	$\bar{y}\bar{z}$
\bar{x}	0	0	1	0	0	0	1	0
x	1	1	1	1	0	0	0	1

$$= \bar{z}$$



28.08.18

Decoder. Expression
8bit Magnitude comparator:
Refer 4 bit:-

 $\Rightarrow \underline{A \geq B} :-$

$$\begin{aligned}
 &= A_8 \bar{B}_8 + X_8 A_7 \bar{B}_7 + X_8 X_7 A_6 \bar{B}_6 + \\
 &\quad X_8 X_7 X_6 A_5 \bar{B}_5 + X_8 X_7 X_6 X_5 A_4 \bar{B}_4 + \\
 &\quad X_8 X_7 X_6 X_5 X_4 A_3 \bar{B}_3 + X_8 X_7 X_6 X_5 X_4 X_3 A_2 \bar{B}_2 + \\
 &\quad X_8 X_7 X_6 X_5 X_4 X_3 X_2 A_1 \bar{B}_1 + X_8 X_7 X_6 X_5 X_4 X_3 X_2 X_1
 \end{aligned}$$

 $\Rightarrow \cancel{\underline{A \leq B}}$

$$\begin{aligned}
 &= A_7 \bar{B}_7 + X_7 A_6 \bar{B}_6 + X_7 X_6 A_5 \bar{B}_5 + \\
 &\quad X_7 X_6 X_5 A_4 \bar{B}_4 + X_7 X_6 X_5 X_4 A_3 \bar{B}_3 + \\
 &\quad X_7 X_6 X_5 X_4 X_3 A_2 \bar{B}_2 + X_7 X_6 X_5 X_4 X_3 X_2 A_1 \bar{B}_1 + \\
 &\quad X_7 X_6 X_5 X_4 X_3 X_2 X_1 A_0 \bar{B}_0
 \end{aligned}$$

 $\Rightarrow \underline{A < B}$

$$\begin{aligned}
 &= \bar{A}_7 B_7 + X_7 \bar{A}_6 B_6 + X_7 X_6 \bar{A}_5 B_5 + \\
 &\quad X_7 X_6 X_5 \bar{A}_4 B_4 + X_7 X_6 X_5 X_4 \bar{A}_3 B_3 + \\
 &\quad X_7 X_6 X_5 X_4 X_3 \bar{A}_2 B_2 + X_7 X_6 X_5 X_4 X_3 X_2 \bar{A}_1 B_1 + \\
 &\quad X_7 X_6 X_5 X_4 X_3 X_2 X_1 \bar{A}_0 B_0
 \end{aligned}$$

 $\Rightarrow \underline{A = B}$

$$X_7 X_6 X_5 X_4 X_3 X_2 X_1 X_0$$

$$X_C = A_C \odot B_C$$

Accept
Mostly

2 to

A

B

E

T

I/P

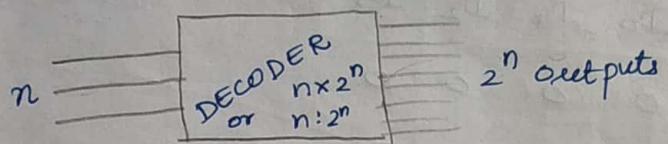
0 0

0 1

1 0

1 1

DECODER



$$\begin{array}{ll} n & 2^n \\ 2 & 2^2 = 4 \\ 3 & 2^3 = 8 \\ 4 & 2^4 = 16 \end{array}$$

example:-

$$2 : 4$$

$$3 : 8$$

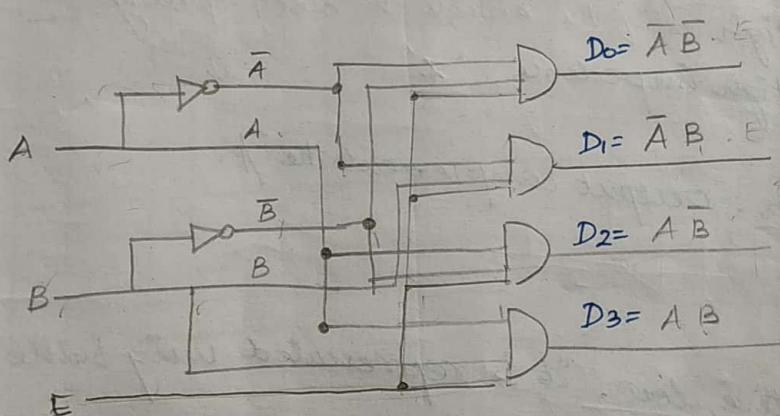
$$4 : 16$$

input output

Accepts n inputs and gives 2^n outputs.
Mostly we USE AND gates.

if 4 outputs are required,
we use 4 AND gates.

2 to 4 Decoder:



Truth table

i/p	D ₀	D ₁	D ₂	D ₃
0 0	1	0	0	0
0 1	0	1	0	0
1 0	0	0	1	0
1 1	0	0	0	1

[Decoder generates 1 in one of the bits]

Use :-

Interconnecting
peripherals
between i/p and
processor

(At the time any 1 of
the o/p generates 1)

$E \rightarrow$ enable

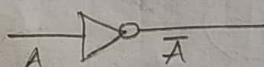
E	A	B	D ₀	D ₁	D ₂	D ₃
0	0	0	0	0	0	0
1	0	0	1	0	0	0
1	0	1	0	1	0	0
1	1	0	0	0	1	0
1	1	1	0	0	0	1

E is the extra bit given to i/p

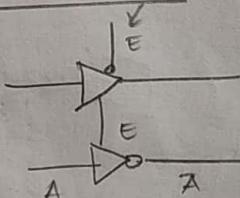
The above concept represents
TRISTATE device.

1. Low \rightarrow If enable is properly given 0
2. High \rightarrow If the enable is not properly 1
3. High impedance. Z given

Inverter: output complements the i/p.



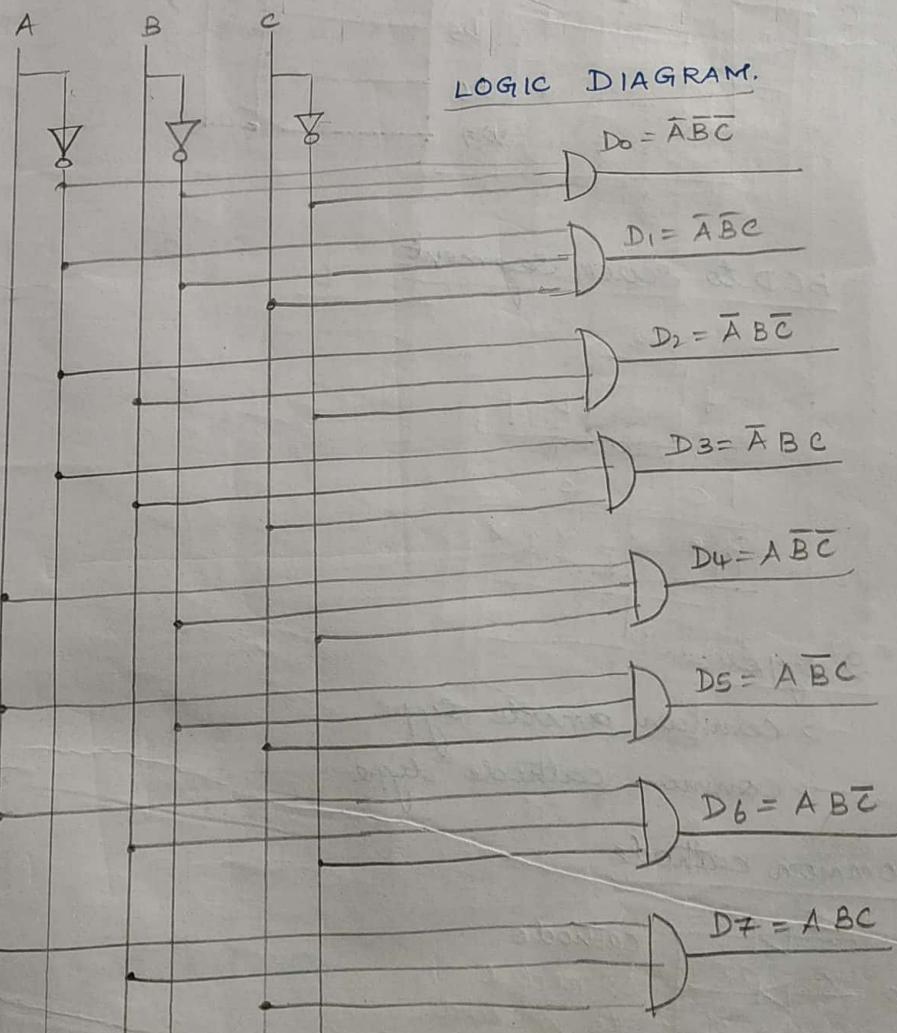
If active low, it is represented using bubble.



3 to 8 is widely used. 74LS138

3 to 8 decoder without Enable

i/p	o/p									
A	B	C	D ₀	D ₁	D ₂	D ₃	D ₄	D ₅	D ₆	D ₇
0	0	0	1	0	0	0	0	0	0	0
0	0	1	0	1	0	0	0	0	0	0
0	1	0	0	0	1	0	0	0	0	0
0	1	1	0	0	0	1	0	0	0	0
1	0	0	0	0	0	0	1	0	0	0
1	0	1	0	0	0	0	0	1	0	0
1	1	0	0	0	0	0	0	0	1	0
1	1	1	0	0	0	0	0	0	0	1

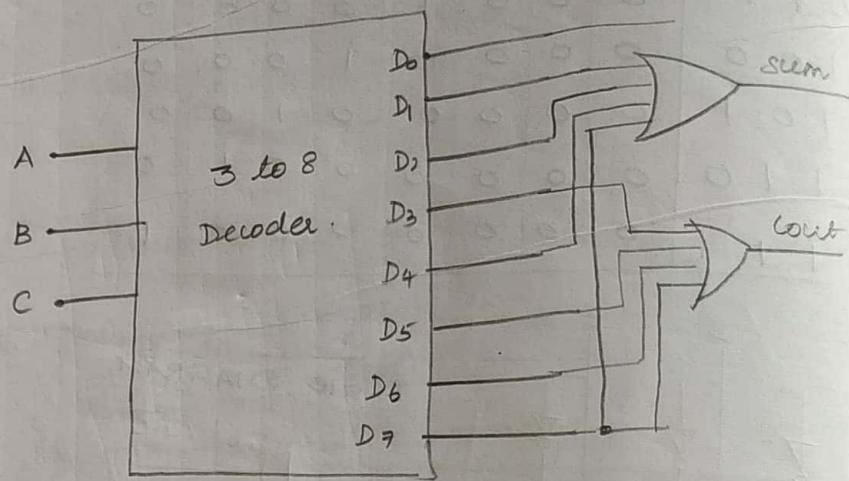


An example of Decoder is
BCD to decimal.

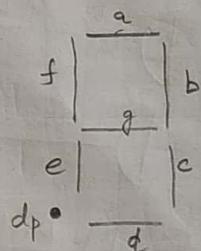
Full adder using Decoder.

$$\text{Sum} = \sum (1, 2, 4, 7)$$

$$\text{Cout} = \sum (3, 5, 6, 7)$$



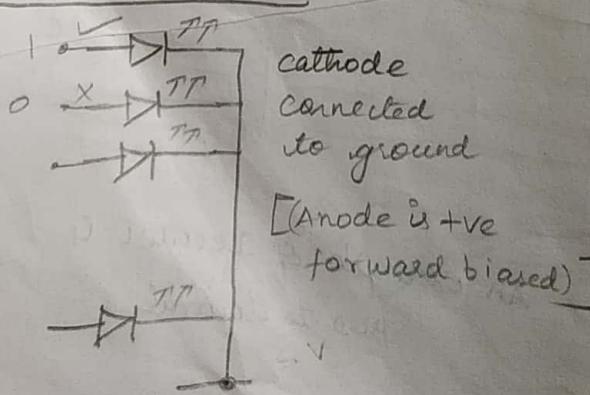
BCD to Seven segment



2 types :-

- common anode type
- common cathode type

* Common cathode



* common

0 ✓
1 ✗

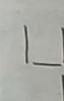
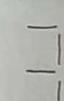
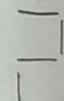
HW

Q) How will

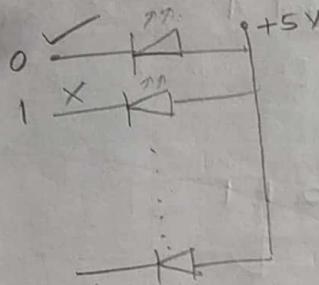
1.08.18

Digital

DIGIT



* common anode type:



Q) HW How will you design 7-segment display

31.08.18

Digit to ASA + IAA - abcde

DIGIT A₃ A₂ A₁ A₀ a b c d e f g

0 0 0 0 1 1 1 1 1 1 0

0 0 0 1 0 1 1 0 0 0 0

0 0 1 0 1 1 0 1 1 0 1

0 0 1 1 1 1 1 1 0 0 1

0 1 0 0 0 1 1 0 0 1 1

0 1 0 1 1 0 1 1 0 1 1

0 1 1 0 1 0 1 1 1 1 1

0 1 1 1 1 1 1 0 0 0 0

Digit $A_3 A_2 A_1 A_0$ $a b c d e f g$
 $\begin{array}{|c|} \hline 1 \\ \hline 0 \\ \hline 0 \\ \hline 0 \\ \hline \end{array}$ $\begin{array}{|c|} \hline 1 \\ \hline \end{array}$

$\begin{array}{|c|} \hline 1 \\ \hline 0 \\ \hline 0 \\ \hline 1 \\ \hline \end{array}$ $\begin{array}{|c|} \hline 1 \\ \hline 1 \\ \hline 1 \\ \hline 0 \\ \hline 0 \\ \hline 1 \\ \hline \end{array}$

Kmap for a :

		$A_1 A_0$	$\bar{A}_1 \bar{A}_0$	$\bar{A}_1 A_0$	$A_1 \bar{A}_0$	$A_1 A_0$
		00	01	11	10	
$A_3 A_2$	00	1	0	1	1	
	01	0	1	1	1	
$A_3 A_2$	11	X	X	X	X	
	10	1	1	X	X	

$$a = A_3 + A_1 + A_2 A_0 +$$

$$A_3 \bar{A}_0$$

For b :

		$A_1 \bar{A}_0$	$\bar{A}_1 \bar{A}_0$	$\bar{A}_1 A_0$	$A_1 A_0$	$A_1 \bar{A}_0$
		00	01	11	10	
$A_3 A_2$	00	1	1	1	1	
	01	1	0	1	0	
$A_3 A_2$	11	X	X	X	X	
	10	1	1	X	X	

$$b = A_3 + \bar{A}_2 +$$

$$\bar{A}_1 \bar{A}_0 + A_1 A_0$$

For c :

$A_3 A_2$	$\bar{A}_3 A_2$	A_1
00	1	0
01	0	1

$$A_3 A_2 \mid \mid$$

$$A_3 \bar{A}_2 \mid 0$$

c =

For C:			
	$A_1 A_0$	$\bar{A}_1 \bar{A}_0$	$\bar{A}_1 A_0$
	$A_1 \bar{A}_0$	$\bar{A}_1 A_0$	$A_1 \bar{A}_0$
$A_3 A_2$	1	0	1
$\bar{A}_3 \bar{A}_2 00$	0	0	1
$\bar{A}_3 A_2 01$	0	1	1
$A_3 A_2 11$	X	X	X
$A_3 \bar{A}_2 10$	1	1	X

$$A_2 + \bar{A}_1 + A_1 A_0 = C$$

+ $A_2 A_0 +$

For D:			
	$A_1 A_0$	$\bar{A}_1 \bar{A}_0$	$\bar{A}_1 A_0$
	$A_1 \bar{A}_0$	$\bar{A}_1 A_0$	$A_1 \bar{A}_0$
$A_3 A_2$	1	0	1
$\bar{A}_3 \bar{A}_2 00$	0	0	1
$\bar{A}_3 A_2 01$	0	1	1
$A_3 A_2 11$	X	X	X
$A_3 \bar{A}_2 10$	1	0	X

$$d = A_1 \bar{A}_0 + \bar{A}_2 \bar{A}_0 + \bar{A}_2 A_0 + A_2 \bar{A}_1 A_0$$

For f

For f:			
	$A_1 A_0$	01	11
	$A_1 \bar{A}_0$	00	10
$A_3 A_2$	1	0	0
$\bar{A}_3 \bar{A}_2 00$	0	1	1
$\bar{A}_3 A_2 01$	1	1	0
$A_3 A_2 11$	X	X	X
$A_3 \bar{A}_2 10$	1	0	X

$$\bar{A}_1 \bar{A}_0 + A_3 + \bar{A}_1 \bar{A}_0 A_2 + \bar{A}_2 \bar{A}_1$$

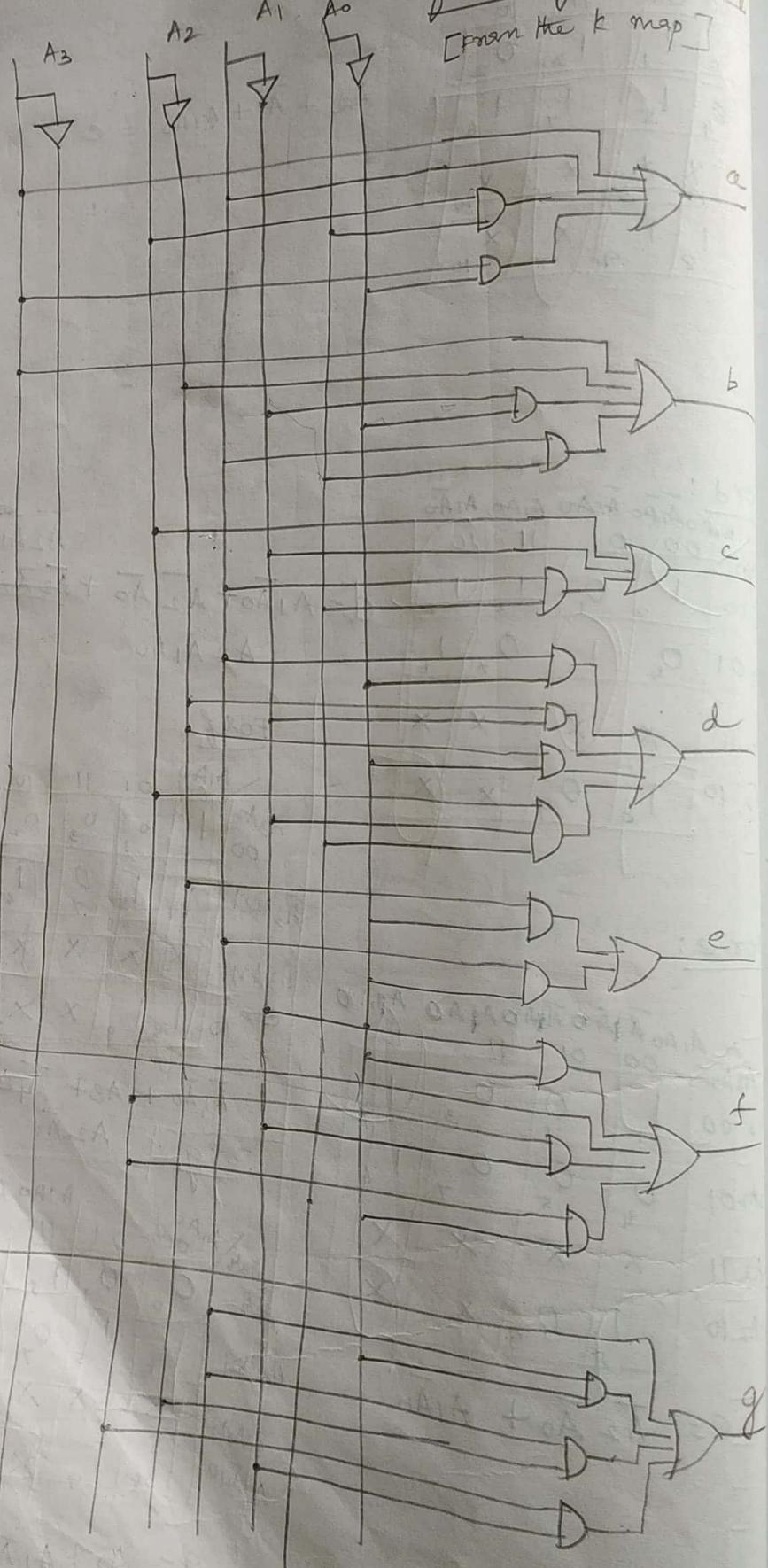
For g $A_2 \bar{A}_0 \Rightarrow f$

For g:			
	$A_1 A_0$	$A_1 \bar{A}_0$	
	$A_1 \bar{A}_0$	00	01
$A_3 A_2$	1	0	1
$\bar{A}_3 \bar{A}_2 00$	0	0	1
$\bar{A}_3 A_2 01$	1	1	0
$A_3 A_2 11$	X	X	X
$A_3 \bar{A}_2 10$	1	0	X

$$g = A_3 + A_1 \bar{A}_0 + A_1 \bar{A}_2 + A_2 \bar{A}_1$$

LOGIC DIAGRAM

for 7 segment display
[From the k map]



2^n inputs

4

Inputs

D₀ D₁

1 0

0 1

0 0

0 0

D₀

D₁

D₂

D₃

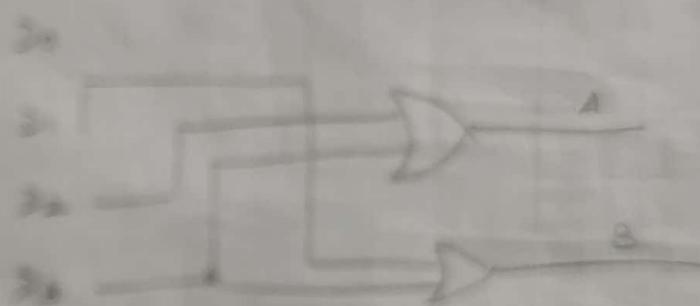
D₄

EX-OR

2ⁿ inputs need n outputs

For 2 inputs

Inputs				Outputs		
D ₁	D ₂	D ₃	D ₄	X	B	A
1	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	1	0	1	0	0
0	0	0	1	1	1	1



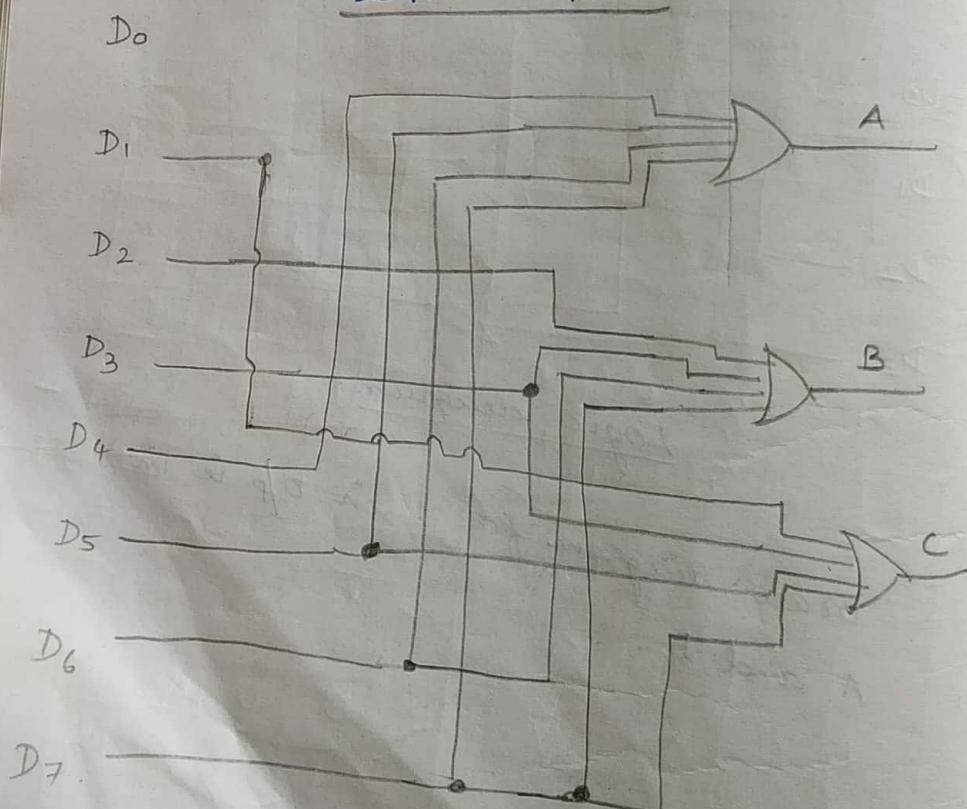
Logic diagram

Block diagram for 1 in of 2 in
A and B

8:3 Encoder:

D_0	D_1	D_2	D_3	D_4	D_5	D_6	D_7	A	B	C
1	0	0	0	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0	0	0	1
0	0	1	0	0	0	0	0	0	1	0
0	0	0	1	0	0	0	0	0	1	1
0	0	0	0	1	0	0	0	1	0	0
0	0	0	0	0	1	0	0	1	0	1
0	0	0	0	0	0	1	0	1	1	0
0	0	0	0	0	0	0	1	1	1	1

LOGIC DIAGRAM.



A B C

0 0 0

0 0 1

0 1 0

0 1 1

1 0 0

1 0 1

1 1 0

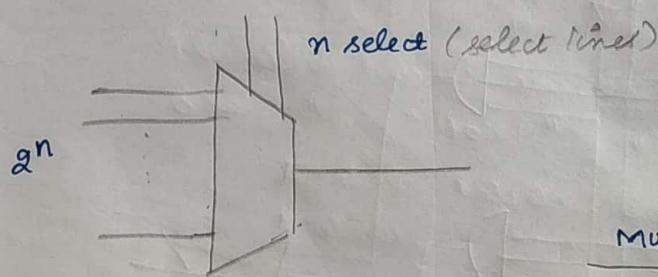
1 1 1

Multiplexer (or) Mux

2^n inputs 1 output

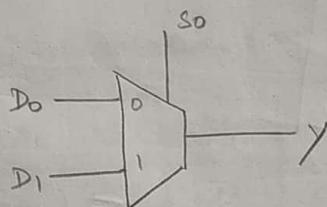
& has n number of select lines

Also called as Data Selector



examples:

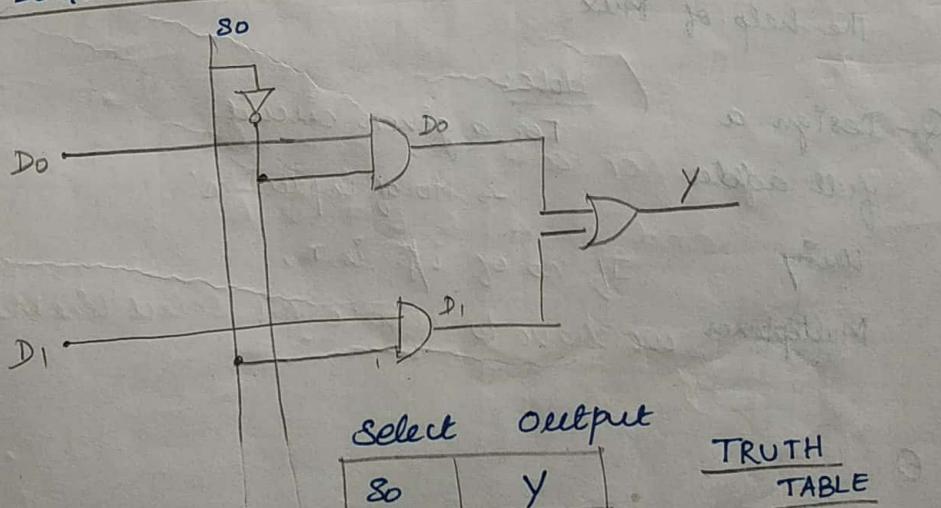
1 \Rightarrow 2:1 MUX



MUX	Select lines
2:1	1
4:1	2
8:1	3
16:1	4

$$\begin{array}{ll} S_0 = 0 & Y = D_0 \\ S_0 = 1 & Y = D_1 \end{array}$$

LOGIC DIAGRAM:

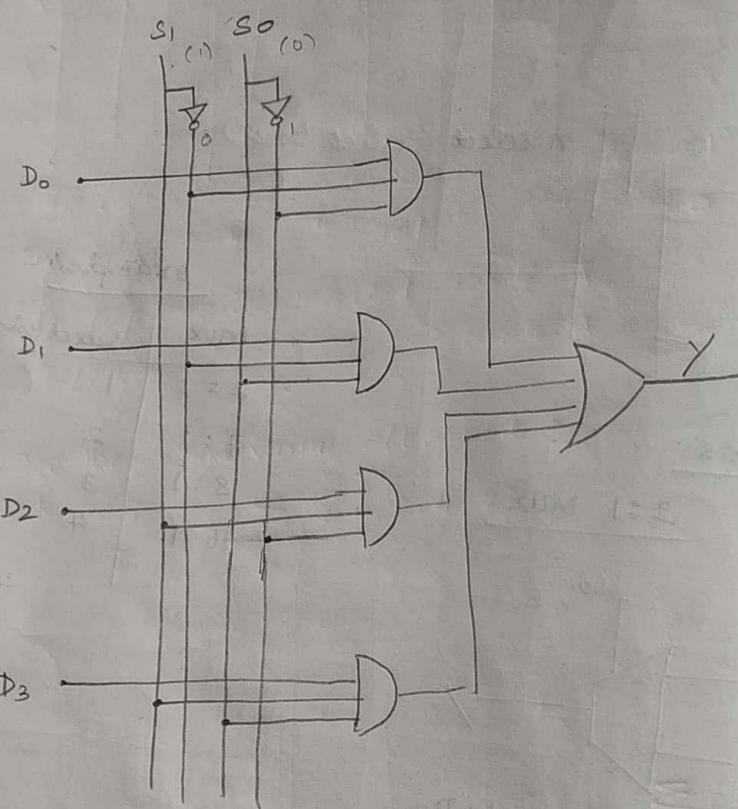
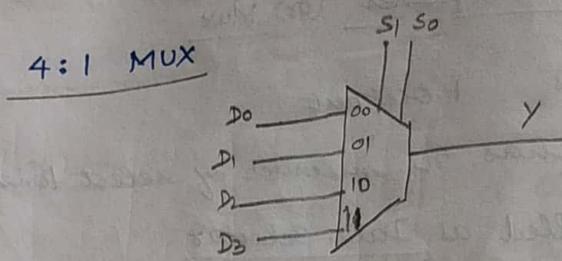


Select	output
0	D_0
1	D_1

TRUTH TABLE

$2 \Rightarrow$

4:1 MUX



Advantage:

We can design any digital ckt with
the help of Mux

Q. Design a
full adder
using
Multiplexer

Note:

For a given circuit.

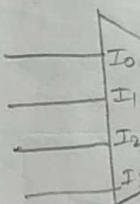
→ No of inputs 'n'

If no of i/p is n,
we have to choose $n-1$ select line Mux

For the true
seen
cout =

i/p \rightarrow 3
(A B C)

4:1 M



for Imple
sel

A B

0	0	0
1	0	0
2	0	1
3	0	1

4	1	0
5	1	1
6	1	1
7	1	1

Form the Truth table of full adder

$$\text{sum} = \Sigma(1, 2, 4, 7)$$

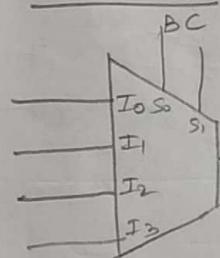
$$\text{cout} = \Sigma(3, 5, 6, 7)$$

i/p $\rightarrow 3$ output
(A B C) sum, carry.

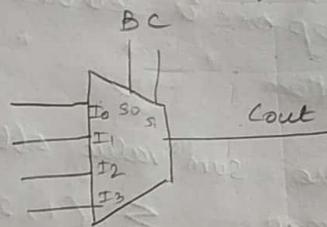
2 select lines \rightarrow so choose 4:1 MUX

(They have 2 select lines)

4:1 MUX



(we use separate mux for sum & carry)



For Implementation table draw the
Select lines truth table of full adder
first.

A	B	C	sum	carry
0	0	0	0	0
1	0	0	1	0
2	0	1	1	0
3	0	1	0	1
4	1	0	0	0
5	1	0	1	0
6	1	1	0	1
7	1	1	1	1

at line MUX)

Implementation table for sum.

	I_0	I_1	I_2	I_3
\bar{A}	0	1	2	3
A	4	5	6	7

(2) If both the nos are circled write as 1
If both " " not " " as 0

If top one is selected write A
" bottom " " " write A

(1) See the sum value obtained from
K map $\Sigma(1, 2, 4, 7)$

Implementation table for carry

	I_0	I_1	I_2	I_3
\bar{A}	0	1	2	3
A.	4	5	6	7
	0	A	A	1

$$\Sigma(3, 5, 6, 7)$$

(from full add)

always for a 0, 1 2 3 $\in A$

and 4 5 6 7 $\in \bar{A}$

Using 8

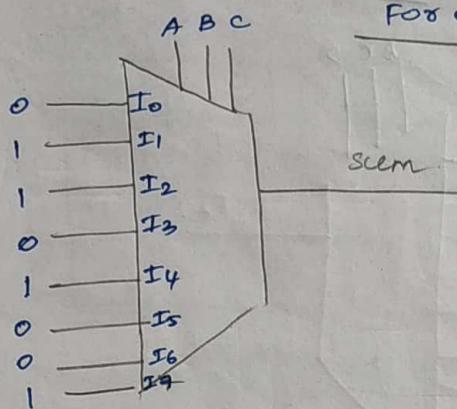
	A	B	C
0	I ₀		
1		I ₁	
1			I ₂
0			I ₃
1			I ₄
0			I ₅
0			I ₆
1			I ₇

Q. $F_1 = \Sigma(0, 1)$
 $F_2 = \Sigma(1, 2)$
 \Rightarrow i/p -

8:1 M

	A	B	C
0	0	0	0
1	0	0	0
2	0	0	1
3	0	0	1
4	0	1	0
5	0	1	0
6	0	1	1
7	0	1	1
8	1	0	0
9	1	0	0
A	1	0	1
10	1	0	1
11	1	0	0
12	1	1	0
13	1	1	0
14	1	1	1
15	1	1	1

Using 8:1 MUX



For example

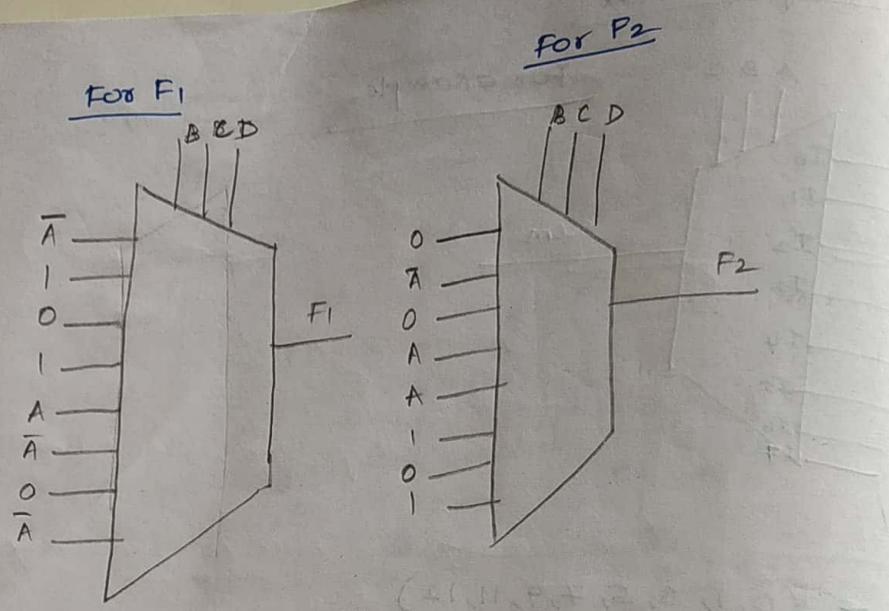
$$Q. F_1 = \{0, 1, 3, 5, 7, 9, 11, 12\}$$

$$F_2 = \{1, 5, 7, 11, 12, 13, 15\}$$

\Rightarrow $i/p \rightarrow s4 \Rightarrow n$
no of select lines $n-1=3$
(choose 8:1 MUX)

8:1 MUX

	A	B	C	D	For F_1							
\bar{A}	0	0	0	0	I_0	I_1	I_2	I_3	I_4	I_5	I_6	I_7
	1	0	0	0	1	0	1	2	3	4	5	6
	2	0	0	1	0							7
	3	0	0	1	1	A	8	9	10	11	12	13
	4	0	1	0	0						14	15
	5	0	1	0	1							
	6	0	1	1	0							
	7	0	1	1	1							
					For F_2							
A	8	1	0	0	I_0	I_1	I_2	I_3	I_4	I_5	I_6	I_7
	9	1	0	0	1							
	10	1	0	1	0	1	2	3	4	5	6	7
	11	1	0	1	1							
	12	1	1	0	0	8	9	10	11	12	13	14
	13	1	1	0	1							
	14	1	1	1	0							
	15	1	1	1	1							



For Y₀

D ₀	D ₁	D ₂	D ₃	Y ₀
00	00	00	00	0
00	00	01	00	1
01	01	10	00	1
11	11	10	00	1
10	10	11	00	0

8:3 F

D ₀	D ₁	D ₂
128	64	32
1	0	0
x	1	0
x	x	1
x	x	x
x	x	x
x	x	x
x	x	x
x	x	x

4/9/18

Priority Encoder.

4:2

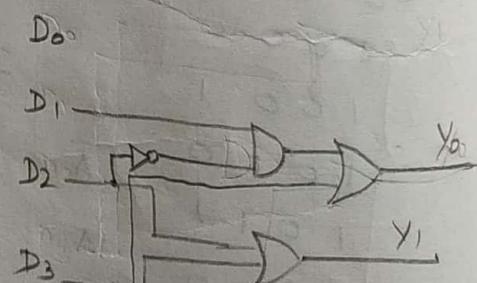
D ₀	D ₁	D ₂	D ₃	Y ₁	Y ₀
8	1	0	0	00	
4, 12	x	1	0	01	
2, 6, 10, 14	x	x	1	10	
1, 3, 5, 7	x	x	x	11	
9, 11, 13, 15					

Y₁ ⇒

D ₀	D ₁	D ₂	D ₃	00	01	11	10
00	00	01	11	1	1	1	1
01	01	11	10	1	1	1	1
11	11	10	11	1	1	1	1
10	10	11	11	1	1	1	1

$$Y_1 = D_3 + D_2$$

Logic Diagram



$$Y_2 = \Sigma(2, 4, 5, 6)$$

$$= D_2 \bar{D}_3$$

$$Y_1 = \Sigma(2, 4, 5, 6, 7, 8, 10, 11, 12, 13, 14, 15)$$

$$= D_2 D_3$$

$$Y_0 = \Sigma(0, 1, 3, 6, 7, 9, 11, 12, 13, 15)$$

Draw

For Y_0

$D_0 D_1$	$D_2 D_3$	00	01	11	10
00	00	0	1	1	3
01	14	1	1	7	6
11	10	1	1	5	14
10	8	1	9	11	10

in priority encoder
we get simultaneous encoder.

$$Y_0 = D_3 + D_1 \bar{D}_2$$

\Rightarrow 8:3 PE

D_0	D_1	D_2	D_3	D_4	D_5	D_6	D_7	Y_2	Y_1	Y_0
0	1	0	0	0	0	0	0	0	0	0
1	x	1	0	0	0	0	0	0	0	1
2	x	x	1	0	0	0	0	0	1	0
3	x	x	x	1	0	0	0	0	1	1
4	x	x	x	x	1	0	0	1	0	0
5	x	x	x	x	x	1	0	1	0	1
6	x	x	x	x	x	x	1	1	1	0
7	x	x	x	x	x	x	x	1	1	1

$$Y_2 = \Sigma(4, 5, 6, 7)$$

expression written from MSB

$$= D_4 + D_5 \bar{D}_6 \bar{D}_7 + D_6 \bar{D}_7 + D_7$$

$$Y_1 = \Sigma(2, 3, 6, 7)$$

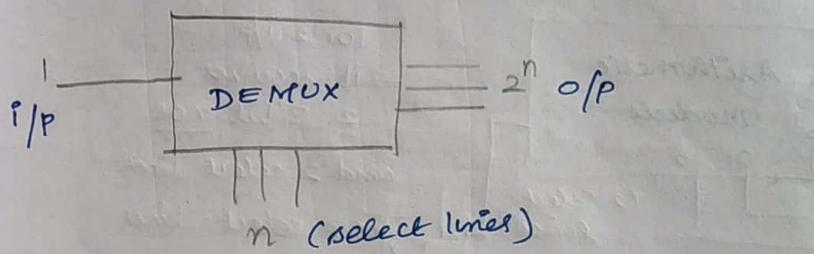
$$= D_2 \bar{D}_3 \bar{D}_4 \bar{D}_5 \bar{D}_6 \bar{D}_7 + D_3 \bar{D}_4 \bar{D}_5 \bar{D}_6 \bar{D}_7 + D_6 \bar{D}_7 + D_7$$

$$Y_0 = \Sigma(1, 3, 5, 7)$$

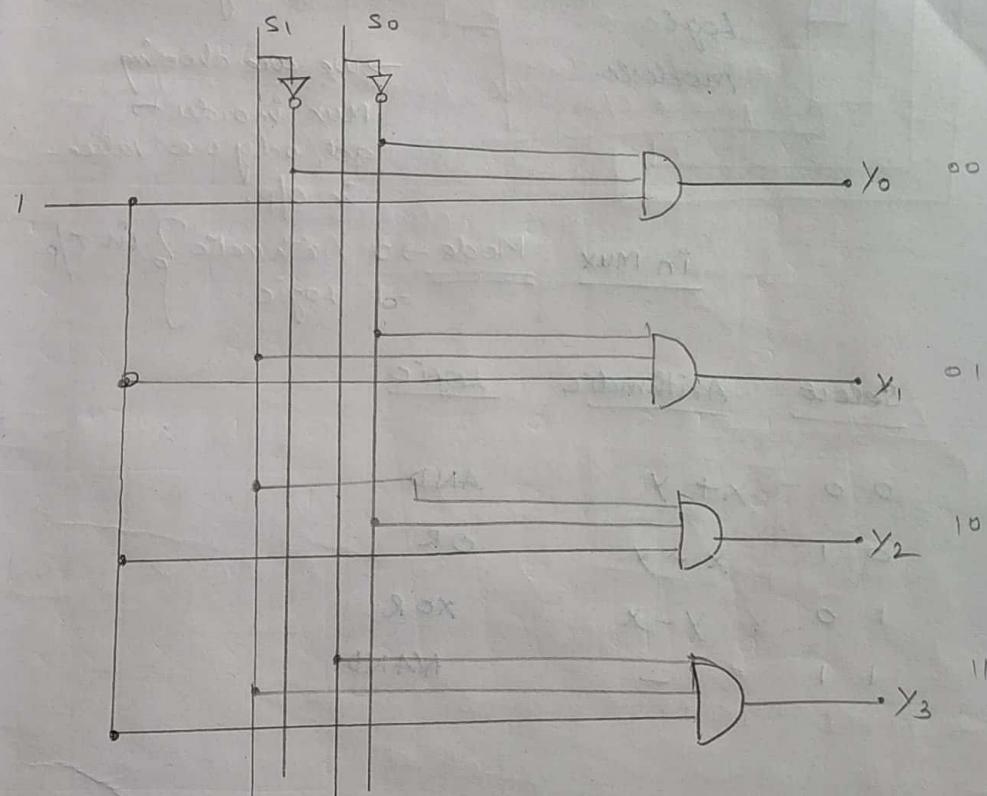
$$= D_7 + D_5 \bar{D}_6 \bar{D}_7 + D_3 \bar{D}_4 \bar{D}_5 \bar{D}_6 \bar{D}_7 + D_1 \bar{D}_2 \bar{D}_3 \bar{D}_4 \bar{D}_5 \bar{D}_6 \bar{D}_7$$

Draw logic diagram:-

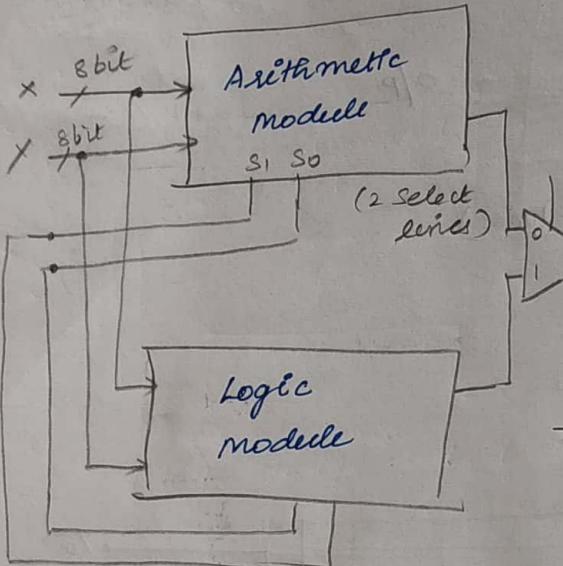
Demultiplexers



1:4 Demux



8-bit ALU:-



For 2 I/P
 → it receives
 2 8 'bit noe
 and 2 select lines
 These select lines
 \downarrow
 are fed to
 the select lines
 of Logic module

→ We are choosing
Max in order to
get only one value
in O/P.

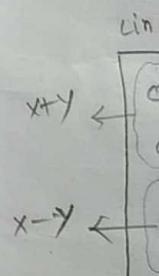
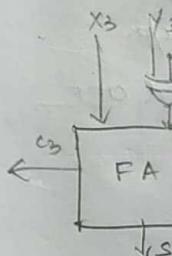
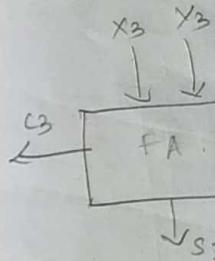
<u>Select</u>	<u>Arithmetic</u>	<u>Logic</u>
0 0	$x + y$	AND
0 1	$x - y$	OR
1 0	$y - x$	XOR
1 1	-	NAND

For performing Arithmetic operations:

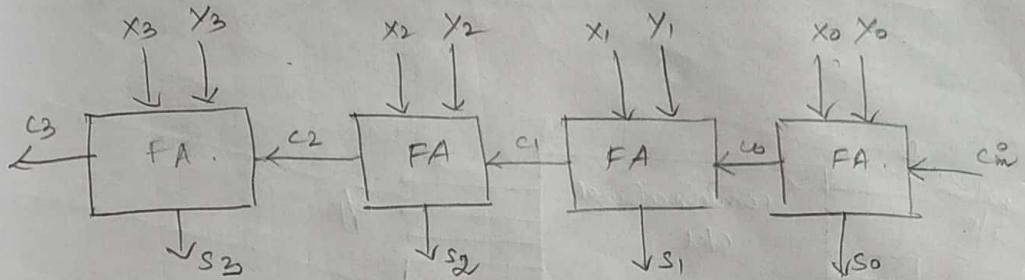
$x+y$ and $x-y$

Using 4 bit \rightarrow construct 4 F.A
(RCA)

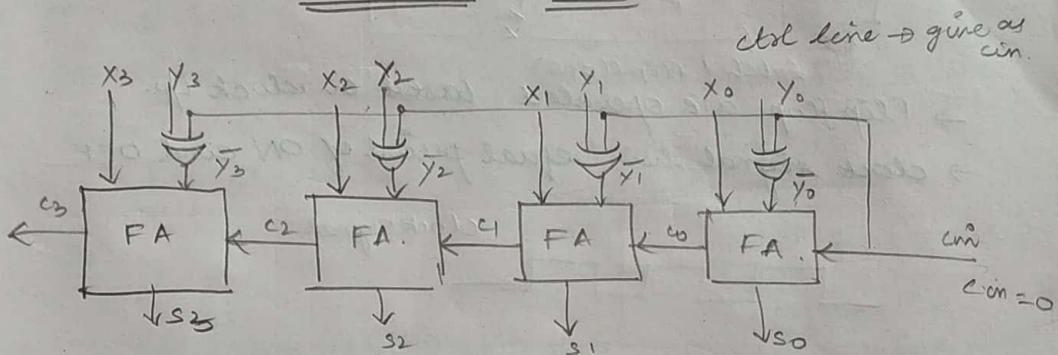
4 bit



4 bit Adder & Subtractor



For $x+y$ & $x-y$



lin \neq Y o/p	
$x+y$	$0\ 0\ 0\ 0$
	$0\ 1\ 1\ 1$
$x-y$	$1\ 0\ 1\ 0$
	$1\ 1\ 0\ 0$

when $c_{in} = 0$

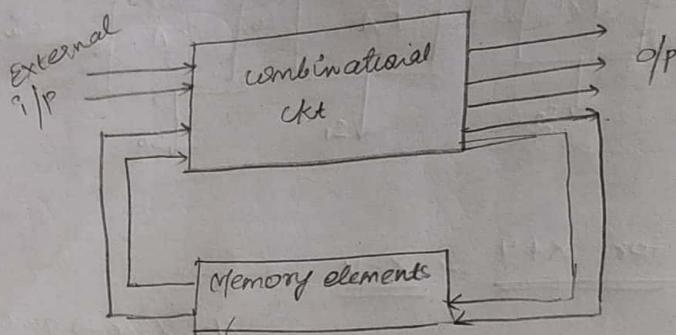
$$x+y+0$$

when $c_{in} = 1$

$$x+\overline{y}+1$$

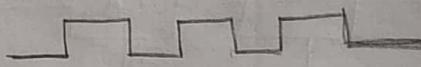
$$= x-y$$

7.9.18 UNIT - 3 SYNCHRONOUS SEQUENTIAL CIRCUITS



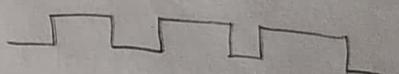
- Flip flops are operated based on clock i/p.
- clock signal has equal period of ON and OFF

clock signal.



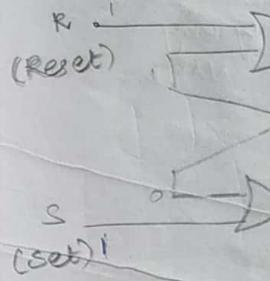
LATCHES:-

- Does not have clock signal
- It has combination of gates
- They are mostly used as feed back elements in asynchronous ckt
- LEVEL TRIGGERED signals (Latches)
- O/P responds during the level
- Flip flops are edge triggered clock signal.



* SR latch (Basic latch)

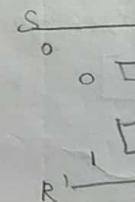
NOR NAND



NOR

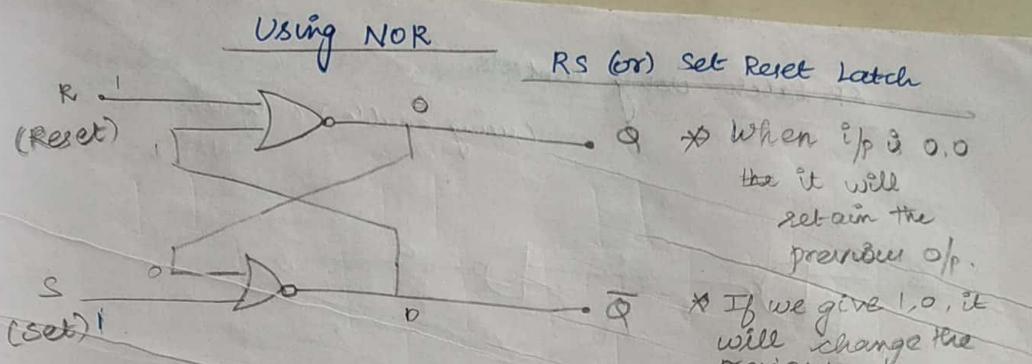
A	B	
0	0	1
0	1	0
1	0	0
1	1	0

SR la



NAND

A	B	
0	0	1
0	1	0
1	0	0
1	1	0



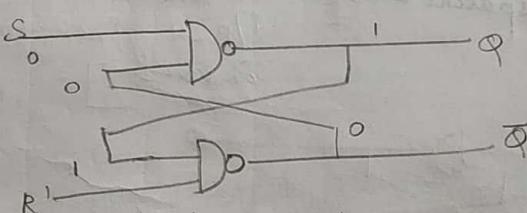
NOR

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	0

Truth table from the above diagram

R	S	Q	\bar{Q}
0	1	1	0
0	0	1	0
1	0	0	1
0	0	0	1
1	1	0	0
0	0	0	0

(in flip flop, it is indetermined state)

SR latch using NAND gate

initial case
assume 0,1;
depending upon o/p
change the previous value.

NAND

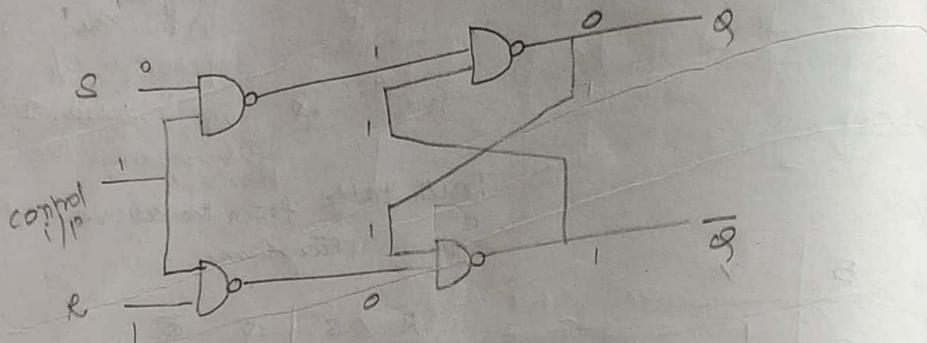
A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

S	R	Q	\bar{Q}
0	1	1	0
1	1	1	0
0	1	0	1
0	0	0	1
1	1	1	1

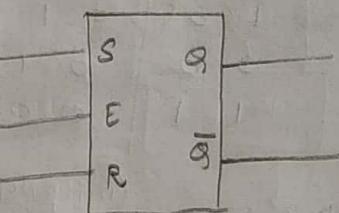
→ retain the previous value

→ invalid

SR latch using controls.
 (using enable) only using NAND

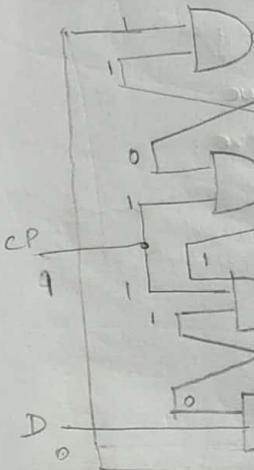


symbol of Latch



For 'Q' we
put bubble

Positive edge



clk ↑

D _____

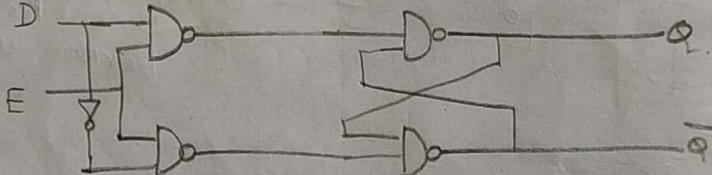
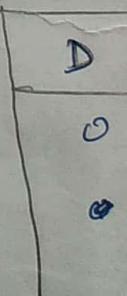
latch Q _____

flip flop Q _____

→ Q

the O/p

TRUE



(Mostly 'D' flip flop
is used for
designing)

- * Respond to changes given to level (in lab)
- * concept of latch & flip flop is it follows the i/p
(op follows i/p)

if D is 1, Q is
if " " 0, " " 0

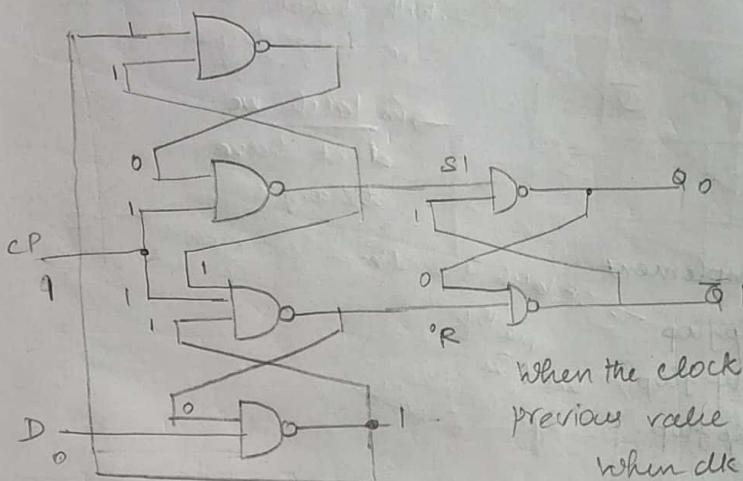
if E is 0, Q is 0
if " " 1, Q " 1

enable) only using
NAND.

Positive edge triggered D-flip flop.

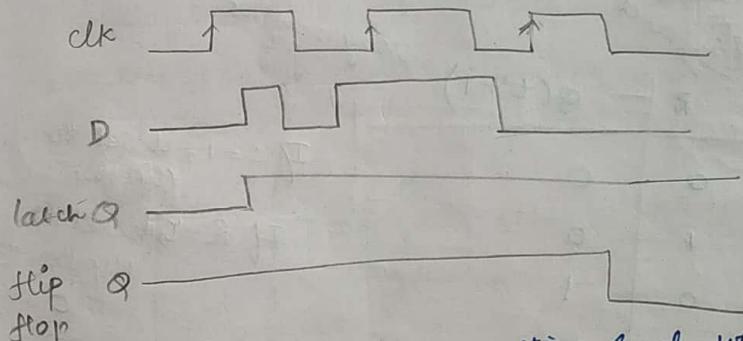
→ one of i/p is 0, the o/p is
1 (first part)

both i/p \Rightarrow 1 o/p is 0



When the clock pulse is 0,
previous value is retained

When clk pulse is 1
there is a change,
output follows the i/p



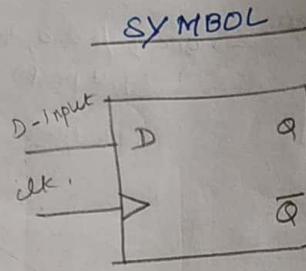
→ Only at the transition level, when
the o/p changes, it is called as flip flop.

TRUTH TABLE for D flip flop (characteristic Table)

D	Q
0	0
1	1

$Q(t)$ before P clock	D	$Q(t+1)$
0	0	0
0	1	1
1	0	0
1	1	1

D value
retained
at t.



- without bubble +ve edge trigger
- with bubble -ve edge trigger
- in latch we don't have triangle

We can implement

S-R flip flop	→ SR latch is used in a synchronous circuit.
J-K flip flop	not yet used in
(Toggle) T flip flop.	synchronous circuits.
D flip flop	$\boxed{01}$

SR FLIP FLOP

Q	S	R	$Q(t+1)$	Using NOT gate.
0	0	0	0	If $S=1$, it sets the flip flop
0	0	1	0	If $R=1$, it resets the flip flop
0	1	0	1	
0	1	1	I.D.	0
1	0	0	1	
1	0	1	0	
1	1	0	1	
1	1	1	I.D.	

General characteristic table of SR Latch.

S	R	$Q(t)$
0	0	$Q(t)$
0	1	0 → (Reset)
1	0	1 → set
1	1	Ineterminate

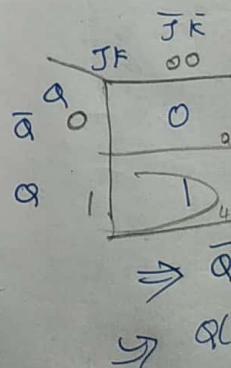
JK FLIP

J	K
0	0
0	1
1	0
1	1

Q	J	K
0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
1	0	1
1	1	0
1	1	1

T flip flop
to avoid

Apply k map



at bubble
edge trigger
bubble
edge trigger

at we
nt have
single
synchronous
circuit

NOT
gate.

If $S=1$, it set the
flip flop

If $R=1$, it reset the
flip flop

0

JK FLIP FLOP

J	K	$Q(t+1)$
0	0	$Q(t)$
0	1	0
1	0	1
1	1	$\overline{Q(t)}$

Q	J	K	$Q(t+1)$
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

T flip flop is implemented from JK flip flop
to avoid racing condition (complemented form)

Apply K map for $Q(t+1)$

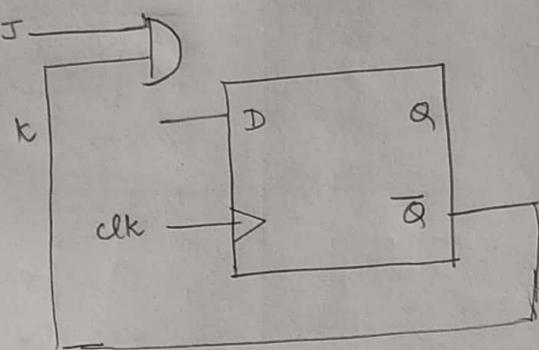
for J-K

	$\bar{J}\bar{K}$	$\bar{J}K$	$J\bar{K}$	$J\bar{K}$
JF	00	01	11	10
\bar{Q}_0	0	0	1	1
Q_1	1	0	0	1

$$\Rightarrow \bar{Q}J + Q\bar{K} \quad \text{characteristic eqn of JK flip flop}$$

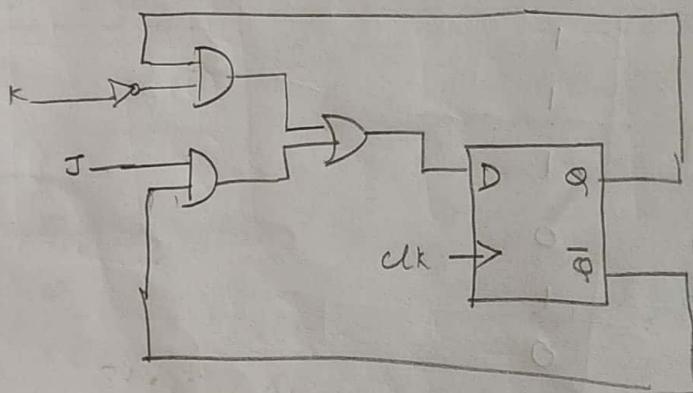
$$\Rightarrow Q(t+1) = \bar{Q}(t)J + Q(t)\cdot K$$

$$= \bar{Q} J + Q \bar{K}$$



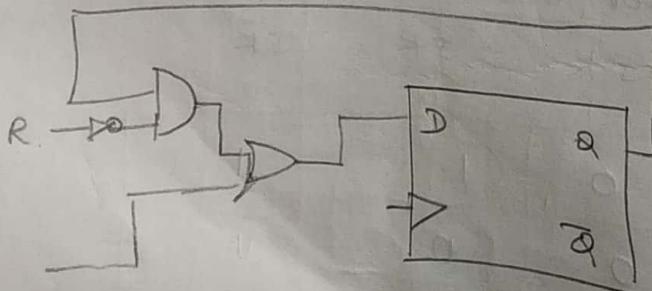
J K flip flop D-Flip flop

char egn of D flip flop is D for $Q(t+1)$
(since it follows the I/P)



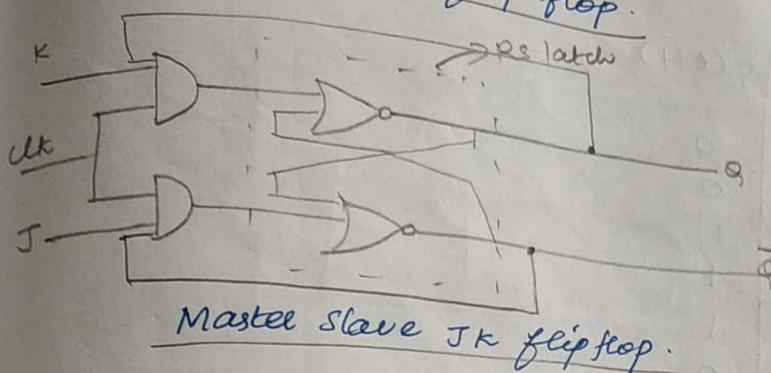
a	SR	$\bar{S}\bar{R}$	$\bar{S}R$	SR	$S\bar{R}$
\bar{Q}	0	1	x	1	
Q	1		x	1	

$$Q(t+1) = S + Q\bar{R}$$



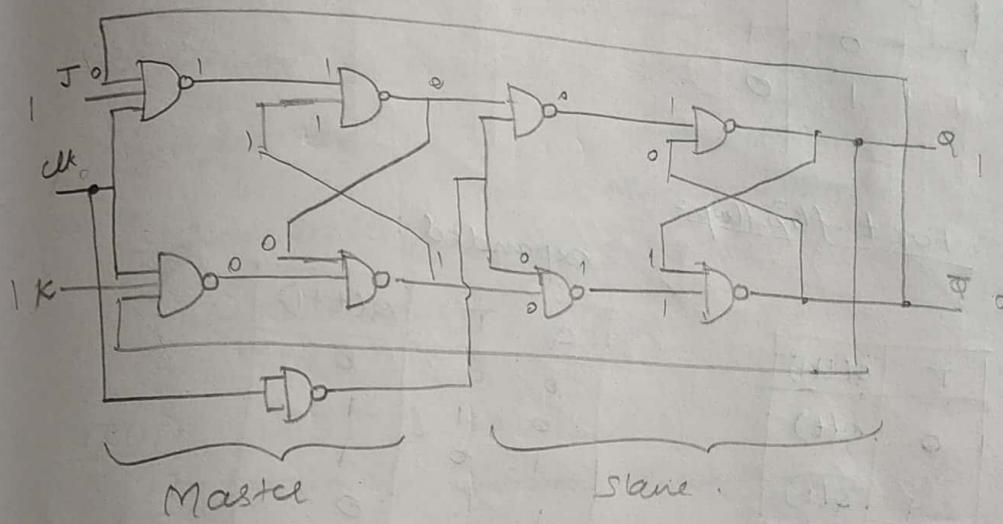
11.09.18

JK flip flop.



J	K	Q(t+1)
0	0	Q(t)
0	1	0
1	0	1
1	1	Q̄(t)

Master slave JK flip flop.



→ Master receives external if
→ Mostly 1 1 condition is used to avoid racing condition

→ During -ve pulse cycle there is no change in the MASTER.

→ no change in slave (positive)
change in Master.

→ NO RACING CONDITION (negative)

No change in master
change in slave.

2 flip flop connected in cascade,
it is master flip flop.

Q	J	K	$Q(t+1)$
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

For T flip flop:-

expanded:

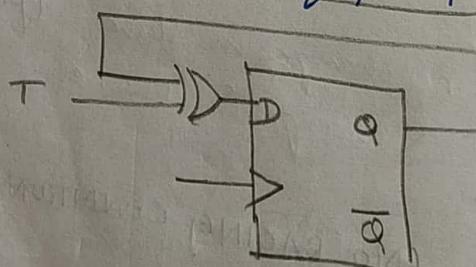
T	$Q(t+1)$
0	$Q(t)$
1	$\overline{Q(t)}$

Q	T	$Q(t+1)$
0	0	0
0	1	1
1	0	1
1	1	0

$$Q(t+1) = \overline{Q}T + Q\overline{T}$$

$$= Q \oplus T$$

T flip flop from D flip flop.



1. TRUTH

FO

TE

2. STATE

O/

IS

3. Tran

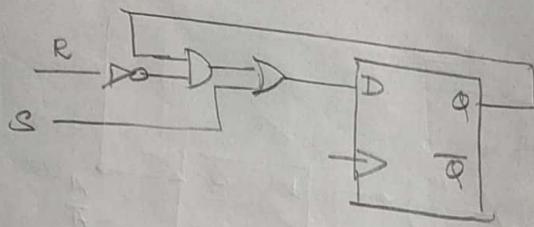
4. Excite

ie's a
flip

5. Chara

i/p

SR from D



Synchronous seq. ckt.

Analysis

⇒ circuit or equations

↓
equations

↓
State table

↓
State diagram

Design

↓ (From problem specification)

state diagram

↓

state table

↓

transition table

↓

equations

↓

logical Diagram

1. TRUTH TABLE:

For known i/p, ~~for gate~~ depending upon the type of gate o/p is generated

2. STATE TABLE:

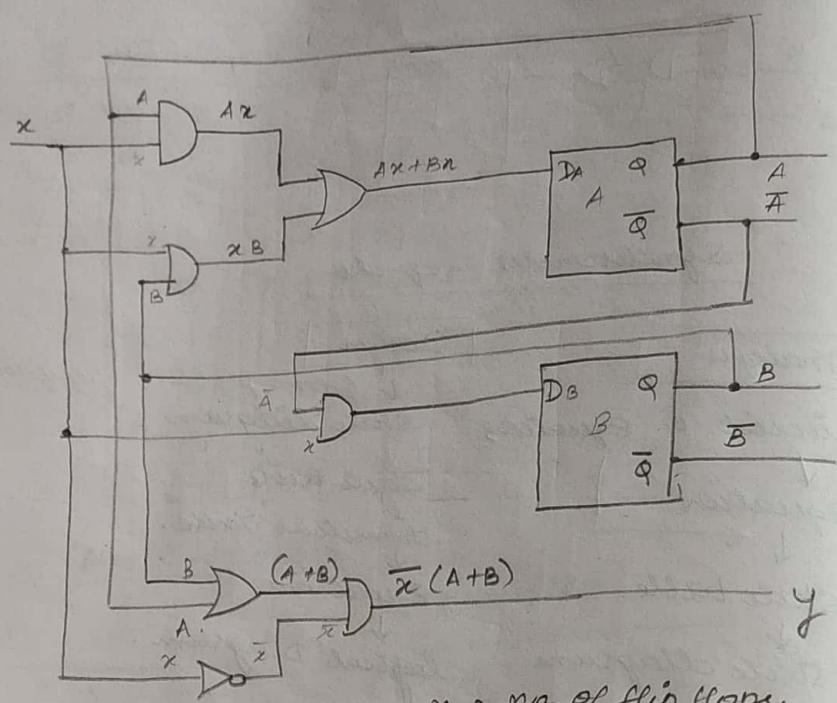
O/p for various i/p + Present state, ^{next} State is obtained.

3. Transition table:

4. Excitation table: O/p is known, $Q(t)$ and $Q(t+1)$ is also known, present state \downarrow next state flip flop inputs are found

5. Characteristic table:

Next state value, we have to find. i/p & present states are known.



$n \rightarrow$ no of flip flops.

$2^n \rightarrow$ no of states.

Equations.

State equations:

$$A(t+1) = D_A = XA + XB = X(A+B)$$

$$B(t+1) = D_B = XB$$

Output Equation:

$$Y = \overline{X}(A+B)$$

State table:

PS \rightarrow Present state (depends on 2 flip flops)

	P	S	X	N.S		Output
00 \rightarrow a	0	0	0	A(t+1)	B(t+1)	$Y = \overline{X}(A+B)$
01 \rightarrow b	0	0	1	0	0	0
10 \rightarrow c	0	0	1	0	1	0
11 \rightarrow d	0	1	0	0	0	1
	0	1	1	1	1	0
	1	0	0	0	0	0
	1	0	1	1	0	1
	1	1	0	0	0	0
	1	1	1	1	0	0

Final State Table

P S	N S
AB	$x=0$
a	a
b	a
c	a
d	a

State Diagram

Change of



01

d

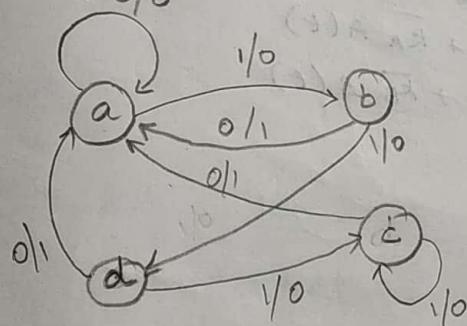
Final State Table \Rightarrow Mealy

PS	NS		Output Y		
AB	$x=0$	$x=1$	$x=0$	$x=1$	
a	a b	b a	0 1	0 0	$00 \rightarrow a$ $01 \rightarrow b$
b	a d	d a	1 1	0 0	$10 \rightarrow c$ $11 \rightarrow d$
c	a c	c a	1 1	0 0	
d	a c	c a	1 1	0 0	

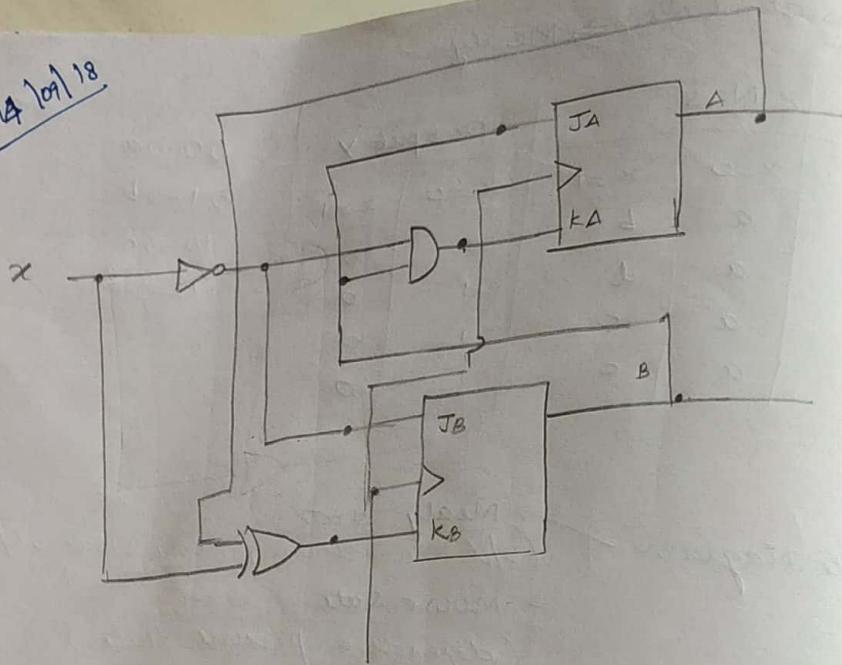
state Diagram

- \nearrow Mealy state diagram
(O/p depends on present state, i/p)
- \searrow Moore state diagram.
(depends on present state)

change in state \rightarrow arrow (represented)



14/09/18



$$Q(t+1) = J \bar{Q}(t) + \bar{K} Q(t)$$

$$A(t+1) = J_A \bar{A}(t) + \bar{K}_A A(t)$$

$$B(t+1) = J_B \bar{B}(t) + \bar{K}_B B(t)$$

$$J_A = B$$

$$J_B = \bar{x}$$

$$K_A = \bar{x} B$$

$$\bar{K}_A = \overline{\bar{x} B}$$

$$= x + \bar{B}$$

$$K_B = \bar{x} \oplus \bar{A} - x \oplus A$$

$$\bar{K}_B = \bar{x} \oplus \bar{A}$$

$$= x A + \bar{x} \bar{A}$$

$$A(t+1) =$$

$$B(t+1) =$$

$$A(t+1)$$

$$B(t+1)$$

$$P$$

$$A$$

$$\begin{cases} 0 \\ 0 \\ \vdots \\ 0 \end{cases}$$

$$\begin{cases} 1 \\ \vdots \\ 0 \end{cases}$$

$$A(t+1) = B\bar{A}(t) + (x + \bar{B}) A(t)$$

$$B(t+1) = \bar{x}\bar{B}(t) + (x_A + \bar{x}\bar{A}) B(t)$$

$$\begin{aligned} A(t+1) &= B\bar{A}(t) + (x + \bar{B}) A(t) \\ &= B\bar{A}(t) + x A(t) + \bar{B} A(t) \\ &= B\bar{A}(t) + \bar{B} A(t) + x A(t) \\ &= \cancel{B \odot \bar{A}(t)} + x A(t) \\ &= B \oplus A(t) + x A(t) \end{aligned}$$

$$\begin{aligned} B(t+1) &= \bar{x}\bar{B}(t) + x A B(t) + \bar{x}\bar{A} B(t) \\ &= \bar{x}\bar{B}(t) + B(t) (x \odot A) \end{aligned}$$

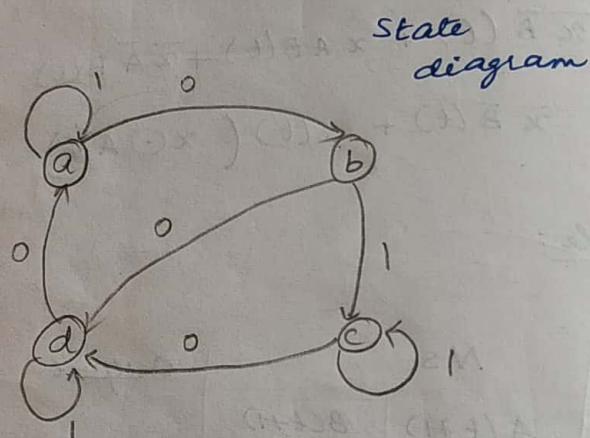
State Table:

P	S	x	Ns		Output
A	B	x	A(t+1)	B(t+1)	
{	0	0	0	1	1
	0	0	0	0	0
	0	1	1	1	0
	0	1	1	1	1
{	1	0	1	0	0
	1	0	1	0	0
	1	1	0	0	1
	1	1	0	1	

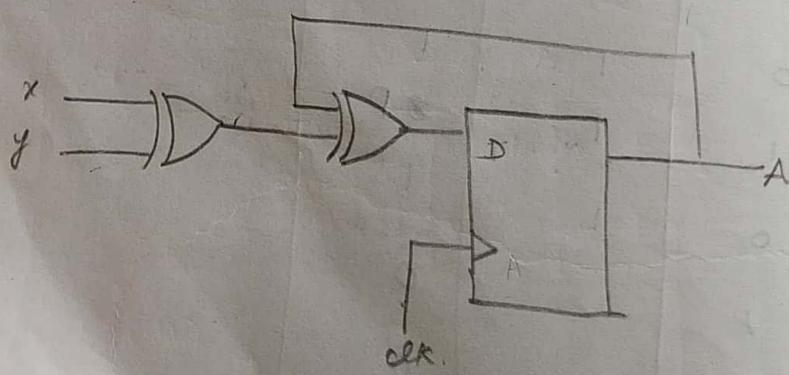
New state table:

P S	NS	
	$x=0$	$x=1$
a	b	a
b	d	c
c	d	c
d	a	d

QD



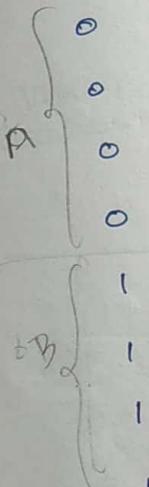
2.



D =

sta

A



Final

B8

$$Q(t+1) = D \quad \text{D flip flop.}$$

$$\begin{aligned} D &= (x \oplus y) \oplus A \\ &= A \oplus (x \oplus y) \\ &= A \oplus x \oplus y. \end{aligned}$$

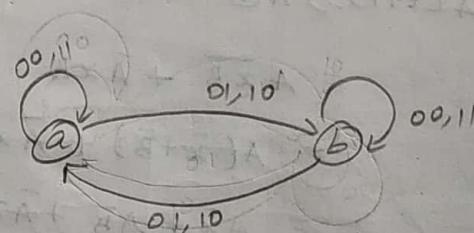
State Table:

A	x	y	Q(t+1) = D
A	0	0	0
	0	1	1
	1	0	1
	1	1	0
B	0	0	1
	0	1	0
	1	0	0
	1	1	1

Final State:

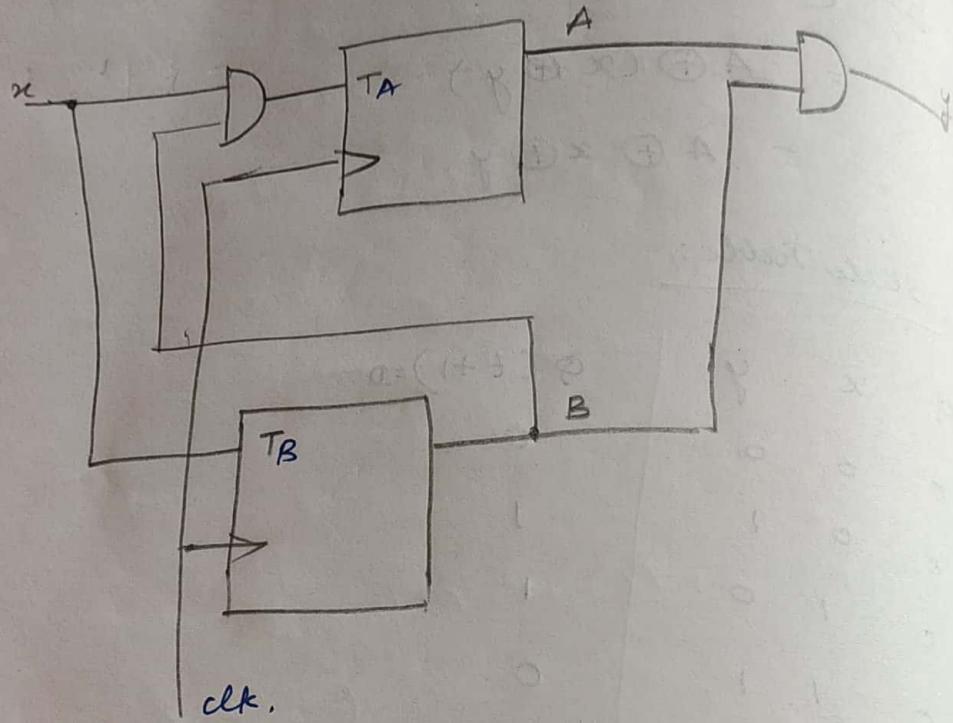
B8

State diagram



PS	NS			
A	$xy = 00$	01	10	11
0	a	b	b	a
1	b	a	a	b

3.



$$Q(t+1) = Q \oplus T$$

$$A(t+1) = A \oplus T_A$$

$$B(t+1) = B \oplus T_B$$

$$T_A = x \cdot B$$

$$T_B = x$$

$$A(t+1) = A \oplus x \cdot B$$

$$= A \bar{x} \cdot B + \bar{A} x \cdot B$$

$$= A(\bar{x} + \bar{B}) + \bar{A} x \cdot B$$

$$= A\bar{x} + A\bar{B} + \bar{A} x \cdot B.$$

$$y = A \cdot B$$

$$B(t+1) = B \oplus x$$

$$= B\bar{x} + \bar{B}x.$$

Moore's state Table: II

P S		N.S		O/P y
A	B	$x=0$	$x=1$	
		A	B	
0	0	b	a	0
0	1	c	b	0
1	0	d	c	0
1	1	a	d	1

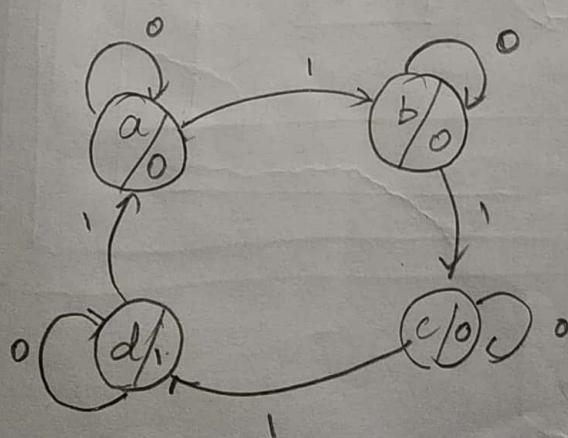
output is represented
in moore state
table.

Table I.

P.S			N.S		$y = A \cdot B$
A	B	x	$A(t+1)$	$B(t+1)$	
a	0	0	0	0	0
	0	1	0	1	0
b	0	0	0	1	0
	0	1	1	0	0
c	1	0	1	0	0
	1	1	1	1	0
d	1	0	1	1	1
	1	1	0	0	1

Moore's state diagram

it depends only on B.



4. A sequential circuit has 2 JK flipflops 'A' and 'B', 2 inputs 'x' and 'y' and 1 output z. The flipflop i/p equations and ctkt o/p eqns are

$$JA = \boxed{Bx + B'y'}$$

$$KA = B'y'$$

$$JB = A'x$$

$$KB = A + xy'$$

$$z = Ax'y' + Bx'y' \Rightarrow (A+B)x'y'$$

- (i) Draw the logic diagram of the ckt
- (ii) Tabulate the state table
- (iii) Derive the state eqns for A and B
- (iv) Draw the state diagram.

refer JK flipflop.

