

# MECH0006 Topic Notes

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# Chapter 1

## Preliminaries

This part is being skipped.

# Chapter 2

## Kinematics of a Particle

What is kinematics?

Kinematics is used to describe the geometry of motion of an object in space, independent of the causes of that motion.

What is a particle?

A particle is an object for which we do not need to worry about its rotation or the tendency of the forces that acts upon it which can cause rotation. Thus, we are not worried about our moment balance equation. A particle is a system idealised by being totally characterised by its position (as a function of time) and its fixed mass.

### 2.1 Position, Velocity and Acceleration

Consider a point mass  $M$  in 3D space with position  $P$  uniquely characterised by the vector  $\underline{r}$  from a fixed reference frame with origin  $O$ . Next consider two adjacent points  $P$  and  $P'$  at the corresponding times of  $t$  and  $t + \Delta t$ . The velocity of the point mass is defined as the limit of the change in position with respect to time given by:

$$\underline{v} = \lim_{\Delta t \rightarrow 0} \frac{\underline{r}(t + \Delta t) - \underline{r}(t)}{\Delta t} = \lim_{\Delta t \rightarrow 0} \frac{\Delta \underline{r}}{\Delta t} = \frac{d\underline{r}}{dt} = \dot{\underline{r}} \quad (2.1)$$

Since the change in position vector  $\Delta \underline{r}$  in the limit as  $\Delta t \rightarrow 0$  is always tangent to the trajectory of  $M$ , it follows that the velocity vector is always *tangent* to the

path. the arc-length  $s$  measures the distance covered by M along its trajectory. The distance covered at  $P$  is  $s$  and the distance covered at  $P'$  is  $s + \Delta s$  where  $|\Delta \underline{r}| = \Delta s$ . Thus, the speed of M is:

$$|\underline{v}| = v = \lim_{\Delta t \rightarrow 0} \frac{\Delta s}{\Delta t} = \frac{ds}{dt} = \dot{s} \quad (2.2)$$

Similarly the velocity of M is defined as:

$$\underline{a} = \lim_{\Delta t \rightarrow 0} \frac{\underline{v}(t + \Delta t) - \underline{v}(t)}{\Delta t} = \lim_{\Delta t \rightarrow 0} \frac{\Delta \underline{v}}{\Delta t} = \frac{d\underline{v}}{dt} = \dot{\underline{v}} = \ddot{\underline{r}} \quad (2.3)$$

## **2.2 Rectangular/Cartesian Coordinate System**