

Q1) Solve the following Questions (13 marks)

30 Pts



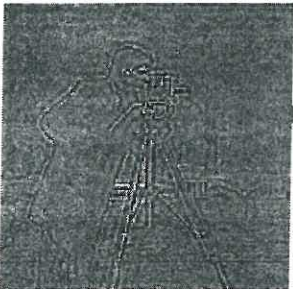
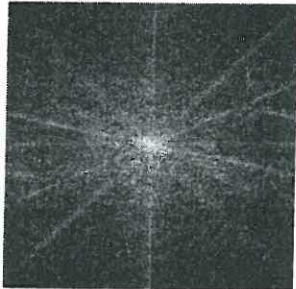

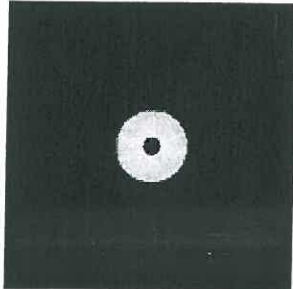

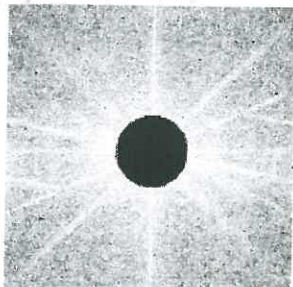
- a) Consider the following image below. Apply a 3*3 median filter on the shaded pixels, and write the filtered image (3 Pts).

20 25 30 30 30 70 80 80 255
0 20 30 70 80 255 100 100
0 70 80 80 100 100 110 120 130
30 80 100

20	30	50	80	100
30	20	80	100	110
25	255	70	0	120
30	30	80	100	130
40	50	90	125	140

- b) For the following table (7 Pts)

- (1) Associate the left images with their corresponding Fourier transform (FFT).
(2) Give the name of each filter applied on the FFT on the right.

	FFT no. <u>2</u>	FFT No 1	Filter Name: <u>low-pass</u>	
	FFT no. <u>4</u>	FFT No 2	Filter Name: <u>no-filter</u>	
	FFT no. <u>1</u>	FFT No 3	Filter Name: <u>band-pass</u>	
	FFT no. <u>3</u>	FFT No 4	Filter Name: <u>high-pass</u>	

- c) If you want to smooth an image in frequency domain, what types of filters do you use? Give three examples of such filters. (3 Pts)

Ideal low pass filter $H(u,v) = \begin{cases} 1 & \text{if } D(u,v) \leq D_0 \\ 0 & \text{if } D(u,v) > D_0 \end{cases}$

Butterworth lowpass filter $H(u,v) = \frac{1}{1 + [D(u,v)/D_0]^{2n}}$

Gaussian lowpass filter $H(u,v) = e^{-D^2(u,v)/2D_0^2}$

Q2) For the following 8 x 8 image $f(x,y)$ with integer intensities in the range from 0 to 7. (6 Pts)

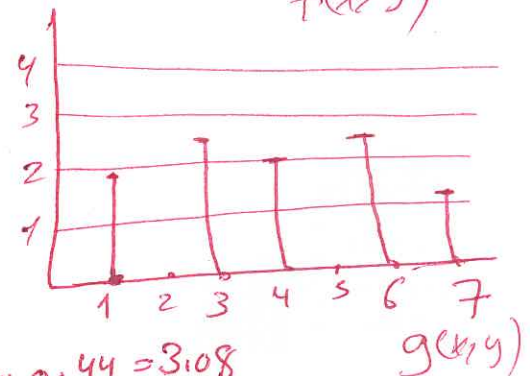
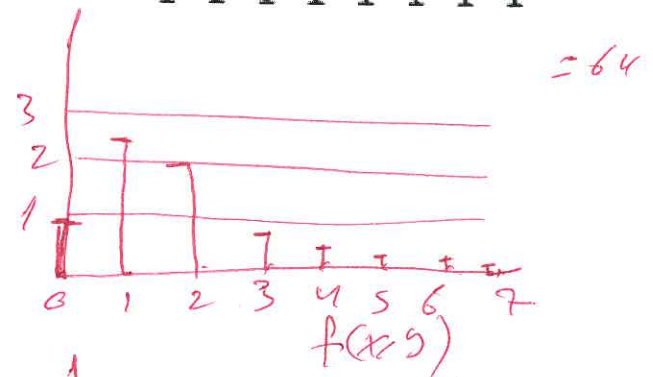
- a) Compute the histogram of the original image $f(x,y)$.
b) Find the transformed (equalized) histogram, $g(x,y)$.

Hint:

$$s_k = T(r_k) = (L-1) \sum_{j=0}^k p_r(r_j) \quad k = 0, 1, 2, \dots, L-1$$

$$p_r(r_k) = \frac{n_k}{MN}$$

1	1	1	1	1	1	1	1
0	2	5	5	5	5	2	0
0	3	2	6	7	2	3	0
0	3	3	2	2	3	3	0
0	2	3	2	2	3	3	0
0	3	2	4	4	2	4	0
0	2	6	4	4	4	2	0
1	1	1	1	1	1	1	1



$$S_0 = 7 * P_0(r_0) = 7 * 0.19 = 1.33$$

$$S_1 = 7 * [P_0(r_0) + P_1(r_1)] = 7 * [0.19 + 0.25] = 7 * 0.44 = 3.08$$

Q3) A 5 x 5 image $f(x,y)$ is given as $f(x,y) =$ (8 marks)
 Compute the output images (only the selected box) after passing through:

a) The operator as specified by the mask w_1 .

$$w_1 = \frac{1}{3} \begin{pmatrix} 1 & 0 & -1 \\ 1 & 0 & -1 \\ 1 & 0 & -1 \end{pmatrix}$$

5.67	2.67	-2
0.67	2.33	1
-2.33	1	2.67

10	3	2	5	4
11	8	3	1	6
7	5	6	2	7
2	1	9	4	2
2	3	3	0	1

b) The mask $w_2 = \frac{1}{3} \begin{pmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ -1 & -1 & -1 \end{pmatrix}$

-1	-1	-1.33
3.33	-0.67	-1.67
3.33	2.33	3.67

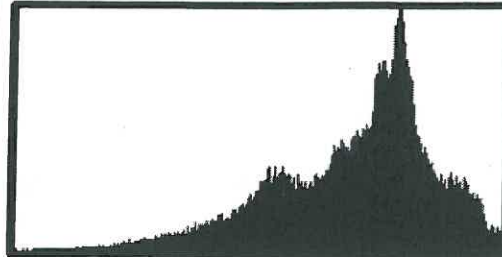
c) Explain what the function of operators w_1 and w_2 in parts a and b.

like sobel operators

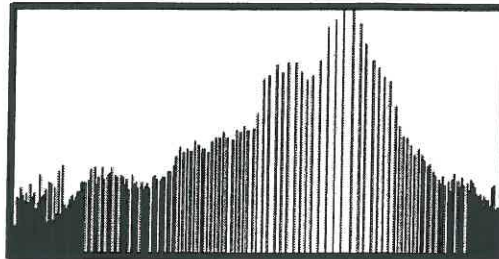
edge detection

Q4) [4 Pts] From the original image below (+ histogram) which does not show a good contrast, we perform some linear transforms in order to improve the contrast. We obtain the next image (+ histogram).

Draw (approximatively) the linear transforms needed to obtain this result. Add extra explanations if needed. Hint: Your linear transform should have at least 3 segments (piecewise linear functions).



Original image + histogram



Result image + histogram

