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2020115015

Reliability Assignment

Question 1

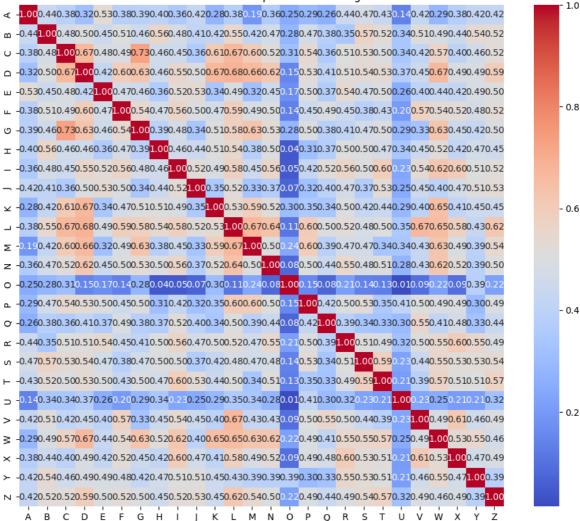
```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns

# import qldata.csv as a pandas dataframe
df = pd.read_csv('qldata.csv')
df.head()
```

Out[]:		Α	В	С	D	E	F	G	Н	I	J	•••	Q	R	S	Т	U	V	W	X	Υ	Z
	0	2	-1	-1	-1	-1	-1	4	-2	3	-2	•••	1	0	-1	1	-4	-1	2	1	-2	4
	1	-3	-2	-2	-3	-3	-4	-4	-2	-1	-3		-2	-1	-2	-2	-1	-1	-4	-1	-4	-1
	2	2	3	1	0	-1	-1	2	-1	2	3		1	0	0	2	-1	2	-1	0	3	4
	3	3	1	-1	-2	-1	-1	-4	-2	-3	0	•••	2	0	0	1	-1	1	-1	-1	1	1
	4	-2	3	-1	1	-1	1	-2	1	3	2		2	0	-1	2	1	2	-2	1	2	3

5 rows × 26 columns

Correlation Heatmap of Advert Ratings



Now, if a participant had made random ratings, we would expect the correlation between the ratings to be close to 0. Hence, the mean of the absolute values of correlations between the person who rated randomly and the others should ideally be the lowest, as there wouldn't be any strongly positive or strongly negative correlations of the random rater.

```
In []: # calculate the mean of the absolute values of correlations for each columean_corr = np.abs(corr_matrix).mean(axis=0)
mean_corr
```

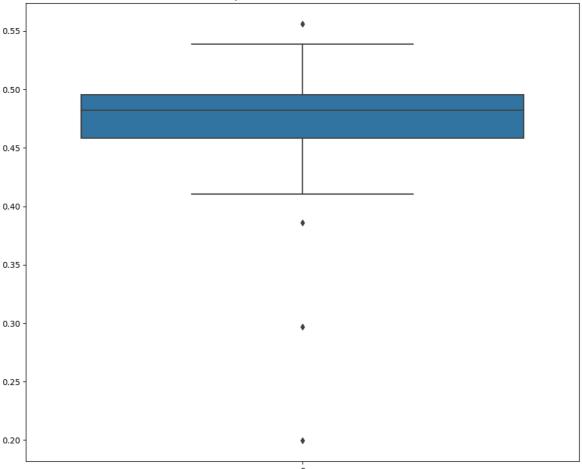
```
Out[]: A
              0.385969
              0.482304
         В
        C
              0.514604
        D
              0.538891
        Ε
              0.456477
         F
              0.490640
        G
              0.493497
        Н
              0.453248
         Ι
              0.505283
         J
              0.437580
              0.472085
              0.555878
        0.483027
        М
        Ν
              0.493915
         0
              0.199568
              0.462734
         0
              0.410257
              0.495683
        R
         S
              0.482357
        Т
              0.478174
        U
              0.296747
         V
              0.470284
              0.529803
        W
        Χ
              0.484479
         Υ
              0.465537
              0.503806
         dtype: float64
In [ ]:
        min_mean_corr = mean_corr.idxmin()
        min_mean_corr_value = mean_corr.min()
        print(f'The minimum mean correlation value is {min_mean_corr_value}, and
       The minimum mean correlation value is 0.19956783530913091, and it correspo
       nds to the rater 0.
In []: # make a boxplot of the mean absolute correlation values
        plt.figure(figsize=(12, 10))
        sns.boxplot(mean_corr)
        plt.title('Boxplot of Mean Correlation Values')
        plt.show()
       /Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/categorica
```

l.py:486: FutureWarning: Series.__getitem__ treating keys as positions is deprecated. In a future version, integer keys will always be treated as la bels (consistent with DataFrame behavior). To access a value by position,

use `ser.iloc[pos]`

if np.isscalar(data[0]):





From the values of correlation matrix and the heatmap, we can conclude that the person who was most likely to give out random ratings to the adverts was 'O'. This is because 'O' has the least mean of absolute values of correlation with others raters, suggesting that his ratings were the least correlated (either positively or negatively) with all other raters on an average, as expected out of a random rating procedure.

Visually, we can see that the colours in the heatmap for 'O' strongest shades of blue, indicating the weak correlation with other raters.

```
In [ ]:
        df = pd.read_csv('q2data.csv')
         df.head()
Out[]:
            JS1
                 JS2
                      JS3
                             JS4
                                   JSAVG JP1
                                                JP2
                                                      JP3
                                                             JP4
                                                                   JPAVG
         0
              9
                  9.5
                      9.75 7.875
                                  9.03125
                                                 1.5
                                                      1.75 4.875
                                                                  2.28125
                                                           7.000 5.25000
         1
                  6.5 6.25
                            7.125 6.21875
                                                 4.0 4.00
              5
                                             6
         2
              4
                  5.0 3.50 6.750 4.81250
                                             5
                                                 6.5 5.25 4.625 5.34375
         3
                     5.50 4.750
                                  5.81250
                                                 7.0 8.50 8.250
              6
                  7.0
                                                                  7.43750
              7
                      6.75
                            7.375
                                  7.15625
                                                 5.0
                                                     4.50 9.250
         4
                  7.5
                                             6
                                                                  6.18750
```

As stated in the paper, "Gliem, Joseph & Gliem, Rosemary. (2003). Calculating, Interpreting, And Reporting Cronbach's Alpha Reliability Coefficient For Likert-Type Scales." 2003 Midwest Research to Practice Conference in Adult, Continuing, and

Community Education. The formula relating the mean of correlation values(r) and the number of items(k) to cronbach's alpha (α)

$\alpha = rk / [1 + (k - 1) r]$

```
In []: def calculate_mean_corr(corr_matrix):
    num = 0
    sum = 0
    for i in range(4):
        for j in range(i+1, 4):
            num += 1
            sum+= corr_matrix.iloc[i, j]

    print(f'The mean correlation value is {sum/num}.')

    return sum/num

def cronbach_alpha(r, k):
    return r*k/(1+ ((k-1)*r) )
```

Chronbach's Alpha for Job Satisfaction

```
In []: JSdf = df.iloc[:, :4]
    JSdf.head()
    corr_matrix = JSdf.corr(method='spearman')
    corr_matrix
```

```
Out[ ]:
                  JS1
                            JS2
                                     JS3
                                               JS4
         JS1
             1.000000 0.824366
                                 0.532531 0.373851
         JS2 0.824366
                       1.000000
                                 0.715501 0.517486
         JS3
             0.532531
                       0.715501 1.000000 0.651675
         JS4
             0.373851  0.517486  0.651675  1.000000
```

```
In [ ]: mean_corr = calculate_mean_corr(corr_matrix)
    print(f'The chronbach\'s alpha value for the items measuring job satisfac
```

The mean correlation value is 0.6025684054632915.

The chronbach's alpha value for the items measuring job satisfaction is 0. 8584496719182925.

Chronbach's Alpha for Job Performance

```
In []: # make another variable JPdf that contains the columns 6-9 of df
    JPdf = df.iloc[:, 5:9]
    JPdf.head()
    corr_matrix = JPdf.corr(method='spearman')
    corr_matrix
```

Out[]:		JP1	JP2	JP3	JP4
	JP1	1.000000	0.536630	0.127395	-0.010899
	JP2	0.536630	1.000000	0.458866	0.038797
	JP3	0.127395	0.458866	1.000000	0.145061
	JP4	-0.010899	0.038797	0.145061	1.000000

```
In [ ]: mean_corr = calculate_mean_corr(corr_matrix)
   print(f'The chronbach\'s alpha value for the items measuring job performa
```

The mean correlation value is 0.21597505470509304.

The chronbach's alpha value for the items measuring job performance is 0.5 242351034090641.

Observations and Inferences

Cronbach's alpha is a measure of internal consistency reliability, which indicates how well the items in a scale or questionnaire correlate with each other. Typically, higher values of Cronbach's alpha indicate greater internal consistency among the items.

- Job Satisfaction (JS): The Cronbach's alpha value for the items measuring job satisfaction (JS) is 0.858, which is relatively high. This suggests that the items in the job satisfaction questionnaire are highly correlated with each other, indicating good internal consistency. In other words, the items within the job satisfaction questionnaire tend to measure the same underlying construct consistently. This suggests that the questionnaire items are reliable in measuring job satisfaction among participants.
- Job Performance (JP): The Cronbach's alpha value for the items measuring job performance (JP) is 0.524, which is lower compared to the Cronbach's alpha for job satisfaction. While a Cronbach's alpha of 0.524 still indicates some level of internal consistency among the items, it is lower than desirable. This suggests that the items within the job performance questionnaire may not be as strongly correlated with each other compared to the job satisfaction questionnaire. It's possible that the items in the job performance questionnaire may not fully capture the same underlying construct consistently, leading to lower internal consistency.

Hence, the job satisfaction questionnaire demonstrates good internal consistency and reliability. However, the job performance questionnaire shows lower internal consistency and reliability. Now, based off the following table, we can see that we can label the reliability level of JS questionaire to be Good and that of JP to be Poor.

No	Coefficient of Cronbach's Alpha	Reliability Level
1	More than 0.90	Excellent
2	0.80-0.89	Good
3	0.70-0.79	Acceptable
4	0.669	Questionable
5	0.5-0.59	Poor
6	Less than 0.59	Unacceptable

Question 3

1. Exploratory Analysis, and Normality Testing

```
In [ ]: # load the data from q3data.csv
        df = pd.read_csv('q3data.csv')
        df.head()
Out[]:
            datetime season holiday workingday weather temp atemp humidity winds
            2011-01-
         0
                 01
                          1
                                  0
                                              0
                                                       1 9.84 14.395
                                                                             81
            00:00:00
            2011-01-
         1
                 01
                          1
                                  0
                                              0
                                                          9.02 13.635
                                                                             80
```

```
01:00:00
   2011-01-
2
                    1
                             0
                                          0
                                                         9.02 13.635
                                                                              80
          01
   02:00:00
   2011-01-
3
                             0
                                          0
                                                         9.84 14.395
                                                                              75
          01
                    1
   03:00:00
   2011-01-
```

0

9.84 14.395

75

```
In [ ]:
        import pandas as pd
        import numpy as np
        import seaborn as sns
        import matplotlib.pyplot as plt
        # from scipy stats import shapiro
        from scipy.stats import shapiro, probplot
        # Select numerical columns for analysis
        numerical_cols = ['season',
                                        'holiday', 'workingday',
                                                                        'weather'
        # Plot histograms for each numerical variable
        for col in numerical_cols:
            plt.figure(figsize=(8, 5))
            sns.histplot(df[col], kde=True, color='skyblue', bins=20)
            plt.title(f'Histogram of {col}')
            plt.xlabel(col)
            plt.ylabel('Frequency')
            plt.show()
```

0

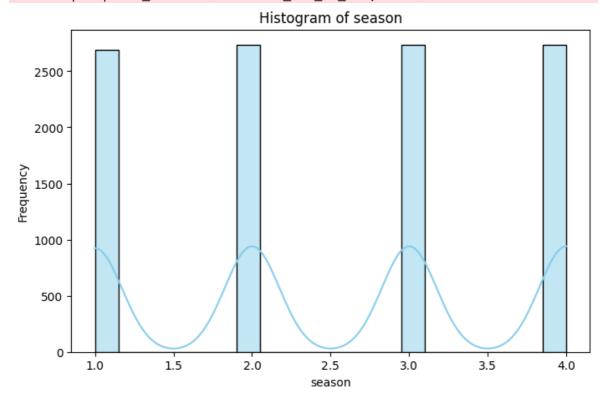
1

01

04:00:00

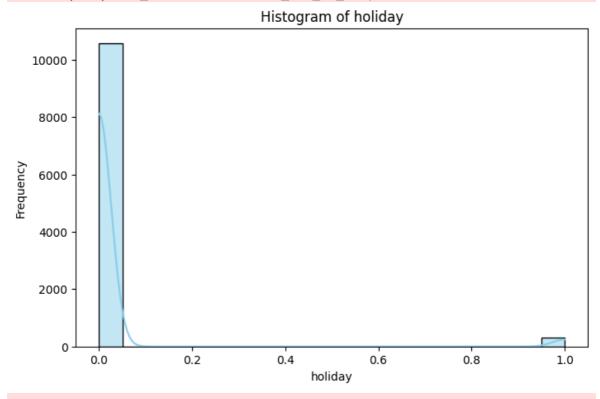
```
# Generate Q-Q plots for each numerical variable
for col in numerical_cols:
    plt.figure(figsize=(8, 5))
    probplot(df[col], dist="norm", plot=plt)
    plt.title(f'Q-Q Plot of {col}')
    plt.xlabel('Theoretical quantiles')
    plt.ylabel(f'Ordered Values of {col}')
    plt.show()
# Perform Shapiro-Wilk test for each numerical variable
for col in numerical cols:
    stat, p = shapiro(df[col])
    print(f'Shapiro-Wilk test for {col}: p-value={p}')
    if p > 0.05:
        print(f'{col} is normally distributed\n')
    else:
        print(f'{col} is not normally distributed\n')
```

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p
y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo
ved in a future version. Use isinstance(dtype, CategoricalDtype) instead
if pd.api.types.is_categorical_dtype(vector):
/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p
y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo
ved in a future version. Convert inf values to NaN before operating instea



/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

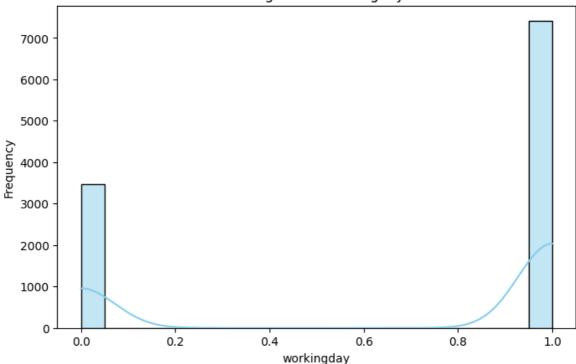
with pd.option_context('mode.use_inf_as_na', True):



/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo ved in a future version. Use isinstance(dtype, CategoricalDtype) instead if pd.api.types.is_categorical_dtype(vector):

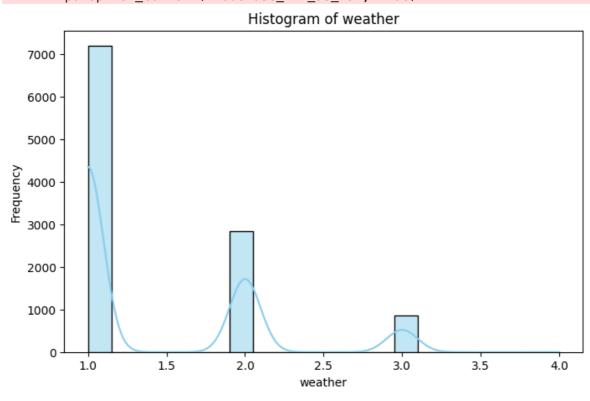
/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instead.

Histogram of workingday



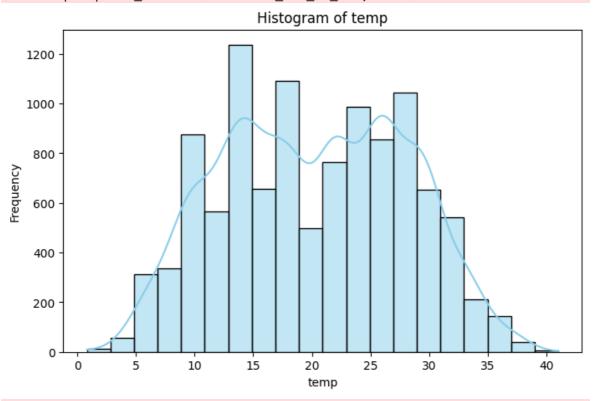
/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo ved in a future version. Use isinstance(dtype, CategoricalDtype) instead if pd.api.types.is_categorical_dtype(vector):

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.



/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

with pd.option_context('mode.use_inf_as_na', True):



/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo ved in a future version. Use isinstance(dtype, CategoricalDtype) instead if pd.api.types.is_categorical_dtype(vector):

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instead

0

0

Histogram of atemp 1200 - 1000 - 800 - 400 - 200 - 1000 -

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo ved in a future version. Use isinstance(dtype, CategoricalDtype) instead if pd.api.types.is_categorical_dtype(vector):

atemp

20

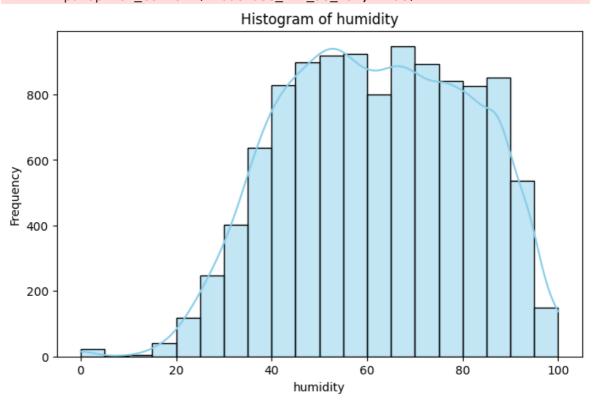
30

40

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

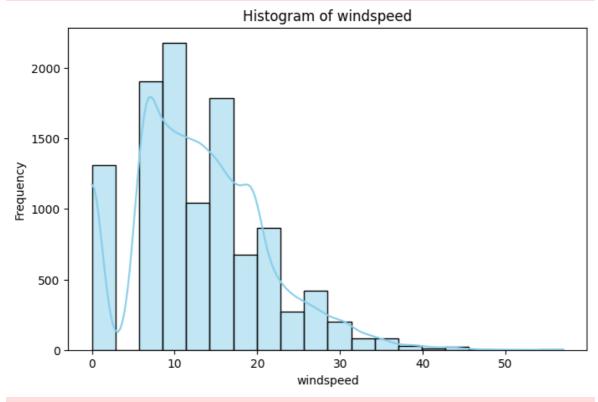
with pd.option_context('mode.use_inf_as_na', True):

10



/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

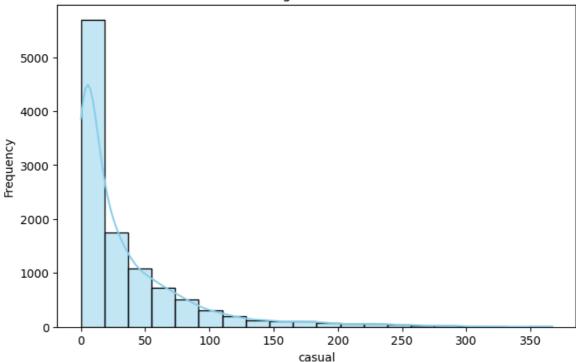
with pd.option_context('mode.use_inf_as_na', True):



/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo ved in a future version. Use isinstance(dtype, CategoricalDtype) instead if pd.api.types.is_categorical_dtype(vector):

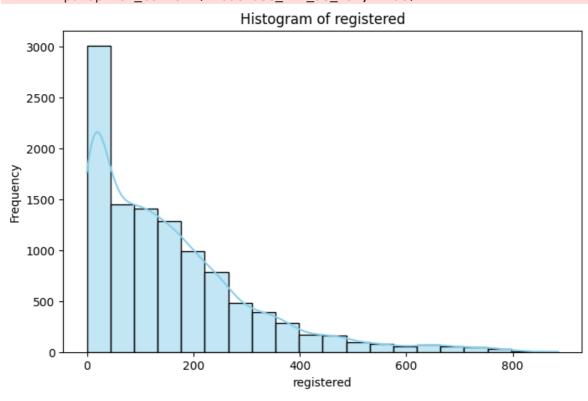
/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instead

Histogram of casual

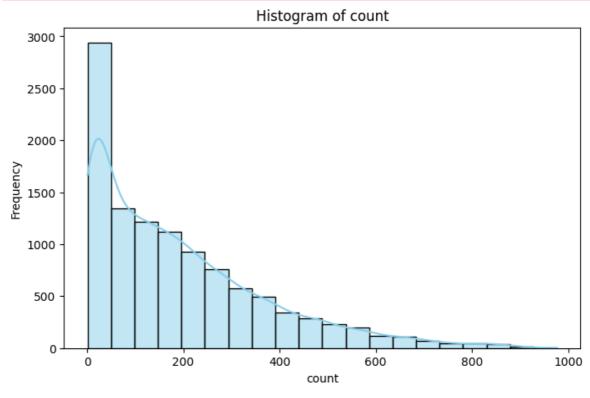


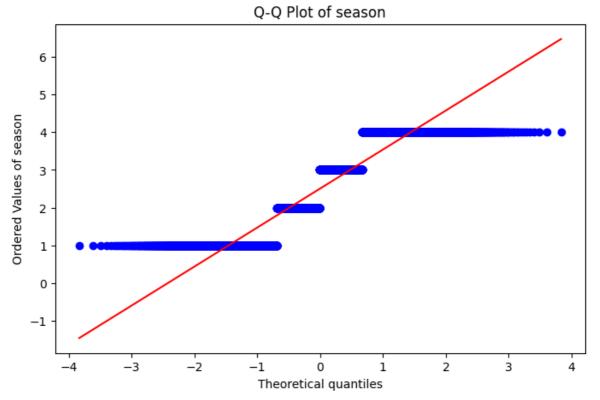
/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo ved in a future version. Use isinstance(dtype, CategoricalDtype) instead if pd.api.types.is_categorical_dtype(vector):

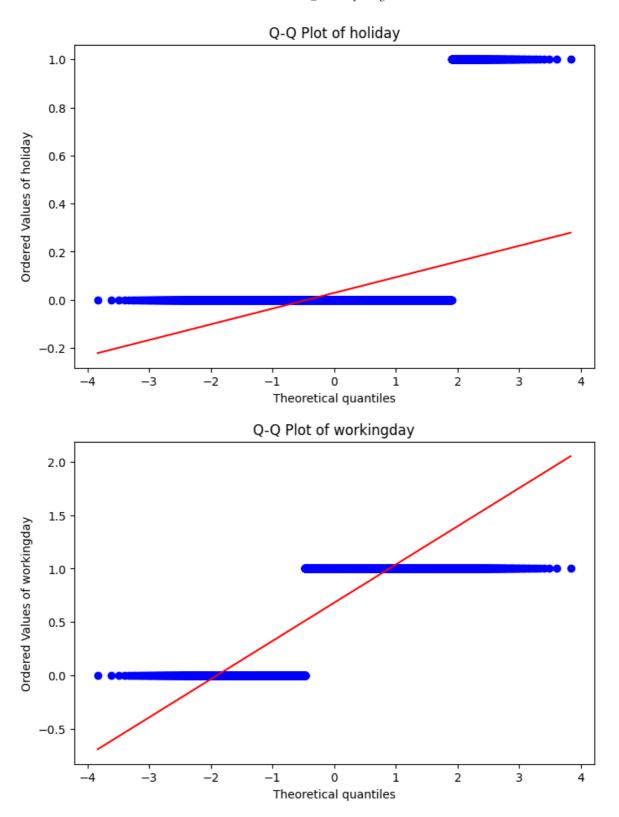
/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

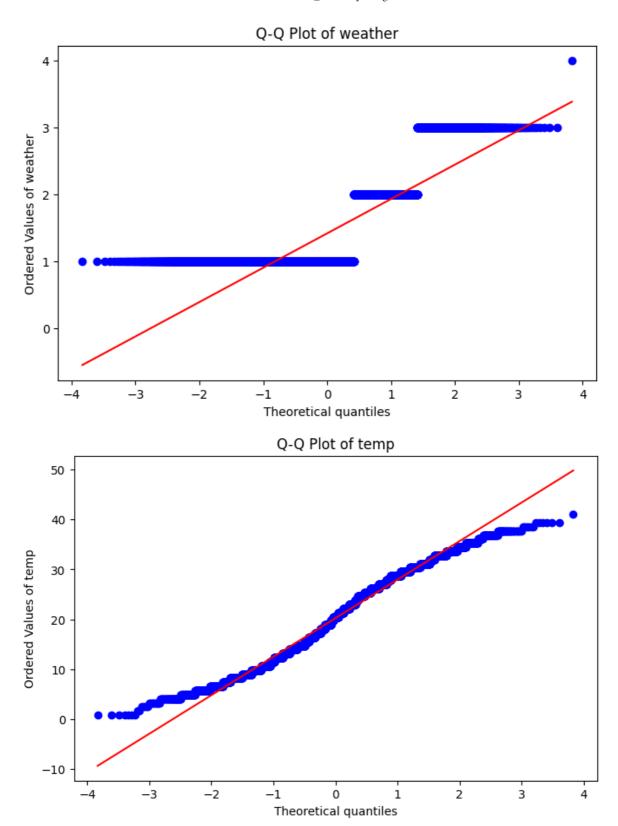


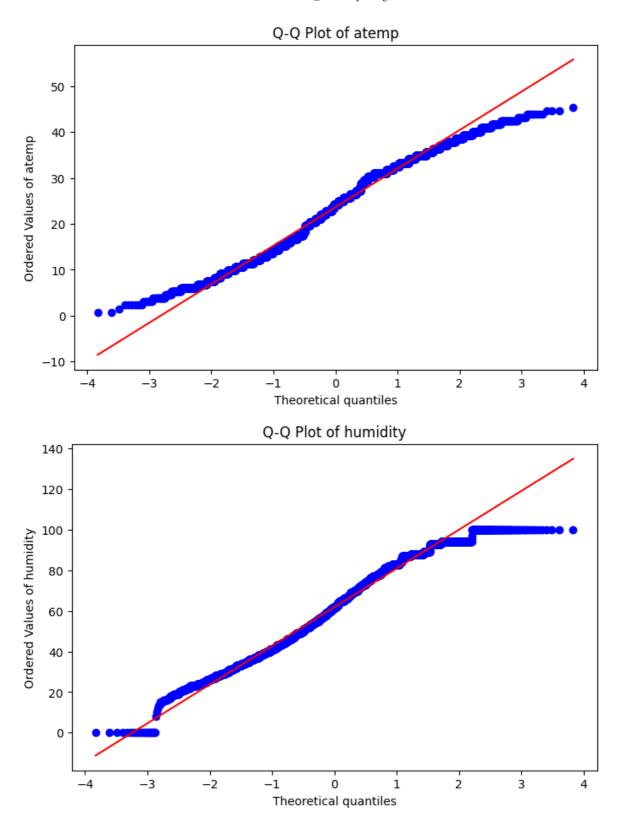
/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

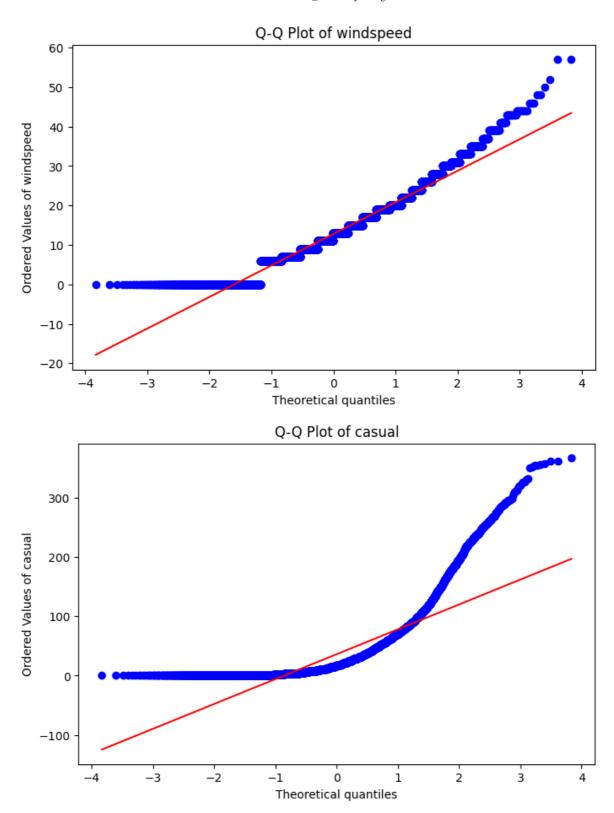


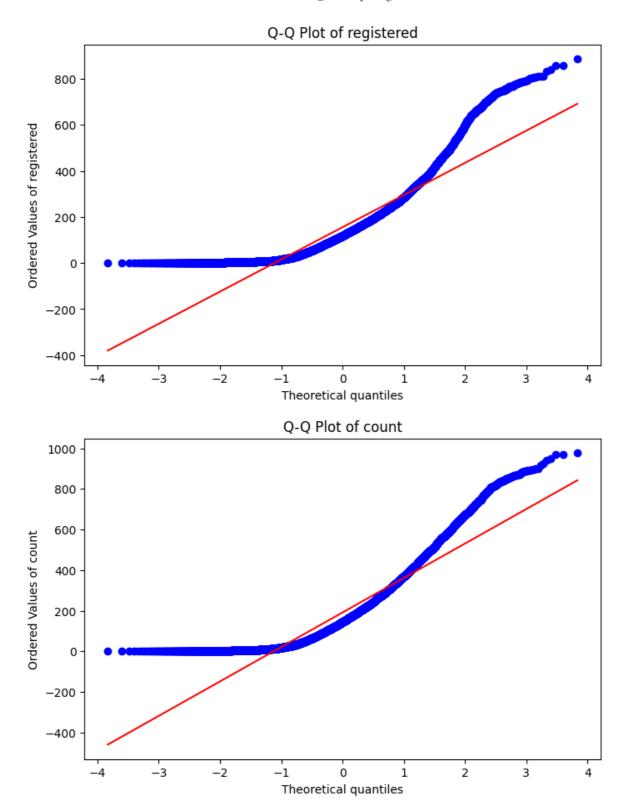












```
Shapiro-Wilk test for season: p-value=0.0
season is not normally distributed
Shapiro-Wilk test for holiday: p-value=0.0
holiday is not normally distributed
Shapiro-Wilk test for workingday: p-value=0.0
workingday is not normally distributed
Shapiro-Wilk test for weather: p-value=0.0
weather is not normally distributed
Shapiro-Wilk test for temp: p-value=4.581396320636487e-36
temp is not normally distributed
Shapiro-Wilk test for atemp: p-value=3.3570672250420043e-35
atemp is not normally distributed
Shapiro-Wilk test for humidity: p-value=1.2437889654838796e-34
humidity is not normally distributed
Shapiro-Wilk test for windspeed: p-value=0.0
windspeed is not normally distributed
Shapiro-Wilk test for casual: p-value=0.0
casual is not normally distributed
Shapiro-Wilk test for registered: p-value=0.0
registered is not normally distributed
Shapiro-Wilk test for count: p-value=0.0
count is not normally distributed
```

```
/Users/hari/Library/Python/3.9/lib/python/site-packages/scipy/stats/_mores tats.py:1882: UserWarning: p-value may not be accurate for N > 5000. warnings.warn("p-value may not be accurate for N > 5000.")
```

As we observe from the Shapiro-Wilk test, none of the variables are normally distributed as the p values are far lesser than 0.05 in all the cases. However, the library does warn that the results may not be accurate for datapoints >5000.

Even after reducing the dataset, similar results were obtained for the Shapiro-Wilk test. Hence, we can conclude that none of the variables are indeed normally distributed. However, the q-q plots and the histograms do give us an indea to the extent of how far or close from normal distribution the variables are. (For e.g. Humidity, Temperature and Weather do seem to be the closest amongst all the variables to having a normal distribution).

```
In []: from scipy.stats import boxcox

transformed_data = pd.DataFrame()
for col in numerical_cols:
    transformed_col, _ = boxcox(df[col] + 1) # Adding 1 to handle zero v
    transformed_data[col] = transformed_col

# Plot histograms of transformed data
for col in transformed_data.columns:
```

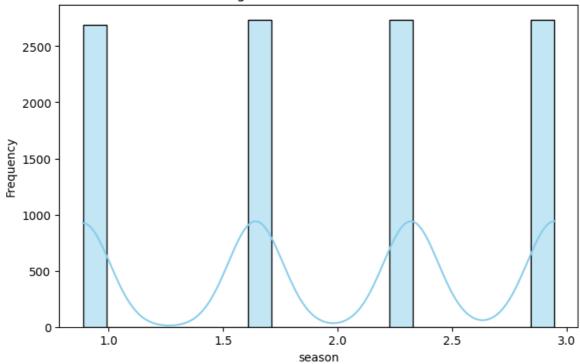
```
plt.figure(figsize=(8, 5))
    sns.histplot(transformed_data[col], kde=True, color='skyblue', bins=2
    plt.title(f'Histogram of Transformed {col}')
    plt.xlabel(col)
    plt.ylabel('Frequency')
    plt.show()

# Generate Q-Q plots of transformed data
for col in transformed_data.columns:
    plt.figure(figsize=(8, 5))
    probplot(transformed_data[col], dist="norm", plot=plt)
    plt.title(f'Q-Q Plot of Transformed {col}')
    plt.xlabel('Theoretical quantiles')
    plt.ylabel(f'Ordered Values of Transformed {col}')
    plt.show()
```

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

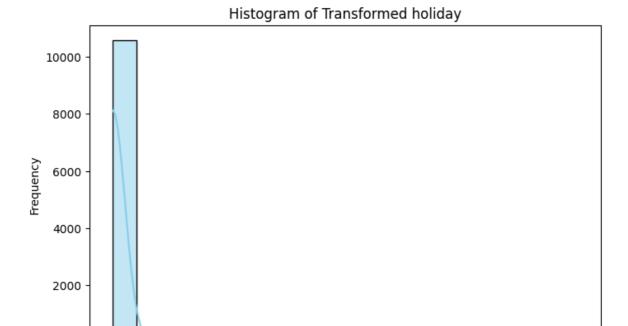
with pd.option context('mode.use inf as na', True):





/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo ved in a future version. Use isinstance(dtype, CategoricalDtype) instead if pd.api.types.is_categorical_dtype(vector):

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.



0.0075

0.0100

holiday

0.0125

0.0150

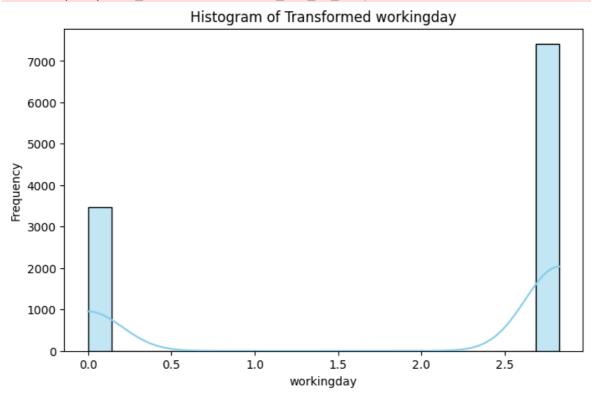
0.0175

0.0200

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

with pd.option_context('mode.use_inf_as_na', True):

0.0050

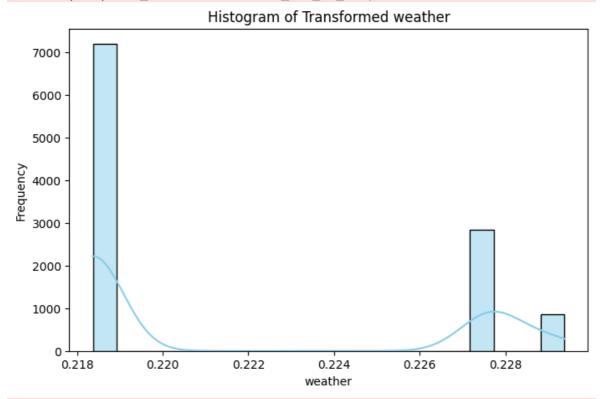


0.0000

0.0025

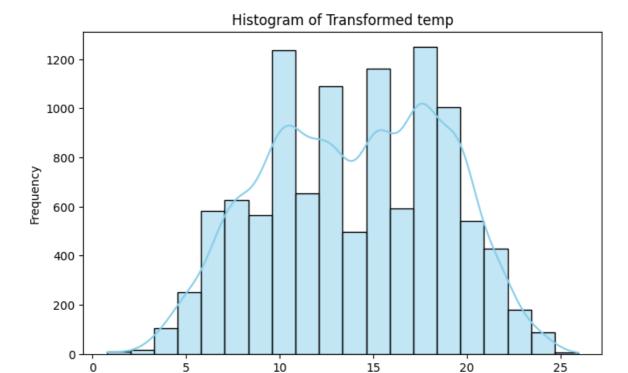
/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

with pd.option_context('mode.use_inf_as_na', True):



/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo ved in a future version. Use isinstance(dtype, CategoricalDtype) instead if pd.api.types.is_categorical_dtype(vector):

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instead



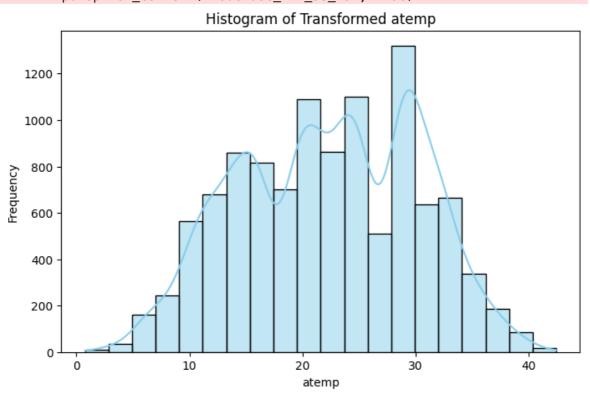
temp

20

10

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea

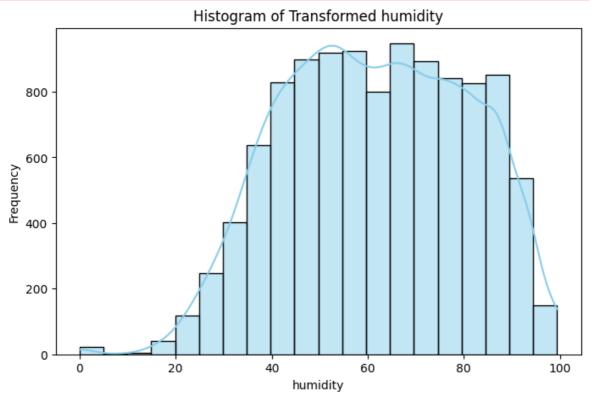
with pd.option_context('mode.use_inf_as_na', True):



0

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

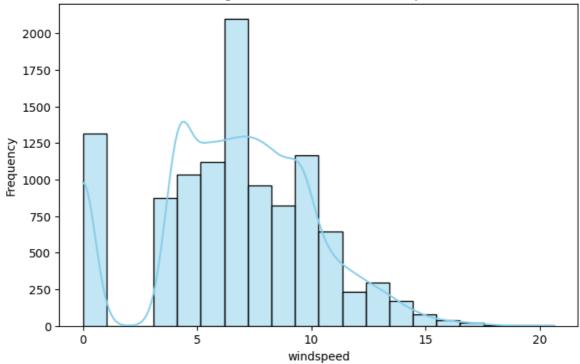
with pd.option_context('mode.use_inf_as_na', True):



/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo ved in a future version. Use isinstance(dtype, CategoricalDtype) instead if pd.api.types.is_categorical_dtype(vector):

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instead

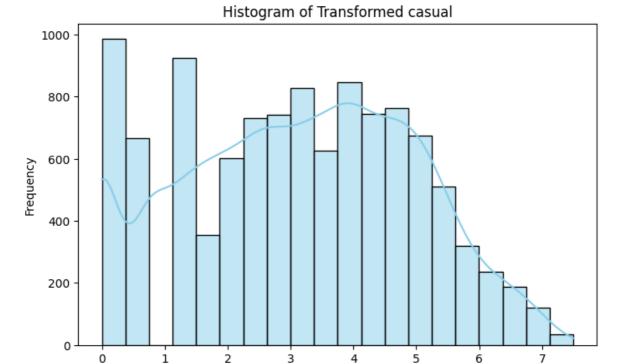
Histogram of Transformed windspeed



/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo ved in a future version. Use isinstance(dtype, CategoricalDtype) instead if pd.api.types.is_categorical_dtype(vector):

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

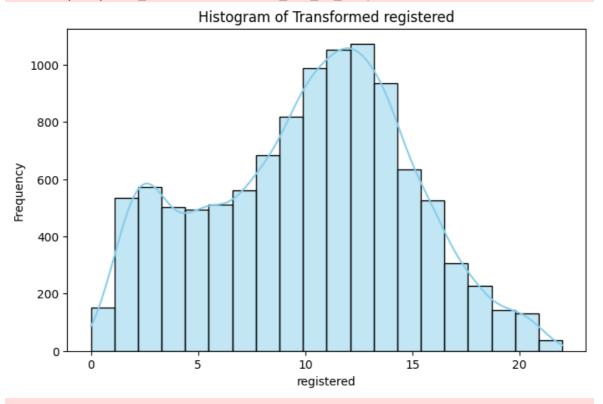
with pd.option_context('mode.use_inf_as_na', True):



casual

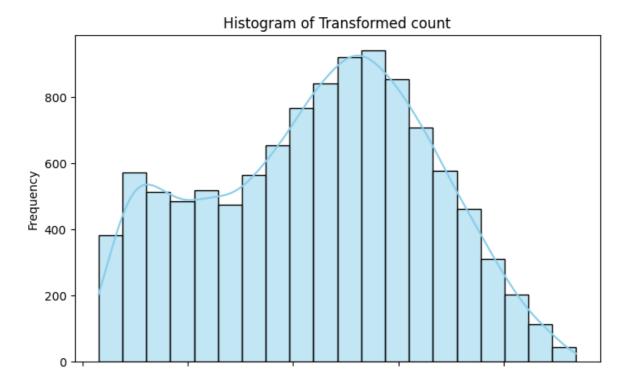
/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instea d.

with pd.option_context('mode.use_inf_as_na', True):



/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1498: FutureWarning: is_categorical_dtype is deprecated and will be remo ved in a future version. Use isinstance(dtype, CategoricalDtype) instead if pd.api.types.is_categorical_dtype(vector):

/Users/hari/Library/Python/3.9/lib/python/site-packages/seaborn/_oldcore.p y:1119: FutureWarning: use_inf_as_na option is deprecated and will be remo ved in a future version. Convert inf values to NaN before operating instead

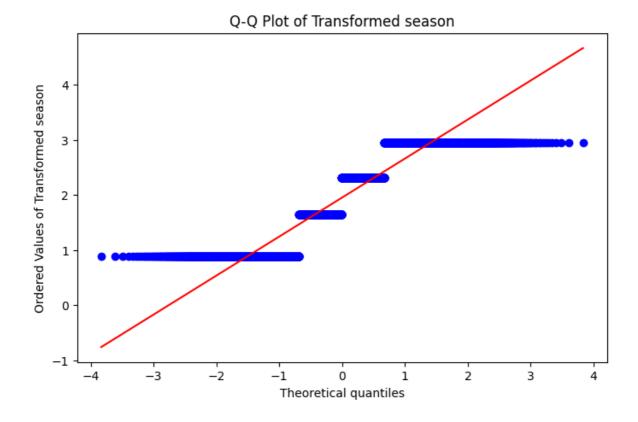


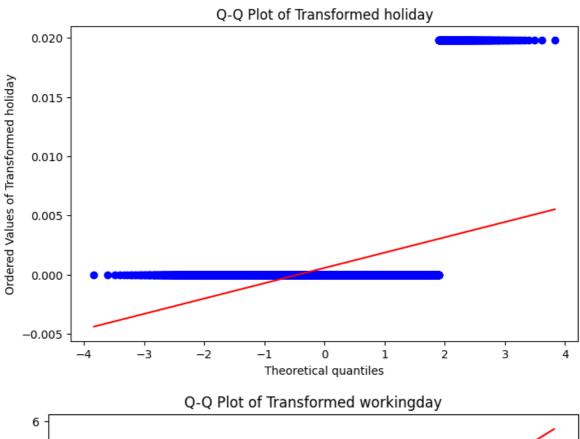
10

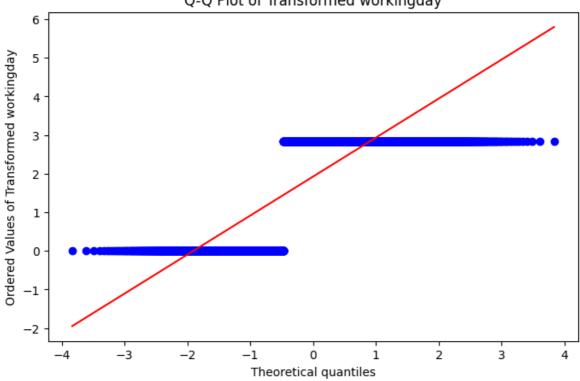
count

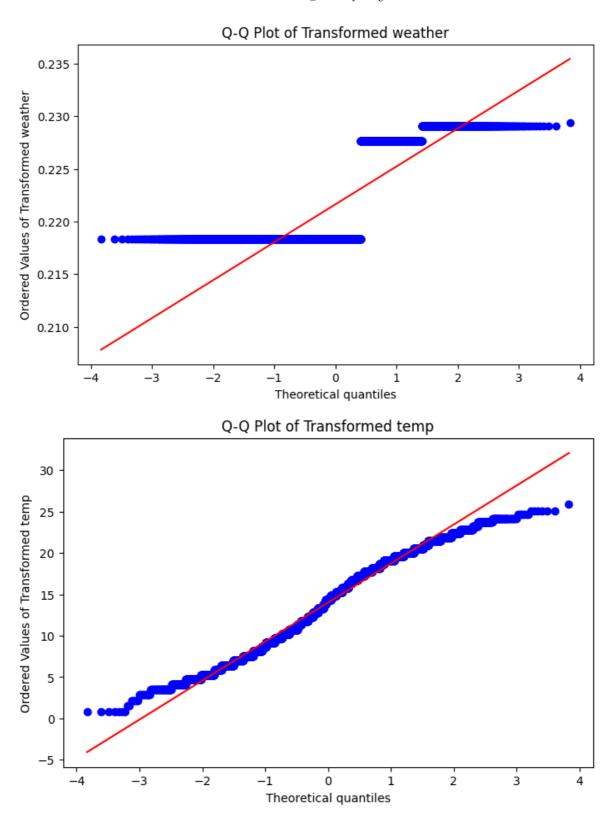
15

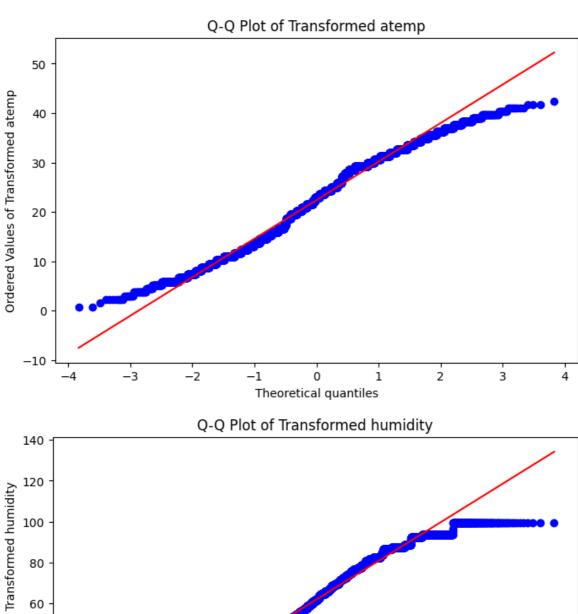
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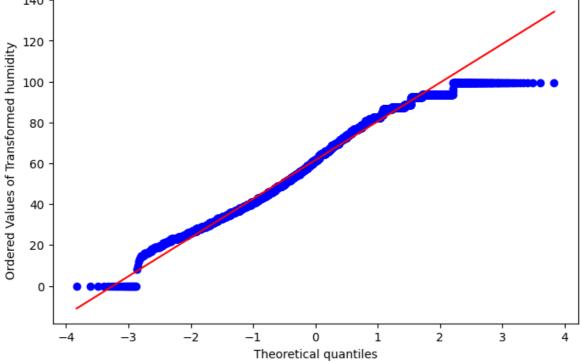


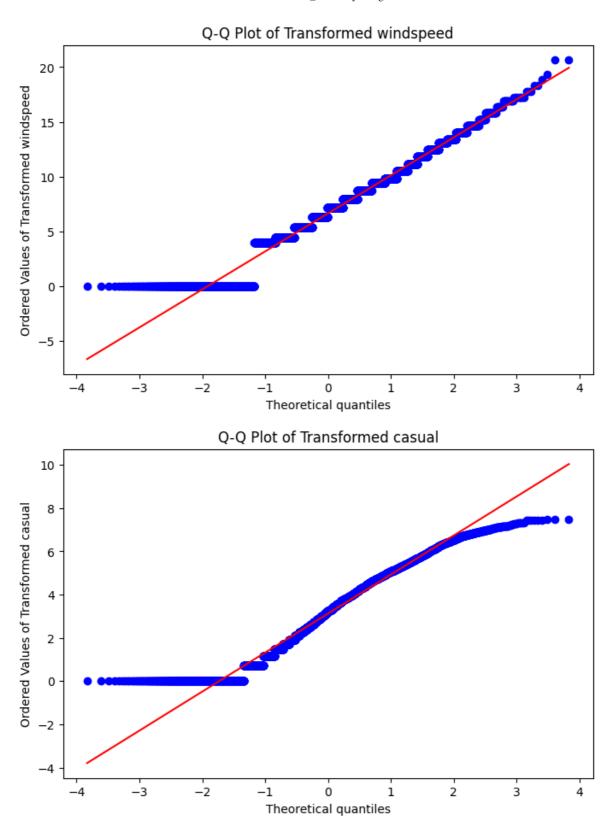


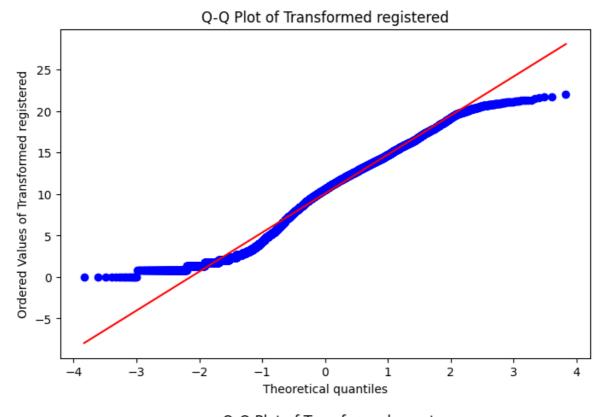


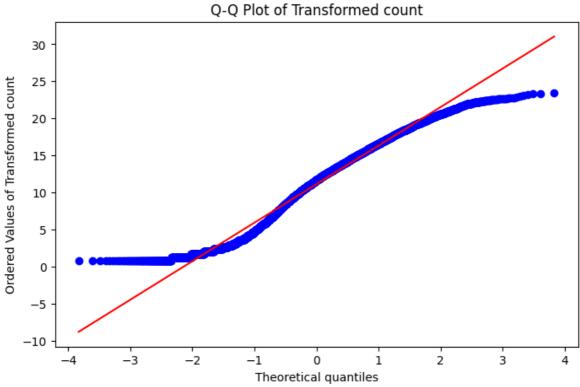










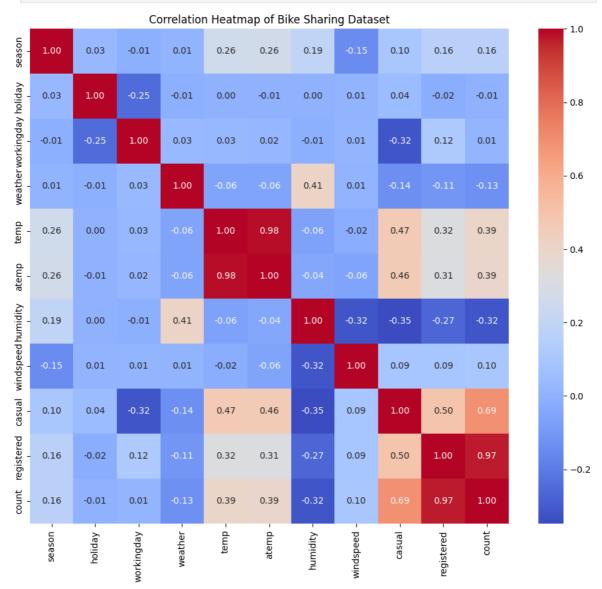


```
import pandas as pd
import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt
from pingouin import partial_corr

# import q3data.csv as a pandas dataframe
df = pd.read_csv('q3data.csv')

df.head()
```

```
#drop the datetime column
df = df.drop('datetime', axis=1)
```



From the correlation matrix above, we notice that some variables do seem to have some sort of partial correlations (the points which have a reddish hue to them) are positively correlated. Extreme shades of blue also point to slight negative correlations.

Variables such as Casual and Count, Registered and Count, Casual and Registered, Temp and atemp etc. have partial correlations.

Partial correlation is a statistical technique used to measure the relationship between two variables while controlling for the influence of one or more additional variables, known as covariates or control variables. It helps to assess the unique association between two variables after removing the shared variance explained by the covariates.