

Please submit using Canvas by 11:59PM on Tuesday, July 5th, 2019

1. This is an individual assignment. You should do your own work. Any evidence of copying will result in a zero grade and additional penalties/actions.
2. Think carefully; formulate your answers, and then write them out concisely using English, logic, mathematics and pseudocode (no programming language syntax).
3. Type your final answers in this Word document.
4. Don't turn in handwritten answers with scribbling, cross-outs, erasures, etc. If an answer is unreadable, it will earn zero points. **Neatly and cleanly handwritten submissions are acceptable.**

$$A = \begin{bmatrix} & \\ & \end{bmatrix}$$

Draw the recursion tree of this algorithm for inputs $A=[10, 3, 9, 4, 8, 5, 7, 6]$, $p=1$, $r=8$, $k=2$. At each non-base case node show all of the following: (1) values of all parameters: input array A , p , r & k ; (2) A after

Partition. At each base case node show values of all parameters: input array A, p, r & k. Beside each downward arrow connecting a parent execution to a child recursive execution, show the value returned upwards by the child execution.

(b) (16 points). This algorithm has two base cases.

Explain what the first base case that the algorithm checks for is, in plain English:

List the steps that the algorithm will execute if the input happens to be this base case:

Complete the recurrence relation using actual constants:

$T(\text{first base case}) = \underline{\hspace{2cm}}$

Explain what the second base case that the algorithm checks for is, in plain English:

List the steps that the algorithm will execute if the input happens to be this base case:

Complete the recurrence relation using actual constants (assume complexity of Partition to be $20n$):

$T(\text{second base case}) = \underline{\hspace{2cm}}$

List the steps that the algorithm will execute if the input is not a base case:

Complete the recurrence relation using actual constants (assume complexity of Partition to be $20n$ and the worst case input size for the recursive call):

$T(n) = \underline{\hspace{2cm}}$

How will the above recurrence change if you instead assume the best case input size for the recursive call):

$T(n) = \underline{\hspace{2cm}}$

3. (10 points) Counting Sort

Show the B and C arrays after Counting Sort finishes on the array A [19, 6, 10, 7, 16, 17, 13, 14, 12, 9] if the input range is 0-19.

4. (5 points) Radix Sort

If Radix Sort is applied to the array of numbers [4567, 3210, 2345, 4321, 5678], show how these numbers will get rearranged after each of the four passes of the algorithm.

Consider the algorithm in the lecture slides. If $\text{length}(A)=15$ then list the range of input numbers that will go to each of the buckets $0 \dots 14$.

Bucket14:

Bucket($n-1$):

Assume a Disjoint Set data structure has initially 20 data items with each in its own disjoint set (one-node tree). Show the final result (only show the array P for parts a, b & c below; no need to draw the trees) of the following sequence of unions (the parameters of the unions specified in this question are data elements; so assume that the find operation without path compression is applied to the parameters to determine the sets to be merged): union(16,17), union(18,16), union(19,18), union(20,19), union(3,4), union(3,5), union(3,6), union(3,10), union(3,11), union(3,12), union(3,13), union(14,15), union(14,3), union(1,2), union(1,7), union(8,9), union(1,8), union(1,3), union(1,20) when the unions are:

[illegible]

[illegible][illegible][illegible]

7. (24 points) Binomial Queue

First show the Binomial Queue that results from merging the two BQs below. Then show the result of an Extract_Max operation on the merged BQ. There may be more than one correct answer.

