

# Two-dimensional Plasmonic Devices

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# Outline

## Preliminary Exam

- Plasmonics Overview
- Background
- Theory and Methods
  - Dispersion Relation
  - Computation of fields
- Results
- Proposed Work

# Plasmonics Overview

- Utilizing the terahertz gap
- High electron mobility transistors (HEMTs)
- Two-dimensional materials
- Subwavelength Plasmonic waves
- Miniaturization of circuit and antenna devices
- Poor energy efficiencies
- Re-engineering of the transistor

Operating Frequency

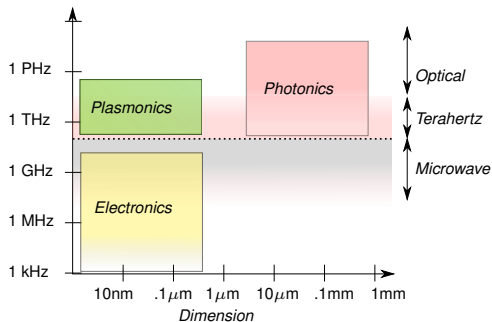


Figure: Typical GaAs/AlGaAs HEMT

# Background and Previous Work

## Surface Plasmons

- Metal-dielectric interface

$$\text{Re} [\varepsilon_{\text{metal}}] (\omega) < 0$$

- Slow surface waves
- Subwavelength Control of electromagnetic waves
- Focusing beyond the diffraction limit

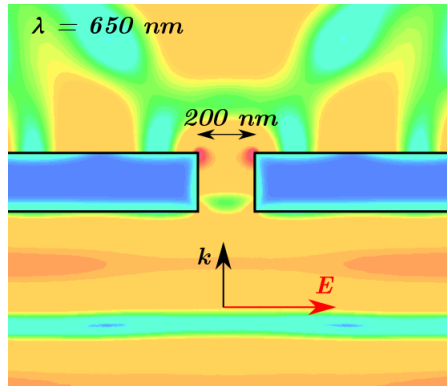


Figure: Subwavelength Transmission through a Silver slit

# Optical Nanoantennas

## Dispersion Relation

- Metal-dielectric Interface

$$k_{sp} = \frac{\omega}{c} \sqrt{\frac{\epsilon_1 \epsilon_2(\omega)}{\epsilon_1 + \epsilon_2(\omega)}}$$

- Accurate material description using Drude-critical points

$$\epsilon_2(\omega) = \epsilon_\infty - \frac{\omega_d^2}{\omega^2 + j\gamma\omega} + \sum_{i=1}^N G_i(\omega)$$

$$G_i(\omega) = C_i \left[ \frac{e^{j\phi_i}}{\omega_i - \omega - j\Gamma_i} + \frac{e^{-j\phi_i}}{\omega_i + \omega + j\Gamma_i} \right]$$

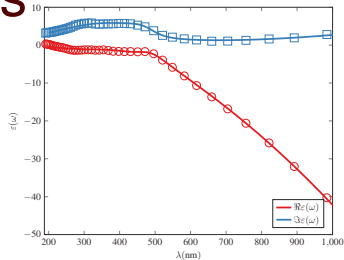
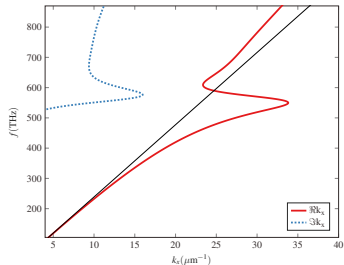


Figure: Dispersion curve for Gold-air SPPs



# Background and Previous Work

## Optical Nanoantennas

- Convert Localized near-field to efficient far-field radiation
- Low Q-factor
- Extremely small size
- **High Purcell Factor**

$$P = \frac{Q}{V}$$

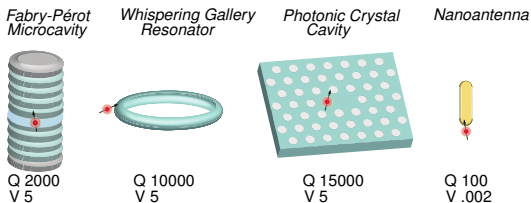


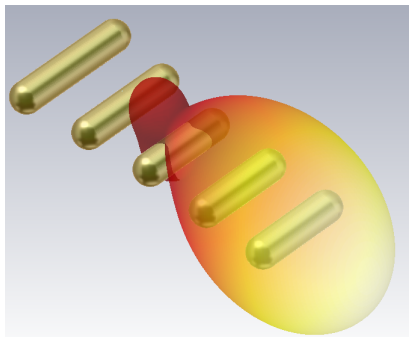
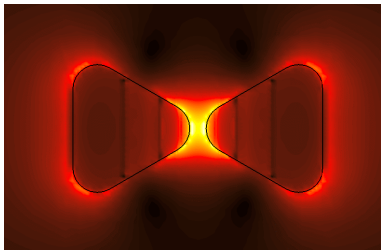
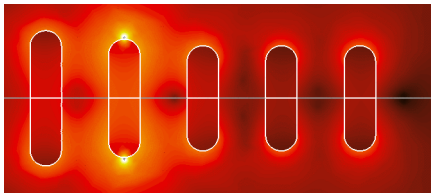
Figure: Optical resonant cavities for electric field enhancement

- Directive radiation

# Background and Previous Work

## Optical Nanoantennas (contd.)

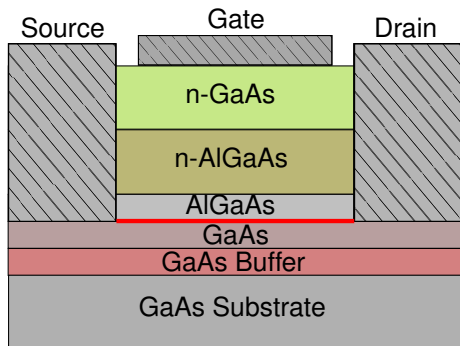
- Scaled-down microwave designs
  - Directivity: Yagi-Uda antenna
  - Broadband: Bowtie antenna



# Background and Previous Work

## Two-dimensional Electron Gas (2DEG)

- Semiconductor Heterostructure Interface
- High electron Mobility
- High concentration of electric charge
- **Two-dimensional Surface waves**
- Formation of Quantum Well  
Two-dimensional confinement of electrons



 2DEG

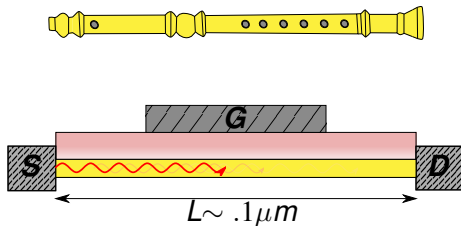
Figure: Typical GaAs/AlGaAs HEMT



# Background and Previous Work

## 2DEG (contd.)

- Plasma waves in 2DEG
- Dyakonov-Shur instability
  - Voltage bias at source and drain terminals
  - Plasma resonance
  - Emission of terahertz radiation
  - External radiation detection
- *Electronic Flute*
- Tunable resonance with gate voltage
- Shallow water waves
  - Surface waves



$$\lambda = \frac{c}{f}$$

$$\implies 300 \mu\text{m}$$

# Theory

## 2DEG formation

- Semiconductor Heterostructure Interface
- High electron concentration
- **Two-dimensional Surface waves**
- Formation of Quantum Well  
Two-dimensional confinement of electrons

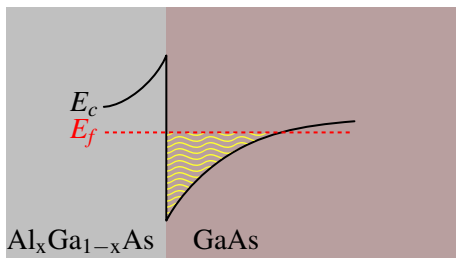


Figure: Band diagram of a GaAs/AlGaAs heterostructure

$E_c$  - Conduction band edge

$E_f$  - Fermi level

# Theory

## 2DEG Dispersion Relation

- TE mode

$$k_{z1} + k_{z2} = \omega \sigma_s(\omega)$$

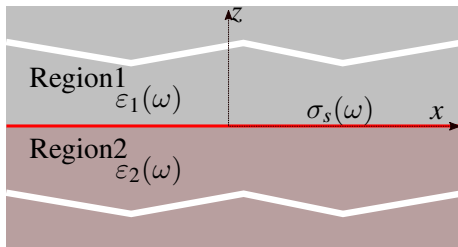
No real solutions for an isotropic environment

- TM mode

$$\frac{\varepsilon_1(\omega)}{k_{z1}} + \frac{\varepsilon_2(\omega)}{k_{z2}} = -\frac{\sigma_s(\omega)}{\omega}$$

Real solution(s). Surface waves exist.

$$k_{zi} = \sqrt{\left(\frac{\omega}{c}\right)^2 \varepsilon_i(\omega) - k_x^2}$$



■ 2DEG

Figure: 2DEG at a semiconductor heterojunction

# Theory

## Material Description

- Complex valued
- Drude-Lorentz oscillator model

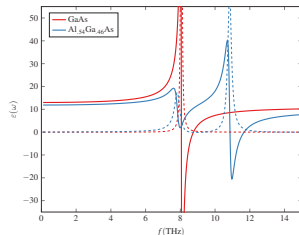
$$\epsilon(\omega) = \epsilon^\infty + \prod_i \frac{\omega_{li}^2 - \omega^2 - j\gamma_{li}\omega}{\omega_{ti}^2 - \omega^2 - j\gamma_{ti}\omega}$$

$\epsilon^\infty$  - High-frequency limit

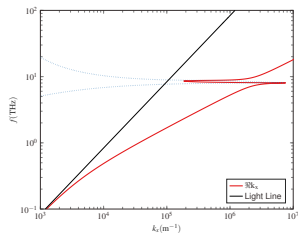
$\omega_{ti}$  - TO phonon frequencies

$\omega_{li}$  - LO phonon frequencies

$\gamma$  - Damping constants



(a)



(b) Dispersion curve

# Theory

## Thin Sheet Simulation

- $TM_z$  polarization
- Dielectric Rod of length  $2.5 \lambda$
- $\epsilon = 4, \mu = 1$

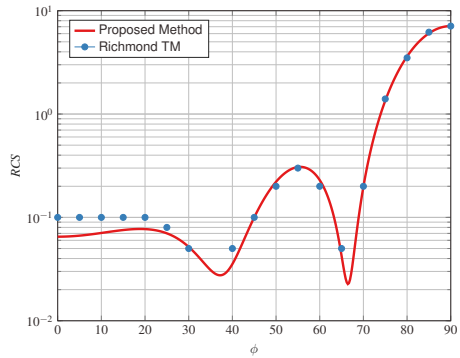
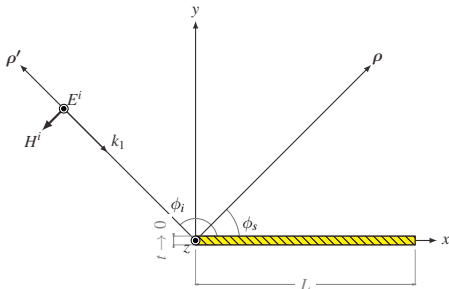


Figure: Radar Cross-section

# Theory

## Thin Sheet Simulation

- $TE_z$  polarization
- Dielectric Rod of length  $2.5 \lambda$
- $\varepsilon = 4$ ,  $\mu = 1$

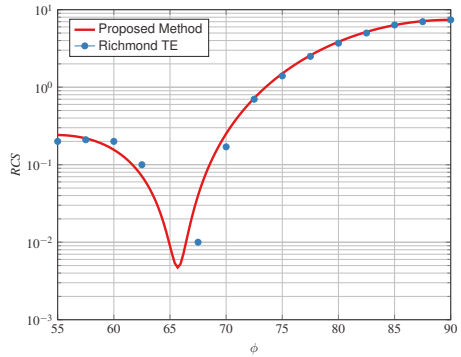
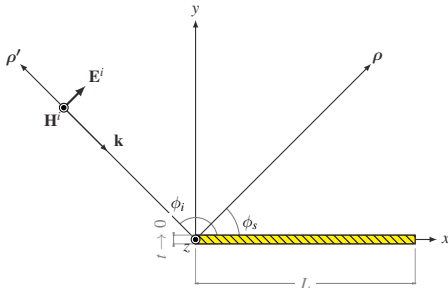


Figure: Radar Cross-section