

1.)

$$F(x, y, z) = xy + x'z + yz$$

$$= xy + x'z + yz(x + x')$$

$$= xy + x'z + xyz + x'yz$$

$$= xy(1 + z) + x'z(1 + y)$$

$$= xy + x'z$$

2.)

$$(x + y)(x' + z)(y + z) = (x + y)(x' + z)$$

x	y	z	x'	x + y	x' + z	y + z	(x + y)(x' + z)(y + z)	(x + y)(x' + z)
0	0	0	1	0	1	0	0	0
0	0	1	1	0	1	1	0	0
0	1	0	1	1	1	1	1	1
0	1	1	1	1	1	1	1	1
1	0	0	0	1	0	0	0	0
1	0	1	0	1	1	1	1	1
1	1	0	0	1	0	1	0	0
1	1	1	0	1	1	1	1	1

Their outputs are equal.

3.)

a.)

A	B	C	D	Minterm	Maxterm
0	0	0	0	$A'B'C'D' = m_0$	$A + B + C + D = M_0$
0	0	0	1	$A'B'C'D = m_1$	$A + B + C + D' = M_1$
0	0	1	0	$A'B'CD' = m_2$	$A + B + C' + D = M_2$
0	0	1	1	$A'B'CD = m_3$	$A + B + C' + D' = M_3$
0	1	0	0	$A'BC'D' = m_4$	$A + B' + C + D = M_4$
0	1	0	1	$A'BC'D = m_5$	$A + B' + C + D' = M_5$
0	1	1	0	$A'BCD' = m_6$	$A + B' + C' + D = M_6$
0	1	1	1	$A'BCD = m_7$	$A + B' + C' + D' = M_7$
1	0	0	0	$AB'C'D' = m_8$	$A' + B + C + D = M_8$
1	0	0	1	$AB'C'D = m_9$	$A' + B + C + D' = M_9$
1	0	1	0	$AB'CD' = m_{10}$	$A' + B + C' + D = M_{10}$
1	0	1	1	$AB'CD = m_{11}$	$A' + B + C' + D' = M_{11}$
1	1	0	0	$ABC'D' = m_{12}$	$A' + B' + C + D = M_{12}$
1	1	0	1	$ABC'D = m_{13}$	$A' + B' + C + D' = M_{13}$
1	1	1	0	$ABCD' = m_{14}$	$A' + B' + C' + D = M_{14}$
1	1	1	1	$ABCD = m_{15}$	$A' + B' + C' + D' = M_{15}$

$$F(A, B, C, D) = B'D + A'D + BD$$

$$= B'D(A + A')(C + C') + A'D(B + B')(C + C') + BD(A + A')(C + C')$$

$$= AB'CD + A'B'CD + AB'C'D + A'B'C'D + A'BCD + A'B'CD + A'BC'D + A'BC'D$$

$$+ ABCD + A'BCD + ABC'D + A'BC'D$$

$$= AB'CD + A'B'CD + AB'C'D + A'B'C'D + A'BCD + A'BC'D + ABCD + ABC'D$$

$$= m_{11} + m_3 + m_9 + m_1 + m_7 + m_5 + m_{15} + m_{13}$$

$$= \epsilon(1, 3, 5, 7, 9, 11, 13, 15)$$

$$= M_0.M_2.M_4.M_6.M_8.M_{10}.M_{12}.M_{14}$$

$$= \pi(0, 2, 4, 6, 8, 10, 12, 14)$$

b.)

$$F(A, B, C, D) = B'D + A'D + BD$$

$$= D(B' + A' + B)$$

$$= D(1 + A')$$

$$= D1$$

$$= D$$