Al and Speech Homework #3

목표

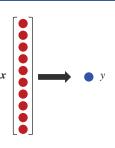
- Task = regression
- System = neural network
 - 가장 간단한 NN 구조 사용
- Supervised learning을 C로 구현
 - Backpropagation에 따라 gradient 계산

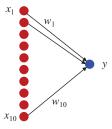
Problem Setting

- Training dataset
 - Input: 10-D vector of floating-point values
 - $-0.5 \le x_k \le 0.5$
 - Output : a floating-point value
 - Example : 10가지 개인 정보 → 신용도 결정
 - 1000 data of $(x_1, x_2, ..., x_{10}, y)$ from 1000 people



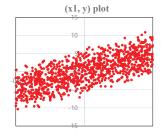
- (x₁, x₂, x₁₀) 와 y 사이의 관계 learning
- Neural network
 - No hidden layers
 - No bias
 - Linear activation function
 - $y = \sum_{k=1}^{10} w_k x_k$

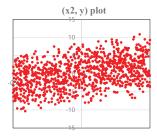


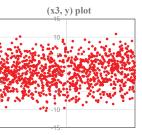


Training Data 특성

Scatter diagram







Different input-output dependency

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NN Training

- · Training by stochastic gradient descent(SGD) algorithm
 - Weight initialization
 - Uniform between -0.5 and 0.5
 - C code : w[k] = ((float)rand() / RAND_MAX) 0.5
 - Batch size = 1
 - 1 epoch → 1000번 update
 - $-\eta = 0.1$

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NN Training

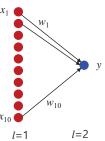
- Update process
 - Forward
 - 각 input x 에 대하여 output y = wx 계산
 - Output error
 - $C = \frac{1}{2}(y^* y)^2$
 - $\delta^{l=2} = \frac{\partial C}{\partial (z=y)} = y y^*$
 - Gradient

•
$$\frac{\partial C}{\partial W^2} = \delta^2 (\boldsymbol{a}^1)^T = (y - y^*) \boldsymbol{x}^T$$

•
$$\frac{\partial C}{\partial w_k} = x_k(y - y^*)$$

Update

•
$$w_k \leftarrow w_k - \eta \frac{\partial c}{\partial w_k} = w_k + \eta x_k (y^* - y)$$



$$\boldsymbol{z}^l = \boldsymbol{W}^l \boldsymbol{a}^{l-1} + \boldsymbol{b}^l$$

$$y = wx$$

File open read write (text file)

```
File open, read, write (text file)
    float input[DIM] = {0.0,}, target;
    fopen_s(&fin, "trainingDB.dat", "rt");
    fopen_s(&fo, "output.dat", "wt");

    for (k = 0; k < DIM; k++)
        fscanf(fin, "%f", input + k);

    for (k = 0; k < DIM; k++)
        fprintf(fo, "%10.7f", weight[k]);
    fprintf(fo, "\n");</li>
```

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C code

C code

• 전체 구조

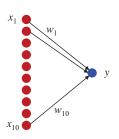
for (input index)

- Data read
- Output computation
- · Gradient computation
- · Weight update
- · Weight and cost write

Check-Point

- 500번째 x 에 대한 $C = \frac{1}{2}(y^* y)^2 \cong 0.00057 \cdots$
- 1000번째 x 에 대한 $C = \frac{1}{2}(y^* y)^2 \cong 0.0000012 \cdots$
- After 1000 updates, weight의 크기 순서

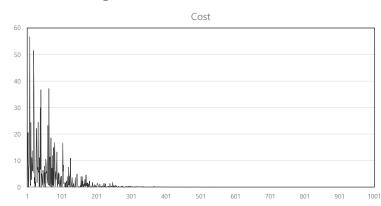
$$- w_1 > w_8 > w_2 > \dots > w_{10}$$



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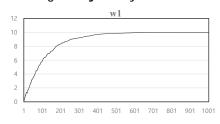
결과 분석

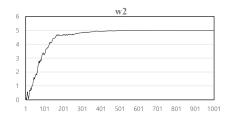
• 각 x 에 대한 $C = \frac{1}{2}(y^* - y)^2$

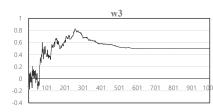


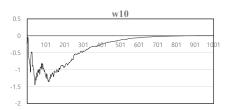
결과 분석

· Weight trajectory



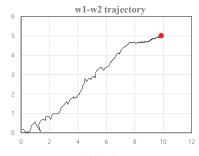


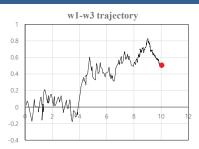


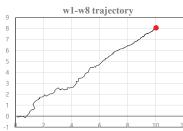


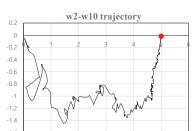
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결과 분석

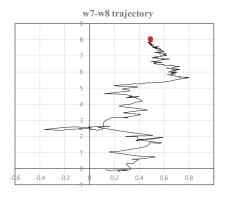


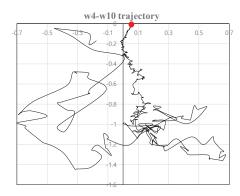






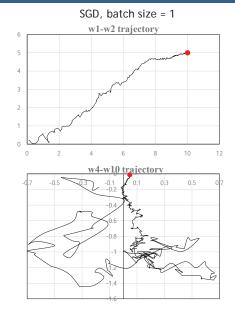
결과 분석

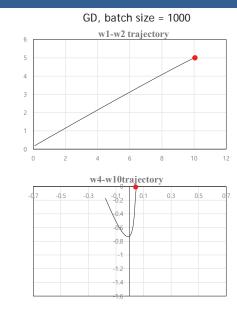




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결과 분석 : Batch Size





과제 제출

• Due: 5월 31일(월) 23:59 13주차

• File name : AI_Speech_HW3_이름_학번.hwp, docx, pdf

• 제출 내용

- C code

Learning output : weight, cost

- 다양한 실험 결과와 설명

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