

EE 352 LAB REPORT

LAB 8: FM in Noise

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8.1 Image Reading

Image Processing Toolbox of MATLAB contains `imread(.)` and `im2double(.)` functions that are used for obtaining a matrix of pixels of a picture with proper size. Frequency modulation and demodulation is implemented to the image file “testpat1.png” in this laboratory experiment.

8.2 Modulation

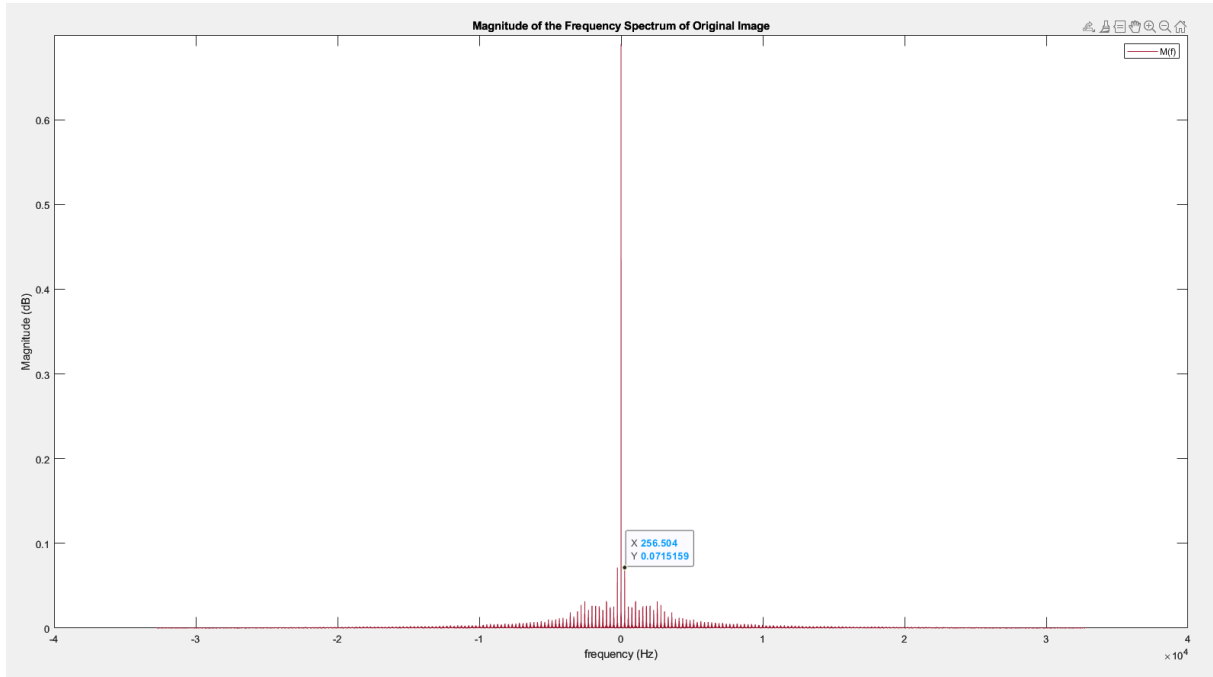


Figure 8.1: Magnitude of Frequency Spectrum of the Original Image

Time vector (t) and sampling frequency are created according to the size parameters of the reshaped original image by using `numel(.)` and `size(.)` functions.

- In order to calculate modulation indices β_1 and β_2 , maximum amplitude and frequency of the original image (A_m and f_m) are needed. Frequency of the original image can be determined by analyzing the second maximum frequency magnitude component. From the figure 8.2 it is observed that original image has 256.504 Hz f_m value. Also A_m is 1. By using the formula,
- $\beta = k_f \cdot A_m / f_m$, β_1 is 0.39 and β_2 is 1.562.
- The results above indicates that first modulation is narrow-band FM since modulation index $\beta < 1$, while second one is wide-band FM.

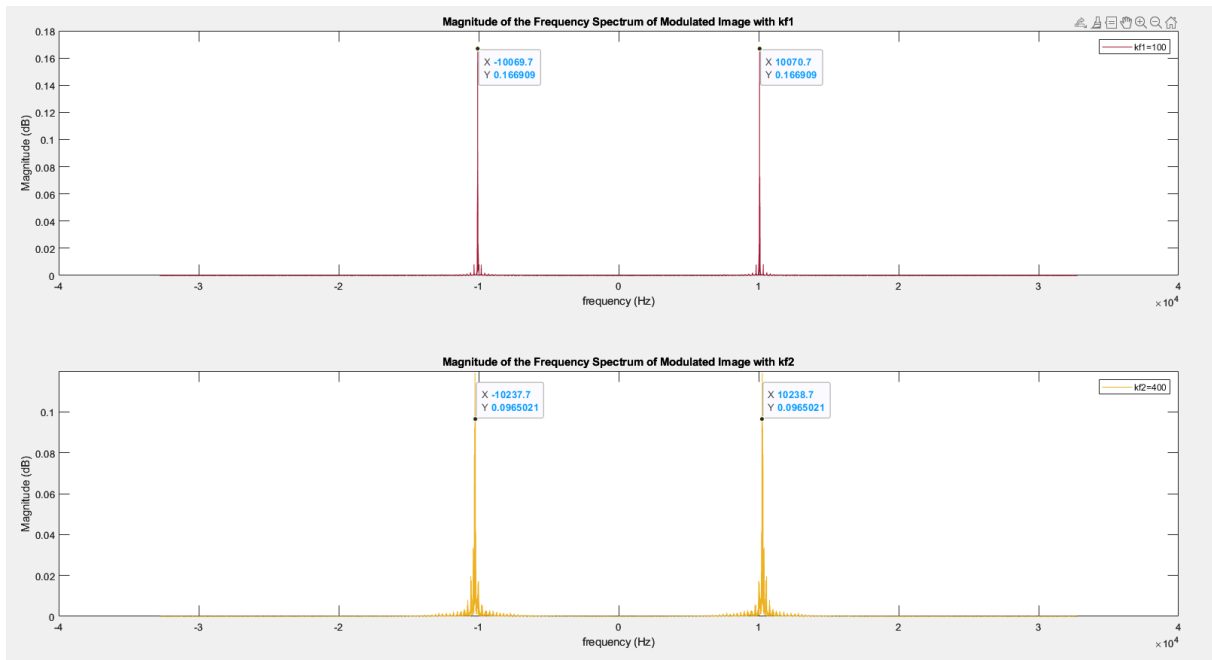


Figure 8.2: Magnitude of Frequency Spectrum of Modulated Images with kf_1 and kf_2 values

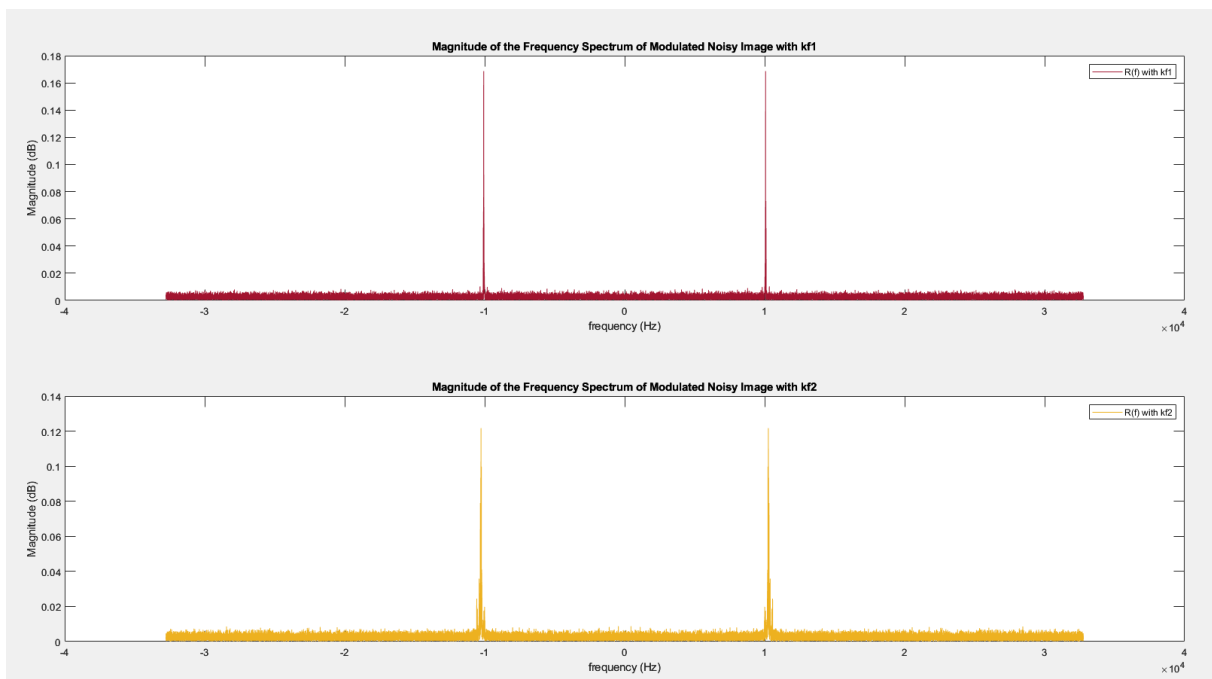


Figure 8.3: Magnitude of Frequency Spectrum of Modulated Noisy Images

White noise is added to modulated images by using `awgn(.)` function. Figure 8.3 is magnitude frequency spectrum of the white noise added modulated image with 0 dB SNR value. A SNR value of 0 dB means that the power of the signal is equal to the power of the noise. In other words, the signal and the noise have the same strength.

8.3 Demodulation

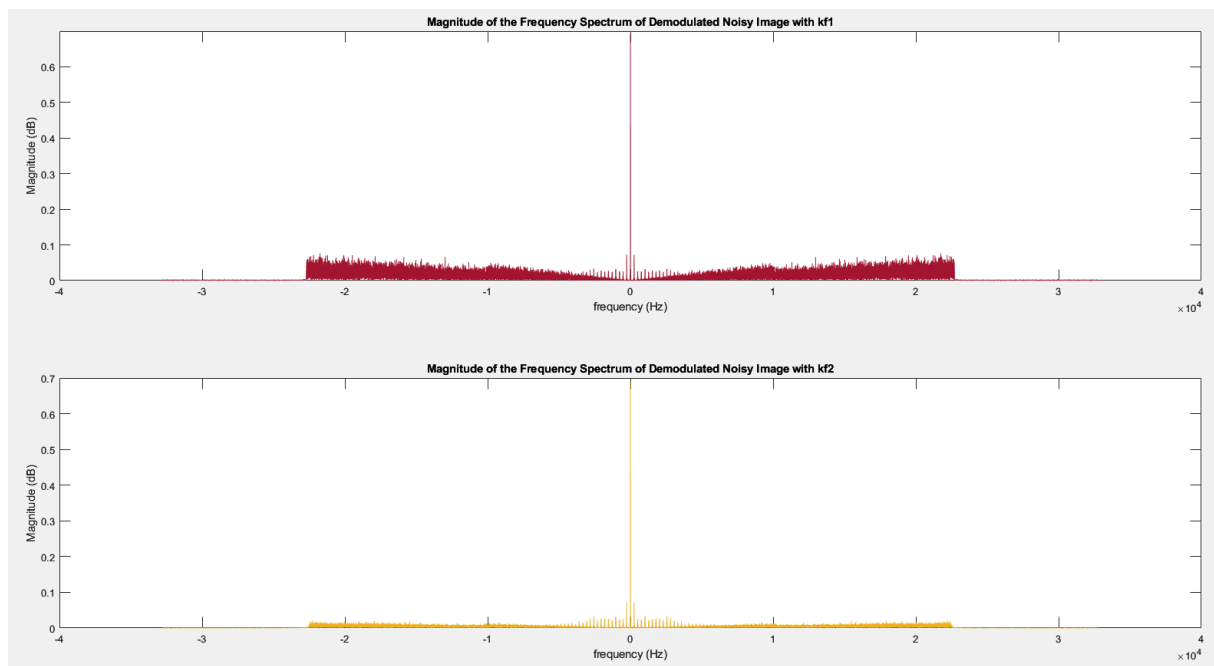


Figure 8.4: Magnitude of Frequency Spectrum of Demodulated Noisy Images

Figure 8.4 indicates that, lower frequency deviation constant (k_f) makes lower power of the FM signal compared to the carrier and noise. With the SNR value 25 dB signal became stronger compared to noise by analyzing two figures (8.3 and 8.4).

Ranking from most bandwidth-efficient to least bandwidth-efficient for noise reducing:

- SSB (Single Sideband) System: Most efficient as it transmits only one sideband along with the carrier, reducing bandwidth by half.
- VSB (Vestigial Sideband) System: Less efficient than SSB but more than FM and PM. It transmits one full sideband and a portion of the other sideband.
- FM (Frequency Modulation) System: Requires a larger bandwidth due to the frequency deviation caused by the modulating signal.
- PM (Phase Modulation) System: Similar to FM, it requires a wider bandwidth due to phase deviation caused by the modulating signal.

PSNR0_1	-36.3358
PSNR0_2	-24.2076
PSNR25_1	-7.9642
PSNR25_2	3.2767
PSNR50_1	10.1476
PSNR50_2	11.1343

Figure 8.5: Power of SNR Values

The required cut-off frequency is the value that makes power of 50 dB SNR value over 10 dB. In order to obtain that range 14.5 kHz is enough for LPF.

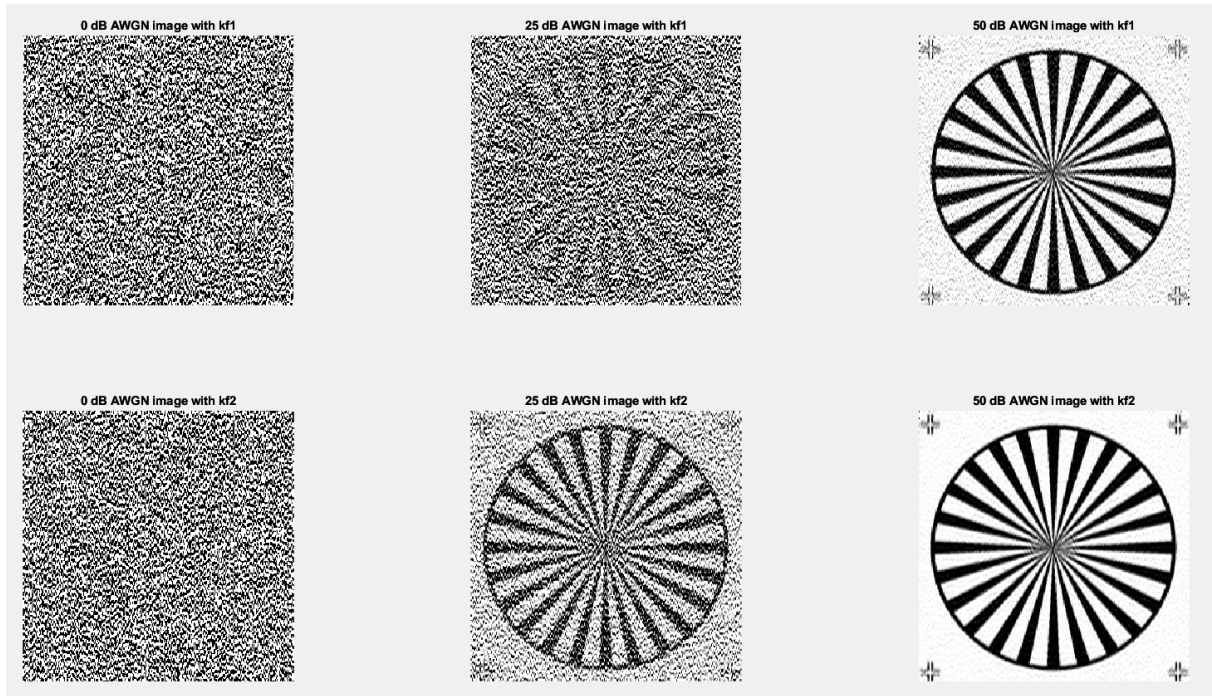


Figure 8.6: Noise Reduced Demodulated Images

Since the power of SNR is very high at 50 dB SNR values (from the figure 8.5), it is understood that higher SNR value is important to observe higher quality.

- By analyzing the images and comparing according to k_f values, when k_f value increases, according to the following formula:

$$s_{FM}(t) = A_c * (\cos(2\pi f_c t) + k_f \int m(\tau) d\tau)$$
, when k_f increases, power of the message signal also increases compared to the noise. That means SNR value increases. So it can be obtained that higher β , indicates higher SNR.

8.4 Mean Square Error (MSE) and PSNR Comparison

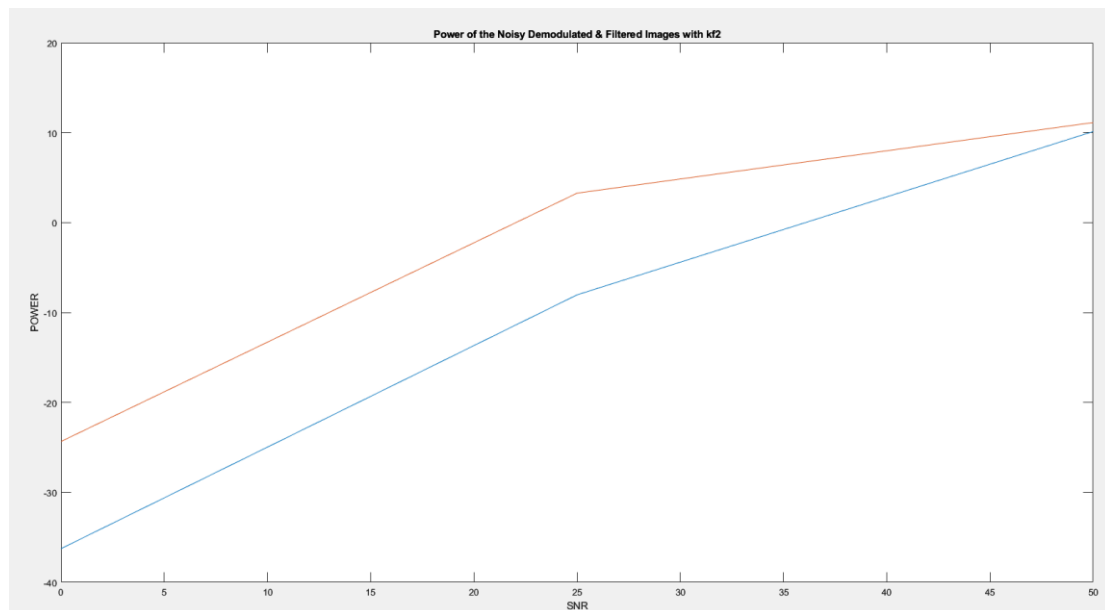


Figure 8.7: Power with different SNR values

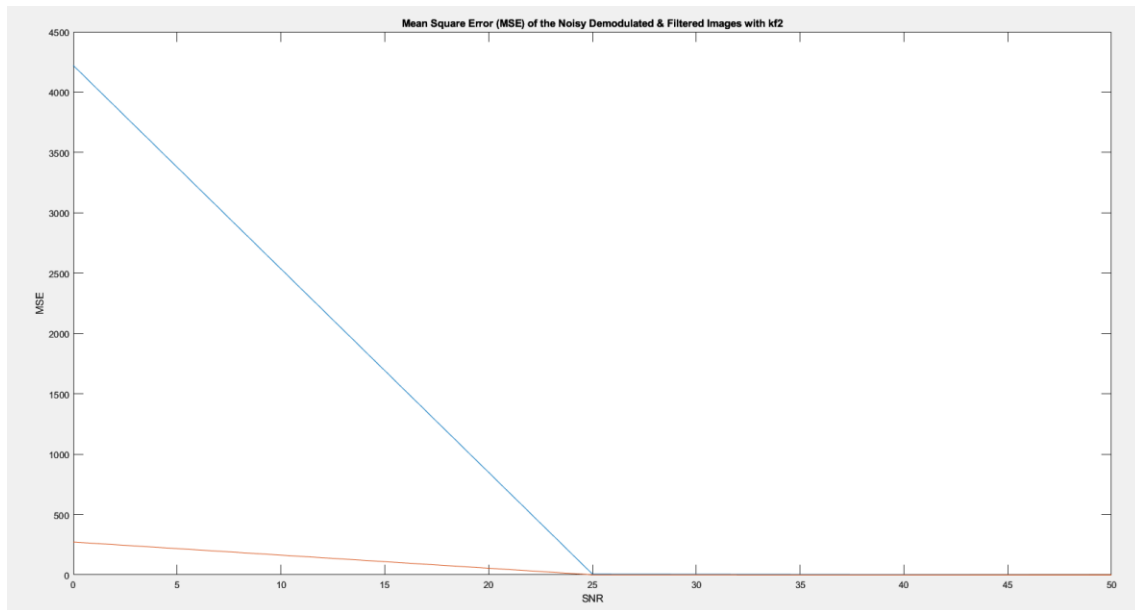


Figure 8.8: MSE with different SNR values

From the figures 8.7 and 8.8 above, it is obtained that mean square error is decreased when power of the signal compared to noise ratio (SNR) is increased. This indicates that better image quality is obtained while power of the signal is much stronger compared to the noise.