CENG 3549 – Functional Programming User-Defined Types & Trees & Input and Output

Burak Ekici

October 13, 2022

Outline

Intermediate Wrap-Up

- 1 Intermediate Wrap-Up
- 2 User-Defined Types

Functions You Need to Know

000000

- infix operators and special syntax
 - (<=), (<), (==), (>=), (>), (||), (-), (,), (:), (/=), (.), (*), (&&), (+), (++), [], [m..n]
- other Prelude functions

abs, compare, concat, const, div, drop, error, even, filter, foldr, foldr1, fromInteger, fst, head, init, last, length, lines, map, max, min, mod, negate, not, null, product, putStr, putStrLn, read, replicate, reverse, show, showList, showsPrec, signum, snd. splitAt, sum, tail, take, unlines, unwords, words, zip, zipWith

- other Prelude constants False, otherwise, True
- other functions Data.Char.isDigit, System.Environment.getArgs

000000

anonymous functions / functions without names

 $(\x -> 2 * x)$ -- an anonymous function for doubling

anonymous functions / functions without names

$$(\x -> 2 * x)$$
 -- an anonymous function for doubling

$$(+) = (\langle x y -> x + y \rangle)$$

• infix operators and sections

$$x \cdot f \cdot y = f \times y$$

 $(a >) = (\langle x - \rangle a > x)$

$$(> b) = (\x -> x > b)$$

infix to prefix

prefix to infix argument smaller than a?

argument greater than b?

anonymous functions / functions without names

$$(\x -> 2 * x)$$
 -- an anonymous function for doubling

$$(+) = (\x y -> x + y)$$

$$x \cdot f \cdot y = f \times y$$

· infix operators and sections

(a >) =
$$(\x -> a > x)$$

(> b) = $(\x -> x > b)$

infix to prefix prefix to infix

argument smaller than a? argument greater than b?

patterns and guards

headIfPositive
$$xs = case xs of$$

anonymous functions / functions without names

 $(\x -> 2 * x)$ -- an anonymous function for doubling

$$(+) = (\langle x y -> x + y \rangle)$$

$$x \cdot f \cdot y = f \times y$$

infix to prefix prefix to infix

infix operators and sections

(a >) =
$$(\x -> a > x)$$

(> b) = $(\x -> x > b)$

argument smaller than a? argument greater than b?

patterns and guards

```
headIfPositive xs = case \times s of x:= |x>0 -> x
```

list comprehensions

```
filter p xs == [x \mid x <-xs, p x]

map f xs == [f x \mid x <-xs]

concat (map f xs) == [y \mid x <-xs, y <-f x]

concat $ map (\x -> map ((,)x) ys) xs == <math>[(x, y) \mid x <-xs, y <-ys]
```

Trees

Intermediate Wrap-Up

000000

• type signatures – annotate functions by types

```
range :: Int -> Int -> [Int]
range m \mid m > n = []
| otherwise = m : range (m + 1) n
```

Trees

Types and Type Classes

type signatures – annotate functions by types

• type synonyms – mnemonic names for types

```
type Height = Int
type Width = Int
```

Types and Type Classes

type signatures – annotate functions by types

• type synonyms – mnemonic names for types

```
type Height = Int
type Width = Int
```

 type classes and class constraints – for every function f, specific to class C, type inference adds a C-constraint to type

Trees

Types and Type Classes

type signatures – annotate functions by types

• type synonyms – mnemonic names for types

```
type Height = Int
type Width = Int
```

 type classes and class constraints – for every function f, specific to class C, type inference adds a C-constraint to type

Example

· without type signature, we get

```
ghci> :t range range :: (Ord a, Num a) \Rightarrow a -> a -> [a]
```

- m > n, hence m and n of class 0rd and m and n of same type
- m + 1. hence m of class Num
- m and n of same type, hence n of class Num

Equational Reasoning

Intermediate Wrap-Up

000000

- a function definition in Haskell is a (set of conditional) equation(s)
- if conditions are met, we may "replace equals by equals"
- in this way we may evaluate function calls by applying equations stepwise, until we reach final result

Equational Reasoning

- a function definition in Haskell is a (set of conditional) equation(s)
- if conditions are met, we may "replace equals by equals"
- in this way we may evaluate function calls by applying equations stepwise, until we reach final result

Kinds of Conditions

- "if b then t else e" is t, when b is true; and e, otherwise
- "case e of { $p_1 \rightarrow e_1$; ...; $p_n \rightarrow e_n$ }" is e_i , if e first matches p_i

Equational Reasoning

000000

- a function definition in Haskell is a (set of conditional) equation(s)
- if conditions are met, we may "replace equals by equals"
- in this way we may evaluate function calls by applying equations stepwise, until we reach final result

Kinds of Conditions

- "if b then t else e" is t, when b is true; and e, otherwise
- "case e of $\{p_1 \rightarrow e_1; \dots; p_n \rightarrow e_n\}$ " is e_i , if e first matches p_i

Primitive Operations

- for primitive operations (like (+), (*), ...), we assume predefined equations
- e.g., 1 + 2 = 3, 0 * 10 = 0, ...

definition

Intermediate Wrap-Up

$$zip (x:xs) (y:ys) = (x, y) : zip xs ys$$

 $zip _ = []$

definition

Intermediate Wrap-Up

$$zip (x:xs) (y:ys) = (x, y) : zip xs ys$$

 $zip _ = []$

• evaluate zip [1,2,3] ['a','b']

```
    definition

 zip (x:xs) (y:ys) = (x, y) : zip xs ys
 zip = = []
```

- evaluate zip [1,2,3] ['a','b']
- definition

Intermediate Wrap-Up

00000

```
factorial n \mid n \le 1 = 1
            otherwise = n * factorial (n - 1)
```

```
    definition

 zip (x:xs) (y:ys) = (x, y) : zip xs ys
 zip = []
• evaluate zip [1,2,3] ['a','b']
```

definition

00000

```
factorial n \mid n \le 1 = 1
            otherwise = n * factorial (n - 1)
```

evaluate factorial 3

```
    definition

 zip (x:xs) (y:ys) = (x, y) : zip xs ys
 zip = []
```

- evaluate zip [1,2,3] ['a','b']
- definition

```
factorial n \mid n \le 1 = 1
            otherwise = n * factorial (n - 1)
```

- evaluate factorial 3
- definition head xs = case xs of x:_ -> x

Trees

Examples (equational reasoning)

```
• definition

zip (x:xs) (y:ys) = (x, y) : zip xs ys

zip _ _ = []
```

- evaluate zip [1,2,3] ['a','b']
- definition

```
factorial n \mid n \le 1 = 1
| otherwise = n * factorial (n - 1)
```

- evaluate factorial 3
- definition head xs = case xs of x:_ -> x
- evaluate head "ab"

Trees

Intermediate Wrap-Up

00000

```
    definition

  zip (x:xs) (y:ys) = (x, y) : zip xs ys
  zip = []
• evaluate zip [1,2,3] ['a','b']

    definition

  factorial n \mid n \le 1 = 1
               otherwise = n * factorial (n - 1)

    evaluate factorial 3

    definition head xs = case xs of x:_ -> x

    evaluate head "ab"

    definitions

  null xs = case xs of { [] -> True; _ -> False }
  tail xs = case xs of _:vs -> vs
  prod xs = if null xs then 1
            else head xs * prod (tail xs)
```

00000

```
    definition

  zip (x:xs) (y:ys) = (x, y) : zip xs ys
  zip = []

    evaluate zip [1,2,3] ['a','b']

    definition

  factorial n \mid n \le 1 = 1
                otherwise = n * factorial (n - 1)

    evaluate factorial 3

    definition head xs = case xs of x:_ -> x

    evaluate head "ab"

    definitions

  null xs = case xs of { [] -> True; _ -> False }
  tail xs = case xs of _:vs -> vs
  prod xs = if null xs then 1
            else head xs * prod (tail xs)
• evaluate prod [5,6]
```

Outline

- 1 Intermediate Wrap-Up
- 2 User-Defined Types
- 3 Trees
- 4 Input and Output

new types are introduced by

$$data T \alpha_1 \cdots \alpha_n = C_1 \tau_{11} \cdots \tau_{1m_1}$$

$$\vdots$$

$$C_k \tau_{k1} \cdots \tau_{km_k}$$

new types are introduced by

$$data T \alpha_1 \cdots \alpha_n = C_1 \tau_{11} \cdots \tau_{1m_1}$$

$$\vdots$$

$$C_k \tau_{k1} \cdots \tau_{km_k}$$

• where T is name of new type (constructor) –starting with capital letter– taking n type parameters α_1 to α_n

new types are introduced by

$$data T \alpha_1 \cdots \alpha_n = C_1 \tau_{11} \cdots \tau_{1m_1}$$

$$\vdots$$

$$C_k \tau_{k1} \cdots \tau_{km_k}$$

- where T is name of new type (constructor) –starting with capital letter– taking n type parameters α_1 to α_n
- and C_i is name of *i*th (data) constructor, taking m_i arguments of types τ_{i1} to τ_{im_i} (with type variables among α_1 to α_n)

new types are introduced by

$$data T \alpha_1 \cdots \alpha_n = C_1 \tau_{11} \cdots \tau_{1m_1}$$

$$\vdots$$

$$C_k \tau_{k1} \cdots \tau_{km_k}$$

- where T is name of new type (constructor) –starting with capital letter– taking n type parameters α_1 to α_n
- and C_i is name of ith (data) constructor, taking m_i arguments of types τ_{i1} to τ_{im_i} (with type variables among α_1 to α_n)

Examples

- data Bool = False | True
- data List a = Nil | Cons a (List a)
- data Pair a b = Pair a b

new types are introduced by

$$data T \alpha_1 \cdots \alpha_n = C_1 \tau_{11} \cdots \tau_{1m_1}$$

$$\vdots$$

$$C_k \tau_{k1} \cdots \tau_{km_k}$$

- where T is name of new type (constructor) –starting with capital letter– taking n type parameters α_1 to α_n
- and C_i is name of ith (data) constructor, taking m_i arguments of types τ_{i1} to τ_{im_i} (with type variables among α_1 to α_n)

Examples

- data Bool = False | True
- data List a = Nil | Cons a (List a)
- data Pair a b = Pair a b

constructors and type names live in different name spaces

Automatically Deriving Type Class Instances

- · for some type classes it is possible to automatically derive instances for algebraic data types
- e.g.,
 data List a = Nil | Cons a (List a)
 deriving (Eq. Show, Read)
- now, we are able to use (==), show, and read for Lists

• for some type classes it is possible to automatically derive instances for algebraic data types

Trees

- e.g.,
 data List a = Nil | Cons a (List a)
 deriving (Eq. Show, Read)
- now, we are able to use (==), show, and read for Lists

Examples

```
ghci> Nil == Cons 1 Nil
False
ghci> show (Cons 1 (Cons 2 Nil))
"Cons_1_(Cons_2_Nil)"
ghci> read it :: List Int
Cons 1 (Cons 2 Nil)
```

Outline

- 1 Intermediate Wrap-Up
- 2 User-Defined Types
- 3 Trees
- 4 Input and Output

Trees

000000

Intermediate Wrap-Up

• (rooted) tree *T* = (*N*, *E*)

Intermediate Wrap-Up

- (rooted) tree T = (N, E)
- with set of nodes/vertices N

Intermediate Wrap-Up

- (rooted) tree T = (N, E)
- with set of nodes/vertices N
- and set of edges $E \subseteq N \times N$

- (rooted) tree T = (N, E)
- with set of nodes/vertices N
- and set of edges $E \subseteq N \times N$
- unique root of T ($root(T) \in N$) without predecessor

- (rooted) tree T = (N, E)
- with set of nodes/vertices N
- and set of edges $E \subseteq N \times N$
- unique root of T ($root(T) \in N$) without predecessor
- all other nodes have exactly one predecessor

Definition (tree)

- (rooted) tree T = (N, E)
- with set of nodes/vertices N
- and set of edges $E \subseteq N \times N$
- unique root of T ($root(T) \in N$) without predecessor
- all other nodes have exactly one predecessor

Exampl

- N = {A, B, C, D, E, F, G}
- $E = \{(A, B), (A, C), (A, E), (C, D), (E, F), (E, G)\}$
- root(T) = A



Trees in Haskell

- possible type for trees with arbitrary nodes
 data Tree a = Empty | Node a [Tree a]
- a tree is either empty (0 nodes) or there is at least one node with content of type a and an arbitrary number of successor trees



Binary Trees

- restrict number of successors (maximum 2)
- type
 data BTree a = Empty | Node a (BTree a) (BTree a)
 deriving (Eq., Show, Read)

Trees

000000

Binary Trees

- restrict number of successors (maximum 2)
- type
 data BTree a = Empty | Node a (BTree a) (BTree a)
 deriving (Eq. Show, Read)

Functions on Binary Trees

• size – number of nodes

```
size :: BTree a -> Integer
size Empty = 0
size (Node _ l r) = size l + size r + 1
```

Trees

- restrict number of successors (maximum 2)
- type

```
data BTree a = Empty | Node a (BTree a) (BTree a)
deriving (Eq. Show, Read)
```

Functions on Binary Trees

• size - number of nodes

```
size :: BTree a -> Integer
size Empty = 0
size (Node _ l r) = size l + size r + 1
```

• height - length of longest path from root to some leaf

```
height :: BTree a \rightarrow Integer
height Empty = 0
height (Node l r) = max (height l) (height r) + 1
```

Creating Trees from Lists

the easy way

Creating Trees from Lists

```
    the easy way
```

```
fromList [] = Empty
fromList (x:xs) = Node x Empty (fromList xs)
```

the balanced way

Creating Trees from Lists

```
    the easy way

  fromList [] = Empty
  fromList (x:xs) = Node x Empty (fromList xs)

    the balanced way

  make [] = Empty
  make xs = Node z (make ys) (make zs)
    where
                 = length xs `div ` 2
      (vs. z:zs) = splitAt m xs

    the orderly way

  searchTree = foldr insert Empty
    where
      insert x Empty = Node x Empty Empty
      insert x (Node v l r)
         x < y = Node y (insert x l) r
         otherwise = Node y l (insert x r)
```

Transforming Trees into Lists

flatten Empty = [] flatten (Node \times l r) = flatten l \leftrightarrow [\times] \leftrightarrow flatten r

Example (a sorting algorithm for lists)

sort = flatten . searchTree

Outline

- 1 Intermediate Wrap-Up
- 2 User-Defined Types
- 3 Trees
- 4 Input and Output

Example

```
• write the file welcomeIO.hs
main = do
  putStrLn "Greetings! What's your name?"
  name <- getLine
  putStrLn (
    "Welcome to Haskell's IO, " ++ name ++ "!")</pre>
```

- compile it with GHC via
- and run it

Example

• write the file welcomeIO.hs

```
main = do
  putStrLn "Greetings! What's your name?"
  name <- getLine
  putStrLn (
   "Welcome to Haskell's IO, " ++ name ++ "!")</pre>
```

- compile it with GHC via
- and run it

Remark

- putStrLn prints string followed by newline
- getLine reads line from standard input
- new syntax: do and <-

Trees

IO and the Type System

consider

ghci> :load welcomeIO.hs
ghci> :t putStrLn
putStrLn :: String -> IO ()
ghci> :t getLine
getLine :: IO String
ghci> :t main
main :: IO ()

Trees

IO and the Type System

consider

```
ghci> :load welcomeIO.hs
ghci> :t putStrLn
putStrLn :: String -> IO ()
ghci> :t getLine
getLine :: IO String
ghci> :t main
main :: IO ()
```

• IO a is type of IO actions delivering results of type a (in addition to their IO operations)

IO and the Type System

consider

```
ghci> :load welcomeIO.hs
ghci> :t putStrLn
putStrLn :: String -> IO ()
ghci> :t getLine
getLine :: IO String
ghci> :t main
main :: IO ()
```

• IO a is type of IO actions delivering results of type a (in addition to their IO operations)

Example:

• String -> I0 () - after supplying a string, we obtain an IO action (in case of putStrLn, "printing")

Trees

- IO () just IO (in case of main, run our program)
- IO String do some IO and deliver a string (in case of getLine, user-input)

IO actions (everything of type IO a) are just descriptions of what should be done; nothing is actually done at time of specification

- IO actions (everything of type IO a) are just descriptions of what should be done; nothing is actually done at time of specification
- inside IO actions, order is important; IO actions are executed in order of appearance (once execution starts); result of sequence of IO actions is result of last action

- IO actions (everything of type IO a) are just descriptions of what should be done; nothing is actually done at time of specification
- inside IO actions, order is important; IO actions are executed in order of appearance (once execution starts); result of sequence of IO actions is result of last action
- inside IO actions, x <- action (where action :: IO a) may be used to bind result of action (which has type a) to name x (but seriously, this is actually only done, once execution starts)

- IO actions (everything of type IO a) are just descriptions of what should be done; nothing is actually done at time of specification
- inside IO actions, order is important; IO actions are executed in order of appearance (once execution starts); result of sequence of IO actions is result of last action
- inside IO actions, x <- action (where action :: IO a) may be used to bind result of action (which has type a) to name x (but seriously, this is actually only done, once execution starts)
- x <- a is not available outside IO actions

- IO actions (everything of type IO a) are just descriptions of what should be done; nothing is actually done at time of specification
- inside IO actions, order is important; IO actions are executed in order of appearance (once execution starts); result of sequence of IO actions is result of last action
- inside IO actions, x <- action (where action :: IO a) may be used to bind result of action (which has type a) to name x (but seriously, this is actually only done, once execution starts)
- x <- a is not available outside IO actions

Implications

- once we are inside an IO action, we cannot escape
- strict separation between purely functional code and IO
- when IO a does not appear inside type signature, we can be absolutely sure that no IO ("side-effect") is performed

Trees

Using Pure Code Inside IO Actions

```
oconsider program reply.hs
reply :: String -> String
reply name =
   "Pleased to meet you, " ++ name ++ ".\n" ++
   "Your name contains " ++ n ++ " characters."
   where
        n = show $ length name

main :: IO ()
main = do
   putStrLn "Greetings again. What's your name?"
   name <- getLine
   let niceReply = reply name
   putStrLn niceReply</pre>
```

Using Pure Code Inside IO Actions

```
oconsider program reply.hs
reply :: String -> String
reply name =
   "Pleased to meet you, " ++ name ++ ".\n" ++
   "Your name contains " ++ n ++ " characters."
   where
        n = show $ length name

main :: IO ()
main = do
   putStrLn "Greetings again. What's your name?"
   name <- getLine
   let niceReply = reply name
   putStrLn niceReply</pre>
```

• that is, we may use let x = e (there is no in here!) to bind result of pure expression e to name x

• return :: a -> I0 a - turn anything into an IO action

- return :: a -> I0 a turn anything into an IO action
- System.Environment.getArgs :: IO [String] get command line arguments

- return :: a -> IO a turn anything into an IO action
- System.Environment.getArgs :: IO [String] get command line arguments
- putChar :: Char -> IO () print character

- return :: a -> IO a turn anything into an IO action
- System.Environment.getArgs :: IO [String] get command line arguments
- putChar :: Char -> IO () print character
- putStr :: String -> IO () print string

- return :: a -> IO a turn anything into an IO action
- System.Environment.getArgs :: I0 [String] get command line arguments
- putChar :: Char -> IO () print character
- putStr :: String -> IO () print string
- putStrLn :: String -> IO () print string followed by newline

- return :: a -> IO a turn anything into an IO action
- System.Environment.getArgs :: IO [String] get command line arguments
- putChar :: Char -> IO () print character
- putStr :: String -> IO () print string
- putStrLn :: String -> IO () print string followed by newline
- getChar :: I0 Char read single character from stdin

- return :: a -> I0 a turn anything into an IO action
- System.Environment.getArgs :: IO [String] get command line arguments
- putChar :: Char -> IO () print character
- putStr :: String -> IO () print string
- putStrLn :: String -> IO () print string followed by newline
- getChar :: I0 Char read single character from stdin
- getLine :: I0 String read line (excluding newline)

- return :: a -> IO a turn anything into an IO action
- System.Environment.getArgs :: IO [String] get command line arguments
- putChar :: Char -> IO () print character
- putStr :: String -> IO () print string
- putStrLn :: String -> IO () print string followed by newline
- getChar :: I0 Char read single character from stdin
- getLine :: I0 String read line (excluding newline)
- interact :: (String -> String) -> IO () use function that gets input as string and produces output as string

- return :: a -> IO a turn anything into an IO action
- System.Environment.getArgs :: IO [String] get command line arguments
- putChar :: Char -> IO () print character
- putStr :: String -> IO () print string
- putStrLn :: String -> IO () print string followed by newline
- getChar :: I0 Char read single character from stdin
- getLine :: I0 String read line (excluding newline)
- interact :: (String -> String) -> IO () use function that gets input as string and produces output as string
- type FilePath = String

Intermediate Wrap-Up

- return :: a -> IO a turn anything into an IO action
- System.Environment.getArgs :: IO [String] get command line arguments
- putChar :: Char -> IO () print character
- putStr :: String -> IO () print string
- putStrLn :: String -> IO () print string followed by newline
- getChar :: I0 Char read single character from stdin
- getLine :: I0 String read line (excluding newline)
- interact :: (String -> String) -> IO () use function that gets input as string and produces output as string
- type FilePath = String
- readFile :: FilePath -> IO String read file content

Input and Output

Trees

- return :: a -> IO a turn anything into an IO action
- System.Environment.getArgs :: IO [String] get command line arguments
- putChar :: Char -> IO () print character
- putStr :: String -> IO () print string
- putStrLn :: String -> IO () print string followed by newline
- getChar :: I0 Char read single character from stdin
- getLine :: I0 String read line (excluding newline)
- interact :: (String -> String) -> IO () use function that gets input as string and produces output as string
- type FilePath = String
- readFile :: FilePath -> IO String read file content
- writeFile :: FilePath -> String -> IO ()

• return :: a -> I0 a - turn anything into an IO action

- recarring the decion
- System.Environment.getArgs :: IO [String] get command line arguments
- putChar :: Char -> IO () print character
- putStr :: String -> IO () print string
- putStrLn :: String -> IO () print string followed by newline
- getChar :: I0 Char read single character from stdin
- getLine :: I0 String read line (excluding newline)
- interact :: (String -> String) -> I0 () use function that gets input as string and produces output as string

Trees

- type FilePath = String
- readFile :: FilePath -> IO String read file content
- writeFile :: FilePath -> String -> IO ()
- appendFile :: FilePath -> String -> IO ()

Examples (imitating some GNU commands)

• cat.hs - print file contents

```
main = do
  [file] <- getArgs
  s <- readFile file
  putStr s</pre>
```

Examples (imitating some GNU commands)

• cat.hs - print file contents

```
main = do
  [file] <- getArgs
  s <- readFile file
  putStr s
```

wc.hs – count newlines/words/characters in input

```
count s = ns ++ " " ++ ws ++ " " ++ bs ++ "\n"
 where ns = show $ length $ lines s
       ws = show $ length $ words s
       bs = show $ length s
```

main = interact count

Trees

Examples (imitating some GNU commands)

```
    cat.hs – print file contents

  main = do
    [file] <- getArgs</pre>
    s <- readFile file
    putStr s

    wc.hs – count newlines/words/characters in input

  count s = ns ++ " " ++ ws ++ " " ++ bs ++ "\n"
    where ns = show $ length $ lines s
          ws = show $ length $ words s
          bs = show $ length s
  main = interact count
• uniq.hs – omit repeated lines of input
  main = interact (nub)
```

Examples (imitating some GNU commands)

```
    cat.hs – print file contents

  main = do
    [file] <- getArgs</pre>
    s <- readFile file
    putStr s
• wc.hs - count newlines/words/characters in input
  count s = ns ++ " " ++ ws ++ " " ++ bs ++ "\n"
    where ns = show $ length $ lines s
          ws = show $ length $ words s
          bs = show $ length s
  main = interact count
• uniq.hs – omit repeated lines of input
  main = interact (nub)
• sort.hs - sort input lines
  main = interact (sort)
```

Intermediate Wrap-Up

- getArgs :: IO [String] is in System.Environment
- nub :: Eq a ⇒ [a] -> [a] is in Data.List; eliminates duplicates
- sort :: Ord a ⇒ [a] -> [a] is in Data.List; sorts a list

Intermediate Wrap-Up

- getArgs :: IO [String] is in System.Environment
- nub :: Eq a ⇒ [a] -> [a] is in Data.List; eliminates duplicates
- sort :: Ord a ⇒ [a] -> [a] is in Data.List; sorts a list

- getArgs :: IO [String] is in System.Environment
- nub :: Eq a ⇒ [a] -> [a] is in Data.List; eliminates duplicates
- sort :: Ord a \Rightarrow [a] -> [a] is in Data.List; sorts a list

Examples (do some IO action for each argument)

- getArgs :: IO [String] is in System.Environment
- nub :: Eq a ⇒ [a] -> [a] is in Data.List; eliminates duplicates
- sort :: Ord a ⇒ [a] -> [a] is in Data.List; sorts a list

Examples (do some IO action for each argument)

Trees

Thanks! & Questions?