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	6.8	Maximum Matching	3						
	6.9	HL Decomposition	3						
7	Line	ear Programming	3						
	7.1	Simplex	3						

```
16 // Algorithm
17 // Algorithm
18 // Algorithm
19 // From 3 Lines
    1 2D Geometry
    1.1 Primitives
 1 typedef complex<double> point;
                                                                       20 // Algorithm
21 // Algorithm
   struct circle {
  point c; double r;
                                                                       22 // Algorithm
      circle(point c, double r):c(c),r(r){}
                                                                       23 // Algorithm
     circle(){}
                                                                        24 // Algorithm
 6 };
   double cross(const point &a, const point &b) {
 7
                                                                           1.4 Heron Triangle Area
     return imag(conj(a)*b);
 9 }
                                                                        1 // Formula
double dot(const point &a, const point &b) {
                                                                         2 // Formula
11
     return real(conj(a)*b);
                                                                         3 // Formula
                                                                           1.5 Polygon Centroid
    1.2 Intersections
                                                                         1 for(int i = 1; i < n-1; i++) {</pre>
 1 // Line - Line
                                                                             pt ai = pts[i] - pts[i-1],
ib = pts[i+1] - pts[i];
 2 // Algorithm
 3 // Algorithm
                                                                             area += (conj(ai)*ib).imag();
 4 // Algorithm
 5 // Algorithm
 6 // Algorithm
                                                                           1.6 Point In Polygon
 7 // Line - Segment
 8 // Algorithm
 9 // Algorithm
                                                                         1 // Algorithm
                                                                         2 // Algorithm
10 // Algorithm
11 // Algorithm
                                                                         3 // Algorithm
12 // Algorithm
                                                                         4 // Algorithm
                                                                         5 // Algorithm
6 // Algorithm
13 // Segment - Segment
14 // Algorithm
15 // Algorithm
                                                                         7 // Algorithm
16 // Algorithm
17 // Algorithm
                                                                         8 // Algorithm
                                                                         9 // Algorithm
                                                                        10 // Algorithm
18 // Algorithm
19 // Circle - Line
                                                                        11 // Algorithm
20 // Algorithm
21 // Algorithm
22 // Algorithm
23 // Algorithm
                                                                        12 // Algorithm
                                                                       13 // Algorithm
14 // Algorithm
                                                                       15 // Algorithm
24 // Algorithm
25 // Circle - Segment
                                                                       16 // Algorithm
                                                                       17 // Algorithm
26 // Algorithm
27 // Algorithm
                                                                       18 // Algorithm
                                                                        19 // Algorithm
                                                                        20 // Algorithm
28 // Algorithm
29 // Algorithm
30 // Algorithm
31 // Circle - Circle
                                                                           1.7 Convex Hull
32 // Algorithm
33 // Algorithm
                                                                         1 // Algorithm
                                                                         2 // Algorithm
34 // Algorithm
35 // Algorithm
                                                                        3 // Algorithm
4 // Algorithm
36 // Algorithm
                                                                         5 // Algorithm
                                                                         6 // Algorithm
37 // Line - Point
                                                                        7 // Algorithm
8 // Algorithm
38 // Algorithm
39 // Algorithm
40 // Algorithm
                                                                         9 // Algorithm
41 // Algorithm
                                                                        10 // Algorithm
                                                                       11 // Algorithm
12 // Algorithm
42 // Algorithm
43 // Segment - Point
44 // Algorithm
                                                                       13 // Algorithm
45 // Algorithm
                                                                        14 // Algorithm
46 // Algorithm
                                                                       15 // Algorithm
47 // Algorithm
                                                                        16 // Algorithm
                                                                       17 // Algorithm
48 // Algorithm
                                                                        18 // Algorithm
                                                                        19 // Algorithm
   1.3 Circle Generation
                                                                        20 // Algorithm
 1 // From 3 Points
 2 // Algorithm
3 // Algorithm
                                                                           1.8 Line Segment Set Intersection
 4 // Algorithm
5 // Algorithm
                                                                         1 // Algorithm
                                                                         2 // Algorithm
 6 // Algorithm
                                                                         3 // Algorithm
                                                                         4 // Algorithm
 7 // From 1 Line 2 Points
 8 // Algorithm
                                                                         5 // Algorithm
 9 // Algorithm
                                                                         6 // Algorithm
                                                                        7 // Algorithm
8 // Algorithm
10 // Algorithm
11 // Algorithm
12 // Algorithm
                                                                         9 // Algorithm
                                                                        10 // Algorithm
13 // From 2 Lines 1 Point
14 // Algorithm
                                                                        11 // Algorithm
15 // Algorithm
                                                                        12 // Algorithm
```

```
13 // Algorithm
                                                           14 // iterate over all the subsets
                                                           15 for (int i=0; i < (1<<n); i++)
14 // Algorithm
15 // Algorithm
                                                               // iterate over all the subsets of the i-th subset
16 // Algorithm
                                                             for(int i2 = i; i2 > 0; i2 = (i2-1) & i)
17 // Algorithm
18 // Algorithm
                                                             4 Data Structures
19 // Algorithm
                                                             4.1 Palindromic Tree
20 // Algorithm
21 // Algorithm
                                                             4.2 Treap
22 // Algorithm
                                                             4.3 Sparse Array
23 // Algorithm
                                                             4.4 Skip Lists
24 // Algorithm
25 // Algorithm
                                                             5 Game Theory
26 // Algorithm
                                                             5.1 Nim Game
27 // Algorithm
28 // Algorithm
                                                             5.2 Grundy Numbers
29 // Algorithm
                                                             6 Graph Theory
30 // Algorithm
31 // Algorithm
                                                             6.1 Articulation Points & Bridges
32 // Algorithm
                                                             6.2 SCC
33 // Algorithm
34 // Algorithm
                                                             6.3 2-SAT
35 // Algorithm
                                                             6.4 Edmonds-Karp Max Flow
36 // Algorithm
                                                             6.5 Dinic's Max Flow
37 // Algorithm
38 // Algorithm
                                                             6.6 Min-Cist Max Flow
39 // Algorithm
                                                             6.7 Euler Cycles
40 // Algorithm
                                                             6.8 Maximum Matching
41 // Algorithm
42 // Algorithm
                                                             6.9 HL Decomposition
43 // Algorithm
                                                             7 Linear Programming
44 // Algorithm
45 // Algorithm
                                                                 Simplex
46 // Algorithm
                                                                Number Theory
47 // Algorithm
48 // Algorithm
                                                              8.1 Extended GCD
49 // Algorithm
                                                           1 long long gcd( long long a, long long b )
  1.9 Voronoi Diagrams
                                                             { return( b == 0 ? a : gcd( b, a % b ) ); }
                                                              //USED BY: egcd, msolve, inverse, ldioph
1 // Algorithm
                                                             template < class Int > struct Triple {
                                                           4
2 // Algorithm
                                                               Int d, x, y;
                                                           5
3 // Algorithm
                                                           6
                                                               Triple(Int q, Int w, Int e):d(q), x(w), y(e){}
 4 // Algorithm
                                                           7 };
5 // Algorithm
                                                             //USED BY: msolve, inverse, ldioph
6 // Algorithm
                                                             template< class Int > Triple< Int > egcd( Int a, Int b ) {
                                                           9
7 // Algorithm
                                                               if( !b ) return Triple< Int >( a, Int( 1 ), Int( 0 ) );
                                                           10
8 // Algorithm
                                                           1.1
                                                               Triple< Int > q = egcd( b, a % b );
9 // Algorithm
                                                               return Triple< Int >( q.d, q.y, q.x - a / b * q.y );
                                                           12
10 // Algorithm
                                                           13 }
11 // Algorithm
12 // Algorithm
                                                              8.2 Modular Inverse
13 // Algorithm
14 // Algorithm
                                                           1 //solves ax = 1 (mod n).
15 // Algorithm
                                                             template< class Int > Int inverse( Int a, Int n ) {
16 // Algorithm
                                                                 Triple< Int > t = egcd( a, n );
17 // Algorithm
                                                                 if( t.d > Int( 1 ) ) return Int( 0 );
18 // Algorithm
                                                                 Int r = t.x % n;
19 // Algorithm
                                                                 return( r < Int( 0 ) ? r + n : r );</pre>
20 // Algorithm
  2 3D Geometry
                                                             8.3 Modular Linear Equation
  2.1 Primitives
                                                             8.4
                                                                   Linear Diophantine Equation
                                                             8.5
                                                                   Modular Powers
  2.2 Convex Hull
  2.3 Great Circle Distance
                                                             8.6 Sieve of Eratosthenes
                                                             8.7 Primality Testing & Factoring
  3 Combinatorics
                                                             8.8 Euler Phi
  3.1 Basics
                                                             8.9 Chinese Remainder
 1 // catalan numbers
                                                             8.10 Discerete Logarithm
  long long C(int n) {
                                                             8.11 Gaussian Elimination
    return (C(n-1)*2*n*(2*n-1))/(n*(n+1));
return NCR(2*n, n) - NCR(2*n, n+1);
                                                             8.12 Fast Fourier-Transform
4
    return NCR(2*n, n)/(n+1);
6 }
                                                             double* GaussianElimination(int N, double **mat) {
7 // derangements
                                                               int i, j, k, L; double t;
8 long long D(int n) {
                                                               for (i = 0; i < N - 1; i++) {
    return n*D(n-1) + pow(-1, n);
                                                                 L = i;
    return (n-1)*(D(n-1) + D(n-2));
                                                                 for (j = i + 1; j < N; j++)
                                                                   if (fabs(mat[j][i]) > fabs(mat[L][i]))
                                                                     L = j;
12 // iterate over all subsets with < m elements
  for (int i = 0; i < (1<<n); i=Integer.bitCount(i) < m ? i</pre>
                                                                 for (k = i; k \le N; k++)
       +1 : (i|(i-1))+1)
                                                                 swap(mat[i][k], mat[L][k]);
```

```
for (j = i + 1; j < N; j++)
for (k = N; k >= i; k--)
10
11
                 mat[j][k] -= (mat[i][k] * mat[j][i]) / mat[i][i];
12
13
       double *res = new double[N];
for (j = N - 1; j >= 0; j--) {
  for (t = 0.0, k = j + 1; k < N; k++)
  t += mat[j][k] * res[k];</pre>
14
15
16
17
          res[j] = (mat[j][N] - t) / mat[j][j];
18
19
20
       return res;
21 }
```

## 8.13 Tortoise & Hare

```
// mu = start of cycle, lambda = cycle length
ii floyd(int x0) {
  int tortoise = f(x0), hare = f(f(x0));

while(tortoise != hare)
  tortoise = f(tortoise), hare = f(f(hare));
  int mu = 0; hare = x0;

while(tortoise != hare)
  tortoise = f(tortoise), hare = f(hare), mu++;
  int lambda = 1; hare = f(tortoise);

while(tortoise != hare)
  hare = f(hare), lambda++;
  return ii(mu, lambda);
}
```

## 9 Search

- 9.1 Binary Search
- 9.2 Ternary Search

```
long double min() {
      long double lo = -1e6, hi = 1e6, res = 3e6;
       while (fabs (lo-hi) > EPS) {
         long double left = (hi-lo)/3 + lo, right = (2*(hi-long))
               10))/3 + 10;
          long double resL = F(left), resR = F(right);
6
          if(resL < resR)</pre>
              hi = right;
          else
            lo = left;
10
           res = min(res, min(resL, resR));
11
      return res;
12
13 }
```

## 10 Strings

- 10.1 Aho Corasick
- 10.2 Hashing
- 10.3 KMP
- 10.4 Suffix Array