# **Computer Vision**

Dr. Syed Faisal Bukhari
Associate Professor
Department of Data Science
Faculty of Computing and Information Technology
University of the Punjab

#### **Textbooks**

Multiple View Geometry in Computer Vision, Hartley, R., and Zisserman

Richard Szeliski, Computer Vision: Algorithms and Applications, 2<sup>nd</sup> edition, 2022

#### Reference books

Readings for these lecture notes:

- Hartley, R., and Zisserman, A. Multiple View Geometry in Computer Vision, Cambridge University Press, 2004, Chapters 1-3.
- □ Forsyth, D., and Ponce, J. Computer Vision: A Modern Approach, Prentice-Hall, 2003, Chapter 2.

These notes contain material c Hartley and Zisserman (2004) and Forsyth and Ponce (2003).

#### References

These notes are based ☐ Dr. Matthew N. Dailey's course: AT70.20: Machine Vision for Robotics and HCI □ Dr. Sohaib Ahmad Khan CS436 / CS5310 Computer Vision Fundamentals at LUMS https://www.photographytalk.com/beginner-photography-tips/7204focal-length-and-field-of-view-explained-in-4-steps □https://ipvm.com/reports/testing-wide-vs-telephotofov#:~:text=Testing%20Wide%20vs%20Narrow%20FoV&text=The%20firs t%2C%20the%20'wide',of%20the%20distant%20parking%20lot. □http://rimstar.org/science electronics projects/pinhole camera.htm □https://www.lorextechnology.com/self-serve/guide-to-field-of-viewlens-types/R-sc2900041

## **Grading breakup**

- I. Midterm = 35 points
- II. Final term = 40 points
- III. Quizzes = 6 points (A total of 6 quizzes)
- **IV.** Group project = 15 points
  - a. Pitch your project idea = 2 points
  - b. Research paper presentation relevant to your project = 3 points
  - c. Project prototype and its presentation = 5 points
  - d. Research paper in IEEE conference template = 5 points
- V. OpenCV based on Python presentation = 2.5 points
- **VI.** Matlab presentation = 2.5 points

# Some top tier conferences of computer vision

- I. Proceedings of the IEEE International Conference on Computer Vision and Pattern Recognition (CVPR).
- II. Proceedings of the European Conference on Computer Vision (ECCV).
- III. Proceedings of the Asian Conference on Computer Vision (ACCV).
- IV. Proceedings of the International Conference on Robotics and Automation (ICRA).
- V. Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS).

#### Some well known Journals

- I. International Journal of Computer Vision (IJCV).
- II. IEEE Transactions on Pattern Analysis and Machine Intelligence (PAMI).
- III. Image and Vision Computing.
- IV. Pattern Recognition.
- V. Computer Vision and Image Understanding.
- VI. IEEE Transactions on Robotics.
- VII. Journal of Mathematical Imaging and Vision

# Why do we like to use vectors or column vectors in particular?

oA linear transformation between vector spaces is represented using matrices, allowing us to express the transformation between one vector space and another as matrix multiplication.

#### **Example:**

$$\vec{x}' = A\vec{x}$$

OHere A is a matrix, and  $\vec{x}$  is a **2D vector**. If we are considering a **2D transformation**, then  $\vec{x}'$  will also be a **2D vector**.

OWe can have transformations between different vector spaces with varying dimensions.

# How you know the size of $\vec{x}$ ?

$$\vec{x}' = A\vec{x}$$
 e.g.,  $\vec{x}'_{2\times 1} = A_{2\times 2}\vec{x}_{2\times 1}$ 

olf A is 2 × 2, then we are transforming from 2D space to another 2D space.

$$A: \mathbb{R}^2 \mapsto \mathbb{R}^2$$

- oThe number of columns of A must be equal to the number of rows of  $\vec{x}$ .
- The number of rows in A must be equal to number of rows in  $\vec{x}'$ .
- oWe will later discuss the **types of transformations** that can be modeled by a **2**×**2** matrix as **linear multiplications** between this matrix and a two-dimensional vector.

# 2D projective geometry

#### The 2D projective plane: lines in $\mathbb{R}^2$

OA line in the plane is typically represented by an equation such as

$$ax + by + c = 0.$$

oThe parameters a, b, and c determine different lines.

This means we can represent a line in  $\mathbb{R}^2$  as the vector  $(a, b, c)^T$ .

## Lines in the plane

#### Slope-y intercept form or slope intercept form:

```
y = mx + c
```

- oWe interpret this equation as follows: x represents the x-coordinate of a point, and y represents the y-coordinate. Therefore, we have a 2D point, which defines a relationship between x and y
- OA line in a plane represents a linear relationship between x and y

m is called the slope of a line and c is called the y-intercept.

## Slope of a line

For example

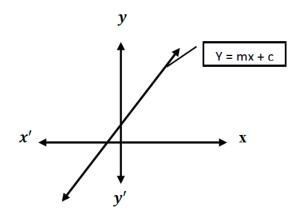
$$y = 3x + 2$$

Here 
$$\mathbf{m} = \frac{3}{1}$$
 and  $\mathbf{c} = \mathbf{2}$ 

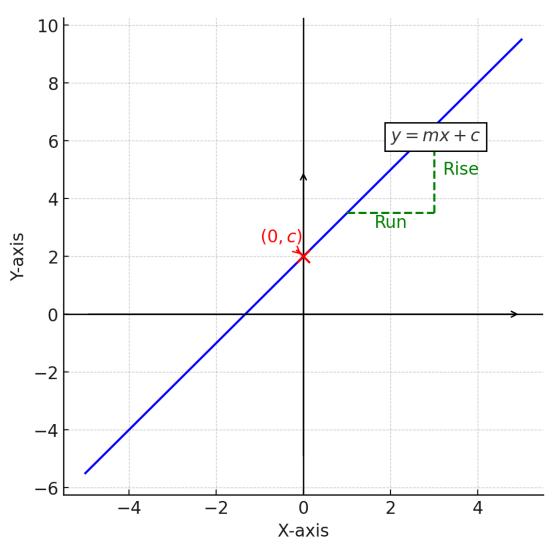
How do we interpret the **slope**? It is the **rise over the run**. The **rise** represents how far you move in **the y-direction**, while the **run** represents how far you move in **the x-direction**.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{rise}{run} = \frac{3}{1}$$

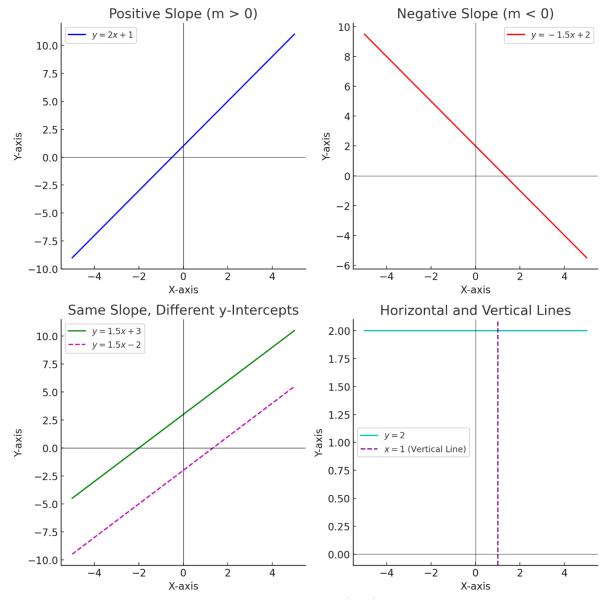
c = 2 means that the line intercepts the y-axis at 2.



# Slope-Intercept Form: A Graphical Illustration



# Slope-y intercept form



# What's wrong with the slopeintercept form of a line?

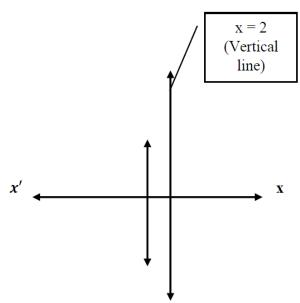
□Vertical lines cannot be represented in slope-intercept form because they have an infinite slope.

☐ This means we have a **rise** of **some amount** divided by a **run of zero**, resulting in an **infinite slope**.

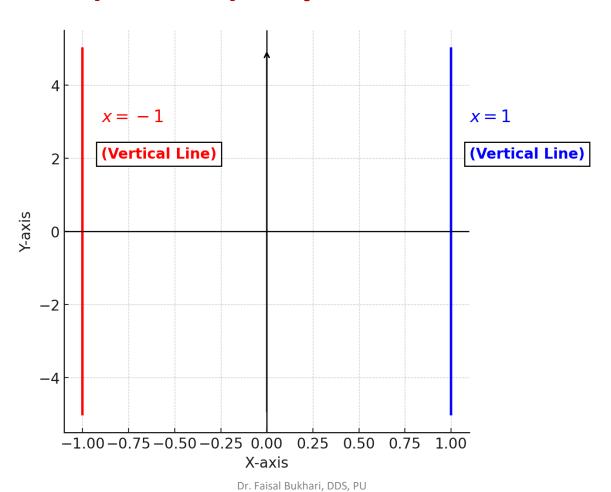
#### For example

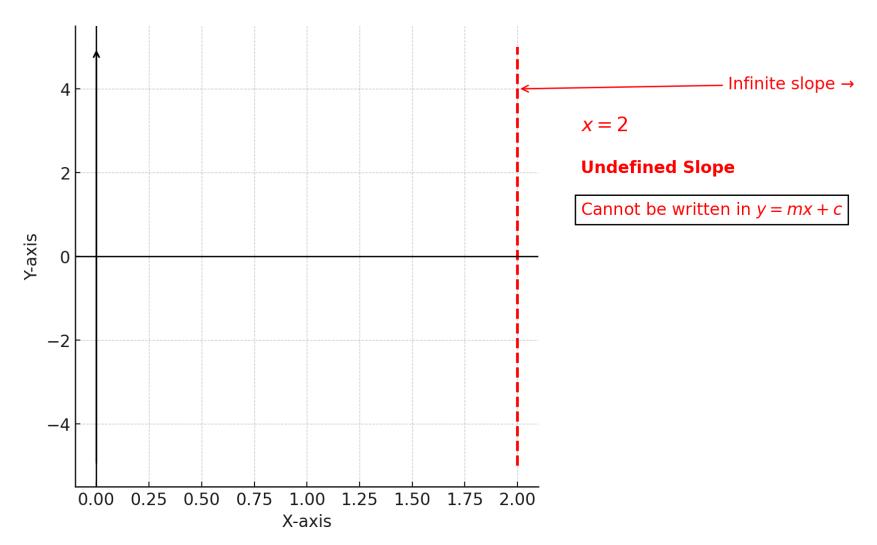
$$x = 2$$

$$m = \frac{rise}{m} = \frac{2}{a} = \infty$$



#### Vertical lines cannot be represented in slopeintercept form y = mx + c because they have an undefined (infinite) slope





## General equation of a line

$$ax + by + c = 0$$

where a, b, and c are arbitrary scalars. Now, we can represent a vertical line using the general equation of a line.

#### For example:

$$x = 2$$
  
 $\Rightarrow 1.x + 0.y - 2 = 0$   
 $a = 1, b = 0 \text{ and } c = -2$ 

So, ax + by + c = 0 can model any line in the plane.

## Parametric vector from of a line [1]

We can write parameters a, b, and c of a general equation of a line in the vector form as

$$\begin{bmatrix} a \\ b \\ c \end{bmatrix}$$
 or  $(\mathbf{a}, \mathbf{b}, \mathbf{c})^T$ 

#### For example:

$$mx - y + b = 0$$

If we divide above equation by m, then we still have the same line.

$$x - (1/m) y + b/m = 0$$
  
a = 1, b = -1/m, and c = b/m

Where a, b, and c are valid scalars.

$$\begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 1 \\ -1/m \\ b/m \end{bmatrix}$$

### Parametric vector from of a line [2]

$$y = 2x + 3$$

We can represent the **slope-intercept form** using the **parametric vector form** 

$$2x - y + 3 = 0$$
  
a = 2, b = -1, and c = 3

$$\begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix} \text{ or } (\mathbf{a}, \mathbf{b}, \mathbf{c})^T = (2, -1, 3)^T$$

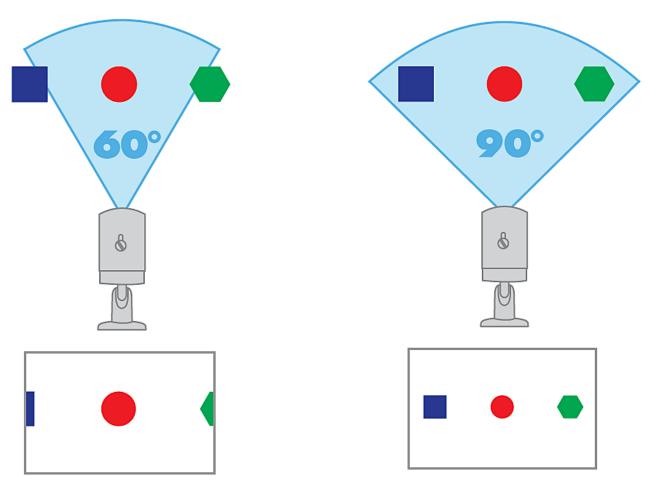
## What is Field of View (FOV)?

□The **field of view** of a security camera, also called the **viewing angle**, is the **area that the camera can see**.

Angular extent to which camera can see is FOV.

- □On a specification sheet, you will see the **field of view** measured in degrees.
- ☐ Think of the field of view as the angle between the two horizontal edges of the camera image.

## What is Field of View (FOV)?



The 60° field of view captures some The 90° field of view captures all of of the objects but in greater detail. The objects but in lesser detail

# What is Field of View (FOV)?

- □ As you can see in the example images in the previous slides, the camera with 90° field of view captures all 3 objects in the scene, though each object takes up a small part of the camera image.
- ☐ The camera with 60° field of view captures some of the objects but in greater detail.
- ☐ Remember, a wider field of view isn't always better!

# Wide-angle Lens



# Wide-angle lenses

□Smaller lenses are known as wide-angle lenses, which produce a greater field of view than cameras with a larger lens. They capture a large area, though objects will appear smaller within the camera image. Wide-angle lenses are designed for monitoring large areas, such as:









**Foyers** 

**Warehouses** 

**Back or Front Yards** 

**Parking Lots** 

# **Narrow-angle Lens**

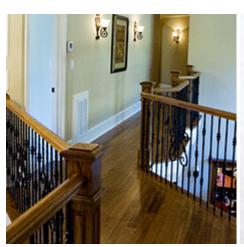


### Narrow-angle Lens

□ Larger lenses, or narrow-angle lenses, have a smaller field of view. They capture a limited area, but objects will appear larger and more detailed within the camera image. Narrow-angle lenses are designed for monitoring a specific target, such as:









**Cash Registers** 

Doorways and Entrances

**Hallways** 

**Objects of Value** 

#### How is lens size related to field of view?

- ☐ The size of the camera lens, or **focal length**, is the main factor that determines **the field of view**.
- ☐ The example images shown in the next slides compare multiple focal lengths and the resulting fields of view:

#### How is lens size related to field of view?



Focal length: 3.6mm Field of view: 78°



Focal length: 5.1mm Field of view: 58°



Focal length: 6mm Field of view: 51°



Focal length: 9mm Field of view: 39°

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#### **Lens Field of View**

- oJust as our eyes serve as windows to the outer world, lenses are the eyes of a camera, allowing it to capture what we see.
- oSimilarly, just as each person has different eyes with varying capabilities, lenses also differ in their characteristics. This means that what one person perceives might not appear the same to another—the same principle applies to camera lenses.
- oSome lenses have a **short focal length**, providing a **wide angle of view**, while others have a **long focal length**, resulting in a **narrow angle of view**.

## **Key Points on Field of View**

#### 1. Focal Length vs. Field of View:

- oFocal length determines how long a lens is.
- oField of view (FoV) defines how much of the scene a lens captures.

#### 2. Understanding Field of View:

- FoV tells us how much of a scene is visible through a lens.
- More useful than focal length alone.

## **Key Points on Field of View**

#### 3. Factors Affecting Field of View:

#### FoV changes based on:

- oFocal length of the lens (shorter = wider, longer = narrower).
- oSize of the camera sensor (larger sensor = wider FoV).

#### 4. Challenges in Measuring Field of View:

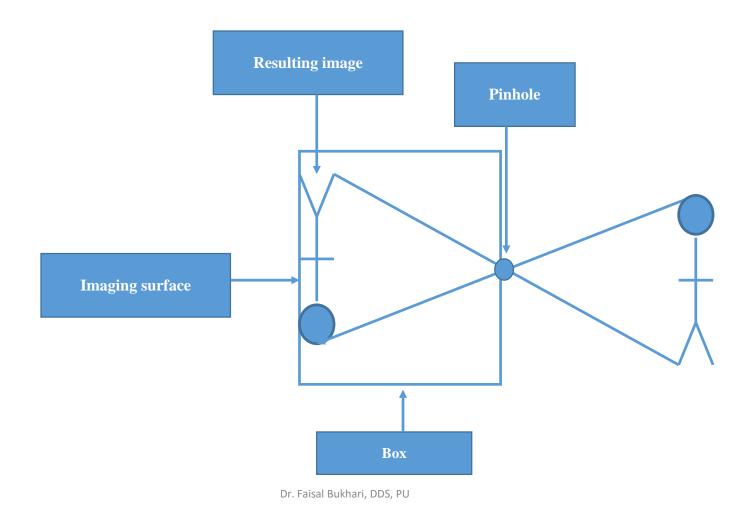
- oFoV varies with sensor size.
- OManufacturers often specify lenses by focal length rather than FoV.



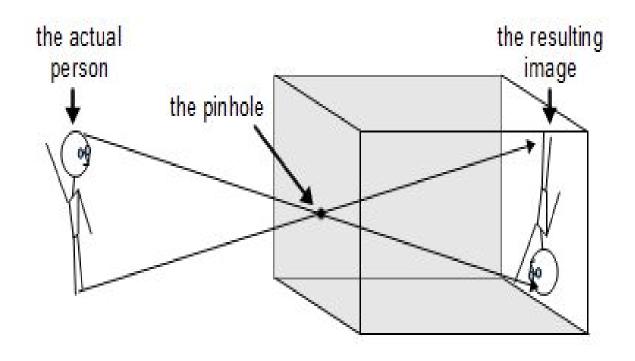
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#### Pinhole model

☐ The classical model of camera is called a pinhole model.



## Pinhole model



#### Pinhole model

OIn the pinhole model of a camera, what happens?

•We have an infinite set of small points emitting light into a box.

oPoints in a scene reflect light.

oSome of these light rays pass through the pinhole in the box

The image of the scene is then reconstructed on the back of the box.

### How to build a pinhole camera?

oSimply take a box, poke a small hole in it, and point it in any direction. If you could open the box and look inside, you would see an image of the scene projected onto the back of the box.

oHowever, opening the box lets in too much light, which can ruin the image. This is how a pinhole camera works.

OIn a pinhole camera, the image is **inverted**.

# How to build a pinhole camera? (cont.)

- oLight reflected from the top of a person's head passes through the pinhole and appears lower on the back of the box.
- oSimilarly, light reflecting from the **person's foot** passes through the pinhole and appears **higher** on the back of the box.
- OAs a result, the **image of the scene appears upside down** on the back of the box.

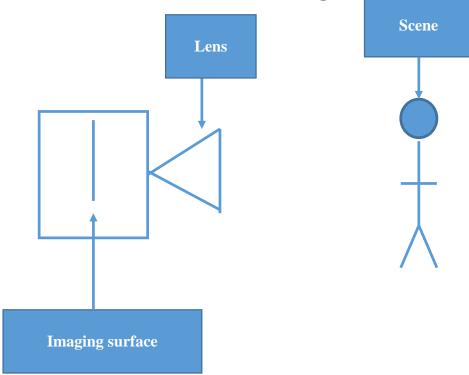
#### Camera model

oA modern camera consists of a lens and an imaging surface.

OWhen we examine a camera, we see a lens on the front, and inside, there is an image surface where the scene is captured.

olf there is a scene, the camera's role is to project the scene

onto the **image surface** to form an image



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# Resemblance Between a Pinhole and a Modern Camera [1]

oThe pinhole camera serves as the fundamental model, and modern cameras are designed to emulate its principles. But why?

OSince this principle applies to real cameras, they share similarities with the pinhole model.

oHowever, modern cameras use a lens to focus light onto a specific point, improving image clarity and brightness.

## Resemblance Between a Pinhole and a Modern Camera [2]

How Light is Processed in a Camera

The lens collects light and focuses it on a focal point.

The light is then spread out and captured by a sensor array or an imaging surface.

### Resemblance Between a Pinhole and a Modern Camera [3]

#### Camera Sensors

oThe imaging surface could be a CCD (Charge-Coupled Device) or a CMOS (Complementary Metal-Oxide-Semiconductor) sensor.

OA variety of semiconductor technologies are used to construct these cameras.

## Resemblance in a pinhole and a modern camera [4]

- How Light is Captured in a Camera
- The lens collects light and focuses it on a focal point.
- oThis light is then captured by the sensor array, which is structured as a 2D grid of picture elements (pixels).
- Similarity to the Pinhole Model
- oThe pinhole model closely resembles how modern cameras function today.

Note: "Lens" is singular. "Lenses" is plural. "Lense" does not exist as an accepted word in English

## Why do we use lens instead of pinhole? [1]

olf the pinhole is not an infinitesimally small point, some scattering of light may occur as it passes through the hole.

The smaller the hole, the less light that passes through, resulting in a dimmer image.

# Why do we use lens instead of pinhole? [2]

- The main role of a lens in computer vision or optics is to:
  - Collect more light
  - Focus light more accurately on a particular point
  - Produce sharper images with better contrast
- Thus, achieving high contrast is a key advantage of using a lens over a pinhole.

#### Why do we use lens instead of pinhole? [3]

In fact, from a machine vision point of view, we're going to see that the pinhole model is mathematically attractive. However, building a perfect pinhole camera is physically impossible.

# Limitations of the Pinhole Model and the Use of Lenses [1]

- Why do we use cameras with lenses?
  - OWe aim to use high-quality lenses to improve image capture.
  - oWhen the field of view is narrow, the resulting image is mathematically similar to what we get from a pinhole camera.
- Challenges with a Wide Field of View:
  - olf the field of view is very wide, it becomes difficult to construct a proper pinhole image.
  - ODistortions may occur, which need corrections in real-world imaging.

# Limitations of the Pinhole Model and the Use of Lenses [2]

Limitations of the Pinhole Model:

oThe **pinhole model** does not perfectly represent how cameras function in the real world.

OHowever, it serves as a valuable mathematical tool for understanding imaging principles

#### 2D projective geometry

- □We talk out about 2D projective geometry, which is essentially the mathematics of this projections, i.e., the projections of world scene onto a 2D surface.
- ☐ The projective geometry is beneficial for the analysis of the images, as we see in the following lectures.

## Recall: Parametric vector from of a line [1]

We can write parameters a, b, and c of a **general equation** of a line in the **vector form** as

$$\begin{bmatrix} a \\ b \end{bmatrix}$$

#### For example:

$$2x - 3y + 5 = 0$$

If we divide above equation by 2, then we still have the same line.

$$x - (3/2) y + 5/2 = 0$$
  
a = 1, b = -3/2, and c = 5/2

These (a, b, and c) are perfectly legitimate scalars.

$$\begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 1 \\ -3/2 \\ 5/2 \end{bmatrix}$$

# Recall: Parametric vector from of a line [2]

$$y = -8x + 5$$

We can represent a **slope intercept** form in a parametric vector form

$$8x - y + 5 = 0$$

$$a = 8$$
,  $b = -1$ , and  $c = 5$ 

$$\begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 8 \\ -1 \\ 5 \end{bmatrix}$$

### Homogeneous Representation of a Line in 2D

How do we derive the vector form from the coefficient form?

1. 
$$ax + by + c = 0$$

2. 
$$\begin{bmatrix} a \\ b \\ c \end{bmatrix}$$
 .  $\begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = 0$  or  $(x, y, 1)$   $(a, b, c)^T = 0$ 

**Recall: Dot product** is the sum of the product of each element.

In projective geometry, we can express a line equation using the

dot product of the coefficient vector 
$$\begin{bmatrix} a \\ b \\ c \end{bmatrix}$$
 with this very special vector,  $\begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$  representing a point in homogeneous coordinates

## Homogeneous Representation of a Line in 2D

How do we derive the vector form from the coefficient form?

#### Mathematically, this can be written as:

$$(x, y, 1) (a, b, c)^T = 0$$

#### or equivalently, using matrix notation:

$$\begin{bmatrix} a & b & c \end{bmatrix}_{1\times3} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}_{3\times1} = 0$$

$$\Rightarrow$$
 ax + by + c = 0

This equation represents a **homogeneous line equation**, a key concept in projective geometry and computer vision.

Note: These are two different ways of saying the same thing.

### Homogeneous Objects in Mathematics

If we take the coefficient form of the equation of a line (ax + by + c = 0):

$$\begin{bmatrix} a \\ b \end{bmatrix}$$

and multiply it by any scalar k, we still have the same line:

$$egin{bmatrix} ka \ kb \ kc \end{bmatrix}$$

$$\begin{bmatrix} ka \\ kb \\ kc \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = 0$$
 remains unchanged, demonstrating that it is a homogeneous object.

### **Definition of Homogeneous Objects:**

OHomogeneous objects are mathematical entities that are determined only up to scale. This means that scaling them by a nonzero factor does not change their fundamental nature.

oIn this case, the vector  $(\mathbf{a}, \mathbf{b}, \mathbf{c})^T$  represents the same line as  $\mathbf{k}(\mathbf{a}, \mathbf{b}, \mathbf{c})^T$  for any nonzero constant  $\mathbf{k}$ .

### What are Homogeneous Coordinates?

- oIn projective geometry, we extend 2D coordinates to 3D for easier transformations.
- A point (x, y) in Cartesian coordinates is represented as (x, y, 1) in homogeneous coordinates.
- oThis allows for uniform representation of transformations like scaling and translation.