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# Advanced Data Structures Lab Report

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## Binary Search Tree Using an Array

```
/* Implement a BST using an array */
#include <iostream>

using namespace std;

struct BST
{
    int info;
    BST* right;
    BST* left;
} *t1, *t2;

// Inserts an element into the BST
BST* insert(BST* root)
{
    int i;
    cout << "Enter the node's value: ";
    cin >> i;
    // Empty tree
    if (root == nullptr)
    {
        root = new BST;
        root->info = i;
        root->left = root->right = nullptr;
    }
    else
    {
        t1 = root;
        t2 = nullptr;
        while ((t1->left != nullptr || t1->right != nullptr) && t2 != t1)
        {
            t2 = t1;
            while (i < t1->info && t1->left != nullptr)
                t1 = t1->left;
            while (i > t1->info && t1->right != nullptr)
                t1 = t1->right;
        }
        t2 = new BST;
        t2->info = i;
        t2->left = t2->right = nullptr;
        if (i < t1->info)
            t1->left = t2;
        else
            t1->right = t2;
    }
    return root;
}
```

```

// Push an element into the stack
int push(BST* stk[], BST* p, int top)
{
    stk[++top] = p;
    return top;
}

// Pop an element from the stack
BST* pop(BST* stk[], int* top)
{
    return stk[(*top)--];
}

// In-Order traversal of the BST
void inorder(BST* t)
{
    BST *p, *stk[20];
    int top = -1;
    p = t;
    do
    {
        while (p != nullptr)
        {
            // Push an element into the stack and move to its left
            top = push(stk, p, top);
            p = p->left;
        }
        // As long as no underflow, keep popping and moving to the right
        if (top != -1)
        {
            p = pop(stk, &top);
            cout << " \t" << p->info;
            p = p->right;
        }
    } while (top != -1 || p != nullptr);
}

int main()
{
    int ch;
    BST* root;
    root = nullptr;
menu:
    cout << "Binary Search Tree Operations" << endl;
    cout << "-----" << endl;
    cout << "1. Insertion/Creation" << endl;
    cout << "2. In-Order Traversal" << endl;
    cout << "3. Exit" << endl;
    cout << "Enter your choice: ";
    cin >> ch;
}

```

```

switch (ch)
{
    case 1:
        root = insert(root);
        goto menu;
    case 2:
        if (root != nullptr)
            inorder(root);
        else
            cout << "No tree exists!" << endl;
        goto menu;
    case 3:
        return 0;
    default:
        goto menu;
}
}

```

## Binary Search Tree Using a Linked List

```

/* Implement a BST using linked lists */
#include <iostream>

using namespace std;

class BST
{
    struct TreeNode
    {
        int data;
        TreeNode* left;
        TreeNode* right;
    };

public:
    TreeNode* root;

    BST()
    {
        root = nullptr;
    }

    bool IsEmpty()
    {
        return root == nullptr;
    }

    bool Inorder(TreeNode*);
}

```

```

        bool Insert(int);
};

// Perform an in-order traversal on the tree
bool BST::Inorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        // The extra if avoids recursion if the node is a leaf node
        if (start_node->left)
            Inorder(start_node->left);
        cout << " " << start_node->data << " ";
        if (start_node->right)
            Inorder(start_node->right);
    }
    return true;
}

// Insert an item in the BST
bool BST::Insert(int item)
{
    // Create a new node
    TreeNode* node = new TreeNode;
    node->data = item;
    node->left = nullptr;
    node->right = nullptr;
    TreeNode* parent = nullptr;
    if (IsEmpty())
        root = node;
    // If not, we need to find the proper to-be parent of element
    else
    {
        TreeNode* current = root;
        while (current)
        {
            parent = current;
            if (node->data > current->data)
                current = current->right;
            else
                current = current->left;
        }
        if (node->data < parent->data)
            parent->left = node;
        else
            parent->right = node;
    }
    return true;
}

int main()
{

```

```

BST bst;
int choice_i, item_i;
while (1)
{
    cout << endl << endl;
    cout << "Binary Search Tree Operations" << endl;
    cout << "-----" << endl;
    cout << "1. Insertion/Creation" << endl;
    cout << "2. In-Order Traversal" << endl;
    cout << "3. Exit" << endl;
    cout << "Enter your choice: ";
    cin >> choice_i;
    switch (choice_i)
    {
        case 1:
            cout << "Enter Number to be inserted: ";
            cin >> item_i;
            if (bst.Insert(item_i))
                cout << "The element was inserted successfully into the
tree.";

            break;
        case 2:
            cout << endl;
            cout << "In-Order Traversal" << endl;
            cout << "-----" << endl;
            bst.Inorder(bst.root);
            break;
        case 3:
            return 0;
        default:
            cout << "Invalid choice! Try again.";
    }
}
}

```

## Traversals of a Binary Search Tree

```

/* Implement In-order, Post-Order and Pre-Order Traversal of a BST
using linked lists */
#include <iostream>

using namespace std;

class BST
{
    struct TreeNode
    {
        int data;

```

```

        TreeNode* left;
        TreeNode* right;
    };

public:
    TreeNode* root;

    BST()
    {
        root = nullptr;
    }

    bool IsEmpty()
    {
        return root == nullptr;
    }

    bool Inorder(TreeNode*);
    bool Preorder(TreeNode*);
    bool Postorder(TreeNode*);
    bool Insert(int);
};

bool BST::Inorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        if (start_node->left)
            Inorder(start_node->left);
        cout << " " << start_node->data << " ";
        if (start_node->right)
            Inorder(start_node->right);
    }
    return true;
}

bool BST::Preorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        cout << " " << start_node->data << " ";
        if (start_node->left)
            Preorder(start_node->left);
        if (start_node->right)
            Preorder(start_node->right);
    }
    return true;
}

bool BST::Postorder(TreeNode* start_node)
{

```



```

        if (start_node != nullptr)
        {
            if (start_node->left)
                Postorder(start_node->left);
            if (start_node->right)
                Postorder(start_node->right);
            cout << " " << start_node->data << " ";
        }
        return true;
    }

bool BST::Insert(int item)
{
    TreeNode* node = new TreeNode;
    node->data = item;
    node->left = nullptr;
    node->right = nullptr;
    TreeNode* parent = nullptr;
    if (IsEmpty())
        root = node;
    // If not, we need to find the proper to-be parent of element
    else
    {
        TreeNode* current = root;
        while (current)
        {
            parent = current;
            if (node->data > current->data)
                current = current->right;
            else
                current = current->left;
        }
        if (node->data < parent->data)
            parent->left = node;
        else
            parent->right = node;
    }
    return true;
}

int main()
{
    BST bst;
    int choice_i, item_i;
    while (1)
    {
        cout << endl << endl;
        cout << "Binary Search Tree Operations" << endl;
        cout << "-----" << endl;
        cout << "1. Insertion/Creation" << endl;
        cout << "2. In-Order Traversal" << endl;
    }
}

```

```

        cout << "3. Pre-Order Traversal" << endl;
        cout << "4. Post-Order Traversal" << endl;
        cout << "5. Exit" << endl;
        cout << "Enter your choice: ";
        cin >> choice_i;
        switch (choice_i)
        {
            case 1:
                cout << "Enter Number to be inserted: ";
                cin >> item_i;
                if (bst.Insert(item_i))
                    cout << "The element was inserted successfully into the
tree.";
                break;
            case 2:
                cout << endl;
                cout << "In-Order Traversal" << endl;
                cout << "-----" << endl;
                bst.Inorder(bst.root);
                break;
            case 3:
                cout << endl;
                cout << "Pre-Order Traversal" << endl;
                cout << "-----" << endl;
                bst.Preorder(bst.root);
                break;
            case 4:
                cout << endl;
                cout << "Post-Order Traversal" << endl;
                cout << "-----" << endl;
                bst.Postorder(bst.root);
                break;
            case 5:
                return 0;
            default:
                cout << "Invalid choice! Try again.";
        }
    }
}

```

## Insertion of Elements in a Binary Search Tree

```

/* Implement a BST using linked lists with the insertion operation */
#include <iostream>

using namespace std;

class BST

```

```

{
    struct TreeNode
    {
        int data;
        TreeNode* left;
        TreeNode* right;
    };

public:
    TreeNode* root;

    BST()
    {
        root = nullptr;
    }

    bool IsEmpty()
    {
        return root == nullptr;
    }

    bool Inorder(TreeNode*);
    bool Insert(int);
};

bool BST::Inorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        if (start_node->left)
            Inorder(start_node->left);
        cout << " " << start_node->data << " ";
        if (start_node->right)
            Inorder(start_node->right);
    }
    return true;
}

bool BST::Insert(int item)
{
    TreeNode* node = new TreeNode;
    node->data = item;
    node->left = nullptr;
    node->right = nullptr;
    TreeNode* parent = nullptr;
    if (IsEmpty())
        root = node;
    // If not, we need to find the proper to-be parent of element
    else
    {
        TreeNode* current = root;

```

```

        while (current)
        {
            parent = current;
            if (node->data > current->data)
                current = current->right;
            else
                current = current->left;
        }
        if (node->data < parent->data)
            parent->left = node;
        else
            parent->right = node;
    }
    return true;
}

int main()
{
    BST bst;
    int choice_i, item_i;
    while (1)
    {
        cout << endl << endl;
        cout << "Binary Search Tree Operations" << endl;
        cout << "-----" << endl;
        cout << "1. Insertion/Creation" << endl;
        cout << "2. In-Order Traversal" << endl;
        cout << "3. Exit" << endl;
        cout << "Enter your choice: ";
        cin >> choice_i;
        switch (choice_i)
        {
            case 1:
                cout << "Enter Number to be inserted: ";
                cin >> item_i;
                if (bst.Insert(item_i))
                    cout << "The element was successfully inserted into the
tree.";

                break;
            case 2:
                cout << endl;
                cout << "In-Order Traversal" << endl;
                cout << "-----" << endl;
                bst.Inorder(bst.root);
                break;
            case 3:
                return 0;
            default:
                cout << "Invalid choice! Try again.";
        }
    }
}

```

```
}
```

## Deletion of an Element from a Binary Search Tree

```
/* Implement a BST using linked lists with deletion operation */
#include <iostream>

using namespace std;

class BST
{
    struct TreeNode
    {
        int data;
        TreeNode* left;
        TreeNode* right;
    };

public:
    TreeNode* root;

    BST()
    {
        root = nullptr;
    }

    bool IsEmpty()
    {
        return root == nullptr;
    }

    bool Inorder(TreeNode*);
    bool Preorder(TreeNode*);
    bool Postorder(TreeNode*);
    bool Insert(int);
    bool Remove(int);
    TreeNode* SearchParent(int item);
    TreeNode* Min(TreeNode* start_node);
};

bool BST::Inorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        if (start_node->left)
            Inorder(start_node->left);
        cout << " " << start_node->data << " ";
    }
}
```

```

        if (start_node->right)
            Inorder(start_node->right);
    }
    return true;
}

bool BST::Preorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        cout << " " << start_node->data << " ";
        if (start_node->left)
            Preorder(start_node->left);
        if (start_node->right)
            Preorder(start_node->right);
    }
    return true;
}

bool BST::Postorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        if (start_node->left)
            Postorder(start_node->left);
        if (start_node->right)
            Postorder(start_node->right);
        cout << " " << start_node->data << " ";
    }
    return true;
}

bool BST::Insert(int item)
{
    TreeNode* node = new TreeNode;
    node->data = item;
    node->left = nullptr;
    node->right = nullptr;
    TreeNode* parent = nullptr;
    if (IsEmpty())
        root = node;
    // If not, we need to find the proper to-be parent of element
    else
    {
        TreeNode* current = root;
        while (current)
        {
            parent = current;
            if (node->data > current->data)
                current = current->right;
            else

```

```

        current = current->left;
    }
    if (node->data < parent->data)
        parent->left = node;
    else
        parent->right = node;
}
return true;
}

bool BST::Remove(int item)
{
    bool found = false;
    if (IsEmpty())
        return false;
    // If tree is not empty, find the element
    TreeNode* current = root;
    TreeNode* parent = nullptr;
    while (current)
    {
        if (current->data == item)
        {
            found = true;
            break;
        }
        parent = current;
        if (item > current->data)
            current = current->right;
        else
            current = current->left;
    }
    if (!found)
        return false;
    // If element was found, there can be 3 cases:
    // 1. We're removing a leaf node
    // 1.1 Is the left child of parent
    // 1.2 Is the right child of parent
    // 2. We're removing a node with only one child
    // 2.1 Only left child present
    // 2.2 Only right child present
    // 3. We're removing a node with two children

    // Node with no child
    if (current->left == nullptr && current->right == nullptr)
    {
        // Is the left child of parent or the right child?
        if (parent->left == current)
            parent->left = nullptr;
        else
            parent->right = nullptr;
        delete current;
    }

```

```

        return true;
    }
    // Node with only left child
    if (current->left != nullptr && current->right == nullptr)
    {
        if (parent->left == current)
        {
            parent->left = current->left;
            delete current;
        }
        else
        {
            parent->right = current->left;
            delete current;
        }
        return true;
    }
    // Node with only right child
    if (current->right != nullptr && current->left == nullptr)
    {
        if (parent->left == current)
        {
            parent->left = current->right;
            delete current;
        }
        else
        {
            parent->right = current->right;
            delete current;
        }
        return true;
    }
    // Node with two children
    // ALGORITHM: Replace the deleted node with the smallest value in the right
    // sub-tree, now remove the smallest value from the right sub-tree to
    // remove the duplicate
    if (current->left != nullptr && current->right != nullptr)
    {
        TreeNode* right_subtree = current->right;
        // The right sub-tree has only a single node
        // Replace with it and remove the right sub-tree
        if (right_subtree->right == nullptr && right_subtree->left == nullptr)
        {
            current = right_subtree;
            delete right_subtree;
            current->right = nullptr;
        }
        // Right sub-tree has children, replace with the inorder predecessor
        else
        {
            // The node's right child has a left child

```



```

        if (current->right->left != nullptr)
        {
            TreeNode* minimum = Min(current->right);
            current->data = minimum->data;
            delete minimum;
            TreeNode* minimum_parent = SearchParent(minimum->data);
            minimum_parent->left = nullptr;
        }
        // The node's right child has no left child
        else
        {
            TreeNode* temp_node = current->right;
            current->data = temp_node->data;
            current->right = temp_node->right;
            delete temp_node;
        }
    }
}
return true;
}

BST::TreeNode* BST::SearchParent(int item)
{
    TreeNode* current = new TreeNode;
    while (current != nullptr)
    {
        if (item > current->right->data || item > current->left->data)
            current = current->right;
        else if (item < current->right->data || item < current->left->data)
            current = current->left;
        if (item == current->right->data || item == current->left->data)
            return current;
    }
    return nullptr;
}

BST::TreeNode* BST::Min(TreeNode* start_node)
{
    TreeNode* current = new TreeNode;
    current = start_node;
    // Traverse to the leftmost leaf node
    while (current->left != nullptr)
        current = current->left;
    return current;
}

int main()
{
    BST bst;
    int choice_i, item_i;
    while (1)

```

```

{
    cout << endl << endl;
    cout << " Binary Search Tree Operations" << endl;
    cout << " -----" << endl;
    cout << " 1. Insertion/Creation" << endl;
    cout << " 2. In-Order Traversal" << endl;
    cout << " 3. Pre-Order Traversal" << endl;
    cout << " 4. Post-Order Traversal" << endl;
    cout << " 5. Removal" << endl;
    cout << " 6. Exit" << endl;
    cout << " Enter your choice : ";
    cin >> choice_i;
    switch (choice_i)
    {
        case 1:
            cout << " Enter Number to be inserted : ";
            cin >> item_i;
            if (bst.Insert(item_i))
                cout << " The element was inserted into the tree.";
            break;
        case 2:
            cout << endl;
            cout << " In-Order Traversal" << endl;
            cout << " -----" << endl;
            bst.Inorder(bst.root);
            break;
        case 3:
            cout << endl;
            cout << " Pre-Order Traversal" << endl;
            cout << " -----" << endl;
            bst.Preorder(bst.root);
            break;
        case 4:
            cout << endl;
            cout << " Post-Order Traversal" << endl;
            cout << " -----" << endl;
            bst.Postorder(bst.root);
            break;
        case 5:
            cout << " Enter data to be deleted : ";
            cin >> item_i;
            if (bst.Remove(item_i))
                cout << "The element was deleted from the tree.";
            else
                cout << "The element was not found in the tree!";
            break;
        case 6:
            return 0;
        default:
            cout << " Invalid choice! Try again.";
    }
}

```

```

    }
}

```

## Search for an Element in a Binary Search Tree

```

/* Implement a BST using linked lists with the search operation */
#include <iostream>

```

```

using namespace std;

```

```

class BST
{
    struct TreeNode
    {
        int data;
        TreeNode* left;
        TreeNode* right;
    };

public:
    TreeNode* root;
    // A node that can be used by non-member functions
    TreeNode* node;

    BST()
    {
        root = nullptr;
        node = nullptr;
    }

    bool IsEmpty()
    {
        return root == nullptr;
    }

    bool Inorder(TreeNode*);
    bool Insert(int);
    TreeNode* Search(int);
};

```

```

bool BST::Inorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        if (start_node->left)
            Inorder(start_node->left);
        cout << " " << start_node->data << " ";
    }
}

```

```

        if (start_node->right)
            Inorder(start_node->right);
    }
    return true;
}

bool BST::Insert(int item)
{
    TreeNode* node = new TreeNode;
    node->data = item;
    node->left = nullptr;
    node->right = nullptr;
    TreeNode* parent = nullptr;
    if (IsEmpty())
        root = node;
    // If not, we need to find the proper to-be parent of element
    else
    {
        TreeNode* current = root;
        while (current)
        {
            parent = current;
            if (node->data > current->data)
                current = current->right;
            else
                current = current->left;
        }
        if (node->data < parent->data)
            parent->left = node;
        else
            parent->right = node;
    }
    return true;
}

BST::TreeNode* BST::Search(int item)
{
    TreeNode* current = new TreeNode();
    current = root;
    while (current != nullptr)
    {
        if (item > current->data)
            current = current->right;
        else if (item < current->data)
            current = current->left;
        if (item == current->data)
            return current;
    }
    return nullptr;
}

```

```

int main()
{
    BST bst;
    int choice_i, item_i;
    while (1)
    {
        cout << endl << endl;
        cout << "Binary Search Tree Operations" << endl;
        cout << "-----" << endl;
        cout << "1. Insertion/Creation" << endl;
        cout << "2. In-Order Traversal" << endl;
        cout << "3. Search for an element" << endl;
        cout << "4. Exit" << endl;
        cout << "Enter your choice: ";
        cin >> choice_i;
        switch (choice_i)
        {
            case 1:
                cout << "Enter Number to be inserted: ";
                cin >> item_i;
                if (bst.Insert(item_i))
                    cout << "The element was inserted successfully into the
tree.";

                break;
            case 2:
                cout << endl;
                cout << "In-Order Traversal" << endl;
                cout << "-----" << endl;
                bst.Inorder(bst.root);
                break;
            case 3:
                cout << endl;
                cout << "Enter the element to search for: ";
                cin >> item_i;
                bst.node = bst.Search(item_i);
                if (bst.node != nullptr)
                {
                    cout << item_i << " found in the tree!" << endl;
                    cout << "Left child: " << bst.node->left->data << endl;
                    cout << "Right child: " << bst.node->right->data << endl;
                }
                else
                    cout << "The element " << item_i
                        << " wasn't found in the tree!" << endl;

                break;
            case 4:
                return 0;
            default:
                cout << "Invalid choice! Try again.";
        }
    }
}

```

```
}
```

## Maximum and Minimum Elements in a Binary Search Tree

```
/* Find the maximum and minimum elements in a BST */
#include <iostream>

using namespace std;

class BST
{
    struct TreeNode
    {
        int data;
        TreeNode* left;
        TreeNode* right;
    };

public:
    TreeNode* root;

    BST()
    {
        root = nullptr;
    }

    bool IsEmpty()
    {
        return root == nullptr;
    }

    bool Inorder(TreeNode*);
    bool Preorder(TreeNode*);
    TreeNode* SearchParent(int item);
    bool Postorder(TreeNode*);
    bool Insert(int);
    bool Remove(int);
    TreeNode* Max(TreeNode*);
    TreeNode* Min(TreeNode*);
};

bool BST::Inorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        // Avoid recursion once the next element is found to be null
        if (start_node->left != nullptr)
```

```

        Inorder(start_node->left);
        cout << " " << start_node->data << " ";
        if (start_node->right != nullptr)
            Inorder(start_node->right);
    }
    return true;
}

bool BST::Postorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        // Avoid recursion once the next element is found to be null
        if (start_node->left != nullptr)
            Postorder(start_node->left);
        if (start_node->right != nullptr)
            Postorder(start_node->right);
        cout << " " << start_node->data << " ";
    }
    return true;
}

bool BST::Preorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        cout << " " << start_node->data << " ";
        // Avoid recursion once the next element is found to be null
        if (start_node->left != nullptr)
            Preorder(start_node->left);
        if (start_node->right != nullptr)
            Preorder(start_node->right);
    }
    return true;
}

BST::TreeNode* BST::SearchParent(int item)
{
    TreeNode* current = new TreeNode;
    while (current != nullptr)
    {
        if (item > current->right->data || item > current->left->data)
            current = current->right;
        else if (item < current->right->data || item < current->left->data)
            current = current->left;
        if (item == current->right->data || item == current->left->data)
            return current;
    }
    return nullptr;
}

```

```

bool BST::Insert(int item)
{
    TreeNode* new_node = new TreeNode;
    TreeNode* parent = new TreeNode();
    parent = nullptr;
    // Is this a new tree? If yes, new node will become the root
    if (IsEmpty())
        root = new_node;
    // If not, find the proper parent
    else
    {
        // All insertions occur as leaf nodes
        TreeNode* current = root;
        while (current != nullptr)
        {
            parent = current;
            if (new_node->data > current->data)
                current = current->right;
            else
                current = current->left;
        }
        if (new_node->data < parent->data)
            parent->left = new_node;
        else
            parent->right = new_node;
    }
    return true;
}

bool BST::Remove(int item)
{
    bool found = false;
    if (IsEmpty())
        return false;
    // If tree is not empty, find the element
    TreeNode* current = root;
    TreeNode* parent = nullptr;
    while (current)
    {
        if (current->data == item)
        {
            found = true;
            break;
        }
        parent = current;
        if (item > current->data)
            current = current->right;
        else
            current = current->left;
    }
    if (!found)

```



```

        return false;
// If element was found, there can be 3 cases:
// 1. We're removing a leaf node
// 1.1 Is the left child of parent
// 1.2 Is the right child of parent
// 2. We're removing a node with only one child
// 2.1 Only left child present
// 2.2 Only right child present
// 3. We're removing a node with two children

// Node with no child
if (current->left == nullptr && current->right == nullptr)
{
    // Is the left child of parent or the right child?
    if (parent->left == current)
        parent->left = nullptr;
    else
        parent->right = nullptr;
    delete current;
    return true;
}
// Node with only left child
if (current->left != nullptr && current->right == nullptr)
{
    if (parent->left == current)
    {
        parent->left = current->left;
        delete current;
    }
    else
    {
        parent->right = current->left;
        delete current;
    }
    return true;
}
// Node with only right child
if (current->right != nullptr && current->left == nullptr)
{
    if (parent->right == current)
    {
        parent->right = current->right;
        delete current;
    }
    else
    {
        parent->left = current->right;
        delete current;
    }
    return true;
}
}

```

```

// Node with two children
// ALGORITHM: Replace the deleted node with the smallest value in the right
// sub-tree, now remove the smallest value from the right sub-tree to
// remove the duplicate
if (current->left != nullptr && current->right != nullptr)
{
    TreeNode* right_subtree = current->right;
    // The right sub-tree has only a single node
    // Replace with it and remove the right sub-tree
    if (right_subtree->right == nullptr && right_subtree->left == nullptr)
    {
        current = right_subtree;
        delete right_subtree;
        current->right = nullptr;
    }
    // Right sub-tree has children, replace with the inorder predecessor
    else
    {
        // The node's right child has a left child
        if (current->right->left != nullptr)
        {
            TreeNode* minimum = Min(current->right);
            current->data = minimum->data;
            delete minimum;
            TreeNode* minimum_parent = SearchParent(minimum->data);
            minimum_parent->left = nullptr;
        }
        // The node's right child has no left child
        else
        {
            TreeNode* temp_node = current->right;
            current->data = temp_node->data;
            current->right = temp_node->right;
            delete temp_node;
        }
    }
}
return true;
}

BST::TreeNode* BST::Max(TreeNode* start_node)
{
    TreeNode* current = new TreeNode();
    current = start_node;
    // Traverse to the rightmost leaf node
    while (current->right != nullptr)
        current = current->right;
    return current;
}

BST::TreeNode* BST::Min(TreeNode* start_node)

```

```

{
    TreeNode* current = new TreeNode;
    current = start_node;
    // Traverse to the leftmost leaf node
    while (current->left != nullptr)
        current = current->left;
    return current;
}

int main()
{
    BST bst;
    int choice_i, item_i;
    while (1)
    {
        cout << endl << endl;
        cout << "Binary Search Tree Operations" << endl;
        cout << "-----" << endl;
        cout << "1. Insertion/Creation" << endl;
        cout << "2. In-Order Traversal" << endl;
        cout << "3. Pre-Order Traversal" << endl;
        cout << "4. Post-Order Traversal" << endl;
        cout << "5. Minimum Element" << endl;
        cout << "6. Maximum Element" << endl;
        cout << "7. Removal" << endl;
        cout << "8. Exit" << endl;
        cout << "Enter your choice: ";
        cin >> choice_i;
        switch (choice_i)
        {
            case 1:
                cout << "Enter Number to be inserted: ";
                cin >> item_i;
                if (bst.Insert(item_i))
                    cout << "The element was inserted in the tree.";
                break;
            case 2:
                cout << endl;
                cout << "In-Order Traversal" << endl;
                cout << "-----" << endl;
                bst.Inorder(bst.root);
                break;
            case 3:
                cout << endl;
                cout << "Pre-Order Traversal" << endl;
                cout << "-----" << endl;
                bst.Preorder(bst.root);
                break;
            case 4:
                cout << endl;
                cout << "Post-Order Traversal" << endl;

```

```

        cout << "-----" << endl;
        bst.Postorder(bst.root);
        break;
    case 5:
        cout << endl;
        cout << "Minimum element in the tree is "
              << bst.Min(bst.root)->data;
        break;
    case 6:
        cout << endl;
        cout << "Maximum element in the tree is "
              << bst.Max(bst.root)->data;
        break;
    case 7:
        cout << endl;
        cout << "Enter the element to be deleted: ";
        cin >> item_i;
        if (bst.Remove(item_i) == true)
            cout << "The element was deleted successfully.";
        else
            cout << "The element was not found in the tree.";
        break;
    case 8:
        return 0;
    default:
        cout << "Invalid choice! Try again.";
    }
}
}

```

## Predecessor and Successor of an Element in a Binary Search Tree

```

/* Find the successors and predecessors of a given node in a BST */
#include <iostream>

using namespace std;

class BST
{
    struct TreeNode
    {
        int data;
        TreeNode* left;
        TreeNode* right;
    };

public:

```

```

TreeNode* root;

BST()
{
    root = nullptr;
}

bool IsEmpty()
{
    return root == nullptr;
}

bool Inorder(TreeNode*);
bool Preorder(TreeNode*);
bool Postorder(TreeNode*);
bool Insert(int);
bool Remove(int);
TreeNode* Max(TreeNode*);
TreeNode* Min(TreeNode*);
TreeNode* Predecessor(int, int);
TreeNode* Successor(int, int);
TreeNode* Search(int);
TreeNode* SearchParent(int);
};

bool BST::Inorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        // Avoid recursion once the next element is found to be null
        if (start_node->left != nullptr)
            Inorder(start_node->left);
        cout << " " << start_node->data << " ";
        if (start_node->right != nullptr)
            Inorder(start_node->right);
    }
    return true;
}

bool BST::Postorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        // Avoid recursion once the next element is found to be null
        if (start_node->left != nullptr)
            Postorder(start_node->left);
        if (start_node->right != nullptr)
            Postorder(start_node->right);
        cout << " " << start_node->data << " ";
    }
    return true;
}

```

```

}

bool BST::Preorder(TreeNode* start_node)
{
    if (start_node != nullptr)
    {
        cout << " " << start_node->data << " ";
        // Avoid recursion once the next element is found to be null
        if (start_node->left != nullptr)
            Preorder(start_node->left);
        if (start_node->right != nullptr)
            Preorder(start_node->right);
    }
    return true;
}

bool BST::Insert(int item)
{
    TreeNode* new_node = new TreeNode;
    TreeNode* parent = new TreeNode;
    // Is this a new tree? If yes, new node will become the root
    if (IsEmpty())
        root = new_node;
    // If not, find the proper parent
    else
    {
        // All insertions occur as leaf nodes
        TreeNode* current = root;
        while (current != nullptr)
        {
            parent = current;
            if (new_node->data > current->data)
                current = current->right;
            else
                current = current->left;
        }
        if (new_node->data < parent->data)
            parent->left = new_node;
        else
            parent->right = new_node;
    }
    return true;
}

bool BST::Remove(int item)
{
    bool found = false;
    if (IsEmpty())
    {
        cout << "This tree is empty!" << endl;
        return false;
    }

```

```

}
// If tree is not empty, find the element
TreeNode* current = root;
TreeNode* parent = nullptr;
while (current)
{
    if (current->data == item)
    {
        found = true;
        break;
    }
    parent = current;
    if (item > current->data)
        current = current->right;
    else
        current = current->left;
}
if (!found)
{
    cout << "Data not found in the tree!" << endl;
    return false;
}
// If element was found, there can be 3 cases:
// 1. We're removing a leaf node
// 1.1 Is the left child of parent
// 1.2 Is the right child of parent
// 2. We're removing a node with only one child
// 2.1 Only left child present
// 2.2 Only right child present
// 3. We're removing a node with two children

// Node with no child
if (current->left == nullptr && current->right == nullptr)
{
    // Is the left child of parent or the right child?
    if (parent->left == current)
        parent->left = nullptr;
    else
        parent->right = nullptr;
    delete current;
    return true;
}
// Node with only left child
if (current->left != nullptr && current->right == nullptr)
{
    if (parent->left == current)
    {
        parent->left = current->left;
        delete current;
    }
    else

```

```

        {
            parent->right = current->left;
            delete current;
        }
        return true;
    }
    // Node with only right child
    if (current->right != nullptr && current->left == nullptr)
    {
        if (parent->left == current)
        {
            parent->left = current->right;
            delete current;
        }
        else
        {
            parent->right = current->right;
            delete current;
        }
        return true;
    }
    // Node with two children
    // ALGORITHM: Replace the deleted node with the smallest value in the right
    // sub-tree, now remove the smallest value from the right sub-tree to
    // remove the duplicate
    if (current->left != nullptr && current->right != nullptr)
    {
        TreeNode* right_subtree = current->right;
        // The right sub-tree has only a single node
        // Replace with it and remove the right sub-tree
        if (right_subtree->right == nullptr && right_subtree->left == nullptr)
        {
            current = right_subtree;
            delete right_subtree;
            current->right = nullptr;
        }
        // Right sub-tree has children, replace with the inorder predecessor
        else
        {
            // The node's right child has a left child
            if (current->right->left != nullptr)
            {
                TreeNode* minimum = Min(current->right);
                current->data = minimum->data;
                delete minimum;
                TreeNode* minimum_parent = SearchParent(minimum->data);
                minimum_parent->left = nullptr;
            }
            // The node's right child has no left child
            else
            {

```



```

        TreeNode* temp_node = current->right;
        current->data = temp_node->data;
        current->right = temp_node->right;
        delete temp_node;
    }
}
return true;
}

BST::TreeNode* BST::Search(int item)
{
    TreeNode* current = new TreeNode;
    while (current != nullptr)
    {
        if (item > current->data)
            current = current->right;
        else if (item < current->data)
            current = current->left;
        if (item == current->data)
            return current;
    }
    return nullptr;
}

BST::TreeNode* BST::SearchParent(int item)
{
    TreeNode* current = new TreeNode;
    while (current != nullptr)
    {
        if (item > current->right->data || item > current->left->data)
            current = current->right;
        else if (item < current->right->data || item < current->left->data)
            current = current->left;
        if (item == current->right->data || item == current->left->data)
            return current;
    }
    return nullptr;
}

BST::TreeNode* BST::Max(TreeNode* start_node)
{
    TreeNode* current = new TreeNode;
    current = start_node;
    // Traverse to the rightmost leaf node
    while (current->right != nullptr)
        current = current->right;
    return current;
}

BST::TreeNode* BST::Min(TreeNode* start_node)

```

```

{
    TreeNode* current = new TreeNode;
    current = start_node;
    // Traverse to the leftmost leaf node
    while (current->left != nullptr)
        current = current->left;
    return current;
}

BST::TreeNode* BST::Predecessor(int item, int mode)
{
    // Search for the start_node
    TreeNode* start_node = new TreeNode;
    start_node = Search(item);
    switch (mode)
    {
        // Pre-Order Predecessor
        case 1:
        {
            // If start_node is root of tree, predecessor is undefined
            if (start_node == root)
                return nullptr;
            // If start_node has left sibling ls then predecessor is
            // the rightmost descendant of ls
            TreeNode* parent = SearchParent(start_node->data);
            if (parent->right == start_node && parent->left != nullptr)
                return Max(parent->left);
            // Else the parent
            return parent;
        }
        // In-Order Predecessor
        case 2:
        {
            // If start_node has left child l, then predecessor is rightmost
            // descendant of l
            if (start_node->left != nullptr)
                return Max(start_node->left);
            // Predecessor is the closest ancestor v of start_node such that
            // start_node is in the right subtree of v
            TreeNode* parent = SearchParent(start_node->data);
            if (parent->right == start_node)
                return parent;
            // If not an immediate right child, recurse
            TreeNode* subtree_node = parent;
            while (true)
            {
                if (subtree_node->right == parent)
                    return subtree_node;
                parent = subtree_node;
                // If we reached the top and still couldn't find it, give up
                if (parent == root)
                    return nullptr;
            }
        }
    }
}

```

```

        return nullptr;
        subtree_node = SearchParent(subtree_node->data);
    }
}
// Post-Order Predecessor
case 3:
{
    // If start_node has a right child
    // then the predecessor is the right child
    if (start_node->right != nullptr)
        return start_node->right;
    // If start_node has a left child
    // then the predecessor is the left child
    if (start_node->left != nullptr)
        return start_node->left;
    // If start_node has left sibling then predecessor is the sibling
    TreeNode* parent = SearchParent(start_node->data);
    if (parent->left != nullptr)
        return parent->left;
    // If start_node has an ancestor which:
    // is a right child AND has a left sibling vls then pred is vls
    TreeNode* ancestor = SearchParent(parent->data);
    if (ancestor->right == parent && ancestor->left != nullptr)
        return ancestor->left;
    // If not an immediate ancestor, recurse
    while (true)
    {
        if (ancestor->right == parent && ancestor->left != nullptr)
            return ancestor->left;
        parent = ancestor;
        // If we reached the top and still couldn't find it, give up
        if (parent == root)
            return nullptr;
        ancestor = SearchParent(ancestor->data);
    }
}
default:
    break;
}
return nullptr;
}

```

```

BST::TreeNode* BST::Successor(int item, int mode)
{
    // Search for the start_node
    TreeNode* start_node = new TreeNode;
    start_node = Search(item);
    switch (mode)
    {
        // Pre-Order Successor
        case 1:
    }
}

```

```

{
    // If start_node has a left child then successor is the left child.
    if (start_node->left != nullptr)
        return start_node->left;
    // If start_node has a right child then successor is right child
    if (start_node->right != nullptr)
        return start_node->right;
    // If the start_node is a leaf
    // 1. And a left child and has a right sibling rs, rs is successor
    TreeNode* parent = SearchParent(item);
    if (start_node == parent->left)
        if (parent->right != nullptr)
            return parent->right;
    // 2. start_node has an ancestor which is a left child and
    // has a right sibling then the sibling is the successor
    TreeNode* ancestor = SearchParent(parent->data);
    if (ancestor->left == parent && ancestor->right != nullptr)
        return ancestor->right;
    // If not an immediate ancestor, recurse
    while (true)
    {
        if (ancestor->left == parent && ancestor->right != nullptr)
            return ancestor->right;
        parent = ancestor;
        // If we reached the top and still couldn't find it, give up
        if (parent == root)
            return nullptr;
        ancestor = SearchParent(ancestor->data);
    }
}
// In-Order Successor
case 2:
{
    // If start_node has a right child then successor is the leftmost
    // descendant of start_node
    if (start_node->right != nullptr)
        return Min(start_node);
    // Else the closest ancestor of start_node such that start_node
    // is in the left subtree of the ancestor
    TreeNode* parent = SearchParent(start_node->data);
    if (parent->right == start_node)
        return parent;
    // If not an immediate right child, recurse
    TreeNode* subtree_node = parent;
    while (true)
    {
        if (subtree_node->right == parent)
            return subtree_node;
        parent = subtree_node;
        // If we reached the top and still couldn't find it, give up
        if (parent == root)

```

```

        break;
        subtree_node = SearchParent(subtree_node->data);
    }
    return nullptr;
}
// Post-Order Successor
case 3:
{
    // If start_node is the root, the successor is undefined
    if (start_node == root)
        return nullptr;
    // If start_node is a right child, the successor is it's parent
    TreeNode* parent = SearchParent(item);
    if (start_node == parent->right)
        return parent;
    // If start_node is a left child and has a right sibling rs
    // the successor is the leftmost leaf in the rs's subtree
    if (start_node == parent->left)
        if (parent->right != nullptr)
            return Min(start_node);
    // Else the successor is the parent of start_node
    return parent;
}
default:
    break;
}
return nullptr;
}

int main()
{
    BST bst;
    int choice_i, item_i, mode_i;
    while (true)
    {
        cout << endl << endl;
        cout << "Binary Search Tree Operations" << endl;
        cout << "-----" << endl;
        cout << "1. Insertion/Creation" << endl;
        cout << "2. In-Order Traversal" << endl;
        cout << "3. Pre-Order Traversal" << endl;
        cout << "4. Post-Order Traversal" << endl;
        cout << "5. Predecessor" << endl;
        cout << "6. Successor" << endl;
        cout << "7. Removal" << endl;
        cout << "8. Exit" << endl;
        cout << "Enter your choice: ";
        cin >> choice_i;
        switch (choice_i)
        {
            case 1:

```

```

        cout << "Enter Number to be inserted: ";
        cin >> item_i;
        bst.Insert(item_i);
        break;
case 2:
    cout << endl;
    cout << "In-Order Traversal" << endl;
    cout << "-----" << endl;
    bst.Inorder(bst.root);
    break;
case 3:
    cout << endl;
    cout << "Pre-Order Traversal" << endl;
    cout << "-----" << endl;
    bst.Preorder(bst.root);
    break;
case 4:
    cout << endl;
    cout << "Post-Order Traversal" << endl;
    cout << "-----" << endl;
    bst.Postorder(bst.root);
    break;
case 5:
    cout << endl;
    cout << "Enter the element whose predecessor you want: "
        << endl;
    cin >> item_i;
    cout << "1. Pre-Order predecessor" << endl;
    cout << "2. In-Order predecessor" << endl;
    cout << "3. Post-Order predecessor" << endl;
    cin >> mode_i;
    cout << "The predecessor of " << item_i << " is "
        << bst.Predecessor(item_i, mode_i);
    break;
case 6:
    cout << endl;
    cout << "Enter the element whose successor you want: "
        << endl;
    cin >> item_i;
    cout << "1. Pre-Order successor" << endl;
    cout << "2. In-Order successor" << endl;
    cout << "3. Post-Order successor" << endl;
    cin >> mode_i;
    cout << "The successor of " << item_i << " is "
        << bst.Successor(item_i, mode_i);
    break;
case 7:
    cout << "Enter data to be deleted: ";
    cin >> item_i;
    bst.Remove(item_i);
    break;

```

```

        case 8:
            return 0;
        default:
            cout << "Invalid choice! Try again.";
    }
}
}

```

## Implementation of a Huffman Tree to Perform Huffman Encoding of a String

```

#include <iostream>
#include <string>
#include <fstream>
#include <array>

// Maximum height of the Huffman Tree
#define MAX_TREE_HT 100

using namespace std;

class Huffman
{
public:
    // A Huffman Tree node
    struct minHeapNode
    {
        char data;
        int freq;
        minHeapNode* left;
        minHeapNode* right;
    };

    // The Huffman Tree itself
    struct minHeap
    {
        int current_size;
        int capacity;
        minHeapNode** array; // Array of minHeap node pointers
    };

    // Allocate a new minHeap node with passed character and freq
    minHeapNode* newNode(unsigned char, int);
    // Create a minHeap of passed capacity
    minHeap* create(int);
    // Swap two minHeap nodes
    void swapNode(minHeapNode**, minHeapNode**);
    // Heapify

```

```

void heapify(minHeap*, int);

// Returns true if current size of minHeap is 1
bool isSizeOne(minHeap* min_heap)
{
    if (min_heap->current_size == 1)
        return true;
    return false;
}

// Find minimum node
minHeapNode* getMin(minHeap*);
// Insert a new node in the minHeap
void insert(minHeap*, minHeapNode*);
// Build a minHeap
void build(minHeap*);

// Return true if it a leaf
bool isLeaf(minHeapNode* root)
{
    if (!root->left && !root->right)
        return true;
    return false;
}

// Creates a minHeap of capacity equal to size and insert all character of
// data[] in minHeap. Initially size of minHeap is equal to capacity.
minHeap* generate(unsigned char[], int[], int);
// The main function that builds Huffman tree
minHeapNode* buildHuffmanTree(unsigned char[], int[], int);
// Print the huffman coded input
void printCodes(minHeapNode*, int[], int);
// Builds a Huffman Tree and print codes by traversing it
void huffmanCodes(unsigned char[], int[], int);
};

Huffman::minHeapNode* Huffman::newNode(unsigned char data, int freq)
{
    // Initialise a node with the passed parameters
    minHeapNode* new_node = new minHeapNode;
    new_node->left = new_node->right = nullptr;
    new_node->data = data;
    new_node->freq = freq;
    return new_node;
}

void printArray(int arr[], int n)
{
    for (int i = 0; i < n; ++i)
        cout << arr[i] << " ";
    cout << endl;
}

```



```

}

Huffman::minHeap* Huffman::create(int capacity)
{
    minHeap* min_heap = new minHeap;
    min_heap->current_size = 0; // current size is 0
    min_heap->capacity = capacity;
    min_heap->array = new minHeapNode*;
    // (minHeapNode**)malloc(min_heap->capacity * sizeof(minHeapNode*));
    return min_heap;
}

void Huffman::swapNode(minHeapNode** a, minHeapNode** b)
{
    minHeapNode* t = *a;
    *a = *b;
    *b = t;
}

void Huffman::heapify(minHeap* minHeap, int idx)
{
    int smallest = idx;
    int left = 2 * idx + 1;
    int right = 2 * idx + 2;
    // The standard heapify algorithm
    if (left < minHeap->current_size &&
        minHeap->array[left]->freq < minHeap->array[smallest]->freq)
        smallest = left;

    if (right < minHeap->current_size &&
        minHeap->array[right]->freq < minHeap->array[smallest]->freq)
        smallest = right;

    if (smallest != idx)
    {
        swapNode(&minHeap->array[smallest], &minHeap->array[idx]);
        heapify(minHeap, smallest);
    }
}

Huffman::minHeapNode* Huffman::getMin(minHeap* min_heap)
{
    minHeapNode* minimum = min_heap->array[0];
    min_heap->array[0] = min_heap->array[min_heap->current_size - 1];
    min_heap->current_size--;
    heapify(min_heap, 0);
    return minimum;
}

void Huffman::insert(minHeap* min_heap, minHeapNode* min_heapNode)
{

```

```

        ++min_heap->current_size;
        int i = min_heap->current_size - 1;
        while (i && min_heapNode->freq < min_heap->array[(i - 1) / 2]->freq)
        {
            min_heap->array[i] = min_heap->array[(i - 1) / 2];
            i = (i - 1) / 2;
        }
        min_heap->array[i] = min_heapNode;
    }

void Huffman::build(minHeap* min_heap)
{
    int n = min_heap->current_size - 1;
    for (int i = (n - 1) / 2; i >= 0; --i)
        heapify(min_heap, i);
}

Huffman::minHeap* Huffman::generate(unsigned char data[], int freq[], int size)
{
    minHeap* min_heap = create(size);
    for (int i = 0; i < size; ++i)
        min_heap->array[i] = newNode(data[i], freq[i]);
    min_heap->current_size = size;
    build(min_heap);
    return min_heap;
}

Huffman::minHeapNode* Huffman::buildHuffmanTree(unsigned char data[], int freq[], int size)
{
    minHeapNode *left, *right, *top;

    // Create a min heap of capacity equal to size. Initially, there are
    // modes equal to size.
    minHeap* minHeap = generate(data, freq, size);

    // Iterate while size of heap doesn't become 1
    while (!isSizeOne(minHeap))
    {
        // Extract the two minimum freq items from min heap
        left = getMin(minHeap);
        right = getMin(minHeap);

        // Create a new internal node with freq equal to the
        // sum of the two nodes frequencies. Make the two extracted node as
        // left and right children of this new node.
        // Add this node to the min heap
        top = newNode('$', left->freq + right->freq);
        // Unused symbol $ to mark internal nodes
        top->left = left;
        top->right = right;
        insert(minHeap, top);
    }
}

```

```

    }
    // The remaining node is the root node and the tree is complete.
    return getMin(minHeap);
}

void Huffman::printCodes(minHeapNode* root, int arr[], int top)
{
    // Assign 0 to left edge and recurse
    if (root->left)
    {
        arr[top] = 0;
        printCodes(root->left, arr, top + 1);
    }

    // Assign 1 to right edge and recurse
    if (root->right)
    {
        arr[top] = 1;
        printCodes(root->right, arr, top + 1);
    }

    // If this is a leaf node, then it contains one of the input
    // characters, print the character and its code from arr[]
    if (isLeaf(root))
    {
        cout << root->data << " ";
        printArray(arr, top);
    }
}

void Huffman::huffmanCodes(unsigned char data[], int freq[], int size)
{
    minHeapNode* root = buildHuffmanTree(data, freq, size);
    int arr[MAX_TREE_HT], top = 0;
    printCodes(root, arr, top);
}

int main()
{
    cout << "Enter the filename of the file to be Huffman coded: ";
    string inputFile;
    cin >> inputFile;
    ifstream inFile(inputFile);
    string inputbuffer;
    unsigned char tokens[255];
    int freq[255];
    for (int i = 0; i < 255; i++)
    {
        freq[i] = 0;
        tokens[i] = i;
    }
}

```

```

Huffman hf;
while (!inFile.eof())
{
    getline(inFile, inputbuffer);
    // Find frequency of all possible 256 characters
    for (unsigned int i = 0; i < inputbuffer.length(); i++)
    {
        tokens[inputbuffer[i]] = inputbuffer[i];
        freq[inputbuffer[i]]++;
    }
    unsigned char new_tokens[255];
    int new_freq[255];
    int numoftokens = 0;
    // Filter out only those tokens which have a non-zero frequency
    for (int i = 0; i < 255; i++)
    {
        if (freq[i] != 0)
        {
            new_tokens[numoftokens] = tokens[i];
            new_freq[numoftokens] = freq[i];
            numoftokens++;
        }
    }
    int size = sizeof new_tokens / sizeof new_tokens[0];
    // Encode and print the coded output
    hf.huffmanCodes(new_tokens, new_freq, numoftokens);
}
}

```

## Implementation of an Expression Tree

```

/* Evaluate a postfix expression using expression tree */
#include <iostream>

using namespace std;

struct tree
{
    char data;
    tree* left;
    tree* right;
};

int top = -1;
tree* stack[20];
tree* node;

```

```

void push(tree* node)
{
    stack[++top] = node;
}

tree* pop()
{
    return stack[top--];
}

int check(char c)
{
    // Return 2 if operator otherwise 1
    if (c == '+' || c == '-' || c == '/' || c == '*')
        return 2;
    return 1;
}

int cal(tree* node)
{
    int ch;
    // Check if operand or operator
    ch = check(node->data);
    // If it is an operand, convert it to the corresponding integer by
    // subtracting 48 from it's ascii value
    if (ch == 1)
        return (node->data - 48);
    if (ch == 2)
    {
        if (node->data == '+')
            return (cal(node->left) + cal(node->right));
        if (node->data == '-')
            return (cal(node->right) - cal(node->left));
        if (node->data == '*')
            return (cal(node->left) * cal(node->right));
        if (node->data == '/')
            return (cal(node->right) / cal(node->left));
    }
}

void operands(char b)
{
    node = new tree;
    node->data = b;
    node->left = nullptr;
    node->right = nullptr;
    push(node);
}

void operators(char a)
{

```

```

        node = new tree;
        node->data = a;
        node->left = pop();
        node->right = pop();
        push(node);
    }

    // Perform in-order traversal to evaluate the expression tree
    void traverse(tree* node)
    {
        if (node != nullptr)
        {
            traverse(node->right);
            printf("%c", node->data);
            traverse(node->left);
        }
    }

    int main()
    {
        int i, p, ans;
        char s[20];
        cout << "Enter the expression tree in postfix form: ";
        fgets(s, 19, stdin);
        for (i = 0; s[i] != '\n'; i++)
        {
            p = check(s[i]);
            if (p == 1)
                operands(s[i]);
            else if (p == 2)
                operators(s[i]);
        }
        ans = cal(stack[top]);
        cout << endl << "The value of the postfix expression = " << ans << endl;
        cout << "The actual traversal will be:" << endl;
        traverse(stack[top]);
    }
}

```

## Implementation of a B-Tree and it's Traversal

```

/* C++ Program to Implement B-Tree */
#include <iostream>

using namespace std;

struct BTreeNode
{

```

```

        int *data;
        BTreeNode **child_ptr;
        bool leaf;
        int n;
    }*root = nullptr, *np = nullptr, *x = nullptr;

BTreeNode* init()
{
    int i;
    np = new BTreeNode;
    np->data = new int[5];
    np->child_ptr = new BTreeNode*[6];
    np->leaf = true;
    np->n = 0;
    for (i = 0; i < 6; i++)
        np->child_ptr[i] = nullptr;
    return np;
}

void traverse(BTreeNode* p)
{
    cout << endl;
    int i;
    for (i = 0; i < p->n; i++)
    {
        if (p->leaf == false)
            traverse(p->child_ptr[i]);
        cout << " " << p->data[i];
    }
    if (p->leaf == false)
        traverse(p->child_ptr[i]);
    cout << endl;
}

void sort(int* p, int n)
{
    int i, j, temp;
    for (i = 0; i < n; i++)
    {
        for (j = i; j <= n; j++)
        {
            if (p[i] > p[j])
            {
                temp = p[i];
                p[i] = p[j];
                p[j] = temp;
            }
        }
    }
}

```

```

int split_child(BTreeNode* x, int i)
{
    int j, mid;
    BTreeNode *np1, *np3, *y;
    np3 = init();
    np3->leaf = true;
    if (i == -1)
    {
        mid = x->data[2];
        x->data[2] = 0;
        x->n--;
        np1 = init();
        np1->leaf = false;
        x->leaf = true;
        for (j = 3; j < 5; j++)
        {
            np3->data[j - 3] = x->data[j];
            np3->child_ptr[j - 3] = x->child_ptr[j];
            np3->n++;
            x->data[j] = 0;
            x->n--;
        }
        for (j = 0; j < 6; j++)
            x->child_ptr[j] = nullptr;
        np1->data[0] = mid;
        np1->child_ptr[np1->n] = x;
        np1->child_ptr[np1->n + 1] = np3;
        np1->n++;
        root = np1;
    }
    else
    {
        y = x->child_ptr[i];
        mid = y->data[2];
        y->data[2] = 0;
        y->n--;
        for (j = 3; j < 5; j++)
        {
            np3->data[j - 3] = y->data[j];
            np3->n++;
            y->data[j] = 0;
            y->n--;
        }
        x->child_ptr[i + 1] = y;
        x->child_ptr[i + 1] = np3;
    }
    return mid;
}

void insert(int a)
{

```



```

int i, temp;
x = root;
if (x == nullptr)
{
    root = init();
    x = root;
}
else
{
    if (x->leaf == true && x->n == 5)
    {
        split_child(x, -1);
        x = root;
        for (i = 0; i < x->n; i++)
        {
            if (a > x->data[i] && a < x->data[i + 1])
            {
                i++;
                break;
            }
            if (a < x->data[0])
                break;
        }
        x = x->child_ptr[i];
    }
    else
    {
        while (x->leaf == false)
        {
            for (i = 0; i < x->n; i++)
            {
                if (a > x->data[i] && a < x->data[i + 1])
                {
                    i++;
                    break;
                }
                if (a < x->data[0])
                    break;
            }
            if (x->child_ptr[i]->n == 5)
            {
                temp = split_child(x, i);
                x->data[x->n] = temp;
                x->n++;
            }
            else
                x = x->child_ptr[i];
        }
    }
    x->data[x->n] = a;
}

```

```

        sort(x->data, x->n);
        x->n++;
    }

int main()
{
    int i, n, t;
    cout << "Enter the no of elements to be inserted: ";
    cin >> n;
    for (i = 0; i < n; i++)
    {
        cout << "Enter the element: ";
        cin >> t;
        insert(t);
    }
    cout << "Traversal of constructed tree:" << endl;
    traverse(root);
}

```

## Bubble Sort

```

/* Implement Bubble Sort */
#include <iostream>

using namespace std;

int main()
{
    cout << "Enter the number of elements in the array: ";
    int n;
    cin >> n;
    int array[50];
    for (int i = 0; i < n; i++)
    {
        cout << "Enter the " << i + 1 << "th element: ";
        cin >> array[i];
    }
    for (int x = 0; x < n; x++)
    {
        for (int y = 0; y < n - 1; y++)
        {
            if (array[y] > array[y + 1])
            {
                int temp = array[y + 1];
                array[y + 1] = array[y];
                array[y] = temp;
            }
        }
    }
}

```

```

    }
}
cout << "The Sorted Array is:" << endl;
for (int i = 0; i < n; i++)
    cout << " " << array[i] << " ";
}

```

## Merge Sort

```

/* Implement Merge Sort */
#include <iostream>

using namespace std;

int max(int x, int y)
{
    if (x > y)
        return x;
    return y;
}

// Left is the index of the leftmost element of the subarray.
// Right is one past the index of the rightmost element
void merge(int* input, int left, int right, int* scratch)
{
    // The non-base case, if anything other than this, it must be the base case
    // And in that case we will just return
    if (right != left + 1)
    {
        int i = 0;
        int length = right - left;
        int midpoint_distance = length / 2;
        int l = left, r = left + midpoint_distance;

        // Sort each subarray
        merge(input, left, left + midpoint_distance, scratch);
        merge(input, left + midpoint_distance, right, scratch);

        // Merge the arrays together using scratch for temporary storage
        for (i = 0; i < length; i++)
        {
            // Check to see if any elements remain in the left array
            // If so, we check if there are elements left in the right array
            // If so, we compare them. Otherwise, we know that the merge must
            // use the element from the left array
            if (l < left + midpoint_distance &&
                (r == right || max(input[l], input[r]) == input[l]))

```

```

        {
            scratch[i] = input[l];
            l++;
        }
        else
        {
            scratch[i] = input[r];
            r++;
        }
    }
    // Copy the sorted subarray back to the input
    for (i = left; i < right; i++)
        input[i] = scratch[i - left];
}

}

bool mergesort(int* input, int size)
{
    int* scratch = new int;
    // (int *)malloc(size * sizeof(int));
    if (scratch != nullptr)
    {
        merge(input, 0, size, scratch);
        free(scratch);
        return true;
    }
    return false;
}

int main()
{
    int array[100], n;
    cout << "Enter the size of the array: ";
    cin >> n;
    for (int i = 0; i < n; i++)
    {
        cout << "Enter the " << i + 1 << "th element: ";
        cin >> array[i];
    }
    if (mergesort(array, n))
    {
        cout << "The sorted array is:" << endl;
        for (int i = 0; i < n; i++)
            cout << " " << array[i] << " ";
    }
    else
        cout << "The sorting failed!" << endl;
}

```

## Heap Sort

```
#include <iostream>

using namespace std;

const int MAX = 10;

class Heap
{
    int arr[MAX];
    int count;
public:
    Heap()
    {
        count = 0;
        for (int i = 0; i < MAX; i++)
            arr[i] = 0;
    }

    void Add(int num);
    void MakeHeap(int);
    void HeapSort();
    void Display();
};

void Heap::Add(int num)
{
    if (count < MAX)
    {
        arr[count] = num;
        count++;
    }
    else
        cout << endl << "Array is full!" << endl;
}

void Heap::MakeHeap(int c)
{
    for (int i = 1; i < c; i++)
    {
        int val = arr[i];
        int s = i;
        int f = (s - 1) / 2;
        while (s > 0 && arr[f] < val)
        {
            arr[s] = arr[f];

```

```

        s = f;
        f = (s - 1) / 2;
    }
    arr[s] = val;
}

void Heap::HeapSort()
{
    for (int i = count - 1; i > 0; i--)
    {
        int ivalue = arr[i];
        arr[i] = arr[0];
        arr[0] = ivalue;
        MakeHeap(i);
    }
}

void Heap::Display()
{
    for (int i = 0; i < count; i++)
        cout << arr[i] << "\t";
    cout << endl;
}

int main()
{
    Heap arr;
    int size;
    cout << "Enter the size of the heap: ";
    cin >> size;
    for (int i = 0; i < size; i++)
    {
        int elem;
        cout << "Enter " << i + 1 << "th element: ";
        cin >> elem;
        arr.Add(elem);
    }
    arr.MakeHeap(size);
    cout << endl << "Heap Sort:" << endl;
    cout << endl << "Before Sorting:" << endl;
    arr.Display();
    arr.HeapSort();
    cout << endl << "After Sorting:" << endl;
    arr.Display();
}

```

## Depth First Search in a Graph

```
/* Implement DFS */
#include <iostream>
#include <fstream>

using namespace std;

struct node
{
    int info;
    struct node* next;
};

class stack
{
    struct node* top;
public:
    stack()
    {
        top = nullptr;
    }

    void push(int);
    int pop();

    bool isEmpty()
    {
        return (top == nullptr);
    }

    void display();
};

void stack::push(int data)
{
    node* p;
    if ((p = new node) == nullptr)
    {
        cout << "Memory Exhausted";
        exit(0);
    }
    p = new node;
    p->info = data;
    p->next = nullptr;
    if (top != nullptr)
        p->next = top;
    top = p;
}
```

```

int stack::pop()
{
    struct node* temp;
    int value;
    if (top == nullptr)
    {
        cout << "\nThe stack is Empty" << endl;
        return -1;
    }
    temp = top;
    top = top->next;
    value = temp->info;
    delete temp;
    return value;
}

void stack::display()
{
    struct node* p = top;
    if (top == nullptr)
        cout << "\nNothing to Display\n";
    else
    {
        cout << "\nThe contents of Stack\n";
        while (p != nullptr)
        {
            cout << p->info << endl;
            p = p->next;
        }
    }
}

class Graph
{
    int n;
    int** A;
public:
    Graph(int size = 2);
    ~Graph();

    bool isConnected(int x, int y)
    {
        return (A[x - 1][y - 1] == 1);
    }

    void addEdge(int x, int y)
    {
        A[x - 1][y - 1] = A[y - 1][x - 1] = 1;
    }
}

```



```

        void DFS(int, int);
};

Graph::Graph(int size)
{
    int i, j;
    if (size < 2)
        n = 2;
    else
        n = size;
    A = new int*[n];
    for (i = 0; i < n; ++i)
        A[i] = new int[n];
    for (i = 0; i < n; ++i)
        for (j = 0; j < n; ++j)
            A[i][j] = 0;
}

Graph::~~Graph()
{
    for (int i = 0; i < n; ++i)
        delete[] A[i];
    delete[] A;
}

void Graph::DFS(int x, int required)
{
    stack s;
    // Boolean array to track visited nodes
    bool* visited = new bool[n + 1];
    int i;
    // Mark all as unvisited
    for (i = 0; i <= n; i++)
        visited[i] = false;
    s.push(x);
    visited[x] = true;
    if (x == required)
        return;
    cout << "Depth first Search starting from vertex ";
    cout << x << " : " << endl;
    while (!s.isEmpty())
    {
        int k = s.pop();
        if (k == required)
            break;
        cout << k << " ";
        for (i = n; i >= 0; --i)
            if (isConnected(k, i) && !visited[i])
            {
                s.push(i);
                visited[i] = true;
            }
    }
}

```

```

        }
    }
    cout << endl;
    delete[] visited;
}

int main()
{
    FILE* inFile;
    fopen_s(&inFile, "vertex.txt", "r+");
    int size, matrix[20][20];
    fscanf_s(inFile, "%d", &size);
    for (int i = 1; i <= size; i++)
    {
        for (int j = 1; j <= size; j++)
        {
            fscanf_s(inFile, "%d", &matrix[i][j]);
            cout << matrix[i][j] << " ";
        }
        cout << endl;
    }
    Graph g(size);
    for (int i = 1; i <= size; i++)
        for (int j = 1; j <= size; j++)
            if (matrix[i][j] != 0)
                g.addEdge(i, j);
    cout << "Enter the starting node: ";
    int source;
    cin >> source;
    cout << "Enter the destination node: ";
    int dest;
    cin >> dest;
    cout << endl << endl;
    g.DFS(source, dest);
}

```

## Breadth First Search in a Graph

```

/* Implement BFS */
#include <iostream>
#include <ctime>

using namespace std;

struct node
{
    int info;

```

```

        node* next;
    };

class Queue
{
    node* front;
    node* rear;
public:
    Queue()
    {
        front = nullptr;
        rear = nullptr;
    }

    ~Queue()
    {
        delete front;
    }

    bool isEmpty()
    {
        return (front == nullptr);
    }

    void push(int);
    int pop();
    void display();
};

void Queue::display()
{
    node* p = new node;
    p = front;
    if (front == nullptr)
    {
        cout << "\nNothing to Display\n";
    }
    else
    {
        while (p != nullptr)
        {
            cout << endl << p->info;
            p = p->next;
        }
    }
}

void Queue::push(int data)
{
    node* temp = new node();
    temp->info = data;

```

```

        temp->next = nullptr;
        if (front == nullptr)
            front = temp;
        else
            rear->next = temp;
        rear = temp;
    }

int Queue::pop()
{
    node* temp = new node();
    int value;
    if (front == nullptr)
    {
        cout << "\nQueue is Empty!" << endl;
        return -1;
    }
    temp = front;
    value = temp->info;
    front = front->next;
    delete temp;
    return value;
}

class Graph
{
    int n;
    int** A;
public:
    Graph(int size = 2);
    ~Graph();

    bool isConnected(int u, int v)
    {
        return (A[u - 1][v - 1] == 1);
    }

    void addEdge(int u, int v)
    {
        A[u - 1][v - 1] = A[v - 1][u - 1] = 1;
    }

    void BFS(int);
};

Graph::Graph(int size)
{
    int i, j;
    if (size < 2)
        n = 2;
    else

```

```

        n = size;
        A = new int*[n];
        for (i = 0; i < n; ++i)
            A[i] = new int[n];
        for (i = 0; i < n; ++i)
            for (j = 0; j < n; ++j)
                A[i][j] = 0;
    }

Graph::~~Graph()
{
    for (int i = 0; i < n; ++i)
        delete[] A[i];
    delete[] A;
}

void Graph::BFS(int s)
{
    Queue Q;
    // Keeps track of visited vertices
    bool* explored = new bool[n + 1];
    // Initialise all vertices as unexplored
    for (int i = 1; i <= n; ++i)
        explored[i] = false;

    // Push initial vertex to the queue
    Q.push(s);
    explored[s] = true;
    cout << "Breadth first search starting from vertex ";
    cout << s << " : " << endl;

    while (!Q.isEmpty())
    {
        int v = Q.pop();
        // Display the explored vertices
        cout << v << " ";
        // From the explored vertex v try to explore all the connected vertices
        for (int w = 1; w <= n; ++w)
            // Explore the vertex w if it is connected to v and if it is unexplored
            if (isConnected(v, w) && !explored[w])
            {
                Q.push(w);
                explored[w] = true;
            }
        cout << endl;
        delete[] explored;
    }
}

int main()
{

```

```

FILE* inFile;
fopen_s(&inFile, "vertex.txt", "r+");
int size, matrix[20][20];
fscanf_s(inFile, "%d", &size);
for (int i = 1; i <= size; i++)
{
    for (int j = 1; j <= size; j++)
    {
        fscanf_s(inFile, "%d", &matrix[i][j]);
        cout << matrix[i][j] << " ";
    }
    cout << endl;
}
Graph g(size);
for (int i = 1; i <= size; i++)
    for (int j = 1; j <= size; j++)
        if (matrix[i][j] != 0)
            g.addEdge(i, j);
cout << "Enter the starting node: ";
int source;
cin >> source;
/*cout << "Enter the destination node: ";
int dest;
cin >> dest;*/
cout << endl << endl;
// Explores all vertices findable from the source
g.BFS(source);
}

```

## Dijkstra's Algorithm to Find Shortest Distance between All Pairs of Vertices in a Graph

```

/* Find the shortest path between a given vertex and
all other vertices in a graph */
#include <iostream>
#define PERM 1
#define TEMP 0
#define INF INT_MAX

using namespace std;

struct node
{
    int pre;
    int dist;
    bool status;
};

```

```

int dijkstra(int s, int d, int path[], int weight[][10], int* len, int n)
{
    // s is the source, d is the destination
    // path will store the shortest path, len will give the length of the path
    struct node node[10];
    int i, current, min, u, v, count = 0, newdist;
    *len = 0;
    // Set all vertices' status to temporary and assign infinite weights
    for (i = 1; i <= n; i++)
    {
        node[i].pre = 0;
        node[i].status = TEMP;
        node[i].dist = INF;
    }
    // Force the first vertex to be selected
    node[s].pre = 0;
    node[s].dist = 0;
    node[s].status = PERM;
    current = s;
    // Until we reach the destination node, keep repeating
    while (current != d)
    {
        for (i = 1; i <= n; i++)
        {
            // For all unvisited vertices find the tentative distance and
            // assign whichever is smaller among the tentative distance and
            // the currently assigned distance
            if (weight[current][i] > 0 && node[i].status == TEMP)
            {
                newdist = node[current].dist + weight[current][i];
                if (newdist < node[i].dist)
                {
                    node[i].dist = newdist;
                    node[i].pre = current;
                }
            }
        }
        current = 0;
        min = INF;
        // Select the unvisited vertex with the smallest tentative distance
        // Mark it as the current vertex
        for (i = 1; i <= n; i++)
        {
            if (node[i].status == TEMP && node[i].dist < min)
            {
                min = node[i].dist;
                current = i;
            }
        }
        // If there is no such vertex, the algorithm was unable to find a path
    }
}

```

```

        if (current == 0)
            return 0;
        // Mark the selected vertex as visited
        node[current].status = PERM;
    }
    // Populate the path matrix and the count of elements in path
    while (current != 0)
    {
        count++;
        path[count] = current;
        current = node[current].pre;
    }
    // Find the path length by traversing in reverse order
    for (i = count; i > 1; i--)
    {
        u = path[i];
        v = path[i - 1];
        *len += weight[u][v];
    }
    // Return the number of elements in the path matrix
    return count;
}

int main()
{
    int i, j, n, weight[10][10], s, d, len, count, path[20];
    char ch1;
    // Open the file containing the adjacency matrix
    FILE* f;
    fopen_s(&f, "vertex.txt", "r+");
    fscanf_s(f, "%d", &n);
    // Read the weights from the file
    for (i = 1; i <= n; i++)
    {
        for (j = 1; j <= n; j++)
            fscanf_s(f, "%d", &weight[i][j]);
    }
    // Print the adjacency matrix
    cout << "\nWeight Matrix:" << endl;
    for (i = 1; i <= n; i++)
    {
        for (j = 1; j <= n; j++)
            cout << " " << weight[i][j] << "\t";
        cout << endl;
    }
    // Ask for the source node
    cout << "\nEnter the source node: ";
    cin >> ch1;
    // Convert the entered character into it corresponding alphabet
    s = ch1 - 'a' + 1;
    // Run the algorithm over the set of all possible destination vertices

```



```

for (int c = 1; c <= n; c++)
{
    d = c;
    count = dijkstra(s, d, path, weight, &len, n);
    // If the path exists, print it out
    if (len > 0)
    {
        cout << "\n\nShortest Path between " << char(s + 'a' - 1)
              << " (SOURCE) and " << char(d + 'a' - 1)
              << " (DESTINATION) is: ";
        for (i = count; i >= 1; i--)
            cout << char(path[i] + 'a' - 1);
        cout << "\n\nLength of the shortest path is: " << len;
    }
    else
        cout << "\n\nNo Path exists between the nodes "
              << char(s + 'a' - 1) << " and " << char(d + 'a' - 1);
}
}

```

## Prim's Algorithm to Find Minimum Spanning Tree

```

/* Implement Prim's algorithm to find the MST of a graph */
#include <iostream>
#include <stdio.h>

using namespace std;

int main()
{
    int i, j, k, n, x, u = 0, v = 0, small, smallest, pos = 0, total = 0;
    int weight[10][10], visited[10], parent[10];
    /*
        n is the number of vertices in the graph
        parent is the constructed MST
    */
    // Open the file containing the adjacency matrix
    FILE* f;
    f = fopen("vertex.txt", "r+");
    fscanf(f, "%d", &n);
    // Read all the weights
    for (i = 1; i <= n; i++)
        for (j = 1; j <= n; j++)
            fscanf(f, "%d", &weight[i][j]);
    // Print the weight matrix
    for (i = 1; i <= n; i++)
    {

```

```

        for (j = 1; j <= n; j++)
            cout << " " << weight[i][j] << "\t";
        cout << endl;
    }
    /*
    Algorithm:
    Mark all nodes as unvisited and assign infinite weights to each vertex
    Select the first vertex
    While there are elements not yet selected in the MST, do:
        Pick an unvisited vertex not yet in the MST and,
        which has the shortest edge joining it to a vertex in the MST
        For all the neighbours of the vertex:
            Update the minimum edge length with the value
            of the edge length of the vertex selected earlier
        Add the picked vertex to the MST
    */
    // Set all vertices as unvisited and the MST as empty
    for (i = 1; i <= n; i++)
    {
        parent[i] = -1;
        visited[i] = 0;
    }
    // Pick the first vertex
    x = 1;
    parent[x] = 1;
    visited[x] = 1;
    // Repeat over all remaining vertices
    for (i = 2; i <= n; i++)
    {
        k = 1;
        // The weight of the shortest edge between a vertex in the MST
        // and an unselected vertex
        smallest = 9999;
        // For all vertices cuurently in the MST
        while (parent[k] != -1)
        {
            // The weight of the vertex nearest to a vertex in the MST
            // in a given row
            small = 999;
            for (j = 1; j <= n; j++)
            {
                // Find vertex nearest (with minimum edge weight) to k
                if (weight[k][j] > 0 && visited[j] == 0 && weight[k][j] < small)
                {
                    small = weight[k][j];
                    pos = j;
                    u = parent[k];
                }
            }
            // If the previously decided minimum weight has been beaten
            // update the global minimum

```

```

        if (small <= smallest)
        {
            smallest = small;
            v = pos;
        }
        k++;
    }
    // If we reach here means we have found the shortest edge between
    // a vertex in the MST and an unselected vertex
    // Update the cost of the MST, add the chosen vertex to the MST
    // and mark it as visited
    total += smallest;
    parent[x++] = v;
    visited[v] = 1;
    cout << "\nEdge from " << char(u + 'a' - 1) << "->" << char(v + 'a' - 1) << endl;
}
cout << "\n Weight of the Minimum Spanning Tree : " << total;
}

```

## Kruskal's Algorithm to Find Minimum Spanning Tree

```

#include <iostream>

using namespace std;

int main()
{
    int i, j, k, n, visit, l, v, count = 0, count1, vst, p;
    int weight[10][10], visited[10];
    int dup1, dup2;
    FILE* f;
    fopen_s(&f, "vertex.txt", "r+");
    fscanf_s(f, "%d", &n);
    // Read all the weights
    for (i = 1; i <= n; i++)
        for (j = 1; j <= n; j++)
            fscanf_s(f, "%d", &weight[i][j]);
    // Print the weight matrix
    for (i = 1; i <= n; i++)
    {
        for (j = 1; j <= n; j++)
            cout << " " << weight[i][j] << "\t";
        cout << endl;
    }
    for (i = 1; i <= n; i++)
        for (j = 1; j <= n; j++)
            if (weight[i][j] == 0)
                weight[i][j] = INT_MAX;
}

```

```

visit = 1;
while (visit < n)
{
    v = INT_MAX;
    for (i = 1; i <= n; i++)
        for (j = 1; j <= n; j++)
            if (weight[i][j] != INT_MAX && weight[i][j] < v
                && weight[i][j] != -1)
            {
                int count = 0;
                for (p = 1; p <= n; p++)
                {
                    if (visited[p] == i || visited[p] == j)
                        count++;
                }
                if (count >= 2)
                {
                    for (p = 1; p <= n; p++)
                        if (weight[i][p] != INT_MAX && p != j)
                            dup1 = p;
                    for (p = 1; p <= n; p++)
                        if (weight[j][p] != INT_MAX && p != i)
                            dup2 = p;

                    if (weight[dup1][dup2] == -1)
                        continue;
                }
                l = i;
                k = j;
                v = weight[i][j];
            }
    cout << endl;
    cout << "Edge from " << char(l + 'a' - 1) << "->" << char(k + 'a' - 1)
        << endl;
    weight[l][k] = -1;
    weight[k][l] = -1;
    visit++;
    count1 = 0;
    for (i = 1; i <= n; i++)
    {
        if (visited[i] == l)
            count++;
        if (visited[i] == k)
            count1++;
    }
    if (count == 0)
        visited[++vst] = l;
    if (count1 == 0)
        visited[++vst] = k;
}
}

```