

EE204 Scientific Programming for EE C Review with Example Codes

Mehmet Çalı

Question

Background

Minors of a matrix is can be calculated from the determinant of sub-matrices which acquired by removing selected row/s and column/s of the original matrix.

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$$

To calculate minor M_{21} of matrix A, 2^{nd} row and 1^{st} column should be removed

$$A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{11} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \qquad M_{21} = \det(\begin{bmatrix} a_{12} & a_{13} \\ a_{32} & a_{33} \end{bmatrix})$$

One can extend this example for any row i and column j of matrix A to compute M_{ij}

Question

Write a function to calculate specified minor of a given matrix

Note: In the laboratory experiments you are generally asked to implement your code with a function prototype restriction

To be able to see different structures of C, this problem is defined in multiple versions which basically correspond to multiple different prototype definitions

Version-1: 2D Automatic Allocation

Prototype constraint:

```
double computeMinor(int r_m, int c_m, int r, double Mat[N][N]);
where,
```

- r_m is row index of the minor
- c m is column index of the minor
- r is the row and column number of input matrix
- Mat[N][N] is the input square matrix where N is a sufficiently large number defined at the begining of the program

As you can see the function has a return type of double which the output minor result should be assigned to

Assume the determinant function is given with prototype:

```
double determinant(int r, double Mat[N][N]);
```

```
double computeMinor(int r_m, int c_m, int r, double Mat[N][N]) {
     int k = 0, l = 0;
     double subMat[N][N];
     for(int i = 0; i < r; i++){
         1 = 0;
         for(int j = 0; j < r; j++){
             if((i != (r_m - 1)) \&\& (j != (c_m - 1))){
                 subMat[k][l] = Mat[i][j];
                 1++;
         if(i != (r m - 1)){
             k++;
     printf("sub-mat:\n");
     printMat(r-1, r-1, subMat);
     return determinant (r-1, subMat);
```

```
int main()
{
    double r, det, minor;
    double Mat[N][N];
    printf("Enter the size n of a nxn matrix:\n");
    scanf("%lf",&r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);
    minor = computeMinor(2, 1, r, Mat);
    printf("%f\n", minor);
    return 0;
}
```

Output:

```
Matrix is:
1.000000
                2.000000
                                 3.000000
4.000000
                5.000000
                                 6.000000
7.000000
                8.000000
                                 9.000000
sub-mat:
Matrix is:
2.000000
                3.000000
8.000000
                9.000000
-6.000000
```

Version-2: Pass by Reference

 Assume the question had a different constraint. Instead of returning the minor directly we output it using pass by reference. So intead of

```
double computeMinor(int r_m, int c_m, int r, double Mat[N][N]);
we have the prototype constraint of

void computeMinor(int r_m, int c_m, int r, double Mat[N][N], double *minor);
```

```
double computeMinor(int r m, int c m, int r, double Mat[N][N]) {
     int k = 0, l = 0;
     double subMat[N][N];
     for (int i = 0; i < r; i++) {
         1 = 0;
         for (int j = 0; j < r; j++) {
              if((i != (r_m - 1)) && (j != (c_m - 1))){
                  subMat[k][l] = Mat[i][j];
                  1++;
         if(i != (r_m - 1) ){
              k++;
     printf("sub-mat:\n");
     printMat (r-1, r-1, subMat);
     return determinant (r-1, subMat);
```

```
void computeMinor(int r m, int c m, int r, double Mat[N][N], double *minor){
     int k = 0, 1 = 0;
     double subMat[N][N];
     for (int i = 0; i < r; i++) {
         1 = 0;
         for (int j = 0; j < r; j++) {
              if((i != (r m - 1)) && (j != (c_m - 1))){
                  subMat[k][l] = Mat[i][j];
                  1++;
         if(i != (r m - 1)){
              k++;
     printf("sub-mat:\n");
     printMat (r-1, r-1, subMat);
     return determinant (r-1, subMat);
```

```
void computeMinor(int r m, int c m, int r, double Mat[N][N], double *minor){
     int k = 0, 1 = 0;
     double subMat[N][N];
     for (int i = 0; i < r; i++) {
         1 = 0;
         for (int j = 0; j < r; j++) {
             if((i != (r_m - 1)) && (j != (c_m - 1))){
                  subMat[k][l] = Mat[i][j];
                 1++;
         if(i != (r m - 1)){
             k++;
     printf("sub-mat:\n");
     printMat (r-1, r-1, subMat);
     *minor = determinant(r-1, subMat);
```

```
int main()
{
    double r, det, minor;
    double Mat[N][N];
    printf("Enter the size n of a nxn matrix:\n");
    scanf("%lf", &r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);
    minor = computeMinor(2, 1, r, Mat);
    printf("%f\n", minor);
    return 0;
}
```

```
int main()
{
    double r, det, minor;
    double Mat[N][N];
    printf("Enter the size n of a nxn matrix:\n");
    scanf("%lf", &r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);

    computeMinor(2, 1, r, Mat, &minor);
    printf("%f\n", minor);
    return 0;
}
```

```
int main()
    double r. det. minor:
    double Mat[N][N];
    printf("Enter the size n of a nxn matrix:\n");
    scanf("%lf", &r);
    getMat(r, r, Mat);
    printMat(r, r, Mat);
    computeMinor(2, 1, r, Mat, &minor);
    printf("%f\n", minor);
    return 0;
Output:
Matrix is:
1.000000
              2.000000
                             3.000000
4.000000
              5.000000
                             6.000000
7.000000
              8.000000
                             9.000000
sub-mat:
Matrix is:
2.000000
              3.000000
8.000000
              9.000000
-6.000000
```

Version-3: 1D Representation

 Now we alter the prototype constraint such that we can use one dimentional matrix representation. New prototype constraint is:

```
double computeMinor(int r_m, int c_m, int r, double *Mat);
Or
double computeMinor(int r_m, int c_m, int r, double Mat[N]);
```

which are basically the same for this problem as both of them will be used to represent an array

Version-1

```
double computeMinor(int r m, int c m, int r, double Mat[][N]) double computeMinor(int r m, int c m, int r, double *Mat) {
    int k = 0, l = 0;
    double subMat[N][N];
   for (int i = 0; i < r; i++) {
        1 = 0;
        for (int j = 0; j < r; j++) {
            if((i != (r_m - 1)) \&\& (j != (c_m - 1))){
                subMat[k][l] = Mat[i][j];
                1++;
        if(i != (r_m - 1) ){
            k++;
    printf("sub-mat:\n");
    printMat(r-1, r-1, subMat);
    return determinant (r-1, subMat);
```

Version-3

```
#define subMat(i,j) *(subMat+i*(r-1)+j)
int k = 0, l = 0;
double subMat[N];
for(int i = 0; i < r; i++){
    1 = 0:
    for(int j = 0; j < r; j++){
        if((i != (r m - 1)) && (j != (c m - 1))){
            subMat(k,l) = Mat(i,j);
            1++:
    if(i != (r m - 1)){
printf("sub-mat:\n");
printMat(r-1, r-1, subMat);
return determinant (r-1, subMat);
```

Define Statement

```
#define subMat(i,j) *(subMat+i*(r-1)+j)
```

(r-1) is the maximum column number of subMat matrix for this example, so replace (r-1) with whatever the maximum column number is in other examples *(subMat+i*(r-1)+j) is equivalent to *(subMat+k) where k=i*(r-1)+ j which is also equivalent to subMat[k]

Memory:

subMat[0]
subMat[1]
subMat[2]
subMat[3]
subMat[N] = subMat[4]
subMat[5]
subMat[6]
subMat[7]
subMat[8]

Virtual Matrix Representation:

```
subMat[0] subMat[1] subMat[2]
subMat[N] = subMat[3] subMat[4] subMat[5]
subMat[6] subMat[7] subMat[8]
```

For example if we want to access element (i,j) of a mxn matrix we multiply first index with maximum column number and add with second index k=i*n+j

In this example: 4=1*3+1

```
#include <stdio.h>
#include <stdlib.h>
#define N 100
#define Mat(i,j) *(Mat+i*r+j)
int main()
    double r, det, minor;
    double Mat[N];
    printf("Enter the size n of a nxn matrix:\n");
                                                        Output:
    scanf("%lf",&r);
                                                       Matrix is:
    getMat(r, r, Mat);
                                                       1.000000
                                                                      2.000000
                                                                                     3.000000
                                                       4.000000
                                                                      5.000000
                                                                                     6.000000
   printMat(r, r, Mat);
                                                       7.000000
                                                                      8.000000
                                                                                     9.000000
   minor = computeMinor(2, 1, r, Mat);
                                                       sub-mat:
   printf("%f\n", minor);
                                                       Matrix is:
    return 0:
                                                       2.000000
                                                                      3.000000
                                                       8.000000
                                                                      9.000000
                                                       -6.000000
```

```
double computeMinor(int r m, int c m, int r, double *Mat) {
    #define subMat(i,j) *(subMat+i*(r-1)+j)
    int k = 0, l = 0;
    double subMat[N];
    for(int i = 0; i < r; i++){
        1 = 0:
        for(int j = 0; j < r; j++){
            if((i != (r_m - 1)) && (j != (c_m - 1))){
                subMat(k,l) = Mat(i,i);
                1++;
        if(i != (r m - 1)){
            k++;
    printf("sub-mat:\n");
   printMat(r-1, r-1, subMat);
    return determinant (r-1, subMat);
```

```
double computeMinor(int r m, int c m, int r, double *Mat) {
    #define subMat(i,j) *(subMat+i*(r-1)+j)
   int k = 0, l = 0;
    double *subMat = malloc(sizeof(double)*(r-1)*(r-1));
   for(int i = 0; i < r; i++){
       1 = 0:
       for(int j = 0; j < r; j++){
            if((i != (r m - 1)) && (j != (c m - 1))){
                subMat(k,l) = Mat(i,j);
                1++:
        if(i != (r m - 1)){
            k++;
   printf("sub-mat:\n");
   printMat(r-1, r-1, subMat);
    return determinant (r-1, subMat);
```

```
double computeMinor(int r m, int c m, int r, double *Mat) {
   #define subMat(i,j) *(subMat+i*(r-1)+j)
   int k = 0, l = 0, minor;
    double *subMat = malloc(sizeof(double)*(r-1)*(r-1));
    for(int i = 0; i < r; i++){
       1 = 0:
       for(int j = 0; j < r; j++){
           if((i != (r_m - 1)) && (j != (c_m - 1))){
               subMat(k,l) = Mat(i,i);
               1++:
       if(i != (r m - 1)){
            k++;
   printf("sub-mat:\n");
   printMat(r-1, r-1, subMat);
    return determinant (r-1, subMat);
```

```
double computeMinor(int r m, int c m, int r, double *Mat) {
   #define subMat(i,j) *(subMat+i*(r-1)+j)
   int k = 0, l = 0, minor;
   double *subMat = malloc(sizeof(double)*(r-1)*(r-1));
   for(int i = 0; i < r; i++){
       1 = 0:
       for(int j = 0; j < r; j++){
           if((i != (r m - 1)) && (j != (c m - 1))){
               subMat(k,l) = Mat(i,j);
               1++:
       if(i != (r m - 1)){
           k++;
   printf("sub-mat:\n");
   printMat(r-1, r-1, subMat); minor = determinant(r-1, subMat); free(subMat);
   return determinant (r-1, subMat);
```

```
double computeMinor(int r m, int c m, int r, double *Mat) {
   #define subMat(i,j) *(subMat+i*(r-1)+j)
   int k = 0, l = 0, minor;
   double *subMat = malloc(sizeof(double)*(r-1)*(r-1));
   for(int i = 0; i < r; i++){
       1 = 0:
       for(int j = 0; j < r; j++){
           if((i != (r m - 1)) && (j != (c m - 1))){
               subMat(k,l) = Mat(i,j);
               1++:
       if(i != (r m - 1)){
           k++;
   printf("sub-mat:\n");
   printMat(r-1, r-1, subMat); minor = determinant(r-1, subMat); free(subMat);
   return minor;
```

```
int main()
    double r, det, minor;
    double *Mat:
    printf("Enter the size n of a nxn matrix:\n");
    scanf ("%lf", &r);
    Mat = malloc(sizeof(double)*r*r);
    getMat(r, r, Mat);
    printMat(r, r, Mat);
                                                      Output:
    minor = computeMinor(2, 1, r, Mat);
                                                    Matrix is:
    printf("%f\n", minor);
                                                    1.000000
                                                                   2.000000
                                                                                   3.000000
    return 0:
                                                    4.000000
                                                                   5.000000
                                                                                   6.000000
                                                    7.000000
                                                                   8.000000
                                                                                   9.000000
                                                    sub-mat:
                                                    Matrix is:
                                                    2.000000
                                                                    3.000000
                                                    8.000000
                                                                   9.000000
                                                    -6.000000
```

Question-2

 Lets slightly modify the problem by asking sub-matrix that is obtained by removing row r_m and column c_m

Lets start with 2D automatic allocation:

What is wrong with this code?

```
int main()
{
    double r, det, minor;
    double Mat[N][N];
    printf("Enter the size n of a nxn matrix:\n");
    scanf("%lf",&r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);
    minor = computeMinor(2, 1, r, Mat);
    printf("%f\n", minor);
    return 0;
}
```

```
int main()
{    double sMat[N][N];
    double r, det, minor;
    double Mat[N][N];
    printf("Enter the size n of a nxn matrix:\n");
    scanf("%lf",&r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);
    minor = computeMinor(2, 1, r, Mat);
    printf("%f\n", minor);
    return 0;
}
```

```
int main()
{    double sMat[N][N];
    double r, det, minor;
    double Mat[N][N];
    printf("Enter the size n of a mxm matrix:\n");
    scanf("%lf",&r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);
    computeSubMat(2, 1, r, Mat, sMat);
    printf("%f\n", minor);
    return 0;
}
```

```
int main()
{    double sMat[N][N];
    double r, det, minor;
    double Mat[N][N];
    printf("Enter the size n of a mxm matrix:\n");
    scanf("%lf",&r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);
    computeSubMat(2, 1, r, Mat, sMat);
    printMat(r-1, r-1, sMat);
    return 0;
}
```

```
int main()
   double sMat[N][N];
   double r, det, minor;
   double Mat[N][N];
   printf("Enter the size n of a nxn matrix:\n");
   scanf("%lf",&r);
   getMat(r, r, Mat);
   printMat(r, r, Mat);
   computeSubMat(2, 1, r, Mat, sMat);
   printMat(r-1, r-1, sMat);
   return 0:
Matrix is:
1.000000
              2.000000
                            3.000000
4.000000
              5.000000
                            6.000000
7.000000
              8.000000
                            9.000000
Matrix is:
2.000000
              3.000000
8.000000
              9.000000
```

```
double computeMinor(int r m, int c m, int r, double *Mat) {
    #define subMat(i,i) *(subMat+i*(r-1)+i)
    int k = 0, l = 0;
    double *subMat = malloc(sizeof(double)*(r-1)*(r-1));
    for(int i = 0; i < r; i++){
        1 = 0;
        for(int j = 0; j < r; j++){
            if((i != (r_m - 1)) && (j != (c_m - 1))){
                subMat(k,l) = Mat(i,j);
                1++;
        if(i != (r m - 1)){
            k++;
   printf("sub-mat:\n");
   printMat(r-1, r-1, subMat);
    return determinant (r-1, subMat);
```

```
double computeMinor(int r m, int c m, int r, double *Mat) {
    #define subMat(i,j) *(subMat+i*(r-1)+j)
    int k = 0, l = 0;
    double *subMat = malloc(sizeof(double)*(r-1)*(r-1));
    for(int i = 0; i < r; i++){
        1 = 0;
        for(int j = 0; j < r; j++){
            if((i != (r_m - 1)) && (j != (c_m - 1))){
                subMat(k,l) = Mat(i,j);
                1++;
        if(i != (r m - 1)){
            k++;
    return determinant (r-1, subMat);
```

```
double computeMinor(int r m, int c m, int r, double *Mat) {
    #define subMat(i,j) *(subMat+i*(r-1)+j)
    int k = 0, l = 0;
    double *subMat = malloc(sizeof(double)*(r-1)*(r-1));
    for(int i = 0; i < r; i++){
        1 = 0;
        for(int j = 0; j < r; j++){
            if((i != (r_m - 1)) && (j != (c_m - 1))){
                subMat(k,l) = Mat(i,j);
                1++;
        if(i != (r m - 1)){
            k++;
    return subMat;
```

```
double* computeSubMat(int r m, int c m, int r, double *Mat){
   #define subMat(i,j) *(subMat+i*(r-1)+j)
   int k = 0, l = 0;
   double *subMat = malloc(sizeof(double)*(r-1)*(r-1));
   for(int i = 0; i < r; i++){
       1 = 0;
       for(int j = 0; j < r; j++){
            if((i != (r_m - 1)) && (j != (c_m - 1))){
                subMat(k,l) = Mat(i,j);
                1++;
       if(i != (r m - 1)){
            k++;
    return subMat;
```

```
int main()
{
    double r, det, minor;
    double *Mat;
    printf("Enter the size n of a mxm matrix:\n");
    scanf("%lf",&r);
    Mat = malloc(sizeof(double)*r*r);
    getMat(r, r, Mat);
    printMat(r, r, Mat);
    minor = computeMinor(2, 1, r, Mat);
    printf("%f\n", minor);
    free(Mat);
    return 0;
}
```

```
int main()
{
    double r, det, *sMat;
    double *Mat;
    printf("Enter the size n of a mxm matrix:\n");
    scanf("%lf",&r);
    Mat = malloc(sizeof(double)*r*r);
    getMat(r, r, Mat);
    printMat(r, r, Mat);
    minor = computeMinor(2, 1, r, Mat);
    printf("%f\n", minor);
    free(Mat);
    return 0;
}
```

```
int main()
{
    double r, det, *sMat;  
    double *Mat;
    printf("Enter the size n of a mxm matrix:\n");
    scanf("%lf",&r);
    Mat = malloc(sizeof(double)*r*r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);

    sMat = computeSubMat(2, 1, r, Mat);  
    printf("%f\n", minor);
    free(Mat);
    return 0;
}
```

```
int main()
{
    double r, det, *sMat;  
    double *Mat;
    printf("Enter the size n of a mxm matrix:\n");
    scanf("%lf",&r);
    Mat = malloc(sizeof(double)*r*r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);
    sMat = computeSubMat(2, 1, r, Mat);  
    printMat(r-1, r-1, sMat);  
    free(Mat);
    return 0;
}
```

```
int main()
{
    double r, det, *sMat;
    double *Mat;
    printf("Enter the size n of a mxm matrix:\n");
    scanf("%lf",&r);
    Mat = malloc(sizeof(double)*r*r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);
    sMat = computeSubMat(2, 1, r, Mat);
    printMat(r-1, r-1, sMat);
    free(Mat); free(sMat);
    return 0;
}
```

Version-3 Static 2D Representation

Lets modify from failed attempt at version-1

```
double** computeSubMat(int r m, int c m, int r, double Mat[N][N]) {
    int k = 0, l = 0;
    double subMat[N][N];
    for(int i = 0; i < r; i++){
        1 = 0;
        for(int j = 0; j < r; j++){
            if((i != (r_m - 1)) && (j != (c_m - 1))){
                subMat[k][l] = Mat[i][j];
                1++;
        if(i != (r m - 1)){
            k++;
    return subMat;
```

Version-3 Static 2D Representation

Lets modify from failed attempt at version-1

```
double** computeSubMat(int r m, int c m, int r, double Mat[N][N]) {
    int k = 0, l = 0;
    static double subMat[N][N];
    for(int i = 0; i < r; i++){
        1 = 0;
        for(int j = 0; j < r; j++){
            if((i != (r_m - 1)) && (j != (c_m - 1))){
                subMat[k][l] = Mat[i][j];
                1++;
        if(i != (r m - 1)){
           k++;
    return subMat;
```

```
int main()
{
    double sMat[N][N];
    double r, det;
    double Mat[N][N];
    printf("Enter the size n of a nxn matrix:\n");
    scanf("%lf",&r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);
    computeSubMat(2, 1, r, Mat, sMat);
    printMat(r-1, r-1, sMat);
    return 0;
}
```

```
int main()
{
    double sMat[N][N];
    double r, det;
    double Mat[N][N];
    printf("Enter the size n of a nxn matrix:\n");
    scanf("%lf",&r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);

    sMat = computeSubMat(2, 1, r, Mat);
    printMat(r-1, r-1, sMat);
    return 0;
}
```

```
int main()
{
    double **sMat;
    double r, det;
    double Mat[N][N];
    printf("Enter the size n of a nxn matrix:\n");
    scanf("%lf",&r);
    getMat(r, r, Mat);

    printMat(r, r, Mat);

    sMat = computeSubMat(2, 1, r, Mat);
    printMat(r-1, r-1, sMat);
    return 0;
}
```