

Q4) Write a C Program to find out the value of $F(2.55)$ using Newton's Forward Interpolation Formula from the following table:

x :	2.00	2.25	2.50	2.75	3.00
$F(x)$:	9.00	10.06	11.25	12.56	14.00

Algorithm for Newton's Forward Interpolation: formula :-

- Step 1: Start
- Step 2: Take range n
- Step 3: read x_i, y_i for $i = 1$ to n
- Step 4: read x_1
- Step 5: set $p = n-1, s = y[0], j = 0, s_1 = 0$
- Step 6: take $u = (x_1 - x[0]) / (x[1] - x[0])$
- Step 7: for $i = 1$ to $n-1$
 for $j = 0$ to p
 $y[j] = y[j+1] - y[j]$
 $s_1 = s_1 + (u \times y[j]) / \text{fact}(i)$
- Step 8: $c = c \times (u - i)$
 $p = p - 1$
- Step 9: set $S = s_1 + S$
- Step 10: Print S
- Step 11: Stop

C - code for Newton's forward interpolation

```
#include <stdio.h>
```

```
int fact (int x)
```

```
{ int i, f, f=1;
```

```
for (i=1; i<=x; i++)
```

```
f = f * i;
```

```
return (f);
```

```
}  
void main () {
```

```
float x[10], y[10], x1, u, h, p, s, s1=0, c=1;
```

```
int n, i, j;
```

```
printf("Enter number of terms:");
```

```
scanf("%d", &n);
```

```
printf("Enter the values of x and y \n");
```

```
for (i=0; i<n; i++)
```

```
scanf("%f%f", &x[i], &y[i]);
```

```
printf("Enter the value of x to find:");
```

```
scanf("%f", &x1);
```

```
p = n-1; s = y[0];
```

```
u = (x1 - x[0]) / (x[1] - x[0]);
```

```
for (i=1; i<n-i; i++)
```

```
{ for (j=0; j<p; j++)
```

$$s[i] = y[i+1] - y[i];$$

$$s1 = s1 + (u * c * y[i]) / \text{fact}(i);$$

$$c = c * (u - i);$$

$$p = p - 1;$$

$$s = s1 + s;$$

- printf (" \n Ans is = %.f", s);

}

⊗ Output:- Enter number of terms = 5

Enter values of x and y.

2.00

9.00

2.25

10.06

2.50

11.25

2.75

12.56

3.00

14.00

Enter the values of x to find : 2.35

Ans is = 10.521408.

2. Write a C program to find out the value of $f(4.5)$ using Newton's Backward Interpolation.

Formula from the following table :-

x :	2	3	4	5
$f(x)$:	11	15	23	39

Algorithm for Newton's Backward Interpolation.

Formula :-

- Step 1: start
- Step 2: Take range of n
- Step 3: read x_i, y_i for $i=1$ to n
- Step 4: read $x_p, j=1$
- Step 5: while ($j < n$)
 - for ($i=0$ to $n-j$)

Print $y[i]$
- Step 6: set $p=n-1, s=y[n-1], s_1=0, c=1$
- Step 7: take $u = (x_1 - x[n-1]) / (x[1] - x[0]);$
- Step 8: for $i=1$ to $n-1$

$$s_1 = s_1 + (u \times c \times y[p-1]) / \text{fact}(i)$$
- Step 9: take $c = c \times (u + i)$
take $p = p - 1$
- Step 10: set $s = s_1 + s$
- Step 11: Print s
- Step 12: stop

C - Code for Newton's Backward Interpolation :-

```
#include <stdio.h>
```

```
int fact (int x) {
```

```
    int i, f, f = 1;
```

```
    for (i = 1; i <= x; i++)
```

```
        f = f * i;
```

```
    return (f);
```

```
void main ()
```

```
{ float x[10], y[10], x1, u, h, s, s1 = 0, c = 1;
```

```
  int i, n, j = 1, P;
```

```
  printf("Enter how many terms : ");
```

```
  scanf("%d", &n);
```

```
  printf("Enter values for x \n");
```

```
  for (i = 0; i < n; i++)
```

```
      scanf("%f", &x[i]);
```

```
  printf("Enter values for y \n");
```

```
  for (i = 0; i < n; i++)
```

```
      scanf("%f", &y[i]);
```

```
  printf("Enter values of x to find : ");
```

```
  scanf("%f", &x1);
```

```
  while (j < n) printf("\n Difference table is \n");
```

```
  { for (i = 0; i < n - j; i++)
```

```
      { for (j = 0) y[i] = y[i+1] - y[i];
```



```

printf("%f \t", y[i]);
}
printf("\n");
j++;
}
p = n-1, s = y[n-1];
u = (x1 - x[n-1]) / (x[1] - x[0]);
for (i = 1; i < n-1; i++)
{
    s1 = s1 + (u * C * y[p-1]) / fact(i);
    C = C * (u + i);
    p = p-1;
}
s = s1 + s;
printf("\n Ans is = %f", s);

```

Output:- enter how many terms : 4
 Enter values of x : 2 3 4 5
 Enter values of y : 11 15 23 39
 Enter value of x to find : 4.5
 Difference table is
 4.000000 8.000000
 4.000000 8.000000 16.000000
 4.000000
 Ans is = 29.750000 .

③ Write a C Program to find out the value of $f(10)$ using Lagrange's Interpolation formula.

From the following table:

x :	5	6	9	11
$f(x)$:	12	13	14	16

• Algorithm for Lagrange's Interpolation formula :-

Step 1 : Start

Step 2 : Take range of n

Step 3 : Read x_i & y_i for $i=1$ to n

Step 4 : Read x_p

Step 5 : Initialize $y = 0$, $s[10]$, N , D

Step 6 : for $i = 0$ to n

$N = 1$, $D = 1$

for $j = 0$ to n

if $j \neq i$

$N = N * (x - x[i])$

$D = D * (x[i] - x[j])$

Step 7 : $s[j] = N/D$

Step 8 : $y = y + s[j] * y[j]$

Step 9 : Print y

Step 10 : Stop

• C-code for Lagrange's Interpolation :-

```
#include <stdio.h>
```

```
main ()
```

```
{ int i, j=1, n;
```

```
float x[10], y[10], s[10], x, y, f=0, N, D;
```

```
printf("Enter number of terms : ");
```

```
scanf("%d", &n);
```

```
printf("Enter values for x\n");
```

```
for (i=0; i<n; i++)
```

```
scanf("%f", &x[i]);
```

```
printf("Enter values for y\n");
```

```
for (i=0; i<n; i++)
```

```
scanf("%f", &y[i]);
```

```
printf("Enter value of x for find : ");
```

```
scanf("%f", &x);
```

```
for (j=0; j<n; j++)
```

```
{ N=1
```

```
D=1
```

```
for (i=0; i<n; i++)
```

```
{ if (j != i)
```

```
{ N = N * (x - x[i]);
```

```
D = D * (x[i] - x[j]);
```

```
}
```

```
}
```


$s[i] = n/d;$

$y = y + s[i] * y[i];$

$\text{printf}("Ans is = %.f", y);$

Output:-

Enter number of terms : 4

Enter values of x

5

6

9

11

Enter values of y

12


13

14

16

Enter value of x for find : 10

Ans is = 14.666666.

 20/9/19

04 Write a C Program to Trapezoidal Method.

⇒ Algorithm:-

- Step 1: start the Program.
- Step 2: define the fn $f(x)$
- Step 3: read $a, b, n, S=0, t$.
- Step 4: set $x_0 = a$ and $x_n = b$.
- Step 5: take $h = \frac{b-a}{n}$
- Step 6: For $i = 0(1)n$
- Step 7: $x_i = x_0 + i^*h, y_i = f(x_i)$
- Step 8: for $i = 1(1)n-1$
- Step 9: $S = S + f(x_i)$
- Step 10: $t = \left(\frac{h}{2}\right) * (y_0 + y_n + 2S)$
- Step 11: Print the value of x .
- Step 12: Stop the Program.

C Program:-

```
#include <stdio.h>
#include <conio.h>
#include <math.h>
float f(float x)
{
    return (1/(1+pow(x,2)));
}
```

```
void main ( )
```

```
{ int i, n;
```

```
float x0, xn, h, y[20], so, se, ans, x[20];
```

```
printf("\n Enter values of x0, xn, h: \n");
```

```
scanf("%f%f%f", &x0, &xn, &h);
```

```
n = (xn - x0) / h;
```

```
if (n % 2 == 1)
```

```
{ n = n + 1;
```

```
}  
h = (xn - x0) / n;
```

```
printf("\n refined value of n and h are: %.d %.f \n",  
n, h);
```

```
printf("\n y values \n");
```

```
for (i = 0; i <= n; i++)
```

```
{ x[i] = x0 + i * h;
```

```
y[i] = f(x[i]);
```

```
printf("\n %.f \n", y[i]);
```

```
}  
so = 0;
```

```
se = 0;
```

```
for (i = 1; i < n; i++)
```

```
{ if (i % 2 == 1)
```

```
{
```



```

    s0 = s0 + y[i];
  }
  else
  {
    se = se + y[i];
  }
}
ans = h/3 * (y[0] + y[n] + 4*s0 + 2*se);
printf("\n final integration is %.f", ans);
getch();
}

```

Output

Enter values of x_0 , x_n in: 0 3 0.5

defined value of n and h are: 6 0.500000

y values

1.000000

0.800000

0.500000

0.307692

0.200000

0.137931

0.100000

final integration is 1.247082.

5. Write a Program using Simpson's $\frac{1}{3}$ Rule

→ Algorithm

- Step 1 : Start;
- Step 2 : Input function $f(x)$;
- Step 3 : Read a, b, n ;
- Step 4 : Compute $h = (b-a)/n$;
- Step 5 : $Sum = [f(a) + f(a+nh)]$;
- Step 6 : for $i = 1$ to $n-1$ step 2 do
 Compute $Sum = Sum + 4 * f(a+i*h) + 2 * f(a + (i+1)h)$;
end for;
- Step 7 : Compute $result = Sum * h/3$;
- Step 8 : Print result;
- Step 9 : stop.

- Program :

```
#include <stdio.h>
#include <math.h>

float f(float x)
{
    return exp(x);
}
```

```
int main()
{
    // ...
}
```

```

float a, b, n, h, sum1 = 0, sum2 = 0, sum, y0, yn;
int i;

printf("Enter the upper limit : ");
scanf("%f", &b);

printf("Enter the lower limit : ");
scanf("%f", &a);

printf("Enter the number of intervals : ");
scanf("%d", &n);

h = (b - a) / n;
y0 = f(a + 0 * h);
yn = f(a + n * h);
for (i = 1; i < n; i++)
    if (i % 2 == 0)
        sum1 = sum1 + f(a + i * h);
    else
        sum2 = sum2 + f(a + i * h);
sum = (h / 3) * (y0 + yn + 2 * sum1 + 4 * sum2);
printf("Answer : %.2f", sum);
getch();
return 0;
}

```

Output:

```

Enter the upper limit : 0.6
Enter the lower limit : 0
Enter the number of intervals : 10
Answer : 0.82.

```


Write a C Program using Bisection Method.

Algorithm:

- Step 1: Start the Program;
- Step 2: Define the function $f(x)$;
- Step 3: Select the interval a, b in which the root lies where $f(a) \cdot f(b) < 0$;
- Step 4: Calculate $x = \frac{a+b}{2}$;
- Step 5: If $f(b) \cdot f(x) < 0$:
 set $a = x$;
 otherwise set $b = x$;
- Step 6: If $|a-b| < \epsilon$; ϵ being the Prescribed accuracy then goto step 7;
- Step - else goto step 4;
- Step 7: Print the value of x ;
- Step 8: Stop the Program;

C Program:

```
#include <stdio.h>
#include <conio.h>
#include <math.h>
float F (float x)
{
    return (x*x*x - (5*x)+1);
}
```

```
void main ()
```

```
{ int i=0;
```

```
float a, b, c, err, temp;
```

```
clrscr();
```

```
printf("Enter permissive error \n");
```

```
scanf("%f", &err);
```

```
do
```

```
{ printf("Enter value of a & b \n");
```

```
scanf("%f%f", &a, &b);
```

```
}
```

```
while ( F(a) * F(b) > 0);
```

```
c = 0;
```

```
do
```

```
{ temp = c;
```

```
c = (a+b) / 2;
```

```
if (F(a) * F(b) < 0)
```

```
{ b = c;
```

```
}
```

```
else
```

```
{ a = c;
```

```
}
```

```
i++;
```

```
printf("Iteration %d", i);
```

```
printf("%f\n", c);
```

```
} while (fabs(temp - c) > err);
```

```
printf("root of equation is %f", c);
```

```
getch();
```

```
}
```

output:

enter permissive error : 0.0005

enter value of a & b : 2 3

iteration 1 : 2.500000

iteration 2 : 2.250000

iteration 3 : 2.125000

iteration 4 : 2.062500

iteration 5 : 2.093750

iteration 6 : 2.1093750

iteration 7 : 2.117188

iteration 8 : 2.121094

iteration 9 : 2.123047

iteration 10 : 2.124023

iteration 11 : 2.124512

root of equation is 2.124512.