# Surface wave supporting structures in the terahertz and optical frequency domains

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### ELECTRICAL & COMPUTER ENGINEERING

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### **Outline**



- Overview
- Background
- Theory and Methods
  - Sommerfeld Integral analysis
  - Dispersion relation
  - Surface Integral equation
- Results
  - Super-resolution Imaging
- Conclusions

### Overview



- Plasmonics: subwavelength localization of electromagnetic (EM) fields
- Plasma frequency
  - Metals Optical frequency
  - 2D Electronic Systems (2DES) - Terahertz (THz)
- Bridging the THz gap

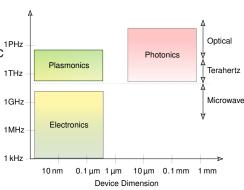


Figure: Communication Technologies at various frequencies

### Overview



#### Terahertz 2DES

- Graphene
  - Grown separately, transferred to substrate
  - Currently not integrable to current electronics technology
  - Superior electronic properties
- Semiconductor heterostructures
  - Conventional epitaxial semiconductor device fabrication techniques
  - On-chip integration with silicon electronics

#### Plasmonics Overview



- Interfacial wave phenomena
  - Metal-dielectric interface
  - Semiconductor heterostructure
- Surface plasmon polaritons (SPPs)
- Plasma frequency
  - Metals Optical frequency
  - Semiconductors Terahertz

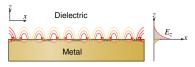


Figure: SPPs at optical frequencies

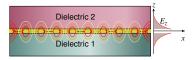


Figure: SPPs in the THz regime



#### Surface Plasmon Polaritons

- Slow surface waves
- Reduced Wavelength
- Focusing beyond the diffraction limit
- Optical SPP

$$\mathrm{Re}\left[\varepsilon_{\mathsf{metal}}(\omega)\right]<0$$

THz SPP

$$\operatorname{Im}\left[\sigma_{s}(\omega)\right] < 0$$

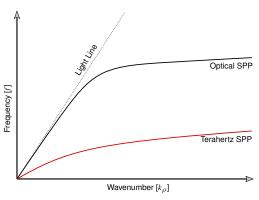


Figure: Dispersion Curve comparison

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#### Optical Nanoantennas

- Convert Localized near-field to efficient far-field radiation
- Low Q-factor
- Extremely small size
- High Purcell Factor

$$P = \frac{Q}{V}$$

Directive radiation

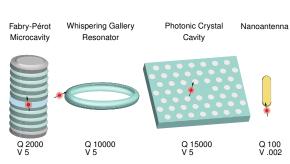
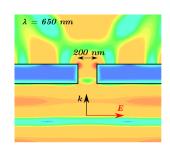


Figure: Optical resonant cavities for electric field enhancement

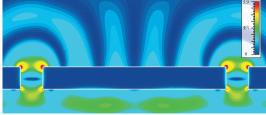
Optical Nanoantennas (contd.)

- Scaled-down microwave antenna designs
  - Aperture antennas for subwavelength focusing
  - Broadband spectral response : Bowtie











#### Two-dimensional Electron Gas (2DEG)

- Semiconductor
   Heterostructure in high electron mobility transistor (HEMT)
- High concentration of free electrons
   (∼ 1 × 10<sup>12</sup> − 1 × 10<sup>14</sup> cm<sup>-2</sup>)
- Very high Mobility  $(\sim 1 \times 10^4 1 \times 10^6 \, \text{cm}^2/\text{V/s})$
- Formation of Quantum Well
  - Two-dimensional confinement of electrons

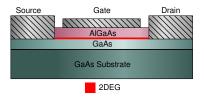


Figure: Typical GaAs/AlGaAs HEMT

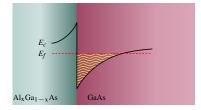


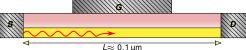
Figure: Band diagram of a GaAs/AlGaAs heterostructure

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2DEG (contd.)

- Plasma waves in 2DEG
- Dyakonov-Shur instability
  - Voltage bias at source and drain terminals
  - Plasma resonance
  - THz emission
- Electronic Flute
  - Tunable resonance with gate voltage
- Shallow water waves





$$\lambda = \frac{c}{f}$$

$$\implies 300 \mu \text{m}$$

## Theory and Methods

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2DEG Circuit model

 Drude-Lorentz Surface Conductivity

$$\sigma_s = \frac{N_s e^2}{m^*} \frac{\tau}{1 + j\tau\omega}$$

 $N_s$  - Surface charge density

au - Scattering time

m\*- Effective electron mass

Equivalent Circuit

$$\sigma_s = \frac{1}{Z} = \frac{1}{R + 1/j\omega C}$$

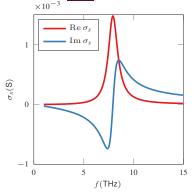


Figure: Room temperature GaN/AlGaN 2DEG surface conductivity

$$Z = R - \frac{1}{\omega C}$$

$$R$$

$$C$$

### Theory and Methods

#### Dispersion Relation for a 2D Sheet

- Conductive Sheet in freespace
- TM mode surface wave

$$k_{\rm P}^{\rm TM} = \frac{\omega}{c} \sqrt{1 - \left(\frac{2}{\eta_0 \sigma_s}\right)^2}$$

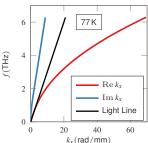
Below plasma frequency

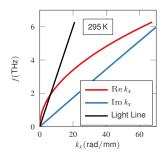
$$\operatorname{Im} \sigma_s < 0$$

At low temperature

$$\operatorname{Im} |\sigma_s| \gg \operatorname{Re} |\sigma_s|$$







# Theory and Methods

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#### Analyzing multilayer structure

- Equivalent transmission line (TL) network
- Dispersion relation
  - Transverse resonance condition

$$Y^{\uparrow}(z_0) + Y^{\downarrow}(z_0) + Y_{\sigma} = 0.$$

Below plasma frequency

