

Metaheuristic Optimization

Assignment 1

Due date:

Assignment should be submitted to Canvas by 23:59 on Sunday October 20th 2019

As per CIT regulations, submitting within 7 days of the deadline will result in a 10% penalty, between 7 and 14 days late will result in a 20% penalty, and later than 14 days after the due date will result in a 100% penalty applied.

Part 1: NP-completeness

This problem concerns the proof of the NP-completeness of 3COL

1. Convert the formula F below into a 3SAT formula F' , find a solution to F' and verify that this is a solution to

- a. If the last digit of your student id is less than 3 use

$$F = (z_1 \vee \neg z_2) \wedge (\neg z_1 \vee z_2 \vee z_3 \vee z_4 \vee z_5)$$

- b. If the last digit of your student id is either 3, 4 or 5 use

$$F = (w_1 \vee \neg w_2 \vee w_3 \vee \neg w_4 \vee \neg w_5) \wedge (\neg w_3 \vee w_4)$$

- c. If the last digit of your student id is either 6 or 7 use

$$F = (\neg p_1 \vee \neg p_3) \wedge (p_1 \vee \neg p_2 \vee p_3 \vee \neg p_4 \vee p_5)$$

- d. If the last digit of your student id is greater than 7 use

$$F = (q_1 \vee q_4) \wedge (\neg q_1 \vee q_2 \vee q_3 \vee \neg q_4 \vee \neg q_5)$$

2. Convert the following subclauses in your F' to a 3Col graph

The last two clauses of F' if the first letter of your first name is in the range A-I

The first two clauses of F' if the first letter of your first name is in the range J-R

The second and third clauses of F' if the first letter of your first name is in the range S-Z

Part 2: Genetic Algorithms

The Traveling Salesman Problem (TSP) is one which has commanded much attention in Artificial Intelligence because it is so easy to describe and so difficult to solve. The problem can simply be stated as: if a traveling salesman wishes to visit exactly once each of a list m cities (where the cost of traveling from city i to city j is c_{ij}) and then return to the home city, what is the least costly route the traveling salesman can take.

The importance of the TSP is that it is representative of a larger class of problems known as combinatorial optimization problems. The TSP problem belongs in the class of combinatorial optimization problems known as NP-hard. Today, no one has found a polynomial-time algorithm for the TSP.

A Simple Genetic Algorithm

A simple genetic algorithm can be defined in the following 9 steps:

Step 1: create an initial population of P chromosomes (generation 0)

Step 2: evaluate the fitness of each chromosome

Step 3: Select P parents from the current population via proportional selection (i.e., the selection probability is proportional to the fitness).

Step 4: choose at random a pair of parents for mating. Exchange bit strings with a crossover operation to create two offspring (e.g., one-point crossover)

Step 5: process each offspring by the mutation operation, and insert the resulting offspring in the new population

Step 6: repeat steps 4 and 5 until all parents are selected and mated (P offspring are created)

Step 7: replace the old population of chromosomes in the new population

Step 8: evaluate the fitness of each chromosome in the new population

Step 9: go back to step 3 if the number of generations is less than some upper bound. Otherwise, the final result is the best chromosome created during the search.

Selection Probability:

The parent chromosomes are selected for mating via Stochastic Universal Sampling, as depicted in the figure below where we create a cell for each chromosome that is proportional the fitness of the chromosome. In the example below, we have 7 chromosomes and we are choosing 4 parents, our equally spaced markers overlap with A, B, C and F so these are the 4 chosen.

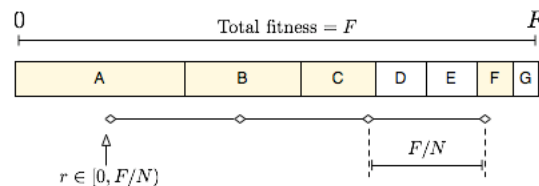


Figure 1: Stochastic Universal Sampling (https://commons.wikimedia.org/wiki/File:Statistically_Uniform.png)

It is defined as follows:

1. Let F be the sum of the fitness values of all chromosomes in the population.
2. Let N be the number of parents to select.
3. Compute the distance P between successive points: $P = F/N$.
4. Generate a random number between 0 and P as the starting point for the ruler. The ruler has N equally spaced points, each P distance apart.
5. Assign each chromosome a range equal in length to its fitness and a starting point that is after the end point of the previous chromosome (e.g. first chromosome 0-1.53, 2nd chromosome 1.54-2.26, 3rd chromosome 2.27-3.42, etc).
6. Select the chromosomes whose range contains a marker (note that a chromosome may have 2 markers in which case it is chosen twice).

Initial population

In addition to the crossover and mutation operators you will also evaluate the impact of the GAs with the following initial populations:

- Randomly generated population
- Nearest neighbor insertion: Choose first city randomly, each city thereafter choose city closest to the last city added to the route and append to the route

Crossover and mutation operators

Write a program that solves the TSP using Genetic Algorithms. Explain and implement the following crossover & mutation operators:

- Uniform order-based crossover
- Partially Mapped Crossover (PMX)
- Reciprocal exchange mutation (already implemented, mutation function in code)
- Inversion Mutation

I/O Specification

In this assignment you will use the same I/O format as defined in the first lab (week 2).

Problem instances

In this project, you will use the following problem instances to evaluate the performance of your algorithms:

if the first letter of your surname is in the range A-I inst-0.tsp, inst-13.tsp, and inst-5.tsp

if the first letter of your surname is in the range J-R inst-4.tsp, inst-16.tsp, and inst-6.tsp

if the first letter of your surname is in the range S-Z inst-19.tsp, inst-20.tsp, and inst-7.tsp

Assignment of Marks:

The deliverable of this project will consists of a python code file(s) and a report. You must follow the correct scheme with last digit of id and first letter of first and last names, you must state what you used to avoid confusion. Marks will be lost if this is not done correctly, similarly random seed must be your student id.

The following is the allocation of marks.

20%: Solution - Part 1.

Rubric (Solution and verification aspect only refers to SAT to 3SAT):

Reduction is logically well designed, documented and explained. Solution is correct (7.5 -10 Marks)	Reduction is logically well designed. Solution is correct (5-7.5 Marks)	Reduction has slight logic errors that do not significantly affect the results. Solution has slight errors (3-5 Marks)	Reduction has significant logic errors. Solution has errors (1-2 Marks)	Reduction is completely incorrect. Solution completely incorrect. (0 Marks)
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Part 2:

- Implementation of Genetic algorithms with the above mentioned crossover and mutation operations: 35 marks

	The Operator is logically well designed without inappropriate design choices (e.g., unnecessary loops)	The Operator always works properly and meets the specification of the operator	The operator works properly in limited cases	The operator is incorrectly implemented
Uniform Order-based Crossover	(5-7 Marks)	(3-5 Marks)	(1-3 Marks)	(0 Marks)
PMX Crossover	(8-12 Marks)	(4-8 Marks)	(1-3 Marks)	(0 Marks)
Inversion Mutation	(5-6 Marks)	(3-4 Marks)	(1-2 Marks)	(0 Marks)
Reciprocal Exchange (contained in code!)	N/A	N/A	N/A	(0 Marks)
Stochastic Universal Sampling	(8-10 Marks)	(4-7 Marks)	(1-3 Marks)	(0 Marks)

- 10%: A basic evaluation: the basic evaluation should describe the following two basic configurations:

Configuration	Initial Solution	Crossover	Mutation	Selection
1	Random	Uniform Crossover	Inversion Mutation	Random Selection
2	Random	PMX Crossover	Reciprocal Exchange	Random Selection

Population size = 100

Mutation rate = 0.1

Rubric:

Excellent presentation, depth and insight analysis of the empirical results (8-10 Marks)	Good presentation of the results (e.g., describing the results with well structured tables) (7-5 Marks)	Incomplete and/or unclear presentation of the results (3-5 Marks)	The results are inconsistent with the logic of the configuration/operators (0-2 Marks)
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- 20%: Extensive evaluation of your GA, i.e., initial population, crossover & mutation operators. You are expected to extensively evaluate the following combination of operations:

Configuration	Initial Solution	Crossover	Mutation	Selection
3	Random	Uniform Crossover	Reciprocal Exchange	Stochastic Universal Sampling
4	Random	PMX Crossover	Reciprocal Exchange	Stochastic Universal Sampling
5	Random	PMX Crossover	Inversion Mutation	Stochastic Universal Sampling
6	Random	Uniform Crossover	Inversion Mutation	Stochastic Universal Sampling
7	Heuristic	PMX Crossover	Reciprocal Exchange	Stochastic Universal Sampling
8	Heuristic	Uniform Crossover	Inversion Mutation	Stochastic Universal Sampling

Additionally, you are expected to investigate the impact of varying the population size, explore different mutation rates, and evaluate the impact of your GA with and without elite survival.

Rubric:

Evaluation configurations [3-8]	Excellent presentation, depth and insight analysis of the empirical results. (8-10 Marks)	Good presentation of the results (e.g., describing the results with well structured tables) (7-5 Marks)	Lack of clear and logical presentation of the results. Missing or incomplete results (3-5 Marks)	The results are inconsistent with the logic of the configuration/operators (0-2 Marks)
Additional Experiments	Excellent design, presentation, analysis, and conclusions of the additional experiments [8-10 Marks]	A reasonable attempt to design and presentation of the additional experiments (7-5 Marks)	Poor design and description of the additional experiments (3-5 Marks)	The results are inconsistent with the logic of operators (0-2 Marks)

- 15%: Your report should contain a comprehensive description of the algorithms and an extensive evaluation of your results. And it should describe the experimental design, what experiments are and what they are intended to show. Use tables and figures where appropriate.

You should assess the overall performance of your optimization algorithms for solving the travelling salesman problem. Typically, to evaluate the performance of your algorithm for a single configuration you would run your algorithm multiple times (at least 5 times in this project with at least 500 iterations per execution) and record the best fitness for all runs. You can then report the mean and median fitness across all runs. Your results should show that you have considered the suggested operators (e.g., crossover, mutation and selection).

Submission:

This assignment is due on Sunday, Oct 20th, 2019. You must submit the following files (in a single zip file):

- All source code.
- A Readme file, which briefly describes all submitted files. In the Readme file, you should also provide information about compiling environment, compiling steps, execution instructions, etc.
- A Sample file, which describes the tests you have run on your program. Also describes any cases for which your program is known not to work correctly.

You must **submit the pdf separately via the Turnitin assignment** submission:

- Report document (pdf) - including your solutions for Part 1 & Part 2.

Academic Integrity:

This is an **individual** assignment. The work you submit must be your own. In no way, shape or form should you submit work as if it were your own when some or all of it is not.

Collusion: Given how much freedom there is in the assignment, everybody's work will be different. It will be obvious if there is collusion. All parties to collusion will be penalized.

Deliberate plagiarism: You must not plagiarise the programs, results, writings or other efforts of another student or any other third-party. Plagiarism will meet with severe penalties, which can include exclusion from the University.

Inadvertent plagiarism: In reporting your exploration of the research literature be careful to avoid inadvertent plagiarism (e.g where paraphrases of the source material are too close to the original).

Falsification and fabrication: The experimental results reported must come from the experiments that you have run. Do not falsify or fabricate results.

Your report will be checked for signs of collusion, plagiarism, falsification and fabrication. You may be called to discuss your submission and implementation with me and this will inform the grading, any penalties and any disciplinary actions.