UCL Mechanical Engineering 2021/2022

MECH0026 Problem Sheet 1 Solutions

HD

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1

1.1

For plane stress, our assumption is that our stress tensors relating to the z-direction are 0. For plane strain, our assumption is that there is no displacement in the z-direction.

 $\mathbf{2}$

$$\phi = \frac{P}{20h^3} \left(15h^2x^2y - 5x^2y^3 - 2h^2y^3 + y^5 \right)$$
 (2.1)

$$\sigma_x = \frac{\partial^2 \phi}{\partial y^2} = \frac{P}{20h^3} \left(20y^3 - 30x^2y - 12h^2y \right)$$
 (2.2)

$$\sigma_y = \frac{\partial^2 \phi}{\partial x^2} = \frac{P}{20h^3} \left(30h^2 xy - 10xy^3 \right) \tag{2.3}$$

$$\tau_{xy} = -\frac{\partial^2 \phi}{\partial x \partial y} = -\frac{P}{20h^3} \left(20h^2 x - 30xy^2 \right) \tag{2.4}$$