

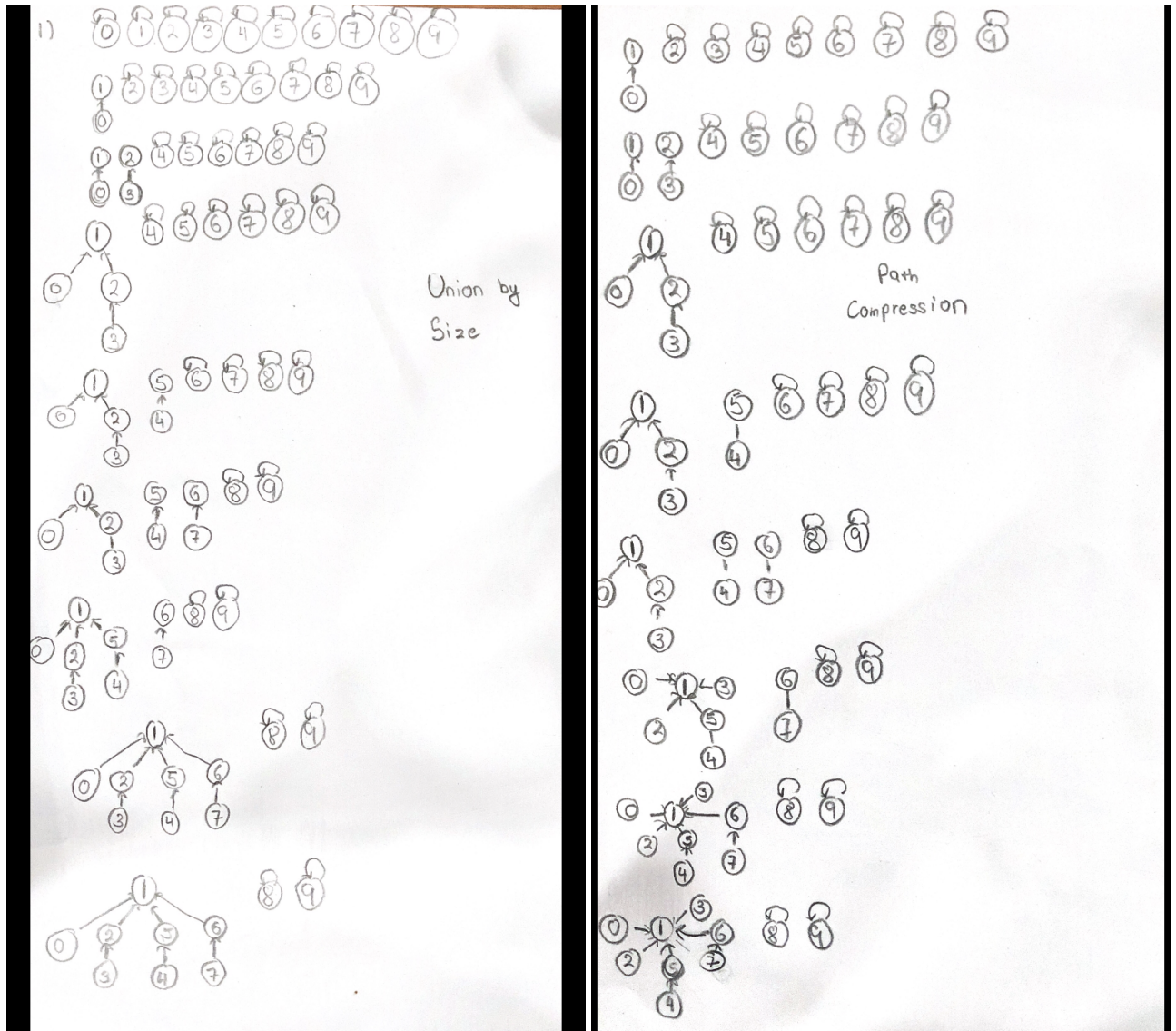
# ICCS200: Assignment 7

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The date

## 1: Union By Hand



## 2: Breadth-First Search Running Time

```
import java.util.Arrays;
import java.util.Set;
import java.util.TreeSet;

public class exercise2 {

    Set<Integer> nbrsExcluding(UndirectedGraph G, Set<Integer> vtxes, Set<Integer> excl) {
        Set<Integer> union = new TreeSet<>();
        for (Integer src : vtxes) {
            for (Integer dst : G.adj(src))
                if (!excl.contains(dst)) {
                    union.add(dst);
                }
        }
        return union; }

    Set<Integer> bfs(UndirectedGraph G, int s) {
        Set<Integer> frontier = new TreeSet<>(Arrays.asList(s));
        Set<Integer> visited = new TreeSet<>(Arrays.asList(s));
        while (!frontier.isEmpty()) {
            frontier = nbrsExcluding(G, frontier, visited);
            visited.addAll(frontier);
        }
        return visited; }

}
```

nbrsExcluding loop takes  $O(m+n\log n)$  as the cost of it is to walk using bfs and the  $\log n$  comes from the add operation. Since the most expensive call comes from frontier in bfs which takes running time not more than nbrsExcluding and visited.addAll takes only  $O(n\log n)$  therefore the code takes  $O(m+n\log n)$ .