

# Regresi Linear Berganda

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## Nomor 1

```
data1 <- data.frame(penjualan <- c(72,76,78,70,68,80,82,65,62,90),
                    jumlah_iklan <- c(12,11,15,10,11,16,14,8,8,18),
                    jumlah_endorse <- c(5,8,6,5,3,9,12,14,3,10))

model1 <- lm(penjualan ~ jumlah_iklan + jumlah_endorse,data1)
summary(model1)

##
## Call:
## lm(formula = penjualan ~ jumlah_iklan + jumlah_endorse, data = data1)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.3551 -1.6237 -0.5034  1.7708  4.4144
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    43.0547     3.6105  11.925 6.63e-06 ***
## jumlah_iklan     2.2630     0.2788   8.116 8.31e-05 ***
## jumlah_endorse   0.4548     0.2505   1.816  0.112
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.74 on 7 degrees of freedom
## Multiple R-squared:  0.9199, Adjusted R-squared:  0.897
## F-statistic: 40.21 on 2 and 7 DF, p-value: 0.0001453
```

- Model:  $\text{penjualan} = 43.0547 + 2.2630 \times (\text{jumlah iklan}) + 0.4548 \times (\text{jumlah endorse})$
- R-squared adalah 0.9199, yang berarti sekitar 91.99% variabilitas dalam penjualan dapat dijelaskan oleh jumlah iklan dan jumlah endorse
- Nilai p-value (0.0001453) bahwa setidaknya satu variabel independen secara signifikan mempengaruhi variabel dependen

## Nomor 2

```
library(readr)
```

```
## Warning: package 'readr' was built under R version 4.3.3
```

```
concrete <- read_csv("D:/UNAIR/SEMESTER 2/METSTAT/PRAK METSTAT AFTER UTS/concrete.csv")
```

```
## Rows: 1030 Columns: 9
## -- Column specification -----
## Delimiter: ","
## dbl (9): cement, slag, ash, water, superplastic, coarseagg, fineagg, age, st...
##
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
```

```
head(concrete)
```

```
## # A tibble: 6 x 9
##   cement slag ash water superplastic coarseagg fineagg age strength
##   <dbl> <dbl> <dbl> <dbl>      <dbl>      <dbl> <dbl> <dbl> <dbl>
## 1  141.  212    0  204.         0        972.   748.   28   29.9
## 2  169.  42.2 124.   158.        10.8       1081.   796.   14   23.5
## 3  250    0  95.7  187.         5.5        957.   861.   28   29.2
## 4  266  114    0  228         0        932    670   28   45.8
## 5  155. 183.    0  193.         9.1       1047.   697.   28   18.3
## 6  255    0    0  192         0        890.   945   90   21.9
```

```
model2 <- lm(strength ~ cement + slag + ash + water + superplastic + coarseagg + fineagg + age, data = concrete)
summary(model2)
```

```
##
## Call:
## lm(formula = strength ~ cement + slag + ash + water + superplastic +
##   coarseagg + fineagg + age, data = concrete)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -28.654  -6.302   0.703   6.569  34.450
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -23.331214  26.585504  -0.878  0.380372
## cement       0.119804   0.008489  14.113 < 2e-16 ***
## slag         0.103866   0.010136  10.247 < 2e-16 ***
## ash          0.087934   0.012583   6.988 5.02e-12 ***
## water       -0.149918   0.040177  -3.731 0.000201 ***
## superplastic 0.292225   0.093424   3.128 0.001810 **
## coarseagg    0.018086   0.009392   1.926 0.054425 .
## fineagg      0.020190   0.010702   1.887 0.059491 .
## age          0.114222   0.005427  21.046 < 2e-16 ***
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.4 on 1021 degrees of freedom
## Multiple R-squared:  0.6155, Adjusted R-squared:  0.6125
## F-statistic: 204.3 on 8 and 1021 DF,  p-value: < 2.2e-16
```

- Model:  $\text{strength} = -23.3312 + 0.1198 \times (\text{cement}) + 0.1039 \times (\text{slag}) + 0.0879 \times (\text{ash}) - 0.1499 \times (\text{water}) + 0.2922 \times (\text{superplastic}) + 0.0181 \times (\text{coarseagg}) + 0.0202 \times (\text{fineagg}) + 0.1142 \times (\text{age})$
- Semua variabel kecuali coarseagg dan fineagg memiliki p-value yang sangat rendah ( $< 0.05$ ), menunjukkan signifikansi statistik yang kuat terhadap strength
- R-squared adalah 0.6155, yang berarti sekitar 61.55% variabilitas dalam kekuatan beton dapat dijelaskan oleh model ini (cukup baik)
- P-value untuk F-statistik sangat rendah, menunjukkan bahwa keseluruhan model regresi tersebut signifikan secara statistik

### Nomor 3

```
library(tidyverse)
```

```
## Warning: package 'tidyverse' was built under R version 4.3.3
```

```
## Warning: package 'ggplot2' was built under R version 4.3.3
```

```
## Warning: package 'tibble' was built under R version 4.3.3
```

```
## Warning: package 'tidyr' was built under R version 4.3.3
```

```
## Warning: package 'purrr' was built under R version 4.3.3
```

```
## Warning: package 'dplyr' was built under R version 4.3.3
```

```
## Warning: package 'stringr' was built under R version 4.3.3
```

```
## Warning: package 'forcats' was built under R version 4.3.3
```

```
## Warning: package 'lubridate' was built under R version 4.3.3
```

```
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
```

```
## v dplyr      1.1.4      v purrr      1.0.2
```

```
## v forcats   1.0.0      v stringr   1.5.1
```

```
## v ggplot2   3.5.1      v tibble    3.2.1
```

```
## v lubridate 1.9.3      v tidyr     1.3.1
```

```
## -- Conflicts ----- tidyverse_conflicts() --
```

```
## x dplyr::filter() masks stats::filter()
```

```
## x dplyr::lag()    masks stats::lag()
```

```
## i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become errors
```

```
library(datarium)
```

```
## Warning: package 'datarium' was built under R version 4.3.3
```

```
data("marketing", package = "datarium")
head(marketing, 4)
```

```
##   youtube facebook newspaper sales
## 1  276.12    45.36    83.04 26.52
## 2   53.40    47.16    54.12 12.48
## 3   20.64    55.08    83.16 11.16
## 4  181.80    49.56    70.20 22.20
```

```
Y = marketing$sales
X1 = marketing$youtube
X2 = marketing$newspaper
X3 = marketing$facebook

#Building Model
model3 <- lm(Y ~ X1 + X2 + X3, data = marketing)
summary(model3)
```

```
##
## Call:
## lm(formula = Y ~ X1 + X2 + X3, data = marketing)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -10.5932  -1.0690   0.2902   1.4272   3.3951
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  3.526667   0.374290   9.422  <2e-16 ***
## X1           0.045765   0.001395  32.809  <2e-16 ***
## X2          -0.001037   0.005871  -0.177    0.86
## X3           0.188530   0.008611  21.893  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.023 on 196 degrees of freedom
## Multiple R-squared:  0.8972, Adjusted R-squared:  0.8956
## F-statistic: 570.3 on 3 and 196 DF, p-value: < 2.2e-16
```

```
#Delete variabel newspaper
model3b <- lm(Y ~ X1 + X3, data = marketing)
summary(model3b)
```

```
##
## Call:
## lm(formula = Y ~ X1 + X3, data = marketing)
##
```

```
## Residuals:
##      Min       1Q   Median       3Q      Max
## -10.5572  -1.0502   0.2906   1.4049   3.3994
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  3.50532    0.35339   9.919  <2e-16 ***
## X1           0.04575    0.00139  32.909  <2e-16 ***
## X3           0.18799    0.00804  23.382  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.018 on 197 degrees of freedom
## Multiple R-squared:  0.8972, Adjusted R-squared:  0.8962
## F-statistic: 859.6 on 2 and 197 DF,  p-value: < 2.2e-16
```

- Variabel newspaper tidak signifikan secara statistik terhadap variabel dependen (p-value 0.86) sehingga dapat dihapus. Model:  $\text{sales} = 3.5053 + 0.0458 \times (\text{youtube}) + 0.1880 \times (\text{facebook})$
- Dengan nilai adjusted R-squared 0.8962, maka sekitar 89.6% variabilitas dalam penjualan dapat dijelaskan oleh variabel independen yang ada dalam model
- Karena p-value sangat rendah, maka model secara keseluruhan signifikan.

## Nomor 4

```
data4 <- data.frame(y <- c(1.45, 1.93, 0.81, 0.61, 1.55, 0.95, 0.45, 1.14, 0.74, 0.98, 1.41, 0.81, 0.89,
                          x1 <- c(0.58, 0.86, 0.29, 0.2, 0.56, 0.28, 0.08, 0.41, 0.22, 0.35, 0.59, 0.22, 0.26,
                          x2 <- c(0.71, 0.13, 0.79, 0.2, 0.56, 0.92, 0.01, 0.6, 0.7, 0.73, 0.13, 0.96, 0.27,

model4 <- lm(y ~ x1 + x2, data = data4)
summary(model4)

##
## Call:
## lm(formula = y ~ x1 + x2, data = data4)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -0.15493 -0.07801 -0.02004  0.04999  0.30112
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  0.433547    0.065983   6.571 1.31e-06 ***
## x1           1.652993    0.095245  17.355 2.53e-14 ***
## x2           0.003945    0.074854   0.053   0.958
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1127 on 22 degrees of freedom
## Multiple R-squared:  0.9399, Adjusted R-squared:  0.9344
## F-statistic: 172 on 2 and 22 DF,  p-value: 3.699e-14
```

- Persamaan regresi:  $y = 0.4335 + 1.653 \times x_1 + 0.0039 \times x_2$
- $x_1$  memiliki p-value yang sangat rendah ( $< 0.001$ ), signifikan secara statistik dalam memprediksi  $y$ . Namun, variabel  $x_2$  memiliki p-value yang tinggi (0.958), tidak signifikan
- R-squared adalah 0.9399, yang berarti sekitar 93.99% variabilitas dalam  $y$  dapat dijelaskan oleh model ini
- Model secara keseluruhan signifikan secara statistik