

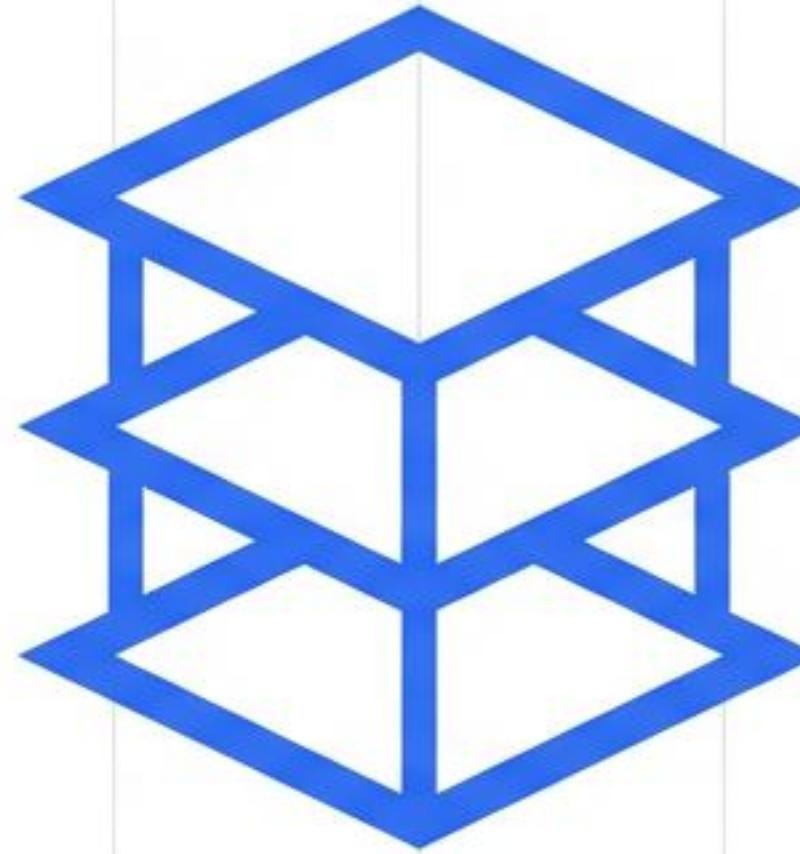


FOUNDATION TIER

MODULE 03

Neural Building Blocks

Constructing the fundamental layers that form neural networks

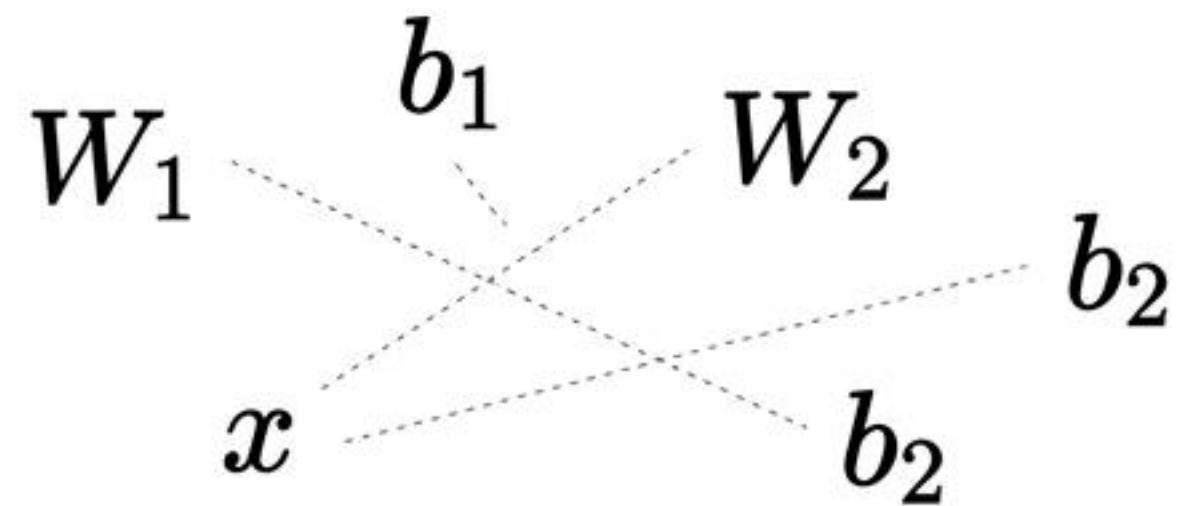


Module 03: Layers

From Tensor Arithmetic to Neural Building Blocks

Why We Need an Abstraction

The Problem: Loose Wires

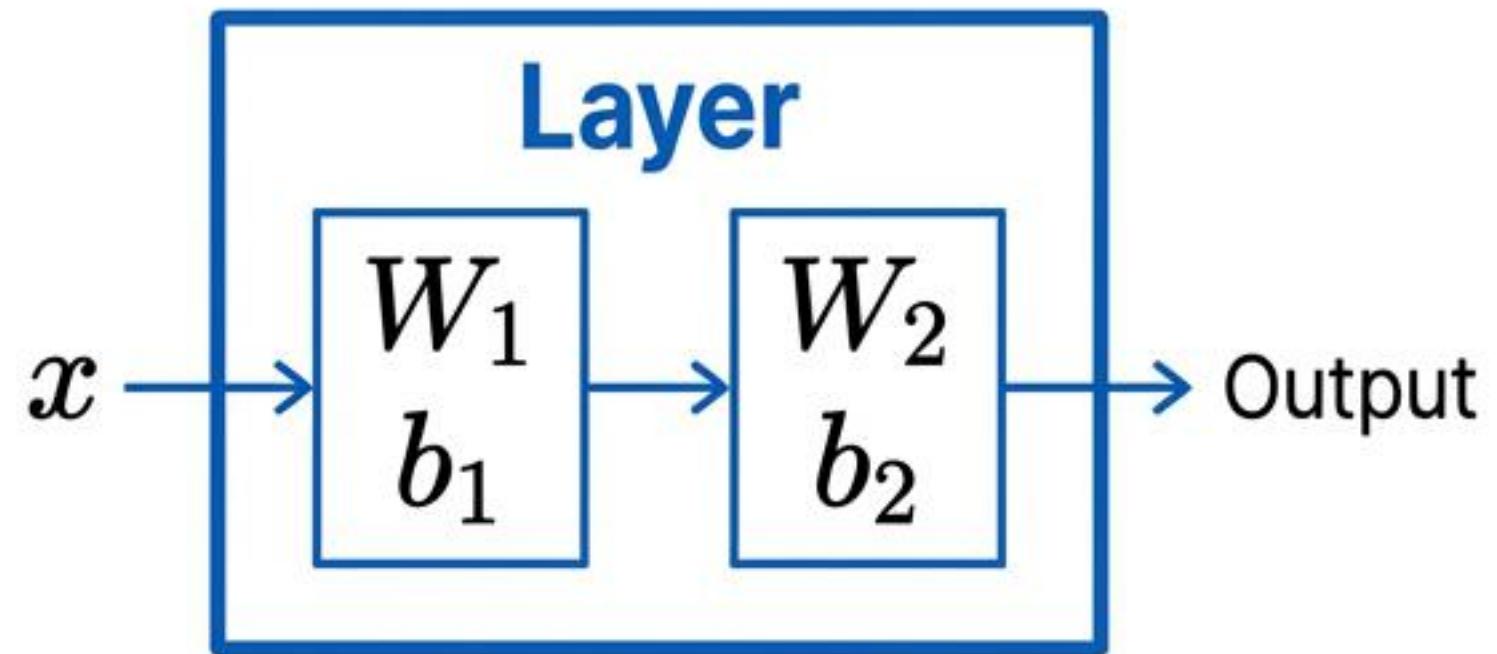


- Manual management of state.
- Complex parameter tracking.
- Prone to shape errors.

Code Snippet

```
y = x @ w + b
```

The Solution: Integrated Chips



- Encapsulates computation (Forward) and state (Parameters).
- Provides a consistent interface.

The Base Class Contract

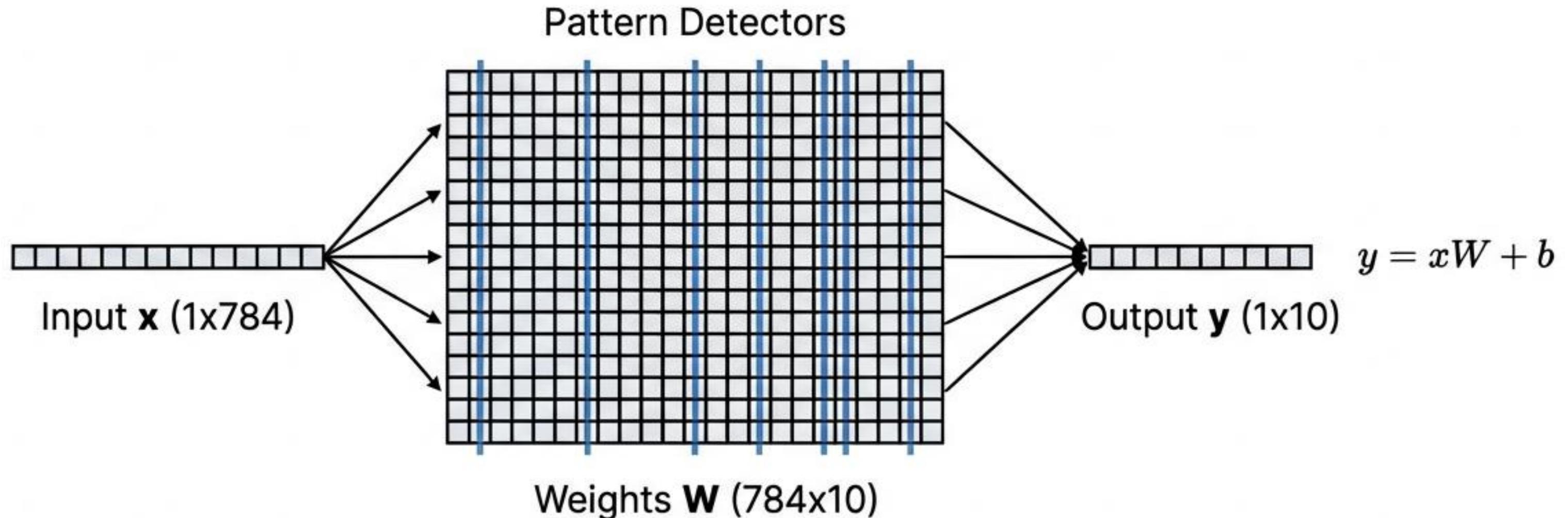
```
class Layer:  
    def forward(self, x):  
        """Compute layer output"""  
        raise NotImplementedError  
  
    def parameters(self):  
        """Return list of trainable parameters"""  
        return []  
  
    def __call__(self, x, *args, **kwargs):  
        return self.forward(x, *args, **kwargs)
```

Consistency: Every layer looks the same to the optimizer.

Callability: Enables intuitive `layer(x)` syntax.

Discovery: A standard way to request trainable weights.

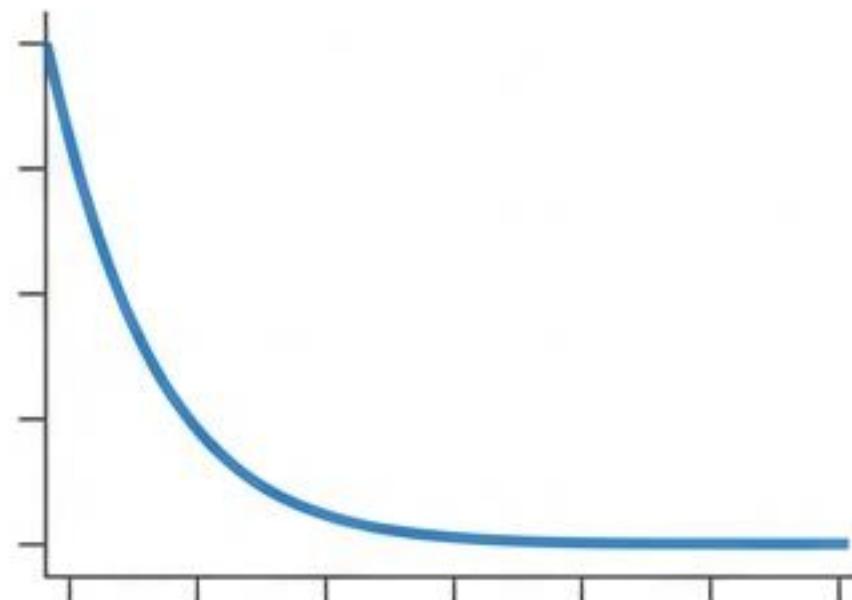
Concept: The Linear Layer



- Role: Feature Transformation (Pixels → Meaning)
- Mechanism: Dot product measures similarity between input and learned patterns.
- Bias: Shifts the activation function independent of input.

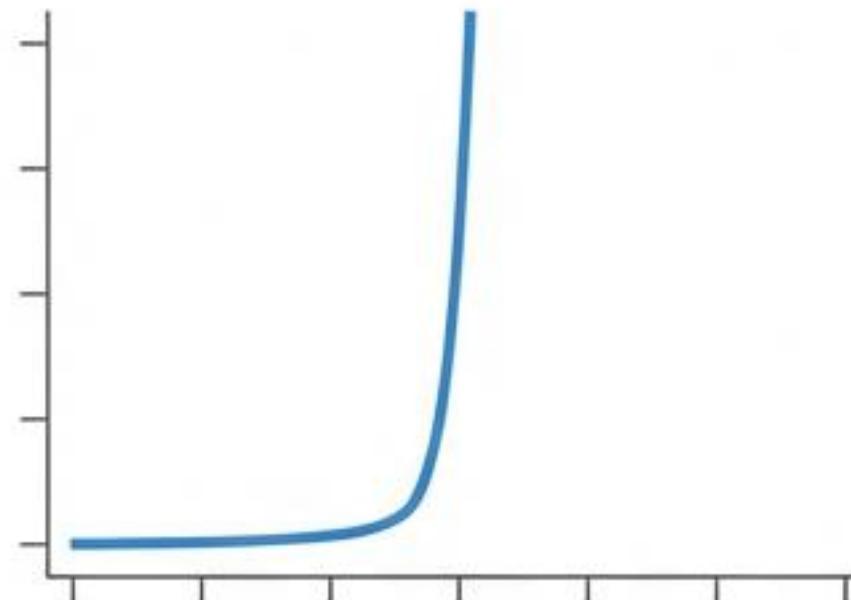
Systems Constraint: Initialization

Too Small



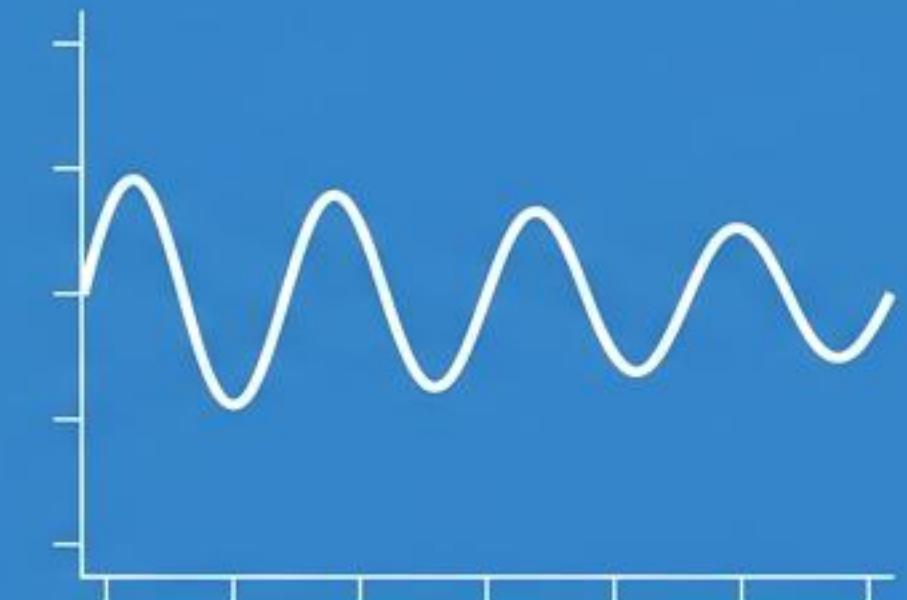
Vanishing Gradients

Too Large



Exploding Gradients

Xavier Init



Stable Variance

The Solution: Scale random weights by $\sqrt{1 / \text{fan_in}}$ to preserve signal variance.

Code: Linear Initialization

Variance
Preservation

```
class Linear(Layer):
    def __init__(self, in_features, out_features, bias=True):
        self.in_features = in_features

        # Xavier Initialization
        scale = np.sqrt(1.0 / in_features)
        weight_data = np.random.randn(in_features, out_features) * scale

        self.weight = Tensor(weight_data) ← Registering State
        if bias:
            self.bias = Tensor(np.zeros(out_features)) ←
        else:
            self.bias = None
```

Registering State

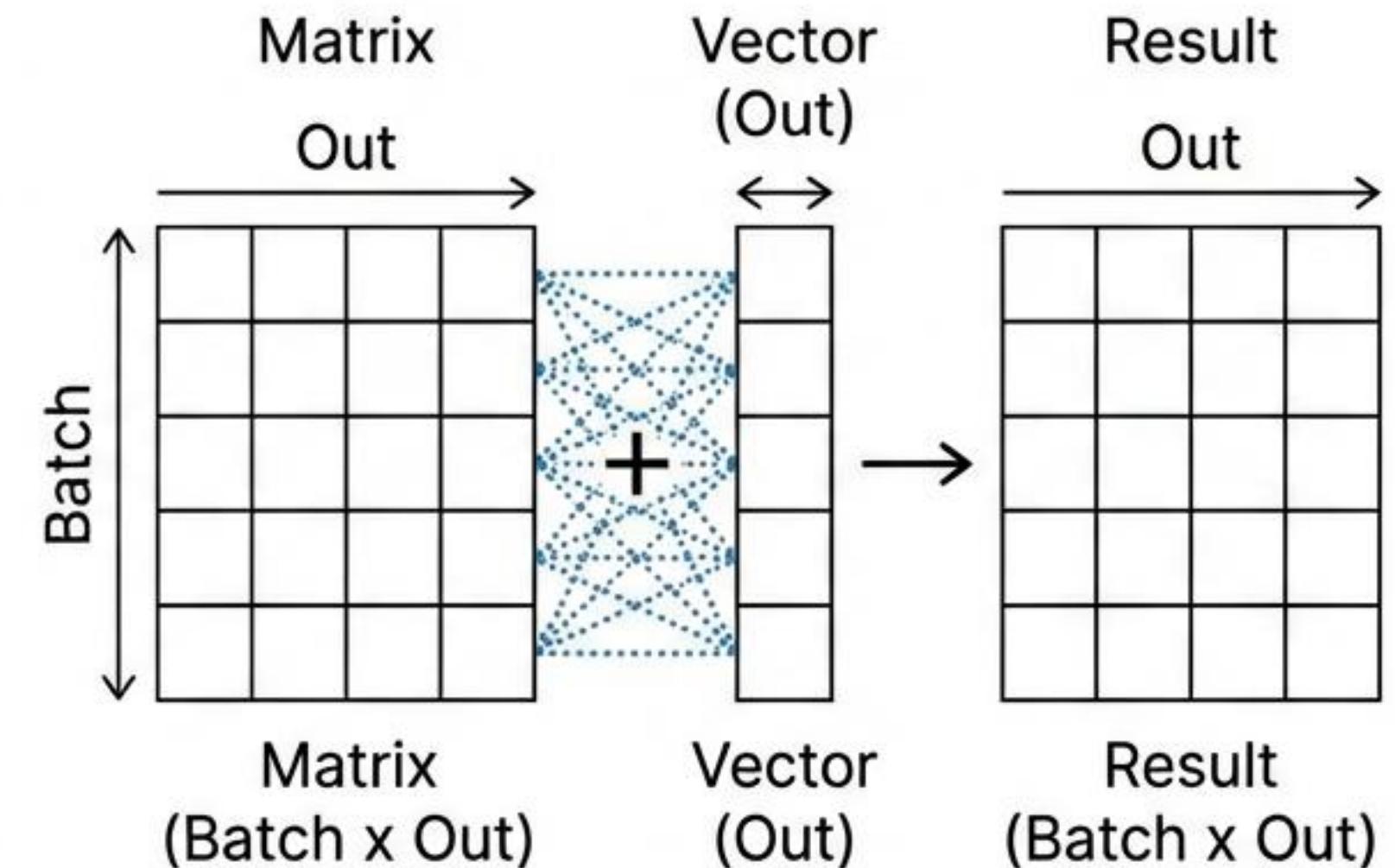
Code: Linear Forward

```
def forward(self, x):
    """y = xW + b"""

    # 1. Matrix Multiplication
    output = x.matmul(self.weight)

    # 2. Bias Addition (Broadcasting)
    if self.bias is not None:
        output = output + self.bias

    return output
```



Code: Parameter Management

```
def parameters(self):
    """Return list of trainable parameters"""
    params = [self.weight]

    if self.bias is not None:
        params.append(self.bias)

    return params
```

The Layer acts as a registry. It is responsible for reporting what it owns to the Optimizer. If the bias is disabled, it is excluded from the list.

Systems Reality: Memory Footprint

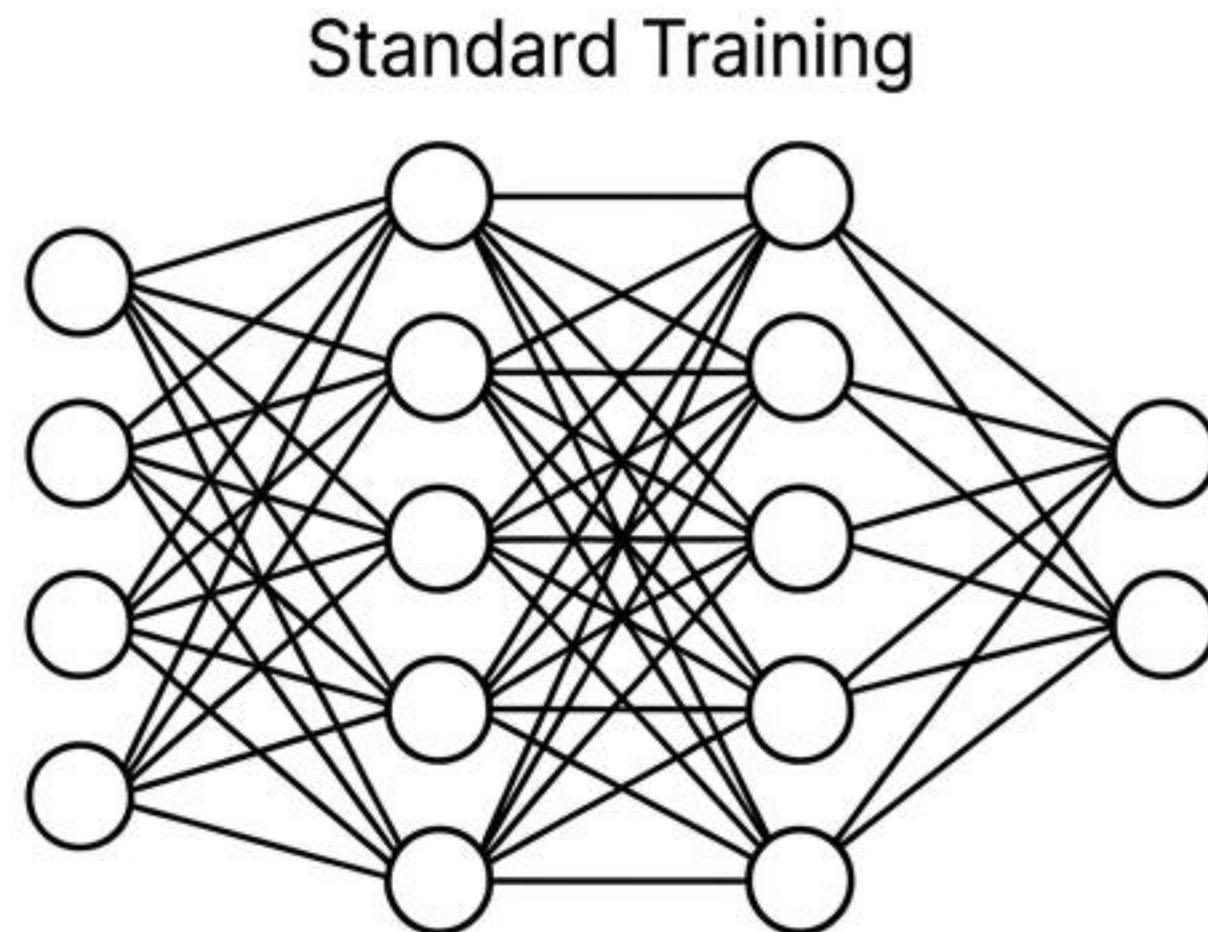


Case Study: Linear(784, 256) [Float32]

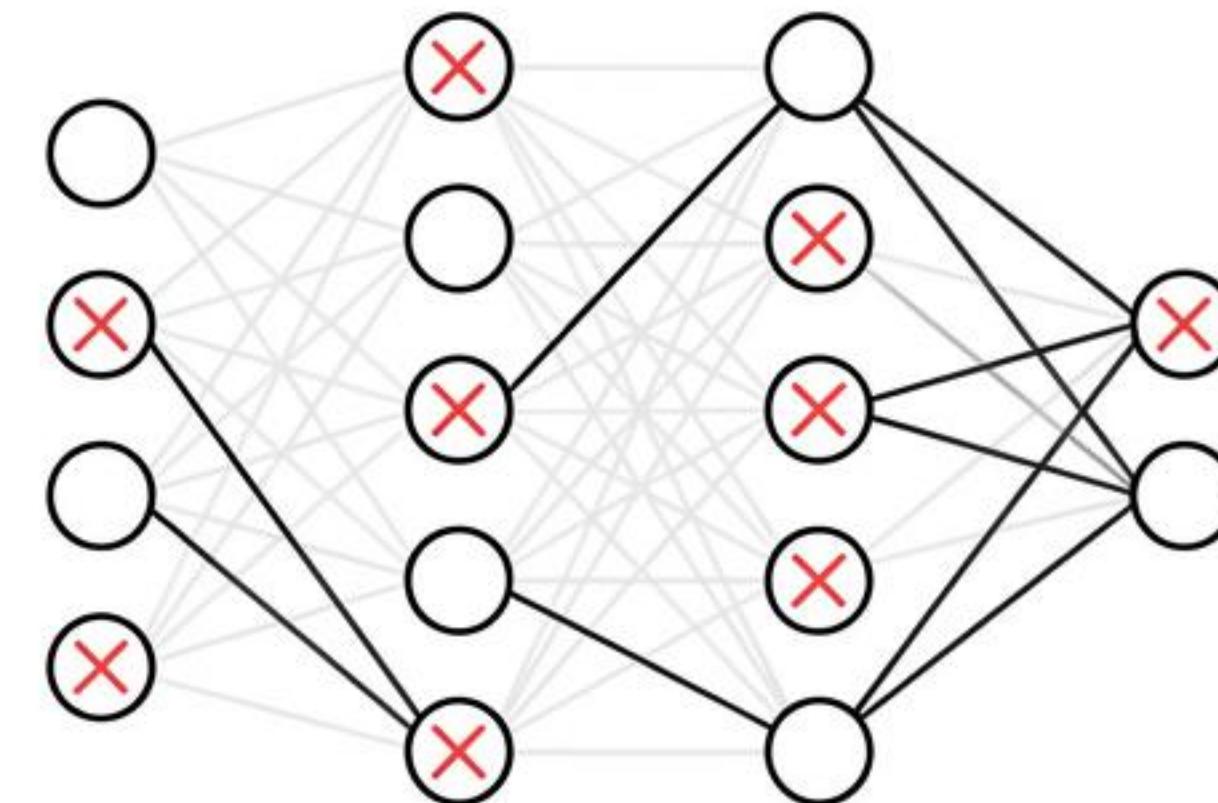
- Weight Matrix: $784 \times 256 \times 4$ bytes ≈ 800 KB
- Bias Vector: 256×4 bytes ≈ 1 KB

Linear layers are memory-heavy. Doubling the width quadruples the parameter count.

Concept: Dropout



Dropout Training ($p=0.5$)

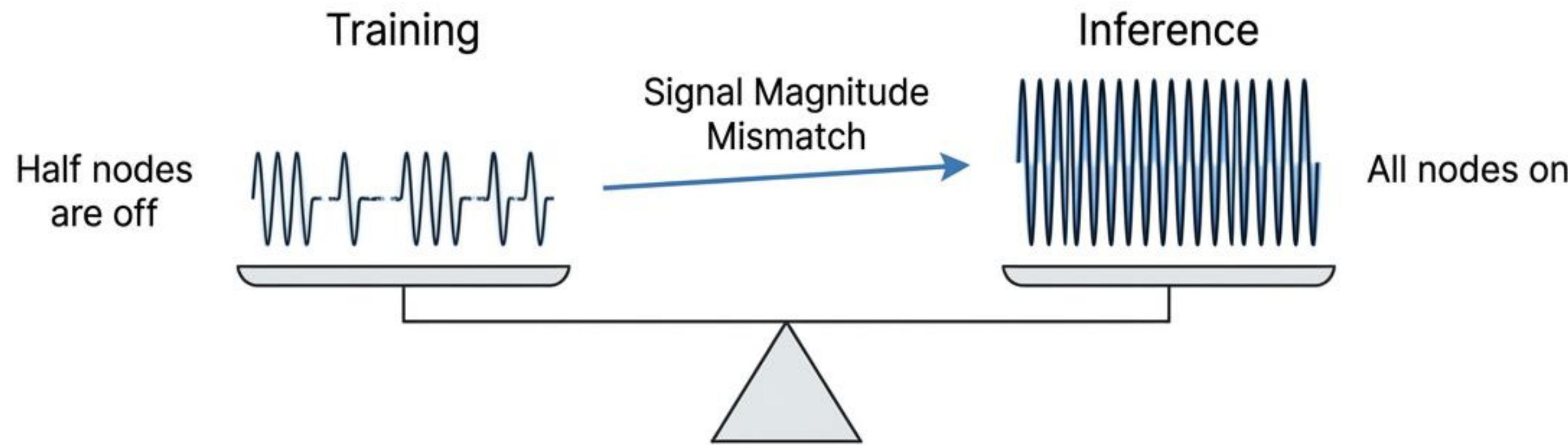


The Problem: Overfitting (Memorization).

The Solution: Randomly disable neurons during training to force redundancy.

Intuition: No single neuron can be a single point of failure.

Constraint: The Scaling Invariant



Inverted Dropout Solution: To fix the mismatch, we boost the signal during training.

$$\text{Scale Factor} = \frac{1}{1 - p}$$

If $p=0.5$ (50% drop), we multiply survivors by 2.0 to maintain expected magnitude.

Code: Dropout Implementation

```
class Dropout(Layer):
    def __init__(self, p=0.5):
        self.p = p

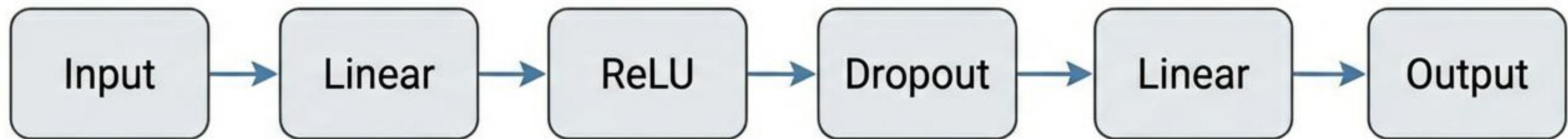
    def forward(self, x, training=True):
        if not training: return x → Pass-through at Inference

        # 1. Create Mask
        keep_prob = 1.0 - self.p
        mask = np.random.random(x.data.shape) < keep_prob

        # 2. Scale Factor (Inverted Dropout)
        scale = 1.0 / keep_prob → Invariant Enforcement

        # 3. Apply
        return x * Tensor(mask) * Tensor(scale)
```

Concept: Composition



$$y = f_2(\text{dropout}(\sigma(f_1(x))))$$

Deep Learning is simply function composition.
We need a container to manage the pipeline.

Code: The Sequential Container

```
class Sequential(Layer):
    def __init__(self, *layers):
        self.layers = list(layers)

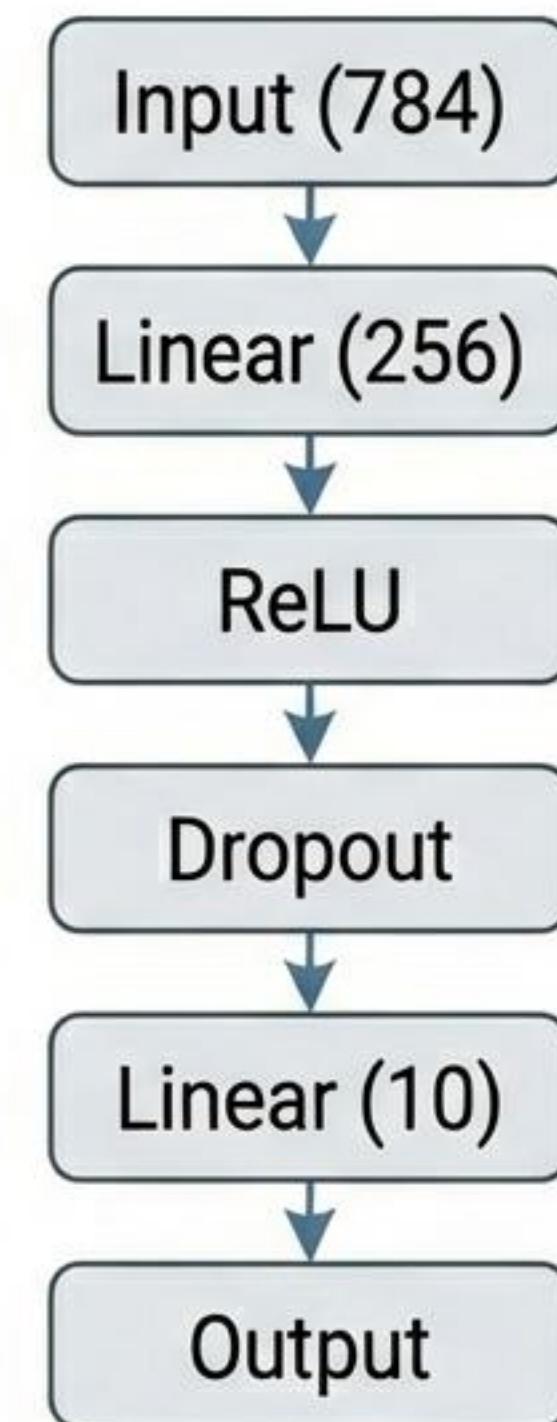
    def forward(self, x):
        for layer in self.layers:
            x = layer(x)
        return x

    def parameters(self):
        params = []
        for layer in self.layers:
            params.extend(layer.parameters())
        return params
```

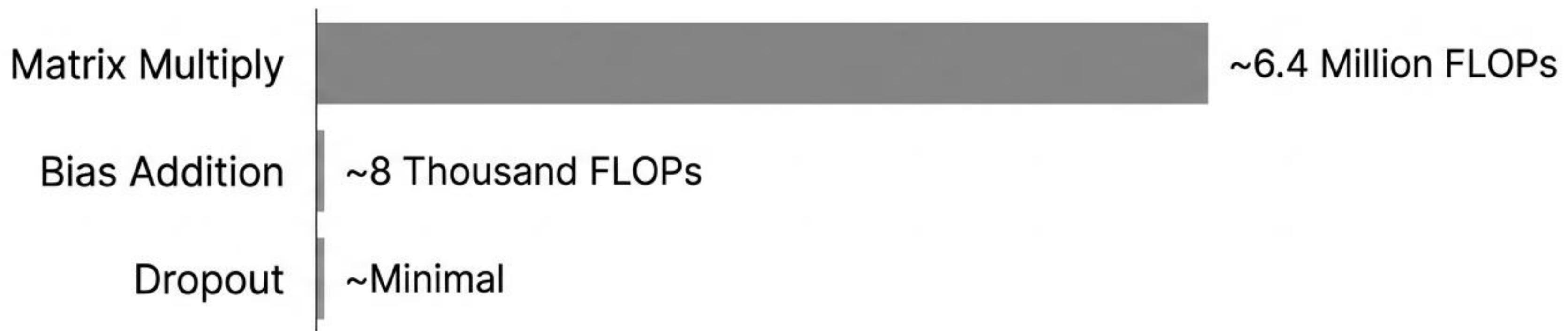
Simplicity is power. `forward` loops through computation. `parameters` recursively collects state.

Putting It Together

```
model = Sequential(  
    Linear(784, 256),  
    ReLU(),  
    Dropout(0.5),  
    Linear(256, 10)  
)
```



Systems Analysis: Compute Intensity

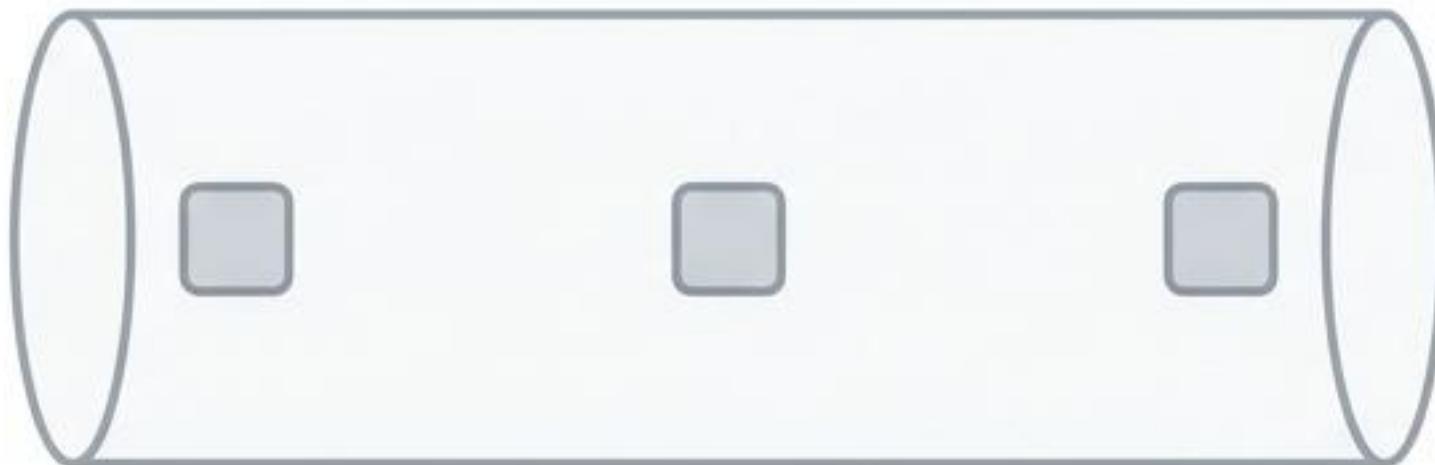


For Linear(784, 256) with Batch=32.

99.9% of compute time is spent in Matrix Multiplication.
Optimizing Deep Learning = Optimizing Matmul.

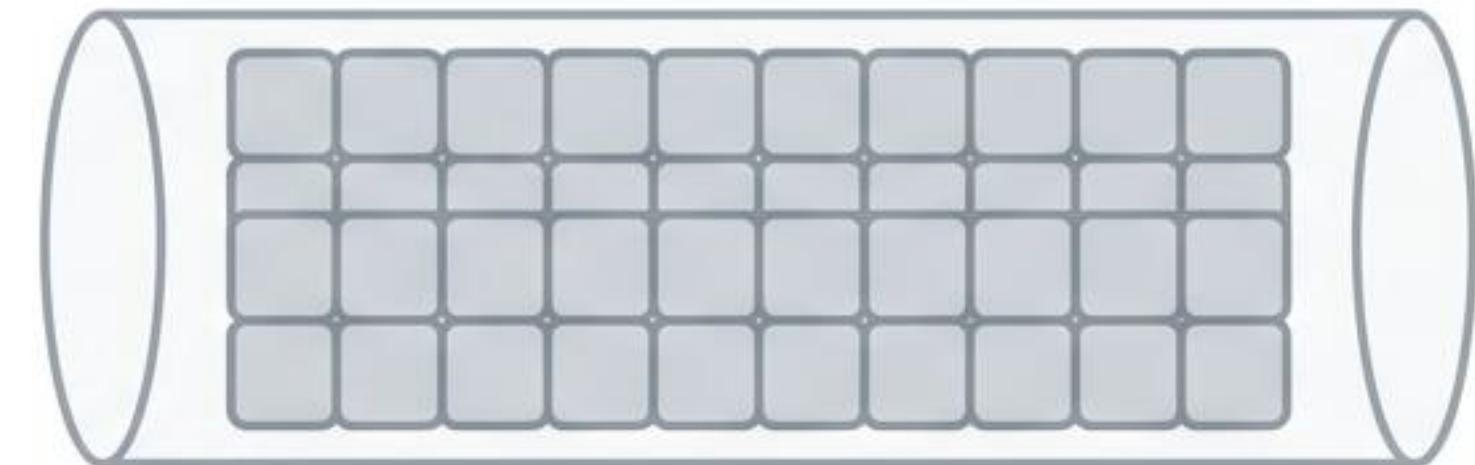
Systems Analysis: The Power of Batching

Batch Size = 1



~800 samples/sec

Batch Size = 32



~10,000 samples/sec

Why Batch?

- 1. Amortizes Python overhead.
- 2. Vectorization (SIMD) efficiency.
- 3. Cache locality.

Common Failure Modes

Shape Mismatch

Symptom: `ValueError: (32, 128) @ (256, 10)`

Fix: Output of Layer N must match Input of Layer N+1.

The Inference Bug

Symptom: Training loss is good, but Test accuracy is terrible.

Fix: Forgot `training=False` during evaluation. Dropout is still killing signals.

Silent Failure

Symptom: Model doesn't learn.

Fix: `parameters()` method is incomplete. Optimizer cannot see the weights.

TinyTorch vs. PyTorch

	TinyTorch	PyTorch
API	<code>Linear(in, out)</code>	<code>nn.Linear(in, out)</code>
Container	<code>Sequential</code>	<code>nn.Sequential</code>
Parameters	returns `List`	returns `Generator`
Backend	NumPy	C++ / CUDA

You have implemented the core API of the industry standard.
The logic is identical; only the engine differs.

Module Summary

- [✓] Abstraction:** Unified ‘Layer’ interface
- [✓] Linear:** The learned transformation ($y = xW + b$)
- [✓] Dropout:** Robustness via randomness
- [✓] Sequential:** Composition logic
- [✓] State:** Parameter management

Coming Next: Module 04

LOSS FUNCTIONS

The network can predict, but it doesn’t know if it’s right or wrong. We need to measure error to drive learning.