

Exercise 1. Answer Sheet

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Problem 1. (30 points) For each function $f(n)$ and time T in the following table, determine the largest size n of a problem that can be solved in time T , assuming that the algorithm to solve the problem takes $f(n)$ milliseconds.

$f(n)$	$T = 1$ second 1000mil	$T = 1$ minute 60000mil	$T = 1$ hour 36000mil	$T = 1$ day 864000mil	$T = 1$ month (30 days) 25920000
\sqrt{n}	10^6	$36 \cdot 10^8$	$1296 \cdot 10^6$	$6746496 \cdot 10^6$	$6718464 \cdot 10^8$
n	10^3	60000	36000	864000	25920000
n^2	$10\sqrt{10}$	$100\sqrt{6}$	$60\sqrt{10}$	$10\sqrt{8640}$	$100\sqrt{2592}$
n^3	10	$10 \cdot (60)^{1/3}$	$10 \cdot (36)^{1/3}$	$10\sqrt{864}$	$10\sqrt{25920}$
2^n	$\log_2(1000)$	$\log_2(60000)$	$\log_2(36000)$	$\log_2(864000)$	$\log_2(25920000)$

Problem 2. (30 points) Consider sorting n numbers stored in array A by first finding the smallest element of A and exchanging it with the first element of the array, i.e. $A[1]$. Then find the second smallest element of A , and exchange it with $A[2]$. Continue in this manner for the first $n-1$ elements of A .

a) Write a pseudo-code for this algorithm which is known as “**Selection Sort**”.

```

SelectionSort(A):
    n = length(A) // Number of elements in array A

    for i from 0 to n-1 do:
        // Find the index of the smallest element in the unsorted part of the array
        minIndex = i

        for j from i+1 to n-1 do:
            if A[j] < A[minIndex] then:
                minIndex = j

        // Swap the smallest element with the first element of the unsorted part
        swap(A[i], A[minIndex])
    
```

b) What is the time complexity of the Selection Sort algorithm?

$G(n) = O(n^2)$

Problem 3. (40 points) Using the pseudo-code for **Merge Sort** algorithm given at the lecture, write a program implementing the **Merge Sort** algorithm. Use any programming language you know. Upload your

source code with instructions how to compile/run it. Give the input data and the program output in the space below.

The way of compile:

1. On the terminal, put “javac MergeSort.java”
2. There are 3 classes, so put “java MergeSort” on the terminal again.
3. Put the num. you will put and put the num for sorting.

Input 5 5 4 3 2 1

Output 1 2 3 4 5