

A REACTOR PHYSICS FRAMEWORK TO DETECT ANOMALIES IN HTGR CORE

BY

HARUN ARDIANSYAH

DISSERTATION

Submitted in partial fulfillment of the requirements
for the degree of Doctor of Philosophy in Nuclear, Plasma, and Radiological Engineering
in the Graduate College of the
University of Illinois Urbana-Champaign, 2025

Urbana, Illinois

Doctoral Committee:

Professor Tomasz Kozlowski, Director of Research, Chair
Professor Angela Di Fulvio
Assistant Professor Syed Bahauddin Alam
Professor Eduard-Wilhelm Kirr
Professor Christophe Demazière

Abstract

This is a comprehensive study of caffeine consumption by graduate students at the University of Illinois who are in the very final stages of completing their doctoral degrees. A study group of six hundred doctoral students. . . .

To my family back home in Indonesia, for their unwavering support and encouragement. To Nafi, the love of my life. To Ali, who makes my life complete.

Acknowledgments

All praises due to Allah, the God Almighty, for guiding me throughout this research endeavor and granting me success along the way. This dissertation is the culmination of many prayers. Most importantly from my family back home in Indonesia. I thank my parents, Mohammad Sholeh and Latifah, for believing in me, for giving me the confidence to move out from our hometown pursue study since I was in high school. I also want to thank my brother, Muhamad Subhan, for allowing me to pursue my study, and always being home during my absences. I would like to thank my wife, Annafiatur Regatra, for always being there for me, for being supportive of my research endeavor and have the confidence in me along my study. For trusting me as a husband, father, and scholar. Finally, I would like to thank my son, Ali Zein Ardiansyah. I will be a while for you to be able to read this dissertation, but your presence complete me. I will do everything in my power for you in the future.

I would like to acknowledge and thank all my teachers, present and the past, for helping me finding my passion in nuclear engineering. Especially, I would like to thank my PhD advisor, Prof. Tomasz Kozlowski, for his confidence in me to pursue neutron noise method as my topic for dissertation. I am thankful for all your encouragement to push me forward towards my study. Prof. Kozlowski also gave me a lot of opportunity for me to grow as a scholar. From writing skills, teaching, mentoring, and being confident in a conference, thank you for your support during my PhD study.

I would like to thank all the professors who served in my committee. Profs. Angela Di Fulvio, Syed Bahauddin Alam, Eduard Wilhelm Kirr, and Christophe Demazière, not only for reviewing my dissertation, but also for giving me meaningful insights along the way. I would like to especially thank Prof. Christophe Demazière for his guidance so far. I still remember my first meeting with Christophe in Gothenburg discussing my initial proposal for this thesis. I did not know a lot about neutron noise back then, but his support and guidance help me to formulate my objectives for this dissertation. Special thanks also to Prof. April Novak. Being Prof. Novak's teaching assistant for the last 3 semesters has helped me with my communication skills with students and how to proactively engage with students.

I would like to also thank NPPE family and staff, for helping me along my study. Coming in to NPPE as "COVID graduates" makes me want to work from home more at the time. But along the way, I learned that being on campus and able to interact with everybody in the department really help me to advance my progress. I would like to appreciate Kristie Stramaski for helping me with all the problems that I got into during my PhD. I would like to also thank Barbara Russell, Sarah Drum, and Becky Meline for helping me during my study at NPPE. Special thanks for all the people at Talbot 223. Thank you Dr. Roberto Agosta, Dr. Alvin Lee, Runxia Wen, Yifan Mao, Silvana Tabares, and all the people whose interaction I really appreciate.

And finally, I would like to thank YOU, the reader, for considering this out of many literatures out there. I hope this dissertation is professionally meaningful and contributes to everything that you are looking for.

Table of contents

Chapter 1	Introduction	1
1.1	Motivation	1
1.2	Objectives	2
1.3	Relevant Works	2
1.4	Outline	3
Chapter 2	Literature Review	4
2.1	Theory of Power Reactor Noise and Its Approaches	5
2.1.1	The Neutron Noise Experiments	5
2.1.2	Neutron Noise Derivation in Frequency Domain	6
2.1.3	Neutron Noise Models and Sources	10
2.1.4	Neutron Noise Source Unfolding	11
2.2	Application to Reactor Diagnostics	14
2.3	Computational Methods and Tools of Neutron Noise Analysis	16
2.3.1	Solving Neutron Noise Problems using Deterministic Methods	16
2.3.2	Solving Neutron Noise Problems using Monte Carlo Methods	18
2.4	Summary	19
Chapter 3	Application Neutron Noise Methods in 2D and 3D HTTR	21
3.1	Simulation of Neutron Noise in 2D and 3D HTTR	21
3.2	Application of Neutron Noise Unfolding methods for HTTR	21
Chapter 4	Novel Neutron Noise Unfolding methods and applications	22
Chapter 5	Conclusions	23
References		24

Chapter 1

Introduction

1.1 Motivation

Core diagnostics have been a key component of nuclear reactor operation to ensure reactor safety and performance. As a multicomponent system, perturbations in nuclear reactors are unavoidable. For power reactors, neutron noise is defined as the stochastic or random process that always happens in a nuclear reactor [1]. In the past, neutron noise experiments were developed to perform online monitoring and diagnostic of research reactors. Some examples include continuous neutron noise monitoring at the High Flux Isotope Reactor (HFIR), neutron and pressure noise monitors at the Molten Salt Reactor Experiment (MSRE) [2], neutron noise diagnostics at the Palisades Nuclear Generating Station in Michigan [3], and German measurements in Boiling Water Reactor (BWR) that showed vibrations quantified using neutron noise simulations [4].

The success of core diagnostics using neutron noise experiments motivates the development of computational models of neutron noise. In the early days, the computational models revolved around accurately modeling perturbations in a reactor as cross section perturbations [5], [6]. Further development of the model led to the concept of noise unfolding method, which is a method to detect the location of neutron noise and determine the magnitude of neutron noise. There are three main methods that have been developed to unfold neutron noise: the inversion method, the zoning method, and the scanning method. All of the methods require the Green function matrix to solve the problem [7]. The input for these methods is the noise fluxes from the detector readings, and the output is the noise locations and magnitude.

The development of advanced reactors has been rising for the last several years. This is backed with the support of the financial market through startups and private funds, and also supportive public perception of nuclear in recent years. While many developers focus on inherent reactor safety of advanced reactors, it is also important to develop a monitoring and diagnostic methods in advanced reactors.

In this work, computational models of neutron noise are developed based on the neutron diffusion equation in the frequency domain. The solver is developed using the box-scheme finite difference for rectangular and hexagonal geometries. The main goal of the solver is application to High-Temperature Gas-Cooled Reactors (HTGRs). However, application to rectangular geometries is also provided to differentiate the characteristics of HTGRs and Light Water Reactors (LWRs) systems. In this work, code-to-code comparisons are provided. Methods for unfolding neutron noise are also developed in the simulator to highlight the advantages and disadvantages of the methods.

1.2 Objectives

The main objective of this work is to develop and demonstrate core diagnostics in HTGR system using neutron noise method. The following objectives are identified to advance this goal:

1. Develop a numerical solver to perform forward, adjoint, and noise (in frequency domain) calculations, based on multigroup diffusion theory, in cartesian and hexagonal geometry.
2. Determine the characteristics of noise in HTGRs compared to LWRs through the zero-power reactor transfer function.
3. Determine the distinct characteristics of noise sources in LWRs and HTGRs for absorber of variable strength and fuel assembly vibration.
4. Perform noise unfolding in prismatic HTGRs using existing methods.
5. Derive new noise unfolding methods and demonstrate their performance relative to the existing methods.

Objective 1 focuses on the development of a numerical solver that could perform simulations in rectangular and hexagonal geometries using provided macroscopic cross-sections. This solver will be used to model and simulate neutron noise in HTGR systems, which is the focus of Objective 2. The HTGR model used in this case is the HTTR benchmark model. The HTTR benchmark is modeled in Monte Carlo code Serpent [8]. This Serpent model is a heterogeneous model with various materials. The details of the HTTR model will be provided in the following sections. This model is mainly used to generate homogenize cross-sections for the solver.

After obtaining the model, Objective 3 and 4 focuses on modeling various neutron noise models and unfolding methods that existed in literature. These models and methods are mainly developed for LWR systems. However, it is meaningful to apply the methods and model to understand the different behavior of HTGR system under small perturbations. The novelty of this works relies on Objective 5. Using all the information known from previous Objectives, it is important to extend these models and methods to reflect the important physics of HTGR system and leveraging all the known parameters from forward and adjoint calculations.

Objectives 1, 2, and 3 are preliminary and background work necessary to advance beyond the current state-of-the-art. Objective 4 establishes baseline performance of existing noise unfolding methods, which is improved by new methods derived in Objective 5. Objectives 3, 4, and 5 all contribute a new body of knowledge. Objective 3 contributes a quantitative explanation of LWR and HTGR neutron physics differences. Objective 4 contributes a consistent performance comparison of existing noise unfolding methods for the HTGR reactor. Objective 5 derives new noise unfolding methods and demonstrates their superior performance relative to existing methods. Objective 5 is a new and original contribution to the body of knowledge.

1.3 Relevant Works

Relevant works and toolsets that are related to the objectives are presented in this section. These works are compared with current work to identify the gaps in the method. The discussion is divided into two criteria. Namely, neutron noise solver and noise unfolding method.

For the neutron noise solver, this work focuses on solving the neutron noise equation using a deterministic approach, namely the diffusion method. This work primarily follows the CORE SIM+ simulator developed at

Chalmers University of Technology, Sweden. CORE SIM+ is a 3D neutron diffusion solver that can solve forward, adjoint, and noise problems for rectangular geometries [9]. This simulator has been used to simulate neutron noise for experiments and has been validated using experimental data [10], [11]. CORE SIM+ uses box-scheme finite difference for spatial discretization, and frequency domain analysis. The difference between the simulator and this work is the energy treatment. This work uses a multigroup approach, while CORE SIM+ only uses two group approach. Having a multigroup approach is generally beneficial to advanced reactors, especially HTGR, since the neutron spectrum is different from PWRs [12]. Another code to be used for comparison is FEMFFUSION, which was developed in Spain as the time-domain counterpart of CORE SIM+ in the CORTEX project [13]. FEMFFUSION uses time-domain for noise analysis and the finite element method for discretization. FEMFFUSION can also solve the neutron transport equation using simplified spherical harmonic (SP_N) approximations. Table 1.1 summarizes the different approaches in the simulators.

Table 1.1: Summary of features of simulators for noise calculation

Parameter	CORE SIM+	FEMFFUSION	Current Work
Working domain	Frequency	Time and Frequency	Frequency
Neutron transport method	Diffusion	Diffusion and SP_N	Diffusion
Energy group	Two group	Multigroup	Multigroup
Spatial discretization	Box-scheme finite difference (rectangular only)	Finite element	Box-scheme finite difference (rectangular and triangular)
Code language	Matlab	C++	Python

In terms of neutron noise unfolding method, [14] provided the theory and derivation of noise unfolding method. The unfolding method is used to diagnose an absorber of variable strength noise source. This is further supported by [15] by providing several additional cases that are solved using hybrid method. This work will focus on improving the existing method to solve generalized noise source. Compared to both papers, the approach in this work will focus on noise flux reconstruction, that later can be integrated with known inverse of Green's function matrix.

1.4 Outline

This dissertation describes the motivation, objectives, methodology, results, and conclusions towards the advancement of the neutron noise unfolding methods and its application HTGR core. The remainder of this dissertation is organized as follows. Chapter 2 presents a literature review of neutron noise methods, its applications for diagnostics, and neutron noise unfolding method. Chapter 3 provide the development of computational tools for forward, adjoint, and noise calculations, and also verification of results in 2D, 3D rectangular and hexagonal geometries. Chapter 4 focuses on the application of neutron noise methods for AVS and FAV in 2D and 3D HTTR core, including application of existing neutron noise unfolding methods. Chapter 5 introduces the novel methods of neutron noise unfolding and their application to 2D and 3D HTTR core.

Chapter 2

Literature Review

In nuclear engineering, “noise” can be categorized into two distinct definitions. The first definition is the zero-power reactor noise, also known as pile noise, which is the random fluctuation of fission chains that could affect the reactor operation in low-powered systems [7], [16], [17]. The other category is the at-power reactor noise, also known as neutron noise, which is defined as the stochastic or random processes in which a nuclear reactor inheres [1]. Another meaning also defines noise as the fluctuation in the detector output when the incident radiation is steady [18]. These random fluctuations are common in a nuclear reactor system. A nuclear reactor is a very delicate and complex system that is expected to produce some noise [19].

Neutron noise has been studied since the early adaptation of power reactors. This is because we have realized the importance of some fluctuating components in the state variables of nuclear reactors, such as thermal power, outlet coolant temperature, control rods, and many others [5], [6]. The original neutron noise theory observation can be found in the reactor oscillator experiments performed at the “Clinton Pile” in Oak Ridge, USA. Clinton Pile is the nickname of the X-10 Reactor built in today’s Oak Ridge National Laboratory [7].

Neutron noise serves several beneficial purposes, one for core monitoring and diagnostics. The monitoring and diagnostics encompass a wide range of nuclear reactor operations, including steady-state and transient operations. During the operation of any system, perturbations are unavoidable, including in nuclear reactor systems. The perturbations could be significant, such as control rod insertion, loss of forced cooling, and many other examples that could lead to unexpected behavior in the transient operation [20]. Detecting any anomalies or perturbations would enable operators to respond appropriately to the problem. This will prevent any accident from occurring [21].

Various aspects can cause the effects of perturbation. For example, several technological processes such as mechanical vibrations in the fuel assemblies and absorbers, boiling of the coolant/moderator in a Boiling Water Reactor (BWR), and instability of flow dynamics in the system may cause some perturbations that will lead to fluctuations of reactor system behavior [19]. Reactor diagnostics using noise analysis have been widely employed globally. Noise analysis relies on measuring fluctuations in process parameters, such as neutron flux, around their mean values. Using noise analysis, non-intrusive, online core monitoring can be done more accurately [22]. These fluctuations represent the localized and instantaneous phenomenon in the nuclear reactor. It is described as the deviation around the mean values

2.1 Theory of Power Reactor Noise and Its Approaches

2.1.1 The Neutron Noise Experiments

In the past, the neutron noise method was used in experiments to perform core monitoring and diagnostics. In general, the neutron noise experiments involve obtaining a statistical descriptor from measurements of statistical signals [19]. The descriptor measured from the reactor is the neutron flux signals. The detector responses are recorded in the time domain. The end goal of the noise analysis is to perform a spectral analysis of the noise, assuming the noise is an oscillation induced by external materials. Before performing the transform from the time domain to the frequency domain, it is essential to note that the detector's signals should be preprocessed to remove any possible trends from the signals. Trend removal is a necessary step since it is assumed that the analysis is done during steady-state conditions [10].

The detector responses are then converted into the frequency domain by performing a fast Fourier transform to perform the spectral analysis. The quantity of interest in this case is the cross-power spectral density (CPSD) [23]. The CPSD represents the correlation of power between two different signals as a function of frequency. The CPSD is defined as follows:

$$S_{xy}(f) = \lim_{T \rightarrow \infty} \frac{1}{T} \mathbb{E} \left(X^*(f) \cdot Y(f) \right) \quad (2.1)$$

where $S_{xy}(f)$ is the CPSD as a function of frequency, T is the period, $X(f)$ and $Y(f)$ is the Fourier transform of $x(t)$ and $y(t)$, and $X^*(f)$ is the complex conjugate of $X(f)$. It should be noted that Equation 2.1 shows that CPSD is essentially the Fourier transform of the cross-correlation function [19]. It should also be noted that the signal is recorded at a particular time value in the noise experiments. Therefore, Equation 1 would be complicated to achieve. Another way to calculate CPSD is to calculate each detector signal's power spectral density (PSD). One method used to estimate the PSD for a detector signal is the Welch method, where the PSD is calculated directly without an autocorrelation function [24]. The Welch method works by introducing a window function to each frequency segment, performing a fast Fourier transform for each segment, and then averaging the resulting PSD estimates over all segments. The Welch method can be written as follows:

$$S_{xy}(f) = \frac{1}{N} \sum_{k=1}^N X_k^*(f) \cdot Y_k(f) \quad (2.2)$$

where N is the number of segments in the Welch method, $X(f)$ and $Y(f)$ are the Fourier transforms of $x(t)$ and $y(t)$, and $X^*(f)$ the complex conjugate of $X(f)$ [23].

Other than the CPSD, another variable of interest in a neutron noise experiment is coherence, which is defined as the measure of commonality between two signals. It can also be defined as the closeness of two signals to have a cause-and-effect relationship. The coherence is described as follows [3]:

$$COH \equiv \gamma^2(f) = \frac{|S_{xy}(f)|^2}{PSD_x(f) \cdot PSD_y(f)} \quad (2.3)$$

Equation 2.3 shows that two perfectly correlated signals would have a coherence of 1, and two uncorrelated signals would have a coherence of 0. The coherence would act as an indicator of the data quality from the signals. It is common to aim for COH ≥ 0.8 for noise experiments [23]. If the two signals have relatively high coherence, it is also meaningful to have the phase relationship between the signals, which is defined as follows [3]:

$$\theta(f) = \tan^{-1} \left(\frac{\text{Im}(S_{xy}(f))}{\text{Re}(S_{xy}(f))} \right) \quad (2.4)$$

The spectral analysis is done by observing the detector signals' CPSD, PSD, and coherence. The PSD analysis can show some fluctuations directly, but using CPSD and coherence will help eliminate some uncertainties that might still be propagated in the PSD.

2.1.2 Neutron Noise Derivation in Frequency Domain

Neutron noise is derived using neutron transport theory, such as P_N transport and S_N transport theory, or diffusion [25], [26], in the case of power reactors. Here, we will focus on the diffusion theory and its application to neutron noise analysis. The diffusion theory is chosen as it satisfies the phenomena for most cases of practical interest [7]. Here, we will consider only one group diffusion, which allows us to understand the general behavior of the system [7].

In general, the derivation of the neutron noise equation begins with the neutron diffusion equation and the precursor equation. We are interested in the local scale case of neutron noise. Therefore, we can assume that temporal fluctuation in diffusion coefficient can be neglected, such that,

$$\nabla D(\mathbf{r}, t) \nabla \phi(\mathbf{r}, t) = \nabla D(\mathbf{r}) \nabla \phi(\mathbf{r}, t) \quad (2.5)$$

For power reactors, neutron noise theory assumes that the stationary deviation in the system is small enough that the overall system would not change significantly [7]. This means that the noise phenomena can be analyzed using linear equations. Additionally, we can separate the form of any time-dependent variable into its mean value and fluctuations.

$$X(\mathbf{r}, t) = X_0(\mathbf{r}) + \delta X(\mathbf{r}, t) \quad (2.6)$$

We can apply these definitions to the time-dependent neutron diffusion equations. Then, to further simplify the equation, we define some approximations,

- The cross-product of the fluctuating terms is neglected. This means that we only keep the first-order behavior of the neutron noise. The higher order might be relevant for a specific case. However, generally, the first order is good enough to explain the behavior of neutron noise in the reactor.

$$\Sigma_t(\mathbf{r}, t) \phi_g(\mathbf{r}, t) = \Sigma_{t,0}(\mathbf{r}) \phi_{g0}(\mathbf{r}) + \delta \Sigma_t(\mathbf{r}, t) \phi_{g0}(\mathbf{r}) + \Sigma_{t,0}(\mathbf{r}) \delta \phi_g(\mathbf{r}, t) \quad (2.7)$$

- The reactor system is assumed to be critical. A critical reactor assumes that the number of neutrons in each cycle is constant at all times, reducing fluctuations in neutron behavior.
- One group of delayed neutron precursors is used.

Applying all of these approximations and fluctuation definitions of the time-dependent neutron diffusion equation and the neutron precursor equation, we get,

$$\begin{aligned}
\frac{1}{v_g} \frac{\partial \delta \phi_g(\mathbf{r}, t)}{\partial t} - \nabla D_g(\mathbf{r}) \nabla \delta \phi_g(\mathbf{r}, t) + \left(\Sigma_{t,g,0}(\mathbf{r}) \delta \phi_g(\mathbf{r}, t) + \delta \Sigma_{t,g}(\mathbf{r}, t) \phi_{g,0}(\mathbf{r}) \right) = \\
\sum_{g'=1}^G \left(\Sigma_{s0,g',g,0}(\mathbf{r}) \delta \phi_{g'}(\mathbf{r}, t) + \delta \Sigma_{s0,g',g}(\mathbf{r}, t) \phi_{g',0}(\mathbf{r}) \right) \\
\chi_g^p \frac{1 - \beta_{\text{eff}}}{k_{\text{eff}}} \left(\sum_{g'=1}^G \nu \Sigma_{f,g',0}(\mathbf{r}) \delta \phi_{g'}(\mathbf{r}, t) + \chi_g \sum_{g'=1}^G \delta \nu \Sigma_{f,g'}(\mathbf{r}, t) \phi_{g',0}(\mathbf{r}) \right) + \lambda \delta C(\mathbf{r}, t)
\end{aligned} \tag{2.8}$$

And the precursor equation:

$$\frac{\partial \delta C(\mathbf{r}, t)}{\partial t} = -\lambda \delta C(\mathbf{r}, t) + \chi_g^d \frac{\beta_{\text{eff}}}{k_{\text{eff}}} \left(\sum_{g'=1}^G \nu \Sigma_{f,g',0}(\mathbf{r}) \delta \phi_{g'}(\mathbf{r}, t) + \sum_{g'=1}^G \delta \nu \Sigma_{f,g'}(\mathbf{r}, t) \phi_{g',0}(\mathbf{r}) \right) \tag{2.9}$$

Using Equation 2.8 and 2.9, the time domain analysis can be conducted to solve for $\delta \phi_g(\mathbf{r}, t)$. If the frequency domain analysis is desired, then we can multiply Equation 2.8 and 2.9 with $\int_{-\infty}^{\infty} \exp(-i\omega t) dt$, which yields to,

$$\begin{aligned}
\frac{i\omega}{v_g} \delta \phi_g(\mathbf{r}, \omega) - \nabla D_g(\mathbf{r}) \nabla \delta \phi_g(\mathbf{r}, \omega) + \left(\Sigma_{t,g,0}(\mathbf{r}) \delta \phi_g(\mathbf{r}, \omega) + \delta \Sigma_{t,g}(\mathbf{r}, \omega) \phi_{g,0}(\mathbf{r}) \right) = \\
\sum_{g'=1}^G \left(\Sigma_{s0,g',g,0}(\mathbf{r}) \delta \phi_{g'}(\mathbf{r}, \omega) + \delta \Sigma_{s0,g',g}(\mathbf{r}, \omega) \phi_{g',0}(\mathbf{r}) \right) \\
\chi_g^p \frac{1 - \beta_{\text{eff}}}{k_{\text{eff}}} \left(\sum_{g'=1}^G \nu \Sigma_{f,g',0}(\mathbf{r}) \delta \phi_{g'}(\mathbf{r}, \omega) + \sum_{g'=1}^G \delta \nu \Sigma_{f,g'}(\mathbf{r}, \omega) \phi_{g',0}(\mathbf{r}) \right) + \lambda \delta C(\mathbf{r}, \omega)
\end{aligned} \tag{2.10}$$

And the precursor equation:

$$i\omega \delta C(\mathbf{r}, \omega) = -\lambda \delta C(\mathbf{r}, \omega) + \chi_g^d \frac{\beta_{\text{eff}}}{k_{\text{eff}}} \left(\sum_{g'=1}^G \nu \Sigma_{f,g',0}(\mathbf{r}) \delta \phi_{g'}(\mathbf{r}, \omega) + \sum_{g'=1}^G \delta \nu \Sigma_{f,g'}(\mathbf{r}, \omega) \phi_{g',0}(\mathbf{r}) \right) \tag{2.11}$$

Further simplification yields to,

$$\begin{aligned}
\frac{i\omega}{v_g} \delta \phi_g(\mathbf{r}, \omega) - \nabla D_g(\mathbf{r}) \nabla \delta \phi_g(\mathbf{r}, \omega) + \left(\Sigma_{t,g,0}(\mathbf{r}) \delta \phi_g(\mathbf{r}, \omega) + \delta \Sigma_{t,g}(\mathbf{r}, \omega) \phi_{g,0}(\mathbf{r}) \right) = \\
\sum_{g'=1}^G \left(\Sigma_{s0,g',g,0}(\mathbf{r}) \delta \phi_{g'}(\mathbf{r}, \omega) + \delta \Sigma_{s0,g',g}(\mathbf{r}, \omega) \phi_{g',0}(\mathbf{r}) \right) \\
\frac{1}{k_{\text{eff}}} \left(\chi_g^p (1 - \beta_{\text{eff}}) + \chi_g^d \frac{\lambda \beta_{\text{eff}}}{i\omega + \lambda} \right) \left(\sum_{g'=1}^G \nu \Sigma_{f,g',0}(\mathbf{r}) \delta \phi_{g'}(\mathbf{r}, \omega) + \chi_g \sum_{g'=1}^G \delta \nu \Sigma_{f,g'}(\mathbf{r}, \omega) \phi_{g',0}(\mathbf{r}) \right)
\end{aligned} \tag{2.12}$$

Equation 2.12 is the neutron noise equation in the frequency domain. The equation shows that the noise equation in the frequency domain is similar to the diffusion equation in a subcritical system (or a fixed source system). However, this diffusion equation has a complex value term and noise source. The complex terms represent the complex-valued absorption of the system. The noise source $S(\mathbf{r}, \omega)$ consists of the fluctuation of the cross-sections multiplied by the static neutron flux $\phi_{g0}(\mathbf{r})$ [27].

The computational method can work in tandem with the experimental method of neutron noise. The experimental method measures the quantity of interest using the known power spectral density of the detectors.

The computational method can extend the analysis by verifying the CPSD at known frequency to detect the location of noise sources [11]. The general workflow is described in Figure 2.1.

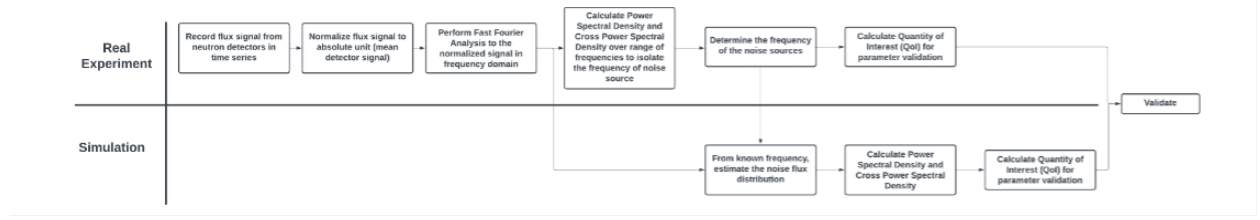


Figure 2.1: General workflow of neutron noise experiment and simulation

Assuming $\delta\phi_g(\mathbf{r}, \omega)$ is known from the computational method, the PSD can be determined using Welch method as follow [10]:

$$\text{CPSD}_{xy} = \left(\frac{\delta\phi_g(\mathbf{r}, \omega)}{\phi_g(\mathbf{r})} \right)_x^* \cdot \left(\frac{\delta\phi_g(\mathbf{r}, \omega)}{\phi_g(\mathbf{r})} \right)_y \quad (2.13)$$

To further understand the physical meaning of neutron noise, we can utilize point kinetic approximations to extract the integral parameters that characterize the reactor. To do this, we start by factorizing the time-dependent forward flux into its amplitude and shape function. Such that,

$$\phi(\mathbf{r}, E, t) = P(t)\psi(\mathbf{r}, E, t) \quad (2.14)$$

with the following normalization condition,

$$\frac{\partial}{\partial t} \int_{\mathbf{E}} \int_{\mathbf{r}} \left(\frac{1}{v} \phi^\dagger(\mathbf{r}, E) \psi(\mathbf{r}, E, t) \right) d\mathbf{r} dE = 0 \quad (2.15)$$

In this case, $\phi^\dagger(\mathbf{r})$ is the solution of the adjoint equation.

Then, we split all the time-dependent components into the main values and the perturbations. Here, we define the initial condition (mean value) of the forward flux as follows,

$$\phi_0(\mathbf{r}, E) = P_0\psi_0(\mathbf{r}, E) \quad (2.16)$$

Therefore, we can write the noise flux as follows (neglecting second-order terms),

$$\begin{aligned} \delta\phi(\mathbf{r}, E, t) &= \phi(\mathbf{r}, E, t) - \phi_0(\mathbf{r}, E) \\ &= \left(P_0 + \delta P(t) \right) \left(\frac{\phi_0(\mathbf{r}, E)}{P_0} + \delta P(t) \right) - \phi_0(\mathbf{r}, E) \\ &= \phi_0(\mathbf{r}, E) \frac{\delta P(t)}{P_0} + P_0 \delta\psi(\mathbf{r}, E, t) \end{aligned} \quad (2.17)$$

Applying Fourier transforms to Equation 2.17 yields the following.

$$\delta\phi(\mathbf{r}, E, \omega) = \phi_0(\mathbf{r}, E) \frac{\delta P(\omega)}{P_0} + P_0 \delta\psi(\mathbf{r}, E, \omega) \quad (2.18)$$

Equation 2.18 shows that the noise flux can be split into two components. The first term on the right-hand side is the point-kinetic term, and the second is the spatial component of the noise flux.

The value of power perturbation can be determined as follows. We can multiply Eq 2.18 by $\phi^\dagger(\mathbf{r})/v$ and integrate over all the spatial and energy domains, which leads to the following.

$$\int_{\mathbf{E}} \int_{\mathbf{r}} \frac{1}{v} \phi^\dagger(\mathbf{r}, E) \delta\phi(\mathbf{r}, E, \omega) d\mathbf{r} dE = \frac{\delta P(\omega)}{P_0} \int_{\mathbf{E}} \int_{\mathbf{r}} \frac{1}{v} \phi^\dagger(\mathbf{r}, E) \phi_0(\mathbf{r}, E) d\mathbf{r} dE + P_0 \int_{\mathbf{E}} \int_{\mathbf{r}} \frac{1}{v} \phi^\dagger(\mathbf{r}, E) \delta\psi(\mathbf{r}, E, \omega) d\mathbf{r} dE \quad (2.19)$$

Notice that due to the normalization in Equation 2.15 and the initial condition of the system, $\delta\psi(\mathbf{r}, 0) = 0$ [28]. This yields to the following.

$$\frac{\delta P(\omega)}{P_0} = \frac{\int_{\mathbf{E}} \int_{\mathbf{r}} \frac{1}{v} \phi^\dagger(\mathbf{r}) \delta\phi(\mathbf{r}, \omega) d\mathbf{r} dE}{\int_{\mathbf{E}} \int_{\mathbf{r}} \frac{1}{v} \phi^\dagger(\mathbf{r}) \phi_0(\mathbf{r}) d\mathbf{r} dE} \quad (2.20)$$

Continuing with the derivation of the point kinetics component, we start from time-dependent neutron diffusion equation, multiply both sides with adjoint fluxes as a weighting function, and integrate over the spatial domain, yielding the following.

$$\begin{aligned} \frac{dP_0}{dt} + \frac{d(\delta P(t))}{dt} &= \frac{\rho_0}{\Lambda} (P_0 + \delta P(t)) + \frac{\delta\rho(t)}{\Lambda} (P_0 + \delta P(t)) - \frac{\beta}{\Lambda} (P_0 + \delta P(t)) + \lambda(C_0 + \delta C(t)) \\ \frac{dC_0}{dt} + \frac{d(\delta C(t))}{dt} &= \frac{\beta}{\Lambda} (P_0 + \delta P(t)) - \lambda(C_0 + \delta C(t)) \end{aligned} \quad (2.21)$$

By neglecting second-order terms and eliminating the time-independent component, we can simplify the equation into:

$$\begin{aligned} \frac{d(\delta P(t))}{dt} &= \frac{\delta\rho(t)}{\Lambda} P_0 - \frac{\beta}{\Lambda} \delta P(t) + \lambda \delta C(t) \\ \frac{d(\delta C(t))}{dt} &= \frac{\beta}{\Lambda} \delta P(t) - \lambda \delta C(t) \end{aligned} \quad (2.22)$$

Applying the Fourier Transform to Equation 2.22 yields to:

$$\begin{aligned} i\omega \delta P(\omega) &= \frac{P_0}{\Lambda} \delta\rho(\omega) - \frac{\beta}{\Lambda} \delta P(\omega) + \lambda \delta C(\omega) \\ i\omega \delta C(\omega) &= \frac{\beta}{\Lambda} \delta P(\omega) - \lambda \delta C(\omega) \end{aligned} \quad (2.23)$$

where $\omega = 2\pi f$. Simplifying the precursor equation of Equation 2.23, yields:

$$\delta C(\omega) = \frac{\beta}{\Lambda(i\omega + \lambda)} \delta P(\omega) \quad (2.24)$$

Then, substituting Equation 2.24 to the power equation of Equation 2.23, yields to:

$$\begin{aligned} i\omega \delta P(\omega) &= \frac{P_0}{\Lambda} \delta\rho(\omega) - \frac{\beta}{\Lambda} \delta P(\omega) + \frac{\lambda\beta}{\Lambda(i\omega + \lambda)} \delta P(\omega) \\ \frac{P_0}{\Lambda} \delta\rho(\omega) &= \left(i\omega + \frac{\beta}{\Lambda} - \frac{\lambda\beta}{\Lambda(i\omega + \lambda)} \right) \delta P(\omega) \\ \delta P(\omega) &= \delta\rho(\omega) P_0 \frac{1}{\Lambda \left(i\omega + \frac{\beta}{\Lambda} - \frac{\lambda\beta}{\Lambda(i\omega + \lambda)} \right)} \\ \delta P(\omega) &= \delta\rho(\omega) P_0 G(\omega) \end{aligned} \quad (2.25)$$

Since we derive Equation 2.25 from Equation 2.9, we can explicitly define $\delta\rho(\omega)$ as follows,

$$\delta\rho(\omega) = \frac{\int_{\mathbf{E}} \int_{\mathbf{r}} \phi^\dagger(\mathbf{r}, E) d\mathbf{S}(\mathbf{r}, E, \omega) d\mathbf{r} dE}{\int_{\mathbf{E}} \int_{\mathbf{r}} \phi^\dagger(\mathbf{r}, E) \mathbf{F}(\mathbf{r}, E) d\mathbf{r} dE} \quad (2.26)$$

where $d\mathbf{S}(\mathbf{r}, \omega)$ is the noise source in the system, and $\mathbf{F}(\mathbf{r})$ is the fission source in the forward equation. This means that we have two ways to calculate the zero-power reactor transfer function $G(\omega)$. They are,

$$G(\omega) = \frac{1}{\Lambda \left(i\omega + \frac{\beta}{\Lambda} - \frac{\lambda\beta}{\Lambda(i\omega + \lambda)} \right)} = \frac{\delta P(\omega)/P_0}{\delta\rho(\omega)} \quad (2.27)$$

The zero-power reactor transfer function is one method for observing a system's behavior during a small sinusoidal perturbation. It could also be used to check whether the reactivity feedback is as expected from the design [29].

2.1.3 Neutron Noise Models and Sources

Neutron noise sources can generally be divided into two categories. The first category is the localized absorbers of variable strength. Although terminology specifies absorbers, these types of noise typically refer to all types of cross-sections. This includes absorption, fission, and scattering [7]. The absorbers of variable strength can be represented as fluctuations in the macroscopic cross-section at a given fixed location \mathbf{r}_0 and the noise sources can be expressed as:

$$\delta\Sigma_x(\mathbf{r}, \omega) = \gamma(\omega)\delta(\mathbf{r} - \mathbf{r}_0) \quad (2.28)$$

where $\gamma(\omega)$ is the noise source strength. Generally, the strength of the noise sources might depend on the noise frequency [7]. Some examples of this type of noise include the perturbations traveling with the coolant flow [30] and vibration in the control rod [31]. In terms of modeling the noise source in a solver, the localized absorbers of variable strength can be intuitively modeled as a perturbation of cross-sections in the center of computational nodes [9].

The second category is the localized vibrating absorber. The vibrating absorbers could include vibration of the fuel assembly [32] or vibration of the core barrel [33]. In the vibration absorber, the perturbation is modeled as the displacement of the vibrating assembly from its nominal position. In a 2D case, the perturbation is defined as follows:

$$\begin{aligned} \delta\Sigma_a(x, y, \omega) = & \varepsilon_x(\omega)\delta(x - a_0)(\Sigma_{a,i,j} - \Sigma_{a,i-1,j}) + \\ & \varepsilon_x(\omega)\delta(x + a_0)(\Sigma_{a,i,j} - \Sigma_{a,i+1,j}) + \\ & \varepsilon_y(\omega)\delta(y - b_0)(\Sigma_{a,i,j} - \Sigma_{a,i,j+1}) + \\ & \varepsilon_y(\omega)\delta(y + b_0)(\Sigma_{a,i,j} - \Sigma_{a,i,j-1}) \end{aligned} \quad (2.29)$$

where $\varepsilon_x(\omega)$ is the displacement x-axis, $\varepsilon_y(\omega)$ is the displacement y-axis, a_0 and b_0 are the equilibrium positions at the boundary of the vibrating assembly.

If the amplitude of $\varepsilon_x(\omega)$ and $\varepsilon_y(\omega)$ significantly lower than the size of the reactor core d, then one can use a weak absorber approach. The vibrating motion of the absorber can be described as a two-dimensional problem, where the vibrating motion will move on a two-dimensional stochastic trajectory [34]. The perturbation of

vibrating absorbers can be represented as:

$$\delta\Sigma_a(x, y, \omega) = \gamma \left(\delta(\mathbf{r} - \mathbf{r}_p - \varepsilon(t)) - \delta(\mathbf{r} - \mathbf{r}_p) \right) \quad (2.30)$$

where \mathbf{r}_p is the equilibrium position of the rods in motion, and $\varepsilon(t)$ is the two-dimensional displacement of the rods in motion from the equilibrium position [7]. This model is also called the ε/d model. In terms of modeling the noise source in a solver, the localized vibrating absorbers can be modeled as a perturbation of cross-sections at the boundary of the vibrating region [9].

2.1.4 Neutron Noise Source Unfolding

Neutron noise source unfolding is a method that is used to identify the type of noise source and locate the position at which the perturbations occur. Generally, the noise source unfolding method primarily depends on Green's function. Hence, determining Green's function from the neutron noise equation is necessary [14]. The following method uses Green's function for the neutron noise unfolding.

Inversion Method

As the name suggests, the inversion method inverts Green's function to estimate the noise sources in the system. Recalling the definition of flux perturbations:

$$\delta\phi(\mathbf{r}, \omega) = \int_{V_p} G(\mathbf{r}, \mathbf{r}_p, \omega) S(\mathbf{r}_p, \omega) dV_p \quad (2.31)$$

In matrix form, Equation 2.31 can be written as matrix-vector multiplication:

$$\delta\phi(\mathbf{r}, \omega) = G(\mathbf{r}_p \rightarrow \mathbf{r}, \omega) S(\mathbf{r}_p, \omega) \quad (2.32)$$

Therefore, the noise source can be determined by inverting the Green's function such that:

$$S(\mathbf{r}_p, \omega) = G^{-1}(\mathbf{r}_p \rightarrow \mathbf{r}, \omega) \delta\phi(\mathbf{r}, \omega) \quad (2.33)$$

Equation 2.32 is trivial to solve if Green's function and the flux perturbations at each computational node are known. However, in practice, only a few detectors can be used to measure the neutron flux. Thus, only a few elements of Green's function and the flux perturbation can be obtained from the detectors.

An alternative proposed by [14] is to interpolate the detector readings to match the vector size $\delta\phi(\mathbf{r}, \omega)$. In the paper, [14] assumes that the detector is sensitive to thermal neutron and the noise source is known to be a perturbation of thermal absorption cross-section. Therefore, the interpolation is written as:

$$S(\mathbf{r}_p, \omega) = G^{-1}(\mathbf{r}_p \rightarrow \mathbf{r}_{\text{interp}}, \omega) \delta\phi(\mathbf{r}_{\text{interp}}, \omega) \quad (2.34)$$

where $G^{-1}(\mathbf{r}_p \rightarrow \mathbf{r}_{\text{interp}})$ has size $N \times N$, $\delta\phi(\mathbf{r}_{\text{interp}}, \omega)$ has size N , and $S(\mathbf{r}_p, \omega)$ has size N .

Using an interpolation method, [14] were able to reconstruct the noise source using an interpolation method. However, the inversion might have some problems in the boundaries because the interpolated thermal flux perturbation is forced to be equal to zero outside the reflector nodes. Even though the reconstruction at the boundaries produced poor approximation, the overall process is still providing promising results. The

result of this method is highly dependent on the interpolation process. Incorrect interpolation would lead to inaccuracies in the unfolding.

Zoning Method

The zoning method is an extension of the inversion method. The difference between the two lies in using zones in the zoning method instead of interpolation. If one assumes that the system is divided into several zones Z_k , where each of the zones has the same number of detectors, then the flux perturbation can be written as [14]:

$$\delta\phi(\mathbf{r}_{\text{meas}}, \omega) = \sum_k G(\mathbf{r}_{Z_k} \rightarrow \mathbf{r}_{\text{meas}}, \omega) S(\mathbf{r}_{Z_k}, \omega) \quad (2.35)$$

Note that all of the $G(\mathbf{r}_{Z_k} \rightarrow \mathbf{r}_{\text{meas}}, \omega)$ are square matrices since $\delta\phi(\mathbf{r}_{\text{meas}}, \omega)$ and $S(\mathbf{r}_{Z_k}, \omega)$ have the same size (number of detectors).

If the fuel assemblies represented in the zone Z_k are set not to be close to each other, the response of the thermal flux detector will be unique to each other. Having the fuel assemblies belonging to a given zone Z_k evenly distributed throughout the core is an easy and practical way to achieve such a goal.

Then, by inverting one of the matrices $G(\mathbf{r}_{Z_k} \rightarrow \mathbf{r}_{\text{meas}}, \omega)$ for zone Z_l , one can obtain:

$$G^{-1}(\mathbf{r}_{Z_l} \rightarrow \mathbf{r}_{\text{meas}}, \omega) \times \delta\phi(\mathbf{r}_{\text{meas}}, \omega) = G^{-1}(\mathbf{r}_{Z_l} \rightarrow \mathbf{r}_{\text{meas}}, \omega) \left(\sum_k G(\mathbf{r}_{Z_k} \rightarrow \mathbf{r}_{\text{meas}}, \omega) S(\mathbf{r}_{Z_k}, \omega) \right) + S(\mathbf{r}_{Z_l}, \omega) \quad (2.36)$$

Moving forward, we will assume that the noise source is located at Z_s , which might be at one of the Z_k or at Z_l . We have two possible cases:

1. If the noise source is located at the zone $Z_l = Z_s$, then one can write:

$$G^{-1}(\mathbf{r}_{Z_l} \rightarrow \mathbf{r}_{\text{meas}}, \omega) \times \delta\phi(\mathbf{r}_{\text{meas}}, \omega) = S(\mathbf{r}_{Z_l}, \omega) \quad (2.37)$$

In this case, $S(\mathbf{r}_{Z_l}) = S(\mathbf{r}_{Z_s})$ is the “true” noise source vector. The noise source vector would have a distinct peak from any other zone, indicating that the noise source is in the zone Z_l .

2. If the inversion is done to the matrix corresponding to zone $Z_l \neq Z_s$ (contains no noise source), then Equation 2.36 becomes:

$$G^{-1}(\mathbf{r}_{Z_l} \rightarrow \mathbf{r}_{\text{meas}}, \omega) \times \delta\phi(\mathbf{r}_{\text{meas}}, \omega) = G^{-1}(\mathbf{r}_{Z_l} \rightarrow \mathbf{r}_{\text{meas}}, \omega) G(\mathbf{r}_{Z_k} \rightarrow \mathbf{r}_{\text{meas}}, \omega) S(\mathbf{r}_{Z_k}, \omega) \quad (2.38)$$

This means that the zone Z_l does not contain the noise source vector. The right-hand side of the equation will be relatively flat and no peak will be visible [14].

To simplify the analysis, we can perform the following calculation.

$$G^{-1}(\mathbf{r}_{Z_l} \rightarrow \mathbf{r}_{\text{meas}}, \omega) \times \delta\phi(\mathbf{r}_{\text{meas}}, \omega) = S_{\text{fict}}(\mathbf{r}_{Z_l}, \omega) \quad (2.39)$$

where $Z_l \in Z_k$. This calculation is done for every zone, which results in k number of $S_{\text{fict}}(\mathbf{r}_{Z_l}, \omega)$. For each $S_{\text{fict}}(\mathbf{r}_{Z_l}, \omega)$, it should return to one of the either cases. If the zone Z_l If the signal contains a noise source, then one of the vector elements should be significantly higher than the others. On the other hand, if a zone Z_l does not contain a noise source, the elements of $S_{\text{fict}}(\mathbf{r}_{Z_l}, \omega)$ would not be different from each other.

The zoning method generally improves the accuracy of the noise unfolding. Some errors were detected when the noise source was located near the boundary of several detectors. In this location, the detector response will not be unique to each other, making the Green's function inaccurate [14].

Scanning method

The third method is the scanning method. This method compares the perturbations detected by the detector with the calculated response for all possible locations of the noise source within the system. The noise source is accurately identified when the calculated neutron noise matches the measured neutron noise [14]. This method was developed by [35], and extended by [36]. Both investigations successfully determined the location of the unseated fuel assembly in the Swedish Forsmark-1 BWR. Both use Green's function as the means to compare detector readings.

This method starts with the definition of noise flux at a given location \mathbf{r} induced by a noise source located at the location \mathbf{r}_p as follows:

$$\delta\phi(\mathbf{r}_i, \omega) = G(\mathbf{r}_{p,j} \rightarrow \mathbf{r}_i, \omega) S(\mathbf{r}_{p,j}, \omega) \quad (2.40)$$

Using Equation 2.40 to compare with the detector reading will be difficult since the location and strength of the noise are unknown. If one has access to two detectors at locations A and B, the ratio between the neutron noise at these two locations can be used to eliminate the noise source strength:

$$\frac{\delta\phi(\mathbf{r}_A, \omega)}{\delta\phi(\mathbf{r}_B, \omega)} = \frac{G(\mathbf{r}_{p,j} \rightarrow \mathbf{r}_A, \omega)}{G(\mathbf{r}_{p,j} \rightarrow \mathbf{r}_B, \omega)} \quad (2.41)$$

Then, the scanning algorithm consists of minimizing the following,

$$\Delta(\mathbf{r}) = \sum_{A,B} \left| \frac{\delta\phi(\mathbf{r}_A, \omega)}{\delta\phi(\mathbf{r}_B, \omega)} - \frac{G(\mathbf{r}_{p,j} \rightarrow \mathbf{r}_A, \omega)}{G(\mathbf{r}_{p,j} \rightarrow \mathbf{r}_B, \omega)} \right| \quad (2.42)$$

Equation 2.42 implies that the summation is done for all detector pairs for all locations \mathbf{r} . If there exist n number of detectors in the reactor, thus the number of detector pairs are as follows:

$$N_{\text{detector pair}} = \frac{n \times (n + 1)}{2} \quad (2.43)$$

The location at which the minimum value of $\Delta(\mathbf{r})$ is found indicates the location of the noise source. The magnitude of the noise source can be calculated as follows:

$$S(\mathbf{r}_p, \omega) = \frac{\delta\phi(r_m, \omega)}{G(\mathbf{r}_p \rightarrow r_m, \omega)} \quad (2.44)$$

for any detector m .

The results from [36] show that the scanning algorithm was able to locate any noise source correctly, provided there is no background. The drawback of this method is that it requires more computational power to compare every possible location of the noise source with every combination of detectors used for the evaluation.

2.2 Application to Reactor Diagnostics

The theory of neutron noise has been applied in various nuclear reactors by utilizing the noise characteristics of these reactors. The reference [19] explained several reasons for using noise analysis in nuclear reactors. This includes the capability to perform specific measurements, design, or model verification, as well as simplicity, low cost, and no interference with operating procedures. Noise can also be used as a substitute for another test or inspection. The use of neutron noise analysis varies depending on the specific interest it is intended for [37]. However, neutron noise theory is widely used for sensor surveillance [38]–[40], core monitoring [41]–[43], and core diagnostics [33], [44]. Table 2.1 provides examples of noise analysis applications for various reactor types.

Table 2.1: Some examples of noise application for power reactors

Reactor Name	Type	Application	References
Novovoronezh-1	PWR	Excessive looseness in the thermal shield	[19]
Fukushima Daiichi-2	BWR	Flow impingement caused excessive tube vibration	[45], [46]
Dresden	BWR	Monitor stability during startup	[47]
Palisades	PWR	Detection of excessive and damaging flow-induced core barrel motion	[3]
High Flux Isotope Reactor (HFIR)	Research	Problems with abnormally loose control rods	[45], [46]
Experimental Breeder Reactor-1 (EBR-1)	FBR	Oscillatory fuel motion	[19]
Dounreay Fast Reactor	FBR	Problems with abnormally loose control rods	[48]
Fort St. Vrain	Gas-cooled	Problems with motion of the core structure	[19]
Browns Ferry-2	BWR	Flow impingement caused excessive tube vibration	[45], [46]
Vermont Yankee	BWR	Flow impingement caused excessive tube vibration	[45], [46]

In the context of core monitoring and surveillance, one example is core barrel motion (CBM) monitoring [33]. This paper develops a methodology for investigating, diagnosing, and surveilling CBM. The surveillance was conducted at the core of Ringhals 2-4 in Sweden by inspecting the amplitude of the peaks in the normalized auto power spectral densities (APSDs) of the ex-core neutron detectors.

In this instance, the CBM was employed because visible vibrations were detected in the radial supports of the core barrel in the Ringhals reactors. In [49], the investigation focuses on the pendulum motion of the core barrel, or it is also known as the beam mode. During the Ringhals operation, monitoring of the beam mode indicated that the amplitude of the APSD increased throughout the fuel cycle. However, the APSD

decreased after the refueling [50].

In the context of reactor core diagnostics, noise analysis is useful for analyzing situations that require changes in state variables, as these changes affect the reactor's status. This was demonstrated in [22] by measuring the moderator temperature coefficient (MTC). Traditionally, at-power MTC measurement techniques require the reactor to be perturbed to induce the change of the moderator temperature. The implementation of the direct perturbation method is the MTC measurement at the Righals-4 reactor using the boron dilution method. The result of this method shows that the uncertainty of using boron dilution method was much more significant than expected due to the necessary reactivity corrections. This prompted the use of non-intrusive methods such as noise analysis for reactor diagnostics.

Some noise experiments were done in two research reactors (AKR-2 and CROCUS) using two different types of neutron noise. The first type of perturbation was generated by a rotating neutron absorber with a varying absorption cross-section with respect to the rotation angle and the second one by fuel rods that oscillate in a controlled manner inside the reactor core [51]–[53]. The experiments consisted of two different parts representing different sources of periodic reactivity perturbation that created neutron flux oscillations. The experiments produced two different quantities of interest: the spectral power density (SPD) and the phase shift angle between detector pairs [23].

AKR-2 reactor is a thermal, homogeneous, polyethylene-moderated zero-power reactor located at TU Dresden. For the first type of experiment in AKR-2, a piece of Cadmium is rotated in the reactor core. Cadmium was chosen due to the variable absorption reaction rate with respect to the rotation angle [54]. For the second type of experiment in AKR-2, the mechanical vibration consists of a neutron absorber that moves linearly back and forth in an experimental channel located outside of the reactor core [51]. The CROCUS reactor is an experimental reactor dedicated to research and teaching in radiation and reactor physics, located at the École Polytechnique Fédérale de Lausanne (EPFL). For noise analysis, the CROCUS reactor used the COLIBRI experimental setup consisting of a fuel rod oscillator and neutron detection instrumentation [51]–[53], [55].

In terms of modeling validation, the CORTEX (COre monitoring Techniques: EXperimental validation and Demonstration) project used two approaches to implement noise analysis based on a given noise source [13]. The first approach uses the formulation of the linearized neutron noise equation in the frequency domain. From the equation, the neutron noise can be determined as a complex quantity. The second approach calculates the evolution of the spatial distribution of the flux as a function of time by solving the time-dependent neutron transport equation [11], [56].

The CORTEX project concluded in 2021; its final phase involves implementing commercial nuclear power plants (NPPs). This is done by demonstrating the approaches to four different commercial reactors. Four reactors are used for the demonstration exercises: a German four-loop pre-Konvoi PWR, a Swiss three-loop pre-Konvoi PWR, a Czech VVER-1000 reactor, and a Hungarian VVER-440 reactor [13], [57]. For the German pre-Konvoi and Konvoi-type PWR, noise measurement and analysis have been topics of interest for several years. Numerous noise observations have been conducted on both reactors during the commissioning and operational phases. It has been observed that during its 30-year operation, fluctuations in neutron noise signals have occurred. These were mainly low-frequency neutron noise, which could cause problems for future reactor operations. Some knowledge of neutron noise and the reactor's operation is necessary to solve the problem [57], [58].

2.3 Computational Methods and Tools of Neutron Noise Analysis

2.3.1 Solving Neutron Noise Problems using Deterministic Methods

Building on the success of neutron noise experiments, computational methods and tools are being developed to support neutron noise’s validation and verification efforts. Deterministic transport methods have been developed to solve the neutron noise equation. It should be noted that knowledge of the forward neutron flux distribution and k-criticality is necessary to perform neutron noise simulations, as these parameters become the input to the neutron noise simulation [26]. The tools developed varied in terms of spatial discretization, energy discretization, angular discretization, and the domain of interest to solve the neutron noise equation.

Diffusion theory is the most widely used approximation in existing tools. Although diffusion theory employs the most approximations compared to other methods for solving the neutron transport equation, it is still deemed compatible with the analysis [59], [60]. Some of the first developments of neutron noise simulators based on neutron diffusion theory are [61] and [26]. The development of the noise simulator began with the need for a dynamic calculation to determine the dynamic reactor transfer function. In the past, calculations of dynamic reactor transfer functions have been performed. However, these calculations are only for a few homogeneous regions. In [61], a 2-group, 2-dimensional Neutron noise simulator based on the nodal method is proposed. The simulator calculates the frequency-dependent detector (adjoint function). Since the simulator employs nodal methods, an iteration procedure is necessary to achieve convergence. In [26], the noise simulator is developed to solve neutron noise problems using both forward and adjoint approaches. In contrast to [61], the noise simulator in [26] uses a finite difference scheme for the spatial discretization. By using a finite difference scheme, the need for an iteration procedure is eliminated. In both simulators, the noise simulator is coupled using a static simulator. Some cases are simulated to verify the capability of the noise simulators. Namely, noise simulators use the vibration and absorber strength case for verification. Subsequently, efforts have been made to enhance the accuracy of the noise simulator. One of the efforts is to use the analytical nodal method [62] to solve the Neutron noise equation. This represents an improvement over using the finite difference scheme for spatial discretization [63]. In [63], the analytical nodal method is used for both forward flux and neutron noise calculations. Other tools, such as CORE SIM [64], [65] and CORE SIM+ [9], [66], [67], are designed to address the neutron noise equation. These specialized codes employ the 3-dimensional, 2-group neutron diffusion equation as the foundational framework for solving the Neutron noise equation in the frequency domain. Notably, these codes exhibit the ability to simulate both critical and subcritical systems, expanding their utility and versatility. Their prowess in handling such systems empowers them to calculate the static flux within the software and then leverage this static flux information to derive dynamic solutions. Moreover, these codes have the capability to solve Green’s functions numerically, further enhancing their computational efficiency and versatility.

As the system of interest becomes more complicated and heterogeneous, one could argue that the approaches mentioned in the previous paragraph are insufficient to solve these problems. Seeing this problem, deterministic codes such as APOLLO3 and SIMULATE-3K developed a noise solver in their system of codes [32], [68]. However, some other developers argue that diffusion theory is insufficient to solve the neutron noise equation. Some disadvantages of using diffusion theory to solve the Neutron noise equation include the incapability of diffusion theory to describe the anisotropy of neutron density in the system, and the use of a time-dependent diffusion equation is deemed inadequate to solve neutron noise equation, since the parabolic nature of diffusion equation results in the particles having an infinite velocity [29], [69]. Therefore, more accurate methods are developed to solve the Neutron noise equation deterministically. One example is to use

the P1 approximations to verify the assumptions and approximations used in diffusion theory-based noise simulators [70], [71]. The use of P1 approximations for noise simulators stems from the fact that both static and dynamic perturbations in noise systems are non-isotropic sources in the subcritical system. Therefore, the solutions of the forward angular flux and the angular noise could be expanded using P1 expansion to consider this behavior. In [70], it is understood that the P1 approximations of a one group noise equation would lead to some difference in noise scenarios. For the case where the perturbation affects only the absorption cross-section (localized absorber and absorption of variable strength cases), the difference between using diffusion and P1 approximation is negligible. However, when perturbations affect the scattering cross-section, the difference between using the diffusion and P1 approximations is significant. The noise source would become a noise field. This is understandable, as the P1 approximation affects the assumptions underlying the definition of the scattering term in the neutron transport equation and the neutron noise equation. In [71] the difference between the P1 approximation and diffusion theory would not be negligible in a heterogeneous system, especially in the near-interface regions where the static flux between the two approximations differs.

Other deterministic methods that are used to solve the neutron noise equation are the simplified P3 method [72], [73], discrete ordinate method [69], [74], and random ray method [75]. For the simplified P3 method, [73] investigate the differences in implementation and results compared to the diffusion approximations. Compared to the general PN Equation, the Simplified PN replaces the second derivatives of angular flux moments in the one-dimensional planar geometry PN equation into general three-dimensional Laplacian operators [72]. The simplified P3 method is implemented in the industry-standard SP3 solver, CORCA-PIN, which is modified into a prototype code, CORCA-NOISE. Compared to the diffusion approximations, the simplified P3 approximations exhibit a considerable difference when applied to heterogeneous reactors, such as the MOX core. For the discrete ordinate method, a solver called NOISE-SN was developed [74]. NOISE-SN simulates Neutron noise problems in the frequency domain. When applying the discrete ordinate method, it is essential to note that the discretization of the angular variable cannot account for all directions of neutron travel. Therefore, it will create the so-called ray effect. The ray effect refers to the anomalous oscillations of the scalar and angular fluxes that occur in certain numerical calculations [76]. The discrete ordinate method captures the spatial distribution of Neutron noise significantly better compared to diffusion approximations. This is crucial for accurately predicting the location of the noise source for diagnostic purposes [77].

Several tools investigate the application of time-domain calculations to neutron noise equations. One of the tools that employs a time-domain analysis approach is FEMFFUSION [78]–[81]. FEMFFUSION is a 3-dimensional, 2-group neutron diffusion simulator that uses a finite element method to solve the neutron diffusion equation [82], [83]. FEMFFUSION solves the neutron noise equation in the time domain and utilizes the frequency domain in the latest version of the code. The calculations in the time domain and frequency domain are then compared by applying a numerical Fast Fourier Transform (FFT) algorithm to the time-dependent results. Another tool that has been utilized for neutron noise simulation in the time domain is DYN3D [84], [85]. DYN3D is a system code that solves the two-group diffusion equation in the time domain using a nodal expansion method with transverse integration for spatial dependence and considering six groups of delayed neutron precursors [85].

It should be noted that in deterministic code, the perturbed cross-sections are not calculated directly from the neutron cross-section libraries [12]. Instead, these cross-sections are already a function of space, time, energy, and direction based on the mesh in which the calculation is performed. Therefore, it is essential to consider that the neutron cross-sections must be defined in advance in deterministic methods.

2.3.2 Solving Neutron Noise Problems using Monte Carlo Methods

For neutron transport calculation, the use of Monte Carlo arises since we can treat the macroscopic cross-sections of neutrons as the probability of interactions per unit distance traveled by neutrons. The Monte Carlo method has proven effective for some cases of neutron transport, especially those related to complex geometries and variations in neutron cross-sections with energy. Monte Carlo eliminates the need for subsidiary calculations such as resonance flux and cross-section group constants [29], [59]. In Monte Carlo, sets of neutrons are generated and simulated. For each individual neutron, the path is traced as it traveled through some materials, including the types of interactions that happened to the neutrons. The generation of neutrons, actual locations, types of interactions, and the results are all determined from a range of possibilities that are set by random numbers generated in Monte Carlo [86], [87].

With the vast capability of Monte Carlo to estimate the solution of the neutron transport equation, one would determine and test the capability of Monte Carlo to estimate the solution of the Neutron noise equation. Compared to deterministic codes, Monte Carlo estimates the neutron cross-sections from the cross-section libraries to calculate the static flux. The application of Monte Carlo to estimate the Neutron noise equation still has some challenges. In the previous section, it was determined that the Neutron noise equation in the frequency domain has some similarities with a fixed-source (or subcritical) neutron transport equation. However, some terms are different and refer to different physical phenomena in the Neutron noise equation. Comparing Equation 28 to the neutron transport equation, the first difference is on the $\delta\phi(\mathbf{r}, \omega)$, which is the complex-valued variable. The second difference is in the source term of the Neutron noise equation, which contains complex-valued variables and negative signs. Finally, the difference is on the time-dependent term, which includes a complex value. In the application of Monte Carlo, these three differences mean that the particle weights W will possibly have real and imaginary values that can be either positive or negative. This is different than the conventional Monte Carlo methods, which only treat real and positive particle weights [88].

With these differences, a new algorithm has been developed to solve these problems. [89] propose the use of complex particle weight such that,

$$W(\omega) = (W_R(\omega), W_I(\omega)) \quad (2.45)$$

where W_R is the real part of particle weight, and W_I is the imaginary part of particle weight. The algorithm also includes the $\frac{i\omega}{v}\delta\phi(\mathbf{r}, \omega)$ term to the random walk process and weight cancellation of positive and negative weights. The noise source is determined using the static flux of the critical calculation and the perturbation in the cross-sections. This method has been developed in the modified MCNP code and verified using 2 group model, and BWR benchmark model.

Another algorithm proposed by [90] chose to change the collision kernel formally, by adding a new term that contains real and complex values, $\frac{(\eta-i)}{\eta}\eta\frac{\omega}{v}\delta\phi(\mathbf{r}, \omega)$, where η is a real constant with the same sign as ω . With this definition, the collision operator in the neutron noise equation is different compared to the neutron transport equation. Consequently, there will be two different types of production to be considered. The first one is the regular fission production, which is like standard neutron transport Monte Carlo calculation. The second one is the ω -production associated with the scalar 'copy' operator. Just like the previous algorithm, the noise source is sampled based on the critical calculation of the flux multiplied by the perturbation of the cross-section. The perturbation of cross-sections is case-by-case, which means that different types of phenomena will have different definitions of cross-section perturbation. The second algorithm has been

implemented to the Monte Carlo code Tripoli-4 [91] and verified against an analytical solution using the infinite homogeneous medium model, infinitely long homogeneous cylindrical core, and one-dimensional homogeneous core surrounded by a reflector. More verification is also done to analyze the Neutron noise in a PWR assembly using simple noise sources and vibration-induced noise sources.

Another topic of interest in Monte Carlo application is neutron noise sampling and variance reduction, which is addressed in [92]. In the paper, a novel method to sample the neutron noise source exactly as a perturbation of isotopic composition is introduced. This paper also addresses the variance reduction using weight cancellation during the calculation. The Monte Carlo-based method is also developed to generate the modified Green's function as proposed in [93]. Driven by the fact that the Neutron noise problem is similar to the case of subcritical assembly with external source, Monte Carlo method is used to calculate modified Green's functions associated to the real part of the dynamic macroscopic cross-sections. Once the modified Green's function is determined, neutron noise induced at any location by any perturbation can be determined [93].

2.4 Summary

This chapter provides a general overview of neutron noise analysis and its implementation for nuclear reactor core diagnostics. Noise has varying definitions depending on the context. In general, it is considered a disruptive or unwanted disturbance. In nuclear reactor engineering, it refers to stochastic processes, such as fluctuations in detector output, inherent to the nature of fission and particle transport processes. Fission and neutron transport, both stochastic processes, are essential for understanding reactor state and uncertainties.

Nuclear reactor core diagnostics plays a critical role in ensuring reactor safety and licensing. Reactor perturbations, like oscillating absorbers, affect core behavior, requiring continuous monitoring. Reactor systems are inherently noisy, and localized and instantaneous fluctuations cannot be adequately explained by time-averaged analysis. Complex factors, such as mechanical vibrations and flow dynamics, introduce perturbations that noise analysis can identify. Neutron noise analysis helps detect malfunctions and anomalies, with real-world examples highlighting its importance.

Neutron noise has been a subject of study since the early development of reactors. Experiments with neutron noise revealed its utility for understanding reactor behavior. This laid the groundwork for using neutron noise analysis in power reactors. Current developments involve applying neutron noise analysis to reactor diagnostics, using numerical methods to solve neutron noise problems efficiently. The focus is now on identifying the fluctuations and noises in nuclear reactors. In power reactors, noise can be classified based on its source or the system variables it affects. In advanced reactors like molten salt reactors, additional factors, such as cross-section changes and molten salt velocity, introduce new noise sources that require consideration in noise analysis. Neutron noise proved a versatile technique used in sensor surveillance, core monitoring, and diagnostics. The CORTEX project demonstrated its effectiveness by employing noise analysis in experiments and modeling for anomaly detection in various reactors.

Neutron is a random phenomenon. This randomness of neutron noise may be represented in both the time and frequency domains. For power reactors, the analysis starts with the neutron transport equation. Several papers have included the use of S_N , P_N , and diffusion theory for noise analysis. Diffusion theory is preferable due to its simplicity. Using neutron diffusion theory, One must apply several approximations to derive the neutron noise equation in the frequency domain. The neutron noise equation would include components such as perturbed flux and reactor transfer functions. The structure of the neutron noise equation is similar to the

fixed source problem of the neutron transport equation. This could be understood that the noise in a reactor system is treated as a source, a noise source. Understanding the different types of noise sources is the key to solving the neutron noise equation.

Neutron noise analysis found extensive application in light water reactors, primarily for assessing perturbations caused by absorbers of variable strength and localized vibrations. In the former case, noise stems from absorption cross-section perturbations. In the latter, vibrations alter macroscopic cross-sections, which can be solved in both the time domain and frequency domain. These vibrations can be categorized as periodic or stochastic. While initial studies focused on simple homogeneous reactor systems, their utility for diagnosing current reactor conditions is clear. Measured data from light-water reactors can validate these models. Notably, Green's function methods facilitate solving neutron noise equations in both scenarios, aiding reactor diagnostics. Currently, specialized software such as CORE SIM and CORE SIM+ have been developed for neutron noise analysis, enabling both critical and subcritical system simulations. Finite element method-based FEMFFUSION enhances computational efficiency in time and frequency domains, allowing accurate prediction of noise sources. Monte Carlo methods, known for their versatility, have also been adapted to address the neutron noise equation's unique challenges, using complex particle weights or altered collision kernels to handle real and imaginary values accurately. These methods enable precise noise analysis in various nuclear reactor scenarios.

Chapter 3

Application Neutron Noise Methods in 2D and 3D HTTR

3.1 Simulation of Neutron Noise in 2D and 3D HTTR

3.2 Application of Neutron Noise Unfolding methods for HTTR

Chapter 4

Novel Neutron Noise Unfolding methods and applications

Chapter 5

Conclusions

We conclude that graduate students like coffee.

References

- [1] K. Saito, “On the Theory of Power Reactor Noise-I,” *Annals of Nuclear Science and Engineering*, vol. 1, pp. 31–48, 1974.
- [2] D. N. Fry, “Experience in Reactor Malfunction Diagnosis Using On-Line Noise Analysis,” *Nuclear Technology*, vol. 10, no. 3, pp. 273–282, Mar. 1971, ISSN: 0029-5450. DOI: [10.13182/NT71-A30959](https://doi.org/10.13182/NT71-A30959). (visited on 09/04/2023).
- [3] D. N. Fry, R. C. Kryter, and J. C. Robinson, “Analysis of neutron-density oscillations resulting from core barrel motion in a PWR nuclear power plant,” *Annals of Nuclear Energy*, Proceedings of the European-American Committee on Reactor Physics Specialist Meeting on Reactor Noise: From Critical Assemblies to Power Reactors, vol. 2, no. 2, pp. 341–351, Jun. 1975, ISSN: 0306-4549. DOI: [10.1016/0306-4549\(75\)90037-7](https://doi.org/10.1016/0306-4549(75)90037-7). (visited on 09/05/2023).
- [4] D. Wach and G. Kosály, “Investigation of the Joint Effect of Local and Global Driving Sources in In-Core Neutron Noise Measurements,” *Atomkernenergie*, vol. 23, no. 4, pp. 244–250, 1974.
- [5] K. Saito, “On the Theory of Power Reactor Noise-II,” *Annals of Nuclear Science and Engineering*, vol. 1, pp. 107–128, Feb. 1974, ISSN: 03022927. DOI: [10.1016/0302-2927\(74\)90056-7](https://doi.org/10.1016/0302-2927(74)90056-7). (visited on 01/14/2023).
- [6] K. Saito, “On the Theory of Power Reactor Noise-III,” *Annals of Nuclear Science and Engineering*, vol. 1, pp. 209–221, 1974.
- [7] I. Pázsit and C. Demazière, “Noise Techniques in Nuclear Systems,” in *Handbook of Nuclear Engineering*, Springer, Boston, MA, 2010, pp. 1629–1737, ISBN: 978-0-387-98130-7.
- [8] J. Leppänen, M. Pusa, T. Viitanen, V. Valtavirta, and T. Kaltiaisenaho, “The Serpent Monte Carlo code: Status, development and applications in 2013,” *Annals of Nuclear Energy*, vol. 82, pp. 142–150, Aug. 2015, ISSN: 03064549. DOI: [10.1016/j.anucene.2014.08.024](https://doi.org/10.1016/j.anucene.2014.08.024). (visited on 09/26/2022).
- [9] A. Mylonakis, P. Vinai, and C. Demazière, “CORE SIM+: A flexible diffusion-based solver for neutron noise simulations,” *Annals of Nuclear Energy*, vol. 155, p. 108 149, Jun. 2021, ISSN: 03064549. DOI: [10.1016/j.anucene.2021.108149](https://doi.org/10.1016/j.anucene.2021.108149). (visited on 01/14/2023).
- [10] A. G. Mylonakis, C. Demazière, P. Vinai, *et al.*, “CORE SIM+ SIMULATIONS OF COLIBRI FUEL RODS OSCILLATION EXPERIMENTS AND COMPARISON WITH MEASUREMENTS,” *EPJ Web of Conferences*, vol. 247, M. Margulis and P. Blaise, Eds., p. 21 006, 2021. DOI: [10.1051/epjconf/202124721006](https://doi.org/10.1051/epjconf/202124721006). (visited on 12/26/2023).
- [11] M. Hursin, A. Zoia, A. Rouchon, *et al.*, “Modeling noise experiments performed at AKR-2 and CROCUS zero-power reactors,” *Annals of Nuclear Energy*, vol. 194, p. 110 066, Dec. 2023, ISSN: 03064549. DOI: [10.1016/j.anucene.2023.110066](https://doi.org/10.1016/j.anucene.2023.110066). (visited on 09/09/2023).

- [12] H. Ardiansyah, V. Seker, T. Downar, S. Skutnik, and W. Wieselquist, “Evaluation of PBMR-400 Core Design Steady State Condition with Serpent and AGREE,” *Journal of Physics: Conference Series*, vol. 2048, no. 1, p. 012024, Oct. 2021, ISSN: 1742-6588, 1742-6596. DOI: [10.1088/1742-6596/2048/1/012024](https://doi.org/10.1088/1742-6596/2048/1/012024). (visited on 10/31/2023).
- [13] C. Demaziere, *The CORTEX project: Improving nuclear fleet operational availability*, <https://www.ans.org/news/article-210/the-cortex-project-improving-nuclear-fleet-operational-availability/>, 2020. (visited on 09/08/2023).
- [14] C. Demazière and G. Andhill, “Identification and localization of absorbers of variable strength in nuclear reactors,” *Annals of Nuclear Energy*, vol. 32, no. 8, pp. 812–842, May 2005, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2004.12.011](https://doi.org/10.1016/j.anucene.2004.12.011). (visited on 06/06/2024).
- [15] S. A. Hosseini and N. Vosoughi, “Noise source reconstruction using ANN and hybrid methods in VVER-1000 reactor core,” *Progress in Nuclear Energy*, vol. 71, pp. 232–247, Mar. 2014, ISSN: 01491970. DOI: [10.1016/j.pnucene.2013.12.007](https://doi.org/10.1016/j.pnucene.2013.12.007). (visited on 06/08/2024).
- [16] I. Pázsit and L. Pál, *Neutron Fluctuations: A Treatise on the Physics on Branching Processes*, 1st ed. Amsterdam ; Boston: Elsevier, 2008, ISBN: 978-0-08-045064-3.
- [17] R. Uhrig, *Random Noise Techniques in Nuclear Reactor Systems*. 1970.
- [18] N. Pacilio, A. Colombino, R. Mosiello, F. Norelli, and V. M. Jorio, “The Analysis of Reactor Noise: Measuring Statistical Fluctuations in Nuclear Systems,” in *Advances in Nuclear Science and Technology: Volume 11*, E. J. Henley, J. Lewins, and M. Becker, Eds., Boston, MA: Springer US, 1979, pp. 67–134, ISBN: 978-1-4613-2862-9. DOI: [10.1007/978-1-4613-2862-9_2](https://doi.org/10.1007/978-1-4613-2862-9_2). (visited on 03/13/2023).
- [19] J. A. Thie, *Power Reactor Noise*. ANS, 1981, ISBN: 978-0-89448-025-6.
- [20] K. O. Ott and R. J. Neuhold, *Introductory Nuclear Reactor Dynamics*. La Grange Park, Ill. USA: American Nuclear Society, 1985, ISBN: 978-0-89448-029-4.
- [21] D. Ferrier and J. A. Thie, *Reactor Noise*. 1963.
- [22] C. Demaziere, “Development of a non-intrusive method for the determination of the moderator temperature coefficient of reactivity (MTC),” Ph.D. dissertation, 2002.
- [23] K. Ambrozic, V. Lamirand, A. Rais, *et al.*, “Noise Analysis Techniques Of In-core Modulation Experiments For The European Project CORTEX,” 2020.
- [24] P. D. Welch, “A Direct Digital Method of Power Spectrum Estimation,” *IBM Journal of Research and Development*, vol. 5, no. 2, pp. 141–156, Apr. 1961, ISSN: 0018-8646. DOI: [10.1147/rd.52.0141](https://doi.org/10.1147/rd.52.0141). (visited on 03/28/2025).
- [25] M. Bahrami and N. Vosoughi, “A new approach for calculation of the neutron noise of power reactor based on Telegrapher’s theory: Theoretical and comparison study between Telegrapher’s and diffusion noise,” *Nuclear Engineering and Technology*, vol. 52, no. 4, pp. 681–688, Apr. 2020, ISSN: 17385733. DOI: [10.1016/j.net.2019.09.017](https://doi.org/10.1016/j.net.2019.09.017). (visited on 01/14/2023).
- [26] C. Demazière, “Development of a 2-D 2-group neutron noise simulator,” *Annals of Nuclear Energy*, vol. 31, no. 6, pp. 647–680, Apr. 2004, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2003.08.007](https://doi.org/10.1016/j.anucene.2003.08.007). (visited on 10/24/2023).
- [27] I. Pázsit and V. Dykin, “The dynamic adjoint as a Green’s function,” *Annals of Nuclear Energy*, Tribute to a GIANT, vol. 86, pp. 29–34, Dec. 2015, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2015.01.029](https://doi.org/10.1016/j.anucene.2015.01.029). (visited on 09/26/2022).

- [28] C. Demazière, V. Dykin, and K. Jareteg, “Development of a point-kinetic verification scheme for nuclear reactor applications,” *Journal of Computational Physics*, vol. 339, pp. 396–411, Jun. 2017, ISSN: 0021-9991. DOI: [10.1016/j.jcp.2017.03.020](https://doi.org/10.1016/j.jcp.2017.03.020). (visited on 01/03/2024).
- [29] G. I. Bell and S. Glasstone, *Nuclear Reactor Theory*. Van Nostrand Reinhold Company, 1970.
- [30] A. Jonsson and I. Pázsit, “Two-group theory of neutron noise in Molten Salt Reactors,” *Annals of Nuclear Energy*, vol. 38, no. 6, pp. 1238–1251, Jun. 2011, ISSN: 03064549. DOI: [10.1016/j.anucene.2011.02.013](https://doi.org/10.1016/j.anucene.2011.02.013). (visited on 09/26/2022).
- [31] I. Pázsit and O. Glöckler, “On the Neutron Noise Diagnostics of Pressurized Water Reactor Control Rod Vibrations. I. Periodic Vibrations,” *Nuclear Science and Engineering*, vol. 85, no. 2, pp. 167–177, Oct. 1983, ISSN: 0029-5639, 1943-748X. DOI: [10.13182/NSE83-A27424](https://doi.org/10.13182/NSE83-A27424). (visited on 12/24/2024).
- [32] D. Chionis, A. Dokhane, L. Belblidia, *et al.*, “SIMULATE-3K Analyses of Neutron Noise Response to Fuel Assembly Vibrations and Thermal-Hydraulics Parameters Fluctuations,” in *International Conference on Mathematics & Computational Methods Applied to Nuclear Science & Engineering*, Jeju, Korea, 2017-04-16/2017-04-20.
- [33] I. Pázsit, C. Montalvo, H. Nylén, T. Andersson, A. Hernández-Solís, and P. B. Cartemo, “Developments in Core-Barrel Motion Monitoring and Applications to the Ringhals PWR Units,” *Nuclear Science and Engineering*, vol. 182, no. 2, pp. 213–227, Feb. 2016, ISSN: 0029-5639, 1943-748X. DOI: [10.13182/NSE15-14](https://doi.org/10.13182/NSE15-14). (visited on 09/08/2023).
- [34] I. Pázsit, “Investigation of the Space-Dependent Noise Induced by A Vibrating Absorber,” Jan. 1977.
- [35] J. K.-H. Karlsson and I. Pázsit, “Localization of a Channel Instability in the Forsmark-1 Boiling Water Reactor,” *Annals of Nuclear Energy*, vol. 26, pp. 1183–1204, 1999. DOI: [10.1016/S0306-4549\(99\)00014-6](https://doi.org/10.1016/S0306-4549(99)00014-6).
- [36] C. Demazière, “Development of a noise-based method for the determination of the moderator temperature coefficient of reactivity (MTC) in pressurized water reactors (PWRs),” Ph.D. dissertation, Chalmers Univ. of Technology, Göteborg, 2002.
- [37] L. A. Torres, D. Chionis, C. Montalvo, A. Dokhane, and A. García-Berrocal, “Neutron noise analysis of simulated mechanical and thermal-hydraulic perturbations in a PWR core,” *Annals of Nuclear Energy*, vol. 126, pp. 242–252, Apr. 2019, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2018.11.032](https://doi.org/10.1016/j.anucene.2018.11.032). (visited on 08/26/2023).
- [38] H. M. Hashemian, “Measurement of Dynamic Temperatures and Pressures in Nuclear Power Plants,” Ph.D. dissertation, University of Western Ontario, London, Ontario, 2011.
- [39] H. M. Hashemian and J. Jiang, “A practical review of methods for measuring the dynamic characteristics of industrial pressure transmitters,” *ISA Transactions*, vol. 49, no. 1, pp. 2–9, Jan. 2010, ISSN: 0019-0578. DOI: [10.1016/j.isatra.2009.09.004](https://doi.org/10.1016/j.isatra.2009.09.004). (visited on 09/08/2023).
- [40] C. Montalvo, A. García-Berrocal, J. A. Bermejo, and C. Queral, “Advanced surveillance of Resistance Temperature Detectors in Nuclear Power Plants,” *Annals of Nuclear Energy*, vol. 65, pp. 35–40, Mar. 2014, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2013.10.034](https://doi.org/10.1016/j.anucene.2013.10.034). (visited on 09/08/2023).
- [41] T. Czibók, G. Kiss, S. Kiss, K. Krinizs, and J. Végh, “Regular neutron noise diagnostics measurements at the Hungarian Paks NPP,” *Progress in Nuclear Energy*, vol. 43, no. 1, pp. 67–74, Jan. 2003, ISSN: 0149-1970. DOI: [10.1016/S0149-1970\(03\)00007-6](https://doi.org/10.1016/S0149-1970(03)00007-6). (visited on 09/08/2023).

- [42] H. M. Hashemian, “On-line monitoring applications in nuclear power plants,” *Progress in Nuclear Energy*, vol. 53, no. 2, pp. 167–181, Mar. 2011, ISSN: 0149-1970. DOI: [10.1016/j.pnucene.2010.08.003](https://doi.org/10.1016/j.pnucene.2010.08.003). (visited on 09/08/2023).
- [43] J. Ortiz-Villafuerte, R. Castillo-Durán, G. Alonso, and G. Calleros-Michelands, “BWR online monitoring system based on noise analysis,” *Nuclear Engineering and Design*, vol. 236, no. 22, pp. 2394–2404, Nov. 2006, ISSN: 0029-5493. DOI: [10.1016/j.nucengdes.2006.02.009](https://doi.org/10.1016/j.nucengdes.2006.02.009). (visited on 09/08/2023).
- [44] C. Montalvo, I. Pázsit, and H. Nylén, “First Evidence of the Pivotal Motion (“Tilting Mode”) of the Core Barrel in the Ringals-4 PWR,” in *PHYSOR 2016*, Sun Valley, Idaho, 2016-05-01/2016-05-05.
- [45] K. Behringer, L. Kostić, and W. Seifritz, “Observation of in-core instrument tube vibrations in a boiling water reactor by evaluating reactor noise data,” *Progress in Nuclear Energy*, Reactor Noise - Smorn II, vol. 1, no. 2, pp. 183–185, Jan. 1977, ISSN: 0149-1970. DOI: [10.1016/0149-1970\(77\)90076-2](https://doi.org/10.1016/0149-1970(77)90076-2). (visited on 09/06/2023).
- [46] M. V. Mathis, C. M. Smith, D. N. Fry, and M. L. Dailey, “Characterization studies of BWR-4 neutron noise analysis spectra,” *Progress in Nuclear Energy*, Reactor Noise - Smorn II, vol. 1, no. 2, pp. 175–181, Jan. 1977, ISSN: 0149-1970. DOI: [10.1016/0149-1970\(77\)90075-0](https://doi.org/10.1016/0149-1970(77)90075-0). (visited on 09/06/2023).
- [47] J. A. Thie, “Elementary Methods of Reactor Noise Analysis,” *Nuclear Science and Engineering*, vol. 15, no. 2, pp. 109–114, Feb. 1963, ISSN: 0029-5639, 1943-748X. DOI: [10.13182/NSE63-A26408](https://doi.org/10.13182/NSE63-A26408). (visited on 01/14/2023).
- [48] F. J. Barclay and D. Tait, “The development of noise analysis techniques in the surveillance of DFR,” *Progress in Nuclear Energy*, Reactor Noise - Smorn II, vol. 1, no. 2, pp. 691–700, Jan. 1977, ISSN: 0149-1970. DOI: [10.1016/0149-1970\(77\)90119-6](https://doi.org/10.1016/0149-1970(77)90119-6). (visited on 09/07/2023).
- [49] C. M. Martín, I. Pázsit, and H. Nylén, “SURVEILLANCE AND DIAGNOSTICS OF THE BEAM MODE VIBRATIONS OF THE RINGHALS PWRs,” in *Topical Meeting on Advances in Reactor Physics*, Knoxville, 2012.
- [50] I. Pázsit, C. M. Martín, V. Dykin, and H. Nylén, “Final Report on the Research Project Ringhals Diagnostics and Monitoring Stage 14,” Chalmers University of Technology, Tech. Rep. CTH-NT-253/RR-16, 2011.
- [51] V. Lamirand, M. Hursin, A. Rais, *et al.*, “Experimental report of the 1st campaign at AKR-2 and CROCUS,” EPFL, Tech. Rep., Dec. 2018.
- [52] V. Lamirand, M. Hursin, A. Rais, *et al.*, “Experimental report of the 2nd campaign at AKR-2 and CROCUS,” EPFL, Tech. Rep., Mar. 2021.
- [53] V. Lamirand, A. Knospe, K. Ambrozic, F. Vitullo, and C. Lange, “Experimental report of the 3rd campaign at AKR-2 and CROCUS,” EPFL, Tech. Rep., Aug. 2021.
- [54] S. Hübner, A. Knospe, M. Viebach, C. Lange, and A. Hurtado, “EXPERIMENTAL DETERMINATION OF THE ZERO POWER TRANSFER FUNCTION OF THE AKR-2,” *EPJ Web of Conferences*, vol. 247, M. Margulis and P. Blaise, Eds., p. 21009, 2021, ISSN: 2100-014X. DOI: [10.1051/epjconf/202124721009](https://doi.org/10.1051/epjconf/202124721009). (visited on 09/11/2023).
- [55] V. Lamirand, P. Frajtag, D. Godat, *et al.*, “The COLIBRI experimental program in the CROCUS reactor: Characterization of the fuel rods oscillator,” *EPJ Web of Conferences*, vol. 225, A. Lyoussi, M. Giot, M. Carette, *et al.*, Eds., p. 04020, 2020, ISSN: 2100-014X. DOI: [10.1051/epjconf/202022504020](https://doi.org/10.1051/epjconf/202022504020). (visited on 09/09/2023).

- [56] A. Brighenti, S. Santandrea, I. Zmijarevic, and Z. Stankovski, “Development and validation of a time-dependent deterministic model for neutron noise on CROCUS experimental measurements,” *Annals of Nuclear Energy*, vol. 165, p. 108 753, Jan. 2022, ISSN: 03064549. DOI: [10.1016/j.anucene.2021.108753](https://doi.org/10.1016/j.anucene.2021.108753). (visited on 02/07/2024).
- [57] M. Seidl, K. Kosowski, U. Schüler, and L. Belblidia, “Review of the historic neutron noise behavior in German KWU built PWRs,” *Progress in Nuclear Energy*, vol. 85, pp. 668–675, Nov. 2015, ISSN: 01491970. DOI: [10.1016/j.pnucene.2015.08.016](https://doi.org/10.1016/j.pnucene.2015.08.016). (visited on 01/14/2023).
- [58] U. Rohde, M. Seidl, S. Kliem, and Y. Bilodid, “Neutron noise observations in German KWU built PWRs and analyses with the reactor dynamics code DYN3D,” *Annals of Nuclear Energy*, vol. 112, pp. 715–734, Feb. 2018, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2017.10.033](https://doi.org/10.1016/j.anucene.2017.10.033). (visited on 09/15/2023).
- [59] J. J. Duderstadt and L. J. Hamilton, *Nuclear Reactor Analysis*. Jun. 1977.
- [60] C. Demazière and I. Pázsit, “Numerical tools applied to power reactor noise analysis,” *Progress in Nuclear Energy*, vol. 51, no. 1, pp. 67–81, Jan. 2009, ISSN: 0149-1970. DOI: [10.1016/j.pnucene.2008.01.010](https://doi.org/10.1016/j.pnucene.2008.01.010). (visited on 02/15/2023).
- [61] S. Khericha, “Development of two-energy group, two-dimensional, frequency dependent detector adjoint function based on the nodal method,” *Annals of Nuclear Energy*, vol. 28, no. 11, pp. 1049–1068, Jul. 2001, ISSN: 03064549. DOI: [10.1016/S0306-4549\(00\)00115-8](https://doi.org/10.1016/S0306-4549(00)00115-8). (visited on 01/14/2023).
- [62] K. S. Smith, “An analytic nodal method for solving the two-group, multidimensional, static and transient neutron diffusion equations,” Thesis, Massachusetts Institute of Technology, 1979. (visited on 10/24/2023).
- [63] V. Larsson, C. Demazière, I. Pázsit, and H. N. Tran, “Neutron noise calculations using the Analytical Nodal Method and comparisons with analytical solutions,” *Annals of Nuclear Energy*, vol. 38, no. 4, pp. 808–816, Apr. 2011, ISSN: 03064549. DOI: [10.1016/j.anucene.2010.11.017](https://doi.org/10.1016/j.anucene.2010.11.017). (visited on 01/14/2023).
- [64] C. Demazière, “CORE SIM: A multi-purpose neutronic tool for research and education,” *Annals of Nuclear Energy*, vol. 38, no. 12, pp. 2698–2718, Dec. 2011, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2011.06.010](https://doi.org/10.1016/j.anucene.2011.06.010). (visited on 10/26/2023).
- [65] V. Dykin and C. Demazière, “DEMONSTRATION OF THE COUPLED CORE SIM NEUTRONIC AND THERMO-HYDRAULIC TOOL,” Aug. 2014.
- [66] A. Mylonakis, P. Vinai, and C. Demazière, “Neutron noise modelling for nuclear reactor diagnostics,” *HNPS Proceedings*, vol. 26, p. 139, Apr. 2019, ISSN: 2654-0088, 2654-007X. DOI: [10.12681/hnps.1809](https://doi.org/10.12681/hnps.1809). (visited on 01/14/2023).
- [67] A. G. Mylonakis, P. Vinai, and C. Demazière, “Numerical solution of two-energy-group neutron noise diffusion problems with fine spatial meshes,” *Annals of Nuclear Energy*, vol. 140, p. 107 093, Jun. 2020, ISSN: 03064549. DOI: [10.1016/j.anucene.2019.107093](https://doi.org/10.1016/j.anucene.2019.107093). (visited on 01/14/2023).
- [68] A. Rouchon, R. Sanchez, and I. Zmijarevic, “The new 3-D multigroup diffusion neutron noise solver of APOLLO3 and a theoretical discussion of fission-modes noise,” 2017.
- [69] M. Bahrami and N. Vosoughi, “SN transport method for neutronic noise calculation in nuclear reactor systems: Comparative study between transport theory and diffusion theory,” *Annals of Nuclear Energy*, vol. 114, pp. 236–244, Apr. 2018, ISSN: 03064549. DOI: [10.1016/j.anucene.2017.12.041](https://doi.org/10.1016/j.anucene.2017.12.041). (visited on 10/23/2023).

- [70] I. Pázsit, “Neutron noise theory in the P1 approximation,” *Progress in Nuclear Energy*, vol. 40, no. 2, pp. 217–236, Jan. 2002, ISSN: 0149-1970. DOI: [10.1016/S0149-1970\(01\)00027-0](https://doi.org/10.1016/S0149-1970(01)00027-0). (visited on 05/11/2023).
- [71] V. Larsson and C. Demazière, “Comparative study of 2-group and diffusion theories for the calculation of the neutron noise in 1D 2-region systems,” *Annals of Nuclear Energy*, vol. 36, no. 10, pp. 1574–1587, Oct. 2009, ISSN: 03064549. DOI: [10.1016/j.anucene.2009.07.009](https://doi.org/10.1016/j.anucene.2009.07.009). (visited on 01/14/2023).
- [72] P. S. Brantley and E. W. Larsen, “The Simplified P_3 Approximation,” *Nuclear Science and Engineering*, vol. 134, no. 1, pp. 1–21, Jan. 2000, ISSN: 0029-5639, 1943-748X. DOI: [10.13182/NSE134-01](https://doi.org/10.13182/NSE134-01). (visited on 10/26/2023).
- [73] H. Gong, Z. Chen, W. Wu, X. Peng, and Q. Li, “Neutron noise calculation: A comparative study between SP3 theory and diffusion theory,” *Annals of Nuclear Energy*, vol. 156, p. 108184, Jun. 2021, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2021.108184](https://doi.org/10.1016/j.anucene.2021.108184). (visited on 10/26/2023).
- [74] H. Yi, P. Vinai, and C. Demazière, “On the simulation of neutron noise using a discrete ordinates method,” *Annals of Nuclear Energy*, vol. 164, p. 108570, Dec. 2021, ISSN: 03064549. DOI: [10.1016/j.anucene.2021.108570](https://doi.org/10.1016/j.anucene.2021.108570). (visited on 10/23/2023).
- [75] P. Cosgrove, M. Kraus, and V. Raffuzzi, “A memory-efficient neutron noise algorithm for reactor physics,” *Annals of Nuclear Energy*, vol. 201, p. 110450, Jun. 2024, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2024.110450](https://doi.org/10.1016/j.anucene.2024.110450). (visited on 02/24/2024).
- [76] K. D. Lathrop, “Ray Effects in Discrete Ordinates Equations,” *Nuclear Science and Engineering*, vol. 32, no. 3, pp. 357–369, Jun. 1968, ISSN: 0029-5639. DOI: [10.13182/NSE68-4](https://doi.org/10.13182/NSE68-4). (visited on 10/29/2023).
- [77] M. Bahrami and N. Vosoughi, “Precise localization of neutron noise sources based on transport theory and comparison with diffusion theory,” *Annals of Nuclear Energy*, vol. 151, p. 107981, Feb. 2021, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2020.107981](https://doi.org/10.1016/j.anucene.2020.107981). (visited on 05/04/2023).
- [78] A. Vidal-Ferràndiz, A. Carreño, D. Ginestar, C. Demazière, and G. Verdú, “Neutronic Simulation of Fuel Assembly Vibrations in a Nuclear Reactor,” *Nuclear Science and Engineering*, vol. 194, no. 11, pp. 1067–1078, Nov. 2020, ISSN: 0029-5639, 1943-748X. DOI: [10.1080/00295639.2020.1756617](https://doi.org/10.1080/00295639.2020.1756617). (visited on 01/14/2023).
- [79] A. Vidal-Ferràndiz, A. Carreño, D. Ginestar, C. Demazière, and G. Verdú, “A time and frequency domain analysis of the effect of vibrating fuel assemblies on the neutron noise,” *Annals of Nuclear Energy*, vol. 137, p. 107076, Mar. 2020, ISSN: 03064549. DOI: [10.1016/j.anucene.2019.107076](https://doi.org/10.1016/j.anucene.2019.107076). (visited on 01/14/2023).
- [80] A. Vidal-Ferràndiz, D. Ginestar, A. Carreño, *et al.*, “Modelling and simulations of reactor neutron noise induced by mechanical vibrations,” *Annals of Nuclear Energy*, vol. 177, p. 109300, Nov. 2022, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2022.109300](https://doi.org/10.1016/j.anucene.2022.109300). (visited on 10/21/2023).
- [81] A. Vidal-Ferràndiz, A. Carreño, Y. Fontenla, D. Ginestar, and G. Verdú, “FEMFFUSION A finite element code to model nuclear reactors,” Tech. Rep., 2023.
- [82] A. Vidal-Ferràndiz, R. Favez, D. Ginestar, and G. Verdú, “Moving meshes to solve the time-dependent neutron diffusion equation in hexagonal geometry,” *Journal of Computational and Applied Mathematics, Mathematical Modeling and Computational Methods*, vol. 291, pp. 197–208, Jan. 2016, ISSN: 0377-0427. DOI: [10.1016/j.cam.2015.03.040](https://doi.org/10.1016/j.cam.2015.03.040). (visited on 10/29/2023).

- [83] A. Vidal-Ferrandiz, R. Fayez, D. Ginestar, and G. Verdú, “Solution of the Lambda modes problem of a nuclear power reactor using an h–p finite element method,” *Annals of Nuclear Energy*, vol. 72, pp. 338–349, Oct. 2014, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2014.05.026](https://doi.org/10.1016/j.anucene.2014.05.026). (visited on 10/29/2023).
- [84] M. Viebach, N. Bernt, C. Lange, D. Hennig, and A. Hurtado, “On the influence of dynamical fuel assembly deflections on the neutron noise level,” *Progress in Nuclear Energy*, vol. 104, pp. 32–46, Apr. 2018, ISSN: 0149-1970. DOI: [10.1016/j.pnucene.2017.08.010](https://doi.org/10.1016/j.pnucene.2017.08.010). (visited on 03/30/2025).
- [85] M. Viebach, C. Lange, S. Kliem, *et al.*, “Verification of the code DYN3D for calculations of neutron flux fluctuations,” *Annals of Nuclear Energy*, vol. 166, p. 108735, Feb. 2022, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2021.108735](https://doi.org/10.1016/j.anucene.2021.108735). (visited on 03/30/2025).
- [86] E. Lewis and W. Miller, *Computational Methods of Neutron Transport*. United States: John Wiley and Sons, Inc, 1984.
- [87] I. Lux and L. Koblinger, *Monte Carlo Particle Transport Methods: Neutron and Photon Calculations*, 1st ed. CRC Press, 1991, ISBN: 978-1-351-07483-4. DOI: [10.1201/9781351074834](https://doi.org/10.1201/9781351074834). (visited on 08/19/2023).
- [88] T. Yamamoto, “Monte Carlo method with complex-valued weights for frequency domain analyses of neutron noise,” *Annals of Nuclear Energy*, vol. 58, pp. 72–79, Aug. 2013, ISSN: 03064549. DOI: [10.1016/j.anucene.2013.03.002](https://doi.org/10.1016/j.anucene.2013.03.002). (visited on 10/20/2023).
- [89] T. Yamamoto, “Implementation of a frequency-domain neutron noise analysis method in a production-level continuous energy Monte Carlo code: Verification and application in a BWR,” *Annals of Nuclear Energy*, vol. 115, pp. 494–501, May 2018, ISSN: 0306-4549. DOI: [10.1016/j.anucene.2018.02.008](https://doi.org/10.1016/j.anucene.2018.02.008). (visited on 10/21/2023).
- [90] A. Rouchon, A. Zoia, and R. Sanchez, “A new Monte Carlo method for neutron noise calculations in the frequency domain,” *Annals of Nuclear Energy*, vol. 102, pp. 465–475, Apr. 2017, ISSN: 03064549. DOI: [10.1016/j.anucene.2016.11.035](https://doi.org/10.1016/j.anucene.2016.11.035). (visited on 01/14/2023).
- [91] A. Rouchon, W. Jarrah, and A. Zoia, “The new neutron noise solver of the Monte Carlo code Tripoli-4,” 2019.
- [92] H. Belanger, D. Mancusi, A. Rouchon, and A. Zoia, “Variance Reduction and Noise Source Sampling Techniques for Monte Carlo Simulations of Neutron Noise Induced by Mechanical Vibrations,” 2022. DOI: [10.48550/ARXIV.2207.09822](https://doi.org/10.48550/ARXIV.2207.09822). (visited on 05/13/2024).
- [93] C. Demazière, A. Tatidis, and P. Vinai, “Monte Carlo-based Dynamic Calculations of Stationary Perturbations,” in *PHYSOR 2020: Transition to a Scalable Nuclear Future*, Cambridge, United Kingdom, 29-03/2020-04-02.