

### Problem 1: Recursive Digital Root

Compute the digital root of an integer recursively until a single-digit value remains.

Function Prototype: `digital_root`

Input:

A single integer  $N$  ( $0 \leq N \leq 10^9$ )

Output:

A single integer — the digital root of  $N$ .

Sample Input:

9875

Sample Output:

2

Explanation:  $9+8+7+5 \rightarrow 29$ ;  $2+9 \rightarrow 11$ ;  $1+1 \rightarrow 2$

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### Problem 2: Maximum and Minimum in an Array

Find both maximum and minimum values in an array using a single function call.

Function Prototype: `find_min_max`

Input:

First line:  $N$  ( $1 \leq N \leq 100$ )

Second line:  $N$  space-separated integers.

Output:

Print the maximum and minimum separated by a space.

Sample Input:

5

3 9 1 4 7

Sample Output:

9 1

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### Problem 3: Matrix Multiplication with Transpose

Compute  $C = A \times B^T$

Input:

First line:  $r_1$   $c_1$   $r_2$

Next  $r_1 \times c_1$  integers for A, followed by  $r_2 \times c_1$  integers for B.

Output:

Matrix C in row-major order.

Sample Input:

- 2 3 2  
1 2 3  
4 5 6  
7 8 9  
10 11 12

Sample Output:

- 50 122  
68 167
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### Problem 4: Factorial with Overflow Detection

Compute factorial recursively and detect overflow ( $> 32$ -bit).

Function Prototype: factorial\_safe

Input:

A single integer N ( $0 \leq N \leq 20$ )

Output:

Print N! or 'OVERFLOW' if it exceeds 32-bit unsigned integer range.

Sample Input:

- 13

Sample Output:

- OVERFLOW
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### Problem 5: Palindrome Check

Check whether a given string is a palindrome using two-pointer traversal.

Function Prototype: `is_palindrome`

Input:

A single string (no spaces, up to 100 chars).

Output:

YES if palindrome, NO otherwise.

Sample Input:

- MADAM

Sample Output:

- YES
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### Problem 6: Centered Pyramid Pattern

Print a centered pyramid of stars using nested loops.

Function Prototype: `print_pyramid`

Input:

A single integer N ( $1 \leq N \leq 10$ )

Output:

A pyramid with N rows of '\*' characters.

Sample Input:

- 3

Sample Output:

- ```
  *
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*****
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