Jawad Chowdhury (801135477) In [1]: import networkx as nx import numpy as np import matplotlib import matplotlib.pyplot as plt import matplotlib.gridspec as gridspec 1 Analyzing the Wikipedia voters network [9 points] In [2]: def get len reciprocated edges(G): C=0for e in G.edges: **if** (e[0] != e[1]) **and** (e[1], e[0]) **in** G.edges: return int(c/2) def get_len_out_degree(G, val_out_degree): out degree view = G.out degree() C = 0for elem in out degree view: if elem[1] == val_out_degree: C+=1return c def get_len_in_degree(G, val_in_degree): in degree view = G.in degree() c = 0for elem in degree view: if elem[1] == val in degree: c+=1return c def get_len_out_degree_gt_10(G): out_degree_view = G.out_degree() for elem in out_degree_view: **if** elem[1] > 10: c+=1return c def get_len_in_degree_lt_10(G): in_degree_view = G.in_degree() c = 0for elem in in_degree_view: **if** elem[1] < 10: c+=1return c # file_name = "test_1.txt" file_name = "Wiki-Vote.txt" dG = nx.read edgelist(file name, create using=nx.DiGraph) uG = dG.to_undirected() no_edges = dG.number_of_edges() no_edges_uG = uG.number_of_edges() a1 = dG.number of nodes() a2 = len(list(nx.selfloop_edges(dG))) $a3 = no_edges - a2$ a4 = no edges uG - a2a5 = get_len_reciprocated_edges(dG) a6 = get_len_out_degree(dG,0) a7 = get_len_in_degree(dG,0) a8 = get_len_out_degree_gt_10(dG) a9 = get_len_in_degree_lt_10(dG) print("The number of nodes in the network : ", a1) print("The number of nodes with a self-edge (self-loop) : ", a2) print("The number of directed edges in the network : ", a3) print ("The number of undirected edges in the network: ", a4) print("The number of reciprocated edges in the network : ", a5) print("The number of nodes of zero out-degree : ", a6) print("The number of nodes of zero in-degree : ", a7) print("The number of nodes with more than 10 outgoing edges: ", a8) print("The number of nodes with fewer than 10 incoming edges : ", a9) The number of nodes in the network: 7115 The number of nodes with a self-edge (self-loop) : 0 The number of directed edges in the network: 103689 The number of undirected edges in the network: 100762 The number of reciprocated edges in the network: 2927 The number of nodes of zero out-degree: 1005 The number of nodes of zero in-degree: 4734 The number of nodes with more than 10 outgoing edges: 1612 The number of nodes with fewer than 10 incoming edges: 5165 2 Further Analyzing the Wikipedia voters network [6 points] In [3]: list od = dG.out degree() list sod = sorted(list od, key=lambda tup: tup[1]) $min_x = list_sod[0][1]$ $max_x = list_sod[-1][1]$ $dict od = {}$ for elem in list_sod: if elem[1] not in dict_od.keys(): $dict_od[elem[1]] = 1$ else: $dict_od[elem[1]] += 1$ $list_x = []$ $list_y = []$ for k, v in dict od.items(): list_x.append(k) list_y.append(v) fig1 = plt.figure(constrained_layout=True) spec1 = gridspec.GridSpec(ncols=1, nrows=1, figure=fig1) ax1 = fig1.add_subplot(spec1[0, 0]) fig1.suptitle('Plot : Out Degree Distribution (scale: log-log)') # ax1.plot(list_x, list_y, color='blue', marker='.') ax1.loglog(list_x, list_y, color='blue', marker='.') ax1.set_xlabel('Out Degree') ax1.set_ylabel('Count') Out[3]: Text(0, 0.5, 'Count') Plot : Out Degree Distribution (scale: log-log) 10^{3} 10^{2} 10¹ 10° 10° 10¹ 10² Out Degree 3 Finding Experts on the Java Programming Language on StackOverflow[5 points] In [4]: | file name = "stackoverflow-java.txt" dG_stack = nx.read_edgelist(file_name, create_using=nx.DiGraph) no wcc stack = len(list(nx.weakly connected components(dG stack))) largest_wcc_stack = dG_stack.subgraph(sorted(nx.weakly_connected_components(dG_stack), key=len, reverse =**True**) [0]) no_nodes_lwccs = largest_wcc_stack.number_of_nodes() no_edges_lwccs = largest_wcc_stack.number_of_edges() print ("1. The number of weakly connected components in the network: ", no wcc stack) print ("2a. The number of nodes in the largest weakly connected component: ", no nodes lwccs) print("2b. The number of edges in the largest weakly connected component : ", no_edges_lwccs) 1. The number of weakly connected components in the network: 10143 2a. The number of nodes in the largest weakly connected component: 131188 2b. The number of edges in the largest weakly connected component: 322486 4 Network Characteristics [40 points]: In [5]: import random class CustomGnm: def init (self, n, m, directed=False): self.n = nself.m = mself.directed = directed self.nodes = self.build nodes() self.edges = self.build edges() self.graph = self.build_graph() def build nodes(self): return [i for i in range(self.n)] def build edges(self): list edges = [] list possible edges = [] if not self.directed: i = 0 for i in range(self.n): a = self.nodes[i] for b in self.nodes[i+1:]: list possible edges.append((a,b)) len possible edges = (len(list possible edges)) count_edge = 0 while (count_edge < self.m):</pre> i = random.randint(0,len_possible_edges-1) possible edge = list possible edges[i] if possible edge not in list edges: list_edges.append(possible_edge) count edge +=1 return list edges def build_graph(self): G = nx.Graph()G.add nodes from(self.nodes) G.add_edges_from(self.edges) return G.to_undirected() class CustomSmallWorldRandomNetwork: def __init__(self, n, m=0, directed=False, no_random_edge=0): self.no_random_edge = no_random_edge self.n = nself.directed = directed self.nodes = self.build nodes() self.edges = self.build_edges() self.m = len(self.edges) if self.m != m: raise Exception("Error on Graph Formulation!!!") self.graph = self.build_graph() def build nodes(self): return [i for i in range(self.n)] def build_edges(self): list edges = [] if not self.directed: i = 0for i in range(self.n): a = self.nodes[i] $next_1_node = (i+1) % self.n$ prev_1_node = (self.n + i-1)%self.n $next_2_node = (i+2) %self.n$ prev_2_node = (self.n + i-2)%self.n if (a,next_1_node) not in list_edges: list_edges.append((a,next_1_node)) if (prev_1_node,a) not in list_edges: list_edges.append((prev_1_node,a)) if (a,next_2_node) not in list_edges: list_edges.append((a,next_2_node)) if (prev_2_node,a) not in list_edges: list_edges.append((prev_2_node,a)) count_edge = 0 while (count_edge < self.no_random_edge):</pre> a = random.randint(0, self.n-1) b = random.randint(0, self.n-1) **if** a != b: if (a,b) not in list_edges and (b,a) not in list_edges: list_edges.append((a,b)) count edge +=1return list_edges def build_graph(self): G = nx.Graph()G.add_nodes_from(self.nodes) G.add_edges_from(self.edges) return G.to undirected() cgnm = CustomGnm (5242, 14484)cswrn = CustomSmallWorldRandomNetwork(5242,14484,no_random_edge=4000) $ngnm = nx.gnm_random_graph(5242,14484)$ # cgnm = CustomGnm(6,14)# cswrn = CustomSmallWorldRandomNetwork(6,14,no_random_edge=2) # ngnm = nx.gnm_random_graph(6,14) In [13]: def plot_degree_distribution(list_graph, scale='normal'): plt.figure(figsize=(21,6)) plt.subplot(1,3,1) $G = list_graph[0]$ $list_d = G.degree()$ list sd = sorted(list d, key=lambda tup: tup[1]) $min_x = list_sd[0][1]$ $max_x = list_sd[-1][1]$ $dict_d = \{\}$ for elem in list_sd: if elem[1] not in dict d.keys(): dict d[elem[1]] = 1else: dict d[elem[1]] += 1 $list_x = []$ $list_y = []$ for k, v in dict d.items(): list_x.append(k) list y.append(v) if scale == 'normal': plt.plot(list x, list y, 'r') if scale == 'log': plt.loglog(list_x, list_y, 'r') plt.title('Custom Gnm') plt.subplot(1,3,2)G = list graph[1]list_d = G.degree() list_sd = sorted(list_d, key=lambda tup: tup[1]) $min_x = list_sd[0][1]$ $max_x = list_sd[-1][1]$ $dict d = \{\}$ for elem in list_sd: if elem[1] not in dict_d.keys(): dict d[elem[1]] = 1 $dict_d[elem[1]] += 1$ $list_x = []$ list y = []for k, v in dict d.items(): list x.append(k) list_y.append(v) if scale == 'normal': plt.plot(list_x, list_y, 'g') if scale == 'log': plt.loglog(list x, list y, 'g') plt.title('Custom Small World Random Network') plt.subplot(1,3,3) $G = list_graph[2]$ list d = G.degree() list_sd = sorted(list_d, key=lambda tup: tup[1]) min x = list sd[0][1] $max_x = list_sd[-1][1]$ $dict d = \{\}$ for elem in list_sd: if elem[1] not in dict d.keys(): $dict_d[elem[1]] = 1$ else: dict d[elem[1]] += 1 $list_x = []$ $list_y = []$ for k, v in dict d.items(): list_x.append(k) list_y.append(v) if scale == 'normal': plt.plot(list_x, list_y, 'b') if scale == 'log': plt.loglog(list_x, list_y, 'b') plt.title('NetworkX Gnm Implementation') In [14]: def get_clustering_coefficient(G): return nx.average clustering(G) In [15]: def get_diameter(G): if nx.is connected(G): d = nx.diameter(G)else: d = 0list cc = nx.connected components(G) for cc in list cc: component = G.subgraph(cc) local d = nx.diameter(component) if local d > d: d = local dreturn d **Degree Distribution (Count vs Degree)** In [16]: plot_degree_distribution([cgnm.graph, cswrn.graph, ngnm], scale='normal') Custom Gnm Custom Small World Random Network NetworkX Gnm Implementation 1750 -800 800 1500 1250 600 600 400 400 750 500 200 200 250 12.5 15.0 10.0 Log-log Degree Distribution (Count vs Degree) plot_degree_distribution([cgnm.graph, cswrn.graph, ngnm], scale='log') In [17]: Custom Small World Random Network Custom Gnm NetworkX Gnm Implementation 10³ 10³ 103 10² 102 10² 101 101 101 100 10° 101 $4 \times 10^{\circ}$ 6 × 10° 10° 101 **Clustering Coefficient** In [18]: cc cgnm = get clustering coefficient(cgnm.graph) cc cswrn = get clustering coefficient(cswrn.graph) cc ngnm = get clustering coefficient(ngnm) print('Clustering Coefficient (Custom Gnm) : ', cc_cgnm) print('Clustering Coefficient (Small World Random Network) : ', cc_cswrn) print('Clustering Coefficient (NetworkX Implementation) : ', cc ngnm) Clustering Coefficient (Custom Gnm): 0.0006461023820810161 Clustering Coefficient (Small World Random Network): 0.2839837025071631 Clustering Coefficient (NetworkX Implementation): 0.0008180636185214584 Diameter In [12]: d cgnm = get diameter(cgnm.graph) d cswrn = get diameter(cswrn.graph) d ngnm = get diameter(ngnm) print('Diameter (Custom Gnm) : ', d cgnm) print('Diameter (Small World Random Network) : ', d cswrn) print('Diameter (NetworkX Implementation) : ', d ngnm) Diameter (Custom Gnm): 11 Diameter (Small World Random Network): 10 Diameter (NetworkX Implementation): 10 5 Random Graphs with Clustering [40 points] Consider the following random graph model with clustering. For n nodes, we have $\binom{n}{3}$ distinct 'triplets'. For each triplet, with independent probability p we connect the nodes belonging to this triplet in the graph using three edges to form a triangle, where $p=rac{c}{\binom{n-1}{2}}$, where c is a constant. Assume n is very large. Question 1: Prove that the expected degree in this model is 2c. [Hint: expected degree of a node u in this generative model is equal to twice the expected number of triangles incident on u] Answer 1: To form a triplet, for each node a, we need a pair (b,c) where $a \neq b \neq c$. So, for each node, the possible number of pairs (to form a triplet) = possible number of triplets = $\binom{n-1}{2}$ Given that, for each triplet, independent probability of forming a triangle = pTherefore, for each node, expected number of triangles $= p*\binom{n-1}{2}$ Here, $p=rac{c}{{n-1 \choose 2}}$ so, for each node, expected number of triagles $=\frac{c}{\binom{n-1}{2}}*\binom{n-1}{2}=c$ so, expected degree of each node = 2* expected number of triangles for that node = 2c. Question 2: What is the clustering coefficient C? What is the value of C as n tends to infinity? Question 3: Implement this model to computationally derive degree distribution, diameter, and clustering coefficient.

