

UCL Mechanical Engineering 2020/2021

ENGF0004 Coursework 2

NCWT3

April 16, 2021

1 Question 1

1.1 a

For the line integral to be independent from the path of integration, the following conditions must be fulfilled:

$$I = \int_A^B \left(\frac{\partial u}{\partial x} dx + \frac{\partial u}{\partial y} dy \right) \quad (1.1)$$

$$P(x, y) = \frac{\partial u}{\partial x} \text{ and } Q(x, y) = \frac{\partial u}{\partial y} \quad (1.2)$$

$$\frac{\partial P(x, y)}{\partial y} = \frac{\partial Q(x, y)}{\partial x} \quad (1.3)$$

Considering the integral:

$$I = \int_A^B \left[e^{-\alpha xy} \left(\frac{\alpha - 2}{x} \right) dx - \frac{1}{\alpha y} (e^{-\alpha xy} - 1) dy \right] \quad (1.4)$$

$$P(x, y) = e^{-\alpha xy} \left(\frac{\alpha - 2}{x} \right) \text{ and } Q(x, y) = -\frac{1}{\alpha y} (e^{-\alpha xy} - 1) \quad (1.5)$$

$$\frac{\partial P(x, y)}{\partial y} = -\alpha x \left(\frac{\alpha - 2}{x} \right) e^{-\alpha xy} = (2\alpha - \alpha^2) e^{-\alpha xy} \quad (1.6)$$

$$\frac{\partial Q(x, y)}{\partial x} = -\frac{1}{\alpha y} (-\alpha y) e^{-\alpha xy} = e^{-\alpha xy} \quad (1.7)$$

$$\therefore 2\alpha e^{-\alpha xy} - \alpha^2 e^{-\alpha xy} = e^{-\alpha xy} \quad (1.8)$$

$$e^{-\alpha xy} (\alpha^2 - 2\alpha + 1) = 0 \quad (1.9)$$

$$e^{-\alpha xy} = 0 \rightarrow \text{no solutions} \quad (1.10)$$

$$(\alpha - 1)^2 = 0 \quad (1.11)$$

$$\alpha = 1 \quad (1.12)$$

1.2 b

Calculating the line integral of 1.13 from $O(0, 0)$ to $A(1, e - 1)$ along $y = e^x - 1$:

$$I = \int_O^A (ye^{-2x}) (dx + dy) \quad (1.13)$$

$$y = e^x - 1 \quad (1.14)$$

$$dy = e^x dx \quad (1.15)$$

$$I = \int_0^1 \left((e^x - 1)(e^{-2x}) + (e^x - 1)(e^{-2x})(e^x) \right) dx \quad (1.16)$$

$$= \int_0^1 (e^{-x} - e^{-x} - e^{-2x} + 1) dx \quad (1.17)$$

$$= \int_0^1 (1 - e^{-2x}) dx \quad (1.18)$$

$$= \left[x + \frac{e^{-2x}}{2} \right]_0^1 \quad (1.19)$$

$$= 1 + \frac{e^{-2}}{2} - 0 - \frac{1}{2} \quad (1.20)$$

$$I = \frac{1}{2} (e^{-2} + 1) \quad (1.21)$$

1.3 c

1.3.1 i

$$\underline{F}(x, y, z) = \begin{pmatrix} \frac{y}{x^2} \\ \frac{x}{y^2} \end{pmatrix} \quad (1.22)$$

$$\nabla \cdot \underline{F} = \begin{pmatrix} \frac{\partial}{\partial x} \\ \frac{\partial}{\partial y} \end{pmatrix} \cdot \begin{pmatrix} \frac{y}{x^2} \\ \frac{x}{y^2} \end{pmatrix} \quad (1.23)$$

$$= \frac{\partial}{\partial x} \left(\frac{y}{x^2} \right) + \frac{\partial}{\partial y} \left(\frac{x}{y^2} \right) \quad (1.24)$$

$$= -\frac{2y}{x^3} - \frac{2x}{y^3} \quad (1.25)$$

$$= -2 \left(\frac{y}{x^3} + \frac{x}{y^3} \right) \quad (1.26)$$

1.3.2 ii

$$I = \int_1^2 \int_1^2 \left(-2 \left(\frac{y}{x^3} + \frac{x}{y^3} \right) \right) dx dy \quad (1.27)$$

$$= \int_1^2 \left[-2 \left(\frac{y}{-2x^2} + \frac{x^2}{2y^3} \right) \right]_1^2 dy \quad (1.28)$$

$$= \int_1^2 \left[-2 \left(-\frac{y}{8} + \frac{2}{y^3} + \frac{y}{2} - \frac{1}{2y^3} \right) \right] dy \quad (1.29)$$

$$= \int_1^2 \left(-\frac{3y}{4} - \frac{3}{y^3} \right) dy \quad (1.30)$$

$$= \left[-\frac{3y^2}{8} + \frac{3}{2y^2} \right]_1^2 \quad (1.31)$$

$$= -\frac{3}{2} + \frac{3}{8} + \frac{3}{8} - \frac{3}{2} \quad (1.32)$$

$$I = -\frac{9}{4} \quad (1.33)$$

1.4 d

1.4.1 i

$$I = \int (\sin x \cos y dy + \cos x \sin y dx) \quad (1.34)$$

$$y = 0 \quad dy = 0 \quad (1.35)$$

$$I_{AB} = \int_{x=0}^{\pi} (\sin x) dx = [-\cos x]_0^{\pi} = 2 \quad (1.36)$$

$$x = \pi \quad dx = 0 \quad (1.37)$$

$$I_{BC} = \int_{y=0}^{\pi} (-\sin y) dy = [\cos y]_0^{\pi} = -2 \quad (1.38)$$

$$\therefore I = I_{AB} + I_{BC} = 2 - 2 = 0 \quad (1.39)$$

1.4.2 ii

$$I = \int (\sin x \cos y dy + \cos x \sin y dx) \quad (1.40)$$

$$y = x \quad dy = dx \quad (1.41)$$

$$I_{AC} = \int_0^{\pi} (\sin x \cos x + \sin x \cos x) dx \quad (1.42)$$

$$= \int_0^{\pi} (\sin (2x)) dx \quad (1.43)$$

$$I_{AC} = \left[-\frac{1}{2} \cos (2x) \right]_0^{\pi} = \frac{1}{2} - \frac{1}{2} = 0 \quad (1.44)$$

$$(1.45)$$

1.5 e

1.5.1 i

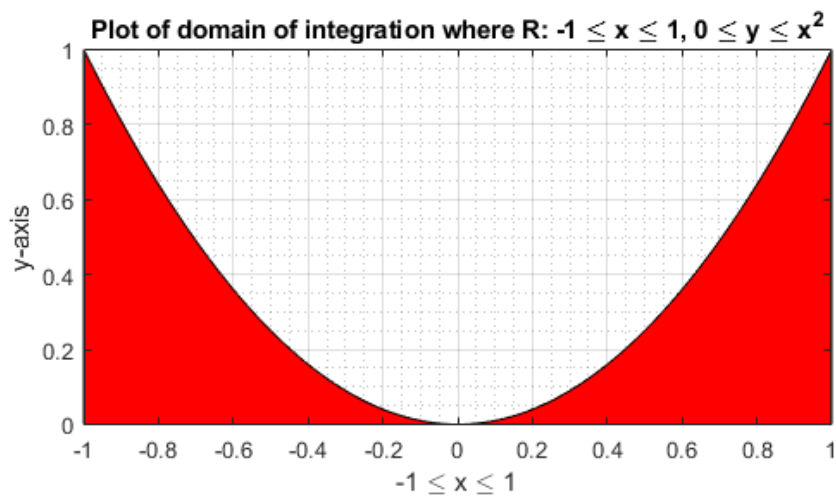


Figure 1: Domain of integration where $R: -1 \leq x \leq 1, 0 \leq y \leq x^2$.

```
1  clf
2  x=-1:0.001:1;
3  y=x.^2;
4  A=area(x,y);
5  set(A(1),'FaceColor','red');
6  axis('image');
7  xlabel('-1 \leq x \leq 1')
8  ylabel('y-axis')
9  title('Plot of domain of integration where R: -1 \leq x \leq 1, 0 \leq y
        \leq x^2')
10 grid on
11 grid minor
```

1.5.2 ii

1.6 f

1.6.1 ii

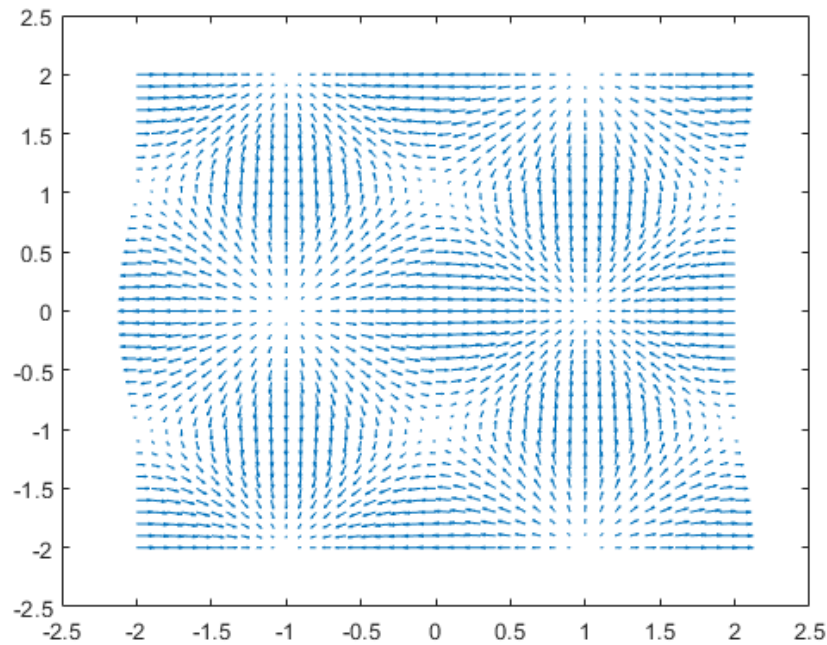


Figure 2:

```
1  clc
2  clear
3  close all
4
5  syms x y
6  z = x*y*exp(-sqrt(x^2 + y^2));
7  f = (sin((pi/2)*x))*(cos((pi/2)*y));
8  g = gradient(f,[x,y]);
9
10 [X, Y] = meshgrid(-2:0.1:2,-2:0.1:2);
11 G1 = subs(g(1),[x y],{X,Y});
12 G2 = subs(g(2),[x y],{X,Y});
13 quiver(X,Y,G1,G2)
```

2 Question 2

2.1 a

In our series of equations, there are three unknown internal bar forces N_{12} , N_{23} , N_{13} , and three unknown reaction forces, R_{2x} , R_{2y} , R_{3y} . We also have two unknown angles, α and β , and the force F . Given that there are six unknowns that we would like to find and six equations with those variables,

the conditions are fulfilled to solve this using matrices. Our answer would be in terms of the variables α , β and F . Values may be assumed for these or we can calculate them, if we have the length of each member.

2.2 b

$$\begin{bmatrix} -\cos \alpha & \cos \beta & 0 & 0 & 0 & 0 \\ -\sin \alpha & -\sin \beta & 0 & 0 & 0 & 0 \\ \cos \alpha & 1 & 0 & 1 & 0 & 0 \\ \sin \alpha & 0 & 0 & 0 & 1 & 0 \\ 0 & -\cos \beta & -1 & 0 & 0 & 0 \\ 0 & \sin \beta & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} N_{12} \\ N_{13} \\ N_{23} \\ R_{2x} \\ R_{2y} \\ R_{3y} \end{bmatrix} = \begin{bmatrix} 0 \\ F \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad (2.1)$$

2.3 c

```

1  clc
2  clear
3  close all
4
5  alpha = 0.927295;
6  beta = 0.643501;
7  F = 1000;
8
9  A = [-cos(alpha) cos(beta) 0 0 0 0;
10      -sin(alpha) -sin(beta) 0 0 0 0;
11      cos(alpha) 0 1 1 0 0;
12      sin(alpha) 0 0 0 1 0;
13      0 -cos(beta) -1 0 0 0;
14      0 sin(beta) 0 0 0 1];
15  B = [0; F; 0; 0; 0; 0];
16
17  sol = A\B;
```

This returned the following:

$$\begin{bmatrix} N_{12} \\ N_{13} \\ N_{23} \\ R_{2x} \\ R_{2y} \\ R_{3y} \end{bmatrix} = \begin{bmatrix} -800 \\ -600 \\ 480 \\ 0 \\ 640 \\ 360 \end{bmatrix} \quad (2.2)$$

2.4 d

```

1  clc
2  clear
3  close all
```

```

4
5 alpha = 0.927295;
6 beta = 0.643501;
7 F = 1000;
8
9 A = [-cos(alpha) cos(beta) 0 0 0 0;
10      -sin(alpha) -sin(beta) 0 0 0 0;
11      cos(alpha) 0 1 1 0 0;
12      sin(alpha) 0 0 0 1 0;
13      0 -cos(beta) -1 0 0 0;
14      0 sin(beta) 0 0 0 1];
15 B = [0; F; 0; 0; 0; 0];
16
17 [L,U] = lu(A); %splits matrix A such that A = L*U, L is lower triangular,
18               U is upper triangular
19 y = L\B;
20 sol = U\y;

```

This returned the following:

$$\begin{bmatrix} N_{12} \\ N_{13} \\ N_{23} \\ R_{2x} \\ R_{2y} \\ R_{3y} \end{bmatrix} = \begin{bmatrix} -800 \\ -600 \\ 480 \\ 0 \\ 640 \\ 360 \end{bmatrix} \quad (2.3)$$

2.5 e

Matlab App Developer was utilised to create a user friendly interface for inputting the Force F , the lengths of each member (as shown in the diagram) and the coefficient matrix (where any mathematical expression can be inputted). The GUI displays the angles α and β as well as a table of values for each of the internal bar and reaction forces. The code is shown below.

```

1 classdef q2eApp_exported < matlab.apps.AppBase
2
3     % Properties that correspond to app components
4     properties (Access = public)
5         UIFigure          matlab.ui.Figure
6         ForceNLabel       matlab.ui.control.Label
7         Force              matlab.ui.control.NumericEditField
8         L12mLabel         matlab.ui.control.Label
9         L12                matlab.ui.control.NumericEditField
10        L23mLabel         matlab.ui.control.Label
11        L23                matlab.ui.control.NumericEditField
12        L13mLabel         matlab.ui.control.Label
13        L13                matlab.ui.control.NumericEditField
14        UITable            matlab.ui.control.Table
15        FindForcesButton   matlab.ui.control.Button
16        betaGaugeLabel     matlab.ui.control.Label
17        betaGauge          matlab.ui.control.NinetyDegreeGauge
18        alphaGaugeLabel    matlab.ui.control.Label

```

```

19         alphaGauge          matlab.ui.control.NinetyDegreeGauge
20         ProgrammetocalculateforcesLabel  matlab.ui.control.Label
21         UITable2             matlab.ui.control.Table
22         Label                matlab.ui.control.Label
23     end
24
25     % Callbacks that handle component events
26     methods (Access = private)
27
28         % Code that executes after component creation
29         function startupFcn(app)
30             %initialise table
31             ATable = ["-cos(alpha)" "cos(beta)" "0" "0" "0" "0";
32                     "-sin(alpha)" "-sin(beta)" "0" "0" "0" "0";
33                     "cos(alpha)" "0" "1" "1" "0" "0";
34                     "sin(alpha)" "0" "0" "0" "1" "0";
35                     "0" "-cos(beta)" "-1" "0" "0" "0";
36                     "0" "sin(beta)" "0" "0" "0" "1"];
37             %display table and assign table properties
38             set(app.UITable2, 'Visible', 'on');
39             set(app.UITable2, 'Data', ATable, 'ColumnFormat', {'char'});
40             set(app.UITable2, 'ColumnEditable', true(1,6))
41         end
42
43         % Button pushed function: FindForcesButton
44         function FindForcesButtonPushed(app, event)
45             %calculate alpha and beta
46             alpha = acos((app.L12.Value^2 + app.L23.Value^2 - app.L13.
47                     Value^2)/(2*app.L12.Value*app.L23.Value));
48             beta = acos((app.L13.Value^2 + app.L23.Value^2 - app.L12.
49                     Value^2)/(2*app.L13.Value*app.L23.Value));
50
51             %conversion for display gauges
52             app.alphaGauge.Value = rad2deg(alpha);
53             app.betaGauge.Value = rad2deg(beta);
54
55             %matrix maths
56             A = get(app.UITable2, 'Data');
57             %convert user inputs into expressions and evaluate
58             c = size(A);
59             c = c(1)*c(2);
60             for i = 1:c
61                 A(i) = eval(A(i));
62             end
63             A = str2double(A);
64             B = [0; app.Force.Value; 0; 0; 0; 0];
65             sol = A\B;
66             for i = 1:length(B)
67                 if sol(i) < 0.01 && sol(i) > -0.01
68                     sol(i) = 0;
69                 end
70             end
71             namesForces = ["L12"; "L13"; "L23"; "R2x"; "R2y"; "R3y"];

```



```

70         vars = [namesForces sol];
71
72         %output to table
73         set(app.UITable, 'Visible', 'on');
74         set(app.UITable, 'Data', vars, 'ColumnFormat',{ 'numeric' });
75
76     end
77 end
78
79 % Component initialization
80 methods (Access = private)
81
82     % Create UIFigure and components
83     function createComponents(app)
84
85         % Create UIFigure and hide until all components are created
86         app UIFigure = uifigure('Visible', 'off');
87         app UIFigure.Position = [100 100 762 598];
88         app UIFigure.Name = 'MATLAB App';
89
90         % Create ForceNLabel
91         app.ForceNLabel = uilabel(app UIFigure);
92         app.ForceNLabel.HorizontalAlignment = 'right';
93         app.ForceNLabel.Position = [32 403 56 22];
94         app.ForceNLabel.Text = 'Force (N)';
95
96         % Create Force
97         app.Force = uieditfield(app UIFigure, 'numeric');
98         app.Force.Position = [103 403 100 22];
99
100        % Create L12mLabel
101        app.L12mLabel = uilabel(app UIFigure);
102        app.L12mLabel.HorizontalAlignment = 'right';
103        app.L12mLabel.Position = [41 370 47 22];
104        app.L12mLabel.Text = 'L12 (m)';
105
106        % Create L12
107        app.L12 = uieditfield(app UIFigure, 'numeric');
108        app.L12.Position = [103 370 100 22];
109
110        % Create L23mLabel
111        app.L23mLabel = uilabel(app UIFigure);
112        app.L23mLabel.HorizontalAlignment = 'right';
113        app.L23mLabel.Position = [41 349 47 22];
114        app.L23mLabel.Text = 'L23 (m)';
115
116        % Create L23
117        app.L23 = uieditfield(app UIFigure, 'numeric');
118        app.L23.Position = [103 349 100 22];
119
120        % Create L13mLabel
121        app.L13mLabel = uilabel(app UIFigure);
122        app.L13mLabel.HorizontalAlignment = 'right';

```

```

123     app.L13mLabel.Position = [41 328 47 22];
124     app.L13mLabel.Text = 'L13 (m)';
125
126     % Create L13
127     app.L13 = uieditfield(app.UIFigure, 'numeric');
128     app.L13.Position = [103 328 100 22];
129
130     % Create UITable
131     app.UITable = uitable(app.UIFigure);
132     app.UITable.ColumnName = {'Force'; 'Value (N)'};
133     app.UITable.RowName = {};
134     app.UITable.Position = [272 59 479 185];
135
136     % Create FindForcesButton
137     app.FindForcesButton = uibutton(app.UIFigure, 'push');
138     app.FindForcesButton.ButtonPushedFcn = createCallbackFcn(app,
        @FindForcesButtonPushed, true);
139     app.FindForcesButton.Position = [103 292 100 22];
140     app.FindForcesButton.Text = 'Find Forces';
141
142     % Create betaGaugeLabel
143     app.betaGaugeLabel = uilabel(app.UIFigure);
144     app.betaGaugeLabel.HorizontalAlignment = 'center';
145     app.betaGaugeLabel.Position = [186 117 29 22];
146     app.betaGaugeLabel.Text = 'beta';
147
148     % Create betaGauge
149     app.betaGauge = uigauge(app.UIFigure, 'ninetydegree');
150     app.betaGauge.Limits = [0 90];
151     app.betaGauge.Position = [154 154 90 90];
152
153     % Create alphaGaugeLabel
154     app.alphaGaugeLabel = uilabel(app.UIFigure);
155     app.alphaGaugeLabel.HorizontalAlignment = 'center';
156     app.alphaGaugeLabel.Position = [62 117 35 22];
157     app.alphaGaugeLabel.Text = 'alpha';
158
159     % Create alphaGauge
160     app.alphaGauge = uigauge(app.UIFigure, 'ninetydegree');
161     app.alphaGauge.Limits = [0 90];
162     app.alphaGauge.Orientation = 'northeast';
163     app.alphaGauge.ScaleDirection = 'counterclockwise';
164     app.alphaGauge.Position = [34 154 90 90];
165
166     % Create ProgrammetocalculateforcesLabel
167     app.ProgrammetocalculateforcesLabel = uilabel(app.UIFigure);
168     app.ProgrammetocalculateforcesLabel.HorizontalAlignment = '
        right';
169     app.ProgrammetocalculateforcesLabel.FontSize = 20;
170     app.ProgrammetocalculateforcesLabel.FontWeight = 'bold';
171     app.ProgrammetocalculateforcesLabel.Position = [441 534 306
        56];

```

```

172         app.ProgrammetocalculateforcesLabel.Text = 'Programme to
           calculate forces';
173
174     % Create UITable2
175     app.UITable2 = uitable(app.UIFigure);
176     app.UITable2.ColumnName = {'L12'; 'L13'; 'L23'; 'R2x'; 'R2y';
           'R3y'};
177     app.UITable2.RowName = {};
178     app.UITable2.ColumnEditable = true;
179     app.UITable2.Position = [272 264 479 193];
180
181     % Create Label
182     app.Label = uilabel(app.UIFigure);
183     app.Label.HorizontalAlignment = 'right';
184     app.Label.Position = [202 479 545 56];
185     app.Label.Text = {'Please input the force F, the lengths of
           the members L12, L23 and L13.'; 'The programme will then
           calculate the values of alpha and beta and display them to
           you.'; 'If you would like to change the coefficient matrix
           , look to the table on the right and adjust as you like.';
           'Click "Find Forces" to calculate the values of the
           internal bar forces and the reaction forces.'};
186
187     % Show the figure after all components are created
188     app.UIFigure.Visible = 'on';
189 end
190
191 % App creation and deletion
192 methods (Access = public)
193
194     % Construct app
195     function app = q2eApp_exported
196
197         % Create UIFigure and components
198         createComponents(app)
199
200         % Register the app with App Designer
201         registerApp(app, app.UIFigure)
202
203         % Execute the startup function
204         runStartupFcn(app, @startupFcn)
205
206         if nargin == 0
207             clear app
208         end
209 end
210
211 % Code that executes before app deletion
212 function delete(app)
213
214     % Delete UIFigure when app is deleted
215     delete(app.UIFigure)
216

```

```

217         end
218     end
219 end

```

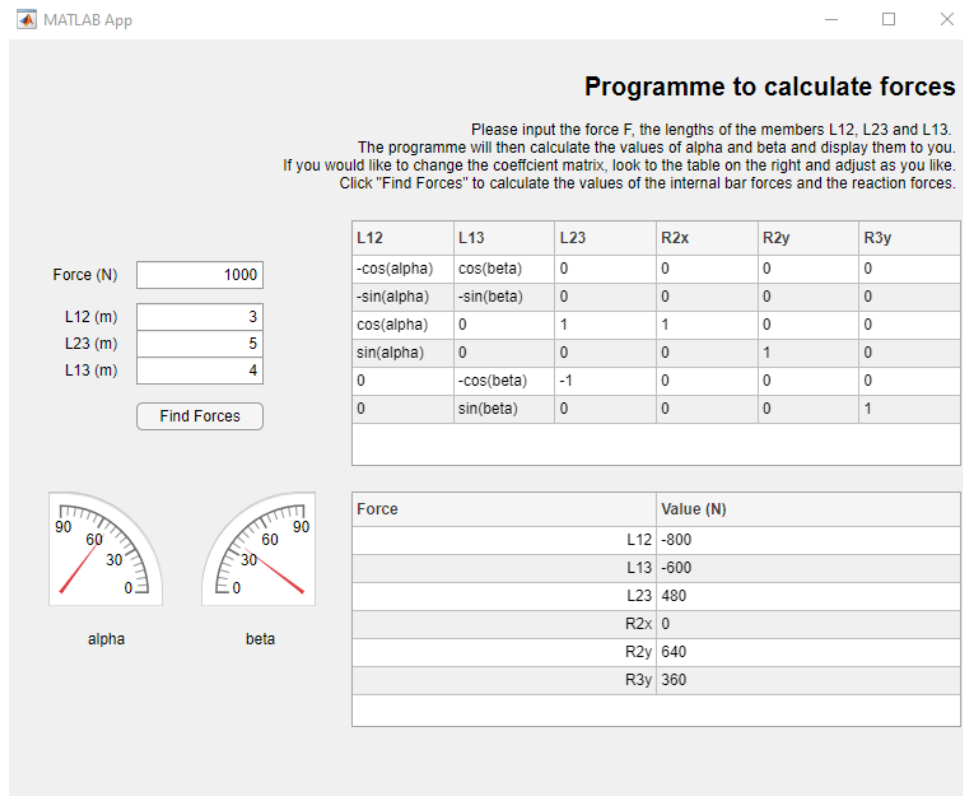


Figure 3: Screenshot from Matlab App, showcasing GUI, input and output parameters.

2.6 f

Code was written to generate a table of data:

```

1  clc
2  clear
3  close all
4  %forces
5  F = [1000 3000 4500];
6
7  %lengths of members
8  L12 = [6 8 5];
9  L23 = [10 12 8];
10 L13 = [9 7 4];
11
12 %initilise matrix
13 sol = zeros(9,10);
14
15 %initilise counter
16 counter = 0;
17
18 %nested loops, iterates between F and then between A1, A2, A3 and stores
    in sol matrix

```

```

19  for i = 1:3
20      for j = 1:3
21          %calculate alpha and beta
22          alpha = acos((L12(j)^2 + L23(j)^2 - L13(j)^2)/(2*L12(j)*L23(j)));
23          beta = acos((L13(j)^2 + L23(j)^2 - L12(j)^2)/(2*L13(j)*L23(j)));
24
25          %calculate A and B matrices
26          A = [-cos(alpha) cos(beta) 0 0 0 0;
27              -sin(alpha) -sin(beta) 0 0 0 0;
28              cos(alpha) 0 1 1 0 0;
29              sin(alpha) 0 0 0 1 0;
30              0 -cos(beta) -1 0 0 0;
31              0 sin(beta) 0 0 0 1];
32          B = [0; F(i); 0; 0; 0; 0];
33
34          %generate result
35          temp = (A\B)';
36
37          %increment counter
38          counter = counter + 1;
39
40          %store result
41          sol(counter, 5:10) = temp;
42      end
43  end
44
45  %table formatting
46  sol(:,1) = repelem(F',3,1);
47  sol(:,2) = repmat(L12',3,1);
48  sol(:,3) = repmat(L13',3,1);
49  sol(:,4) = repmat(L23',3,1);
50
51  %swap L13 and L23 columns
52  v = sol(:, 7);
53  sol(:, 7) = sol(:, 6);
54  sol(:, 6) = v;
55
56  %clean up values
57  for i=1:numel(sol)
58      if sol(i) < 0.01 && sol(i) > -0.01
59          sol(i) = 0;
60      end
61  end
62
63  %table generation
64  T = array2table(sol);
65  T.Properties.VariableNames = {'Force', 'L12', 'L23', 'L13', 'N12', 'N13',
    'N23', 'R2x', 'R2y', 'R3y'};

```

| | 1 Force | 2 L12 | 3 L23 | 4 L13 | 5 N12 | 6 N13 | 7 N23 | 8 R2x | 9 R2y | 10 R3y |
|---|------------|----------|----------|----------|-------------|------------|-------------|----------|------------|------------|
| 1 | 1000 | 6 | 9 | 10 | -815.7246 | 373.8738 | -464.1192 | 0 | 725 | 275.0000 |
| 2 | 1000 | 8 | 7 | 12 | -799.0757 | 661.7346 | -861.7938 | 0 | 447.9167 | 552.0833 |
| 3 | 1000 | 5 | 4 | 8 | -1.0504e+03 | 958.4751 | -1.1153e+03 | 0 | 429.6875 | 570.3125 |
| 4 | 3000 | 6 | 9 | 10 | -2.4472e+03 | 1.1216e+03 | -1.3924e+03 | 0 | 2175 | 825.0000 |
| 5 | 3000 | 8 | 7 | 12 | -2.3972e+03 | 1.9852e+03 | -2.5854e+03 | 0 | 1.3438e+03 | 1.6562e+03 |
| 6 | 3000 | 5 | 4 | 8 | -3.1512e+03 | 2.8754e+03 | -3.3459e+03 | 0 | 1.2891e+03 | 1.7109e+03 |
| 7 | 4500 | 6 | 9 | 10 | -3.6708e+03 | 1.6824e+03 | -2.0885e+03 | 0 | 3.2625e+03 | 1.2375e+03 |
| 8 | 4500 | 8 | 7 | 12 | -3.5958e+03 | 2.9778e+03 | -3.8781e+03 | 0 | 2.0156e+03 | 2.4844e+03 |
| 9 | 4500 | 5 | 4 | 8 | -4.7267e+03 | 4.3131e+03 | -5.0189e+03 | 0 | 1.9336e+03 | 2.5664e+03 |

Table 1: Table of data generated from MATALB, showing forces in three configuration with three different loads.

| Force (N) | L12 (m) | L13 | L23 | N12 (N) | N13 | N23 | R2x | R2y | R3y |
|--------------|------------|-----|-----|------------|--------|---------|-----|--------|--------|
| 1000 | 6 | 9 | 10 | -815.7 | 373.9 | -464.1 | 0 | 725.0 | 275.0 |
| 1000 | 8 | 7 | 12 | -799.1 | 661.7 | -861.8 | 0 | 447.9 | 552.1 |
| 1000 | 5 | 4 | 8 | -1050.4 | 958.5 | -1115.3 | 0 | 429.7 | 570.3 |
| 3000 | 6 | 9 | 10 | -2447.2 | 1121.6 | -1392.4 | 0 | 2175.0 | 825.0 |
| 3000 | 8 | 7 | 12 | -2397.2 | 1985.2 | -2585.4 | 0 | 1343.8 | 1656.3 |
| 3000 | 5 | 4 | 8 | -3151.2 | 2875.4 | -3346.0 | 0 | 1289.1 | 1710.9 |
| 4500 | 6 | 9 | 10 | -3670.8 | 1682.4 | -2088.5 | 0 | 3262.5 | 1237.5 |
| 4500 | 8 | 7 | 12 | -3595.8 | 2977.8 | -3878.1 | 0 | 2015.6 | 2484.4 |
| 4500 | 5 | 4 | 8 | -4726.7 | 4313.1 | -5018.9 | 0 | 1933.6 | 2566.4 |

Table 2: Table formatted as requested in question.