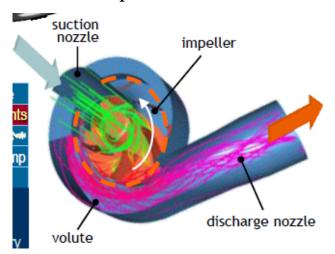
0.1 Centrifugal pumps

0.1.1 Functional principle

Centrifugal pump's working principle can be understood very simply if you think about what happens to the liquid level when you steer a liquid in a glass: the free surface of the liquid becomes concave, and rises from the centre to the periphery - you are raising the flow head at the periphery.

0.1.2 Functional components



The fluid enters axially and receives tangential and radial velocity by momentum transfer from rotating blades. The centrifugal force provides further radial velocity. Then the flow is collected and decelerated, in order to increase its pressure before it leaves the pump. The process produces depression at the pump axis, which sucks new fluid. The functional components of centrifugal pumps are:

- The suction nozzle: leads the fluid from pump inlet to the impeller eye. It is usually a cylindrical or truncated conical tube and can have stationary vanes to induce some spinning to the suction flow
- The impeller: it is rotating component that provides momentum to the fluid. It can have many different features, that we will analyse in more detail later on
- The volute (or scroll): decelerates the fluid, converting the momentum into pressure, and delivers it to the discharge pipe. It has a gradually enlarging section (which gives its snail-shape) and can have stationary blades

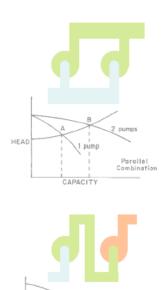
0.1.3 Pumps arrangement

We have already mentioned the main functional limitations of roto-dynamic pumps over positive-displacement pumps:

- Adjustment o capacity requires changes in the operating speed and affects the efficiency
- The net head is lower and its adjustment requires significant changes in the operating speed and efficiency

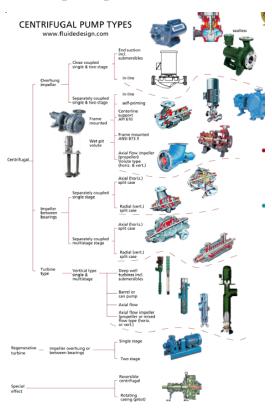
These limitations can be overcome by using two or more pumps in **parallel** or in **series**.

- Pumps operating in parallel: two or more pumps are used to draw fluid from the same source and discharge it to a single pipe. This arrangement allows variable discharge arrangement in terms of capacity
- Pumps operating in series: the discharge from one pump is piped into the suction nozzle of a flowing pump. Each pump adds energy to the same fluid, increasing the final net head. Efficiency decrease for more than 10-12 impellers



CAPACITY

0.1.4 End-suction pump



The different operating requirements have produced a large number of possible centrifugal pump designs. We will consider the most common version, which is called **end-suction centrifugal pump**, and consists of the following parts:

- A rotating component called rotor (red)
 - Impeller blades, hub and shroud
 - Shaft
- A stationary component (green)
 - Suction nozzle
 - Scroll casing (or volute casing)
 - Pump casing
 - Back cover
 - Bearings

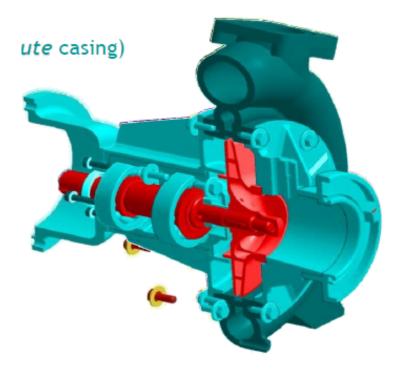


Figure 1: End-suction centrifugal pump

0.1.5 The Impeller

The **impeller** is the rotating component that provides the momentum to the fluid. It can be classified based on the major direction of the flow at the exit from the blades.

- Axial flow the flow leaves the impeller parallel to the axis of rotation
- Mixed flow the flow leaves the impeller at an angle with the axis of rotation
- Radial flow the flow leaves the impeller orthogonal to the axis of rotation

It can be classified based on the suction type.

- Single suction the liquid inlet to the impeller is on one side only
- Double suction the liquid inlet to the impeller is symmetrical from two sides. The provides a very stable hydraulic performance because the hydraulic forces are balanced

It can be classified based on the presence of shrouds.

- Open impeller blades are supported almost entirely by the impeller hub. It is primarily applied to clean, non-abrasive, low-horsepower applications and operates at a high efficiency
- Enclosed impeller incorporates a full front and back shroud. Fluid flows without hydraulic interaction with the casing walls. The friction caused by the small gap between shroud and casing reduces efficiency
- Semi-closed impeller incorporates a single shroud, usually located on the back of the impeller. It is more efficient than an enclosed impeller (lower disc friction and tighter axial clearances). Compared to an open impeller it can be adjusted axially to compensate for casing wear. We will be designing one of these

It can be classified based on the blade geometry.

- Backward inclined have the highest efficiency (the fluid experiences the minimum amount of turning) and intermediate pressure rise
- Radial produce the highest pressure rise. Pressure rise drops suddenly after the BEP. Efficiency is intermediate
- Forward inclined produce a lower but more constant pressure rise over different flow rates. Efficiency is lower

0.1.6 Flow into the impeller

The design of the blades has to take into account the velocity flow through the impeller: The flow field into the impeller is:

- Unsteady
- Fully three-dimensional
- May be compressible

Assumptions:

- Steady flow
- We do not consider axial velocity we consider only the normal (n) and tangential (t) components in the impeller plane
- We consider incompressible flow

- No leakage in practice leakage will be considered by increasing the volume flow rate using in the design calculation
- We consider the flow to be always tangential to the blades surface when viewed from a reference frame rotating with the blades (shockless entry and no flow separation)

Efficient designs are aimed at accommodating the fluid flow into the impeller. The flow velocities into the impeller ensure the requirements to be met (are linked to Q and H) and are the combination of:

- Velocity of the fluid 'relative' to the blades
- Velocity of the blades

Velocities of the blades are known both in direction and magnitude, everywhere in the impeller.

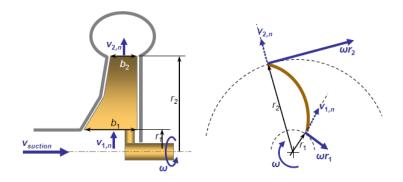
- Direction: orthogonal to the radius (tangential direction)
- Magnitude: depending on the angular velocity ω of the impeller and on the local radius r.

$$v_{r, \text{ blade}} = \omega r$$
 (1)

$$V_{1, \text{ blade}} = \omega r_1 \tag{2}$$

$$V_{2, \text{ blade}} = \omega r_2 \tag{3}$$

(4)



Velocities of the flow relative to the blades, we know the radial component and the direction. Due to conservation of mass and incompressibility

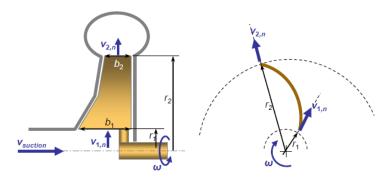
assumption. The flow rate at each radius has to be the same (equal to the suction flow rate).

if
$$Q = A_{\text{suction}} \times v_{\text{suction}}$$
 (5)

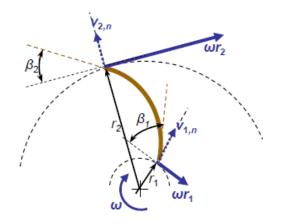
$$Q = 2\pi r_1 b_1 \times v_{1,n} = 2\pi r_2 b_2 \times v_{2,n} \tag{6}$$

$$v_{2,n} = v_{1,n} \frac{r_1 b_1}{r_2 b_2} \tag{7}$$

where subscript n signifies the normal component.



- Direction: due to no-separation condition, direction is parallel to the blade surfaces
- At the inlet and outlet edges $(v_{1,rel} \text{ and } v_{2,rel})$ they form angles with the tangential direction respectively equal to β_1 and β_2



The leading edge angle β_1 is defined as the blade angle relative to the reverse tangential direction at radius r_1 and the trailing edge angle β_2 as the blade angle relative to the reverse tangential direction at radius r_2 . We can combine all information and apply the parallelogram rule to calculate

- $\bullet\,$ The magnitude of $v_{1,rel}$ and $v_{2,rel}$
- ullet The absolute fluid velocities V_1 and V_2 in direction and magnitude

