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1 C++

1.1 template

```
/*
c++:
ios_base::sync_with_stdio(false);
cin.tie(nullptr), cout.tie(nullptr);

python:
import sys
input = sys.stdin.readline
sys.stdout.write("-----")
*/
```

1.2 random

```
#define accuracy chrono::steady_clock::
now().time_since_epoch().count()
mt19937 rng(accuracy);

ll rand(ll l, ll r) {
    uniform_int_distribution<ll> ludo(l,
    r);
    return ludo(rng);
}
```

1.3 gp_hash

```
#include<ext/pb_ds/assoc_container.hpp>
#include<ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template <typename p, typename q> using
ht = gp_hash_table<p, q>;
```

1.4 pbds

```
#include<ext/pb_ds/assoc_container.hpp>
#include<ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
```

```
template <typename T>
using o_set = tree<T, null_type, less<T
    >, rb_tree_tag,
    tree_order_statistics_node_update>;
// find_by_order(k) - returns an
// iterator to the k-th largest element
// (0 indexed);
// order_of_key(k)- the number of
// elements in the set that are
// strictly smaller than k;
```

1.5 debug

```
string to_string(const string &s) {
    return '"' + s + '"'; }
string to_string(const char *s) {
    return to_string(string(s)); }
string to_string(const char c) { return
    "'" + string(1, c) + "'"; }
string to_string(bool b) { return b ? "
    true" : "false"; }
template <typename A, typename B>
string to_string(pair<A, B> p) {
    return "(" + to_string(p.first) + ",
    " + to_string(p.second) + ")"; }
template <typename A> string to_string(
    A v) {
    string res = "{";
    for (const auto &x : v) {
        res += to_string(x) + ", ";
    }
    res += "}";
    return res;
}
void debug_out() { cerr << endl; }
template <typename Head, typename...
    Tail> void debug_out(Head H, Tail...
    T) {
    cerr << " " << to_string(H);
    debug_out(T...);
}
#define dbg(...)
    \
    cerr << __LINE__ << ": [" << #
    __VA_ARGS__ << "]" = ", debug_out(
    __VA_ARGS__)
```

1.6 stress

```
#!/usr/bin/env bash
wrong="solution"
correct="brute"
gen="gen"
g++ -g solution.cpp -DONPC -o "$wrong"
g++ -g brute.cpp -DONPC -o "$correct"
g++ -g gen.cpp -DONPC -o "$gen"

for ((testNum=0;testNum<$1;testNum++))
do
    ./$gen 2>/dev/null > stdinput
    ./$correct < stdinput 2>/dev/
    null > outSlow
    ./$wrong < stdinput 2>/dev/null
    > outWrong
    H1='md5sum outWrong\'
    H2='md5sum outSlow\'
    if !(cmp -s "outWrong" "outSlow
    ")
    then
        echo "Error found!"
        echo "Input:"
        cat stdinput
        echo "Wrong Output:"
        cat outWrong
        echo "Slow Output:"
        cat outSlow
        exit
    fi
done
echo Passed $1 tests
# Usage: ./contest.sh times
```

1.7 vscode

```
{
    "key" : "f5",
    "command" : "workbench.action.
        terminal.sendSequence",
    "args" : {
        "text" : "g++ ${
            fileNameNoExtension}.cpp -o
            ${fileNameNoExtension} &&
            ./ ${fileNameNoExtension} <
            in.txt> out.txt\n "
    }
}
```

2 Dsa

2.1 KMP

```
vector<ll> createLPS(string pattern) {
    ll n = pattern.length(), idx = 0;
    vector<ll> lps(n);
    for (ll i = 1; i < n; i++) {
        if (pattern[idx] == pattern[i]) {
            lps[i] = idx + 1;
            idx++, i++;
        } else {
            if (idx != 0)
                idx = lps[idx - 1];
            else
                lps[i] = idx, i++;
        }
    }
    return lps;
}
ll kmp(string text, string pattern) {
    ll cnt_of_match = 0, i = 0, j = 0;
    vector<ll> lps = createLPS(pattern);
    while (i < text.length()) {
        if (text[i] == pattern[j])
            i++, j++; // i = text, j =
            pattern
        else {
            if (j != 0)
                j = lps[j - 1];
            else
                i++;
        }
        if (j == pattern.length()) {
            cnt_of_match++;
            // the index where match found ->
            (i - pattern.length());
            j = lps[j - 1];
        }
    }
    return cnt_of_match;
}
```

2.2 Hashing

```
const ll N = 2e5 + 5;
const ll MOD1 = 127657753, MOD2 =
    987654319;
const ll p1 = 137, p2 = 277;
ll ip1, ip2;
pair<ll, ll> pw[N], ipw[N];
void prec() {
    pw[0] = {1, 1};
    for (ll i = 1; i < N; i++) {
        pw[i].first = 1LL * pw[i - 1].first
            * p1 % MOD1;
        pw[i].second = 1LL * pw[i - 1].
            second * p2 % MOD2;
    }
    ip1 = binaryExp(p1, MOD1 - 2, MOD1);
    ip2 = binaryExp(p2, MOD2 - 2, MOD2);
    ipw[0] = {1, 1};
    for (ll i = 1; i < N; i++) {
```

```

    ipw[i].first = 1LL * ipw[i - 1].
        first * ip1 % MOD1;
    ipw[i].second = 1LL * ipw[i - 1].
        second * ip2 % MOD2;
}
}
struct Hashing {
    ll n;
    string s; // 0 -
        indexed
    vector<pair<ll, ll>> hs; // 1 -
        indexed
    Hashing() {}
    Hashing(string _s) {
        n = _s.size();
        s = _s;
        hs.emplace_back(0, 0);
        for (ll i = 0; i < n; i++) {
            pair<ll, ll> p;
            p.first = (hs[i].first + 1LL * pw
                [i].first * s[i] % MOD1) %
                MOD1;
            p.second = (hs[i].second + 1LL *
                pw[i].second * s[i] % MOD2) %
                MOD2;
            hs.push_back(p);
        }
    }
    pair<ll, ll> get_hash(ll l, ll r) {
        // 1 - indexed
        assert(1 <= l && l <= r && r <= n);
        pair<ll, ll> ans;
        ans.first =
            (hs[r].first - hs[l - 1].first
                + MOD1) * 1LL * ipw[l - 1].
                first % MOD1;
        ans.second = (hs[r].second - hs[l -
            1].second + MOD2) * 1LL *
            ipw[l - 1].second %
            MOD2;
        return ans;
    }
    pair<ll, ll> get_hash() { return
        get_hash(1, n); }
};

```

2.3 BigInteger

```

struct BigInteger {
    string str;
    // Constructor to initialize
    // BigInteger with a string
    BigInteger(string s) { str = s; }
    // Overload + operator to add
    // two BigInteger objects
    BigInteger operator+(const BigInteger
        &b) {
        string a = str, c = b.str;
        ll alen = a.length(), clen = c.
            length();
        ll n = max(alen, clen);
        if (alen > clen)
            c.insert(0, alen - clen, '0');
        else if (alen < clen)
            a.insert(0, clen - alen, '0');
        string res(n + 1, '0');
        ll carry = 0;
        for (ll i = n - 1; i >= 0; i--) {
            ll digit = (a[i] - '0') + (c[i] -
                '0')
            + carry;
            carry = digit / 10;
            res[i + 1] = digit % 10 + '
                0';
        }
        if (carry == 1) {
            res[0] = '1';
            return BigInteger(res);
        } else
            return BigInteger(res.
                substr(1));
    }
};

```

```

// Overload - operator to subtract
// first check which number is
// greater and then subtract
BigInteger operator-(const BigInteger
    &b) {
    string a = str;
    string c = b.str;
    ll alen = a.length(), clen = c.
        length();
    ll n = max(alen, clen);
    if (alen > clen)
        c.insert(0, alen - clen, '0
            ');
    else if (alen < clen)
        a.insert(0, clen - alen, '0
            ');
    if (a < c) {
        swap(a, c);
        swap(alen, clen);
    }
    string res(n, '0');
    ll carry = 0;
    for (ll i = n - 1; i >= 0; i--) {
        ll digit = (a[i] - '0') - (
            c[i] - '0') - carry;
        if (digit < 0)
            digit += 10, carry = 1;
        else
            carry = 0;
        res[i] = digit + '0';
    }
    // remove leading zeros
    ll i = 0;
    while (i < n && res[i] == '0')
        i++;
    if (i == n)
        return BigInteger("0");
    return BigInteger(res.substr(i));
}

// Overload * operator to multiply
// two BigInteger objects
BigInteger operator*(const BigInteger
    &b) {
    string a = str, c = b.str;
    ll alen = a.length(), clen = c.
        length();
    ll n = alen + clen;
    string res(n, '0');
    for (ll i = alen - 1; i >= 0; i--)
        {
            ll carry = 0;
            for (ll j = clen - 1; j >=
                0; j--) {
                ll digit =
                    (a[i] - '0') * (c[j -
                        '0']) + (res[i +
                            j + 1] - '0') +
                            carry;
                carry = digit / 10;
                res[i + j + 1] = digit %
                    10 + '0';
            }
            res[i] += carry;
        }
    ll i = 0;
    while (i < n && res[i] == '0')
        i++;
    if (i == n)
        return BigInteger("0");
    return BigInteger(res.substr(i));
}

// Overload << operator to output
// BigInteger object
friend ostream &operator<<(ostream &
    out, const BigInteger &b) {
    out << b.str;
    return out;
}
};

```

2.4 Kadane

```
// return maximum subarray sum.
ll kadense(ll arr[], ll n) {
    ll mxsm = arr[0], curr_s = arr[0];
    for (ll i = 1; i < n; i++) {
        curr_s = max(arr[i], curr_s + arr[i]);
        mxsm = max(mxsm, curr_s);
    }
    return mxsm;
}
```

2.5 Segement_tree

```
class SEGMENT_TREE {
public:
    vector<ll> v;
    vector<ll> seg;
    SEGMENT_TREE(ll n) {
        v.resize(n + 5);
        seg.resize(4 * n + 5);
    }
    //! initially: ti = 1, low = 1, high = n
    //(number of elements in the array);
    void build(ll ti, ll low, ll high) {
        if (low == high) {
            seg[ti] = v[low];
            return;
        }
        ll mid = (low + high) / 2;
        build(2 * ti, low, mid);
        build(2 * ti + 1, mid + 1, high);
        seg[ti] = (seg[2 * ti] + seg[2 * ti + 1]);
    }
    //! initially: ti = 1, low = 1, high = n
    //(number of elements in the array),
    //(ql & qr)=user input in 1 based index;
    ll find(ll ti, ll tl, ll tr, ll ql, ll qr) {
        if (tl > qr || tr < ql) {
            return 0;
        }
        if (tl >= ql and tr <= qr) {
            return seg[ti];
        }
        ll mid = (tl + tr) / 2;
        ll l = find(2 * ti, tl, mid, ql, qr);
        ll r = find(2 * ti + 1, mid + 1, tr, ql, qr);
        return (l + r);
    }
    //! initially: ti = 1, tl = 1, tr = n
    //(number of elements in the array),
    // id = user input in 1 based indexing,
    // val = updated value;
    void update(ll ti, ll tl, ll tr, ll id, ll val) {
        if (id > tr or id < tl) {
            return;
        }
        if (id == tr and id == tl) {
            seg[ti] = val;
            return;
        }
        ll mid = (tl + tr) / 2;
        update(2 * ti, tl, mid, id, val);
        update(2 * ti + 1, mid + 1, tr, id, val);
        seg[ti] = (seg[2 * ti] + seg[2 * ti + 1]);
    }
};
// use 1 based indexing;
```

2.6 Fenwick_tree

```
struct FenwickTree {
    vector<ll> bit; // binary indexed tree
    ll n;
```

```
FenwickTree(ll n) {
    this->n = n;
    bit.assign(n, 0);
}
FenwickTree(vector<ll> a) :
    FenwickTree(a.size()) {
    for (size_t i = 0; i < a.size(); i++)
        add(i, a[i]);
}
ll sum(ll r) {
    ll ret = 0;
    for (; r >= 0; r = (r & (r + 1)) - 1)
        ret += bit[r];
    return ret;
}
ll sum(ll l, ll r) { return sum(r) - sum(l - 1); }
void add(ll idx, ll delta) {
    for (; idx < n; idx = idx | (idx + 1))
        bit[idx] += delta;
}
};
// minimum
struct FenwickTreeMin {
    vector<ll> bit;
    ll n;
    const ll INF = (ll)1e9;
    FenwickTreeMin(ll n) {
        this->n = n;
        bit.assign(n, INF);
    }
    FenwickTreeMin(vector<ll> a) :
        FenwickTreeMin(a.size()) {
        for (size_t i = 0; i < a.size(); i++)
            update(i, a[i]);
    }
    ll getmin(ll r) {
        ll ret = INF;
        for (; r >= 0; r = (r & (r + 1)) - 1)
            ret = min(ret, bit[r]);
        return ret;
    }
    void update(ll idx, ll val) {
        for (; idx < n; idx = idx | (idx + 1))
            bit[idx] = min(bit[idx], val);
    }
};
```

2.7 Segment_tree_lazy

```
class SEGMENT_TREE {
public:
    vector<ll> v;
    vector<ll> seg;
    vector<ll> lazy;
    SEGMENT_TREE(ll n) {
        v.resize(n + 5, 0);
        seg.resize(4 * n + 5, 0);
        lazy.resize(4 * n + 5, 0);
    }
    void pull(ll ti) { seg[ti] = (seg[2 * ti] & seg[2 * ti + 1]); }
    void push(ll ti, ll tl, ll tr) {
        if (lazy[ti] == 0)
            return;
        seg[ti] |= lazy[ti];
        if (tl != tr) {
            lazy[2 * ti] |= lazy[ti];
            lazy[2 * ti + 1] |= lazy[ti];
        }
        lazy[ti] = 0;
    }
    //! llially: ti = 1, low = 1, high = n
    //(number of elements in the array);
    void build(ll ti, ll low, ll high) {
```

```

    lazy[ti] = 0;
    if (low == high) {
        seg[ti] = v[low];
        return;
    }
    ll mid = (low + high) / 2;
    build(2 * ti, low, mid);
    build(2 * ti + 1, mid + 1, high);
    pull(ti);
}
/// llially: ti = 1, low = 1, high =
n(number of elements in the array)
, (ql
/// & qr) = user input in 1 based
indexing;
ll query(ll ti, ll tl, ll tr, ll ql,
ll qr) {
    push(ti, tl, tr);
    if (tl > qr || tr < ql) {
        return (1LL << 32) - 1;
    }
    if (tl >= ql and tr <= qr)
        return seg[ti];
    ll mid = (tl + tr) / 2;
    ll l = query(2 * ti, tl, mid, ql,
qr);
    ll r = query(2 * ti + 1, mid + 1,
tr, ql, qr);
    return (l & r);
}
/// llially: ti = 1, tl = 1, tr = n(
number of elements in the array),
id =
/// user input in 1 based indexing,
val = updated value;
void update(ll ti, ll tl, ll tr, ll
idL, ll idR, ll val) {
    push(ti, tl, tr);
    if (idR < tl or tr < idL)
        return;
    if (idL <= tl and tr <= idR) {
        lazy[ti] |= val;
        push(ti, tl, tr);
        return;
    }
    ll mid = (tl + tr) / 2;
    update(2 * ti, tl, mid, idL, idR,
val);
    update(2 * ti + 1, mid + 1, tr, idL
, idR, val);
    pull(ti);
}
/// use 1 based indexing for input and
queries and update;
};

```

2.8 Trie

```

const ll N = 26;
class Node {
public:
    ll EoW;
    Node *child[N];
    Node() {
        EoW = 0;
        for (ll i = 0; i < N; i++)
            child[i] = NULL;
    }
};

void insert(Node *node, string s) {
    for (size_t i = 0; i < s.size(); i++)
    {
        ll r = s[i] - 'A';
        if (node->child[r] == NULL)
            node->child[r] = new Node();
        node = node->child[r];
    }
    node->EoW += 1;
}

ll search(Node *node, string s) {
    for (size_t i = 0; i < s.size(); i++)
    {
        ll r = s[i] - 'A';

```

```

        if (node->child[r] == NULL)
            return 0;
    }
    return node->EoW;
}

void prll(Node *node, string s = "") {
    if (node->EoW)
        cout << s << "\n";
    for (ll i = 0; i < N; i++) {
        if (node->child[i] != NULL) {
            char c = i + 'A';
            prll(node->child[i], s + c);
        }
    }
}

bool isChild(Node *node) {
    for (ll i = 0; i < N; i++)
        if (node->child[i] != NULL)
            return true;
    return false;
}

bool isJunc(Node *node) {
    ll cnt = 0;
    for (ll i = 0; i < N; i++) {
        if (node->child[i] != NULL)
            cnt++;
    }
    if (cnt > 1)
        return true;
    return false;
}

ll trie_delete(Node *node, string s, ll
k = 0) {
    if (node == NULL)
        return 0;
    if (k == (ll)s.size()) {
        if (node->EoW == 0)
            return 0;
        if (isChild(node)) {
            node->EoW = 0;
            return 0;
        }
        return 1;
    }
    ll r = s[k] - 'A';
    ll d = trie_delete(node->child[r], s,
k + 1);
    ll j = isJunc(node);
    if (d)
        delete node->child[r];
    if (j)
        return 0;
    return d;
}

void delete_trie(Node *node) {
    for (ll i = 0; i < 15; i++) {
        if (node->child[i] != NULL)
            delete_trie(node->child[i]);
    }
    delete node;
}

```

2.9 DSU

```

class DisjollSet {
    vector<ll> par, sz, minElmt, maxElmt,
cntElmt;
public:
    DisjollSet(ll n) {
        par.resize(n + 1);
        sz.resize(n + 1, 1);
        minElmt.resize(n + 1);
        maxElmt.resize(n + 1);
        cntElmt.resize(n + 1, 1);
        for (ll i = 1; i <= n; i++)
            par[i] = minElmt[i] = maxElmt[i]
= i;
    }

    ll findUPar(ll u) {
        if (u == par[u])
            return u;

```

```

    return par[u] = findUPar(par[u]);
}
void unionBySize(ll u, ll v) {
    ll pU = findUPar(u);
    ll pV = findUPar(v);
    if (pU == pV)
        return;
    if (sz[pU] < sz[pV])
        swap(pU, pV);
    par[pV] = pU;
    sz[pU] += sz[pV];
    cntElmt[pU] += cntElmt[pV];
    minElmt[pU] = min(minElmt[pU],
        minElmt[pV]);
    maxElmt[pU] = max(maxElmt[pU],
        maxElmt[pV]);
}
ll getMinElementIntheSet(ll u) {
    return minElmt[findUPar(u)];
}
ll getMaxElementIntheSet(ll u) {
    return maxElmt[findUPar(u)];
}
ll getNumofElementIntheSet(ll u) {
    return cntElmt[findUPar(u)];
}
};

```

2.10 HLD

```

ll par[N], sub_tree_sz[N], heavy[N],
wt_from_parent[N], depth[N], head[N],
position[N];
vector<pair<ll, ll>> gd[N];
// HLD part start
ll dfs(ll node, ll p) {
    par[node] = p;
    sub_tree_sz[node] = 1;
    heavy[node] = -1;
    for (auto [v, w] : gd[node]) {
        if (v == p)
            continue;
        depth[v] = depth[node] + 1;
        wt_from_parent[v] = w;
        sub_tree_sz[node] += dfs(v, node);
        if (heavy[node] == -1 ||
            sub_tree_sz[v] > sub_tree_sz[
                heavy[node]]) {
            heavy[node] = v;
        }
    }
    return sub_tree_sz[node];
}
ll pos;
void decompose(ll node, ll hd) {
    head[node] = hd;
    position[node] = ++pos;
    if (heavy[node] != -1) {
        decompose(heavy[node], hd);
    }
    for (auto [v, w] : gd[node]) {
        if (v != par[node] && v != heavy[
            node]) {
            decompose(v, v);
        }
    }
}
// HLD part end
// in main function
ll n, m;
cin >> n;
SEGMENT_TREE seg(n); // Lazy if needed
vector<ll> edge_u(n), edge_v(n),
edge_node(n);
for (int i = 1; i < n; i++) {
    ll u, v, wt = 1;
    cin >> u >> v >> wt;
    gd[u].push_back({v, wt});
    gd[v].push_back({u, wt});
    edge_u[i] = u;
    edge_v[i] = v;
}

```

```

dfs(1, -1);
pos = 0;
decompose(1, 1);
for (int i = 1; i <= n; i++) {
    // seg.v[position[i]] = val[i]; //
    // for node value
    seg.v[position[i]] = wt_from_parent[i]
    ]; // for edge value
}
// work on a specific edge
for (int i = 1; i < n; i++) {
    ll u = edge_u[i], v = edge_v[i];
    edge_node[i] = (depth[u] > depth[v])
        ? u : v;
}
seg.build(1, 1, n);
auto updatePath = [&](ll u, ll v, ll x)
{
    while (head[u] != head[v]) {
        if (depth[head[u]] < depth[head[v]
            ])
            swap(u, v);
        seg.update(1, 1, n, position[head[u]
            ], position[u], x);
        u = par[head[u]];
    }
    if (depth[u] > depth[v])
        swap(u, v);
    // edge value
    if (u != v) {
        seg.update(1, 1, n, position[u] +
            1, position[v], x);
    }
    // node value
    // seg.update(1, 1, n, position[u],
        position[v], x);
};
auto queryPath = [&](ll u, ll v) {
    ll ans = -inf;
    while (head[u] != head[v]) {
        if (depth[head[u]] < depth[head[v]
            ])
            swap(u, v);
        ans = max(ans, seg.query(1, 1, n,
            position[head[u]], position[u]));
        u = par[head[u]];
    }
    if (depth[u] > depth[v])
        swap(u, v);
    // upward + downward
    if (u != v) {
        ans = max(ans, seg.query(1, 1, n,
            position[u] + 1, position[v]));
    }
    // only upward
    // ans = max(ans, seg.query(1, 1, n,
        position[u], position[v])); // for
    // node value
    return ans;
};
seg.update(1, 1, n, position[edge_node[
    s]], position[edge_node[s]], x); //
    single point update. if path update
    need call update path
cout << queryPath(x, s) << '\n';

```

2.11 Manacher

```

struct Manacher {
    vector<ll> p[2];
    string s;
    // p[1][i] = (max odd length
        palindrome centered at i) / 2 [
        floor division]
    // p[0][i] = same for even, it
        considers the right center
    // e.g. for s = "abbabba", p[1][3] =
        3, p[0][2] = 2
    Manacher(string s) {
        this->s = s;
    }
}

```



```

11 n = s.size();
p[0].resize(n + 1);
p[1].resize(n);
for (11 z = 0; z < 2; z++) {
    for (11 i = 0, l = 0, r = 0; i <
        n; i++) {
        11 t = r - i + !z;
        if (i < r)
            p[z][i] = min(t, p[z][l + t]);
        11 L = i - p[z][i], R = i + p[z][i] - !z;
        while (L >= 1 && R + 1 < n && s[L - 1] == s[R + 1])
            p[z][i]++, L--, R++;
        if (R > r)
            l = L, r = R;
    }
}
bool is_palindrome(11 l, 11 r) {
    11 mid = (l + r + 1) / 2, len = r - l + 1;
    return 2 * p[len % 2][mid] + len % 2 >= len;
}
string get_palin(11 i, bool odd = true) {
    11 len = p[odd][i];
    return s.substr(i - len, 2 * len + 1 - !odd);
}
};

```

3 Dynamic Programming

3.1 LCS

```

/*
Fact about LCS:
1. Longest Increasing Substring
To solve this, we just care about when
two char equals. Rest of the things
should be neglected.
2. Longest Palindromic Subsequence (LPS)
To solve this, we just take a new
string which is the reverse of the
original string. Then just call the
LCS function to find LPS.
3. Minimum insertions to make a string
palindrome To solve this, we just
basically do string length - LPS.
Why this?
Let's take an example: string s =
aabca; Let's say aca is our LPS.
Now we find how many char we
need to insert to make the
string palindrome while our LPS
is fixed.
a ab c a now to make the string
palindrome we just need to
insert the reverse of ab after c
. So the new string looks like a
ab c ba a
4. Minimum Number of Deletions and
Insertions to make the string equals
To solve this we just find the LCS
of those string then just do: n + m
- 2 * LCS.length() where n, m =
strings length
*/

```

3.2 MCM

```

// TC: O(n ^ 3)
const 11 N = 1005;
vector<11> v;
11 dp[N][N], mark[N][N];
11 MCM(11 i, 11 j) {
    if (i == j)
        return dp[i][j] = 0;
    if (dp[i][j] != -1)

```

```

        return dp[i][j];
    11 mn = INT_MAX;
    for (11 k = i; k < j; k++) {
        11 x = mn;
        mn = min(mn, MCM(i, k) + MCM(k + 1,
            j) + v[i - 1] * v[k] * v[j]);
        if (x != mn)
            mark[i][j] = k;
    }
    return dp[i][j] = mn;
}
void print_order(11 i, 11 j) {
    if (i == j)
        cout << "X" << i;
    else {
        cout << "(";
        print_order(i, mark[i][j]);
        print_order(mark[i][j] + 1, j);
        cout << ")";
    }
}
// memset(dp, -1, sizeof dp);
// print_order(1, n);

```

3.3 LIS length

```

vector<11> v = {7, 3, 5, 3, 6, 2, 9,
    8};
vector<11> seq;
/*
here we basically check is the current
element from v is greater than the
last element of the sequence. if it
is then push it to the seq array and
if not then replace that index
value. let's take an example:
v = 7 3 5 3 6 2 9 8
1st iteration seq = 7;
2nd iteration seq = 3;
3rd iteration seq = 3 5;
4th iteration seq = 3 3;
5th iteration seq = 3 3 6;
6th iteration seq = 2 3 6;
7th iteration seq = 2 3 6 9;
8th iteration seq = 2 3 6 8;
*/
for (auto i : v) {
    auto id = lower_bound(seq.begin(),
        seq.end(), i);
    if (id == seq.end())
        seq.push_back(i);
    else
        seq[id - seq.begin()] = i;
}
cout << seq.size() << endl;

```

3.4 LCIS

```

11 a[100] = {0}, b[100] = {0}, f[100] =
    {0};
11 n = 0, m = 0;
11 main(void) {
    cin >> n;
    for (11 i = 1; i <= n; i++)
        cin >> a[i];
    cin >> m;
    for (11 i = 1; i <= m; i++)
        cin >> b[i];
    for (11 i = 1; i <= n; i++) {
        11 k = 0;
        for (11 j = 1; j <= m; j++) {
            if (a[i] > b[j] && f[j] > k)
                k = f[j];
            else if (a[i] == b[j] && k + 1 >
                f[j])
                f[j] = k + 1;
        }
    }
    11 ans = 0;
    for (11 i = 1; i <= m; i++)
        if (f[i] > ans)
            ans = f[i];
}

```

```
cout << and << endl;
return 0;
}
```

3.5 SOS DP

```
// sum over subsets
for (int i = 0; i < B; i++) {
    for (int mask = 0; mask < (1 << B);
        mask++) {
        if ((mask & (1 << i)) != 0) {
            f[mask] += f[mask ^ (1 << i)];
        }
    }
}

// sum over supersets
for (int i = 0; i < B; i++) {
    for (int mask = (1 << B) - 1; mask >=
        0; mask--) {
        if ((mask & (1 << i)) == 0)
            g[mask] += g[mask ^ (1 << i)];
    }
}

// submask
for (int mask = 1; mask < (1 << 5);
    mask++) {
    for (int submask = mask; submask > 0;
        submask = (submask - 1) & mask) {
        int subset = mask ^ submask;
    }
}

/**
 * we have to use SOS dp te idea is
 * that we can iterate over all
 * mask and using there subset get
 * the actual value
 * the first is we have to find for
 * each value in the array how many
 * y we have so that x/y = x
 * if a binary is 1010 all possible
 * y is 1000 0010 0000
 * so basically the subset of x
 * using sos dp we can find some
 * properties from somethings
 * subset
 * the idea is that we will consider
 * first what if we can't change
 * any bit to manipulate x what
 * would be the ans
 * the 1 bit , 2 bit...log2(x)bit
 * change from the right(LSB)
 * we will check what are the
 * changes between binary
 * for example in the property of x/
 * y = x
 * dp[i][x] = from right i bit can
 * change and for x value
 * so initially this is the
 * frequency of the x
 * then dp[1][x] will be dp[0][x] if
 * 1 bit is 0, because we
 * obviously can't change it
 * otherwise it will not be same
 * after OR'ed
 * but if lth bit is 1
 * dp[1][x] = dp[0][x] + dp[0][
 * different with the mask or (x
 * -(1<<i-1))] -> here is the right
 * side part we basically needs to
 * find in order to complete the
 * code thats it
 * for example another case is x&y =
 * x;
 * now lets see when is this
 * property hold
 * if x is 1010
 * for 0 we can use other value
 * for 1 we can use only 1
 * now lets see 1010 -> for 1 bit
 * change the subset(superset) is
 * 1011
 * for 2 bit change 1011 1010
```

```
* for 3 bit change 1110 1011 1111
  1010
* so if you see what are the diff
  between bit 2 change and bit 3
  change it is just the 1110 and
  1111 now this is 1011+0100 ->
  1111 and 1010 + 0100 -> 1110 so
  each element in 2 bit change +
  (1<<(bit-1)); <--- this is the
  observation part
* and now final one is x&y !=0
* if 1010 ->
* for 1 bit change 1010 1011
* for 2 bit change 1010 1000 1001
  1011
* for 3 bit change 1010 1000 1001
  1011 1100 ..
* for 4 bit change 1010 1000 0010
  ...
* for 1010 just before mx bit all
  subset of 101 will be discared,
  if use any subset of 0101 like
  0100 it will not change anything
  cause 1010 & 0100 is 1000 the
  change is not on 0 bits
* now how the code goes?
* we iterate over all x
* the we iterate from 0 bit change
  to max bit change and store in
  dp
* TC of sos dp is (b*2^b);
**/
```

3.6 BS optimization

```
bitset<100005> bs = 1;
for (auto i : a) {
    bs |= (bs << i);
    // if previous 1 value pos is
    // possible now ith bit or ith sm is
    // also possible
}
cout << bs.count() - 1 << endl;
for (ll i = 1; i <= 100003; i++)
    if (bs[i])
        cout << i << " ";
cout << endl;
```

4 Graph

4.1 Dijkstra

```
// TC: O(V + ElogV)
typedef pair<ll, ll> pairi;
ll N = 20000 + 5;
vector<vector<pairi>> adj(N);
vector<ll> dis(N, inf), parent(N);

void dijkstra(ll src) {
    priority_queue<pairi, vector<pairi>,
        greater<pairi>> pq;
    dis[src] = 0;
    pq.push({0, src});
    while (pq.size()) {
        auto top = pq.top();
        pq.pop();
        for (auto i : adj[top.second]) {
            ll v = i.first;
            ll wt = i.second;
            if (dis[v] > dis[top.second] + wt) {
                dis[v] = dis[top.second] + wt;
                pq.push({dis[v], v});
                parent[v] = top.second;
            }
        }
    }
}

ll node = n;
while (parent[node] != node) {
    path.push_back(node);
}
```



```

    node = parent[node];
}
path.push_back(1);

```

4.2 BellmanFord

```

// TC : O(V.E)
vector<ll> dist;
vector<ll> parent;
vector<vector<pair<ll, ll>>> adj;
// resize the vectors from main
function
void bellmanFord(ll n, ll src) {
    dist[src] = 0;
    for (ll step = 0; step < n; step++) {
        for (ll i = 1; i <= n; i++) {
            for (auto it : adj[i]) {
                ll u = i;
                ll v = it.first;
                ll wt = it.second;
                if (dist[u] != inf && ((dist[u]
                    + wt) < dist[v])) {
                    if (step == n - 1) {
                        cout << "Negative cycle
                            found\n ";
                        return;
                    }
                    dist[v] = dist[u] + wt;
                    parent[v] = u;
                }
            }
        }
    }
    for (ll i = 1; i <= n; i++)
        cout << dist[i] << " ";
    cout << endl;
}

```

4.3 FloydWarshall

```

// TC : O(n ^ 3)
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
typedef vector<ll> VI;
typedef vector<VI> VVI;
bool FloydWarshall(VVT &w, VVI &prev) {
    ll n = w.size();
    prev = VVI(n, VI(n, -1));
    for (ll k = 0; k < n; k++) {
        for (ll i = 0; i < n; i++) {
            for (ll j = 0; j < n; j++) {
                if (w[i][j] > w[i][k] + w[k][j]) {
                    w[i][j] = w[i][k] + w[k][j];
                    prev[i][j] = k;
                }
            }
        }
    }
    // check for negative weight cycles
    for (ll i = 0; i < n; i++)
        if (w[i][i] < 0)
            return false;
    return true;
}

```

4.4 Toposort

```

// TC : O(V + E)
map<ll, vector<ll>> adj;
map<ll, ll> degree;
set<ll> nodes;
vector<ll> ans;
// adj: graph input, degree: cnt
// indegree,
// node: unique nodes, ans: path
ll c = 0;
void topo_sort() {
    queue<ll> qu;

```

```

// traverse all the nodes and check
// if its degree is 0 or not..
for (ll i : nodes) {
    if (degree[i] == 0)
        qu.push(i);
}
while (!qu.empty()) {
    ll top = qu.front();
    qu.pop();
    ans.push_back(top);
    for (ll i : adj[top]) {
        degree[i]--;
        if (degree[i] == 0) {
            qu.push(i);
        }
    }
}
}

```

4.5 Kruskal

```

// TC : O(ElogE)
typedef pair<ll, ll> edge;
class Graph {
    vector<pair<ll, edge>> G, T;
    vector<ll> parent;
    ll cost = 0;
public:
    Graph(ll n) {
        for (ll i = 0; i < n; i++)
            parent.push_back(i);
    }
    void add_edges(ll u, ll v, ll wt) { G
        .push_back({wt, {u, v}}); }
    ll find_set(ll n) {
        if (n == parent[n])
            return n;
        else
            return find_set(parent[n]);
    }
    void union_set(ll u, ll v) { parent[u]
        = parent[v]; }
    void kruskal() {
        sort(G.begin(), G.end());
        for (auto it : G) {
            ll uRep = find_set(it.second.
                first);
            ll vRep = find_set(it.second.
                second);
            if (uRep != vRep) {
                cost += it.first;
                T.push_back(it);
                union_set(uRep, vRep);
            }
        }
    }
    ll get_cost() { return cost; }
    void print() {
        for (auto it : T)
            cout << it.second.first << " " <<
                it.second.second << ": " <<
                it.first << endl;
    }
};
// g.add_edges(u, v, wt);
// g.kruskal();

```

4.6 Prims

```

// TC: O(ElogV)
typedef pair<ll, ll> pll;
class Prims {
    map<ll, vector<pll>> graph;
    map<ll, ll> visited;
public:
    void addEdge(ll u, ll v, ll w) {
        graph[u].push_back({v, w});
        graph[v].push_back({u, w});
    }
    vector<ll> path(pll start) {

```

```

vector<ll> ans;
priority_queue<pll, vector<pll>,
    greater<pll>> pq;
// cost vs node
pq.push({start.second, start.first});
while (!pq.empty()) {
    pair<ll, ll> curr = pq.top();
    pq.pop();
    if (visited[curr.second])
        continue;
    visited[curr.second] = 1;
    ans.push_back(curr.second);
    for (auto i : graph[curr.second]) {
        if (visited[i.first])
            continue;
        pq.push({i.second, i.first});
    }
}
return ans;
};

```

4.7 LCA

```

// TC: preprocessing O(nlogn), each
// query O(logn)
ll n, l;
vector<vector<ll>> adj;
ll timer;
vector<ll> tin, tout;
vector<vector<ll>> up;

void dfs(ll v, ll p) {
    tin[v] = ++timer;
    up[v][0] = p;
    for (ll i = 1; i <= l; ++i)
        up[v][i] = up[up[v][i-1]][i-1];

    for (ll u : adj[v]) {
        if (u != p)
            dfs(u, v);
    }
    tout[v] = ++timer;
}

bool is_ancestor(ll u, ll v) { return
    tin[u] <= tin[v] && tout[u] >= tout[
    v]; }

ll lca(ll u, ll v) {
    if (is_ancestor(u, v))
        return u;
    if (is_ancestor(v, u))
        return v;
    for (ll i = l; i >= 0; --i) {
        if (!is_ancestor(up[u][i], v))
            u = up[u][i];
    }
    return up[u][0];
}

void preprocess(ll root) {
    tin.resize(n);
    tout.resize(n);
    timer = 0;
    l = ceil(log2(n));
    up.assign(n, vector<ll>(l + 1));
    dfs(root, root);
}

```

4.8 Rerooting

```

namespace reroot {
const auto exclusive = [] (const auto &a
    , const auto &base,
                                const auto &
                                merge_into
                                , int
                                vertex) {

    int n = (int)a.size();
    using Aggregate = decay_t<decltype(
        base)>;
    vector<Aggregate> b(n, base);

```

```

    for (int bit = (int)lg(n); bit >=
        0; --bit) {
        for (int i = n - 1; i >= 0; --i)
            b[i] = b[i >> 1];
        int sz = n - (n & !bit);
        for (int i = 0; i < sz; ++i) {
            int index = (i >> bit) ^ 1;
            b[index] = merge_into(b[index], a
                [i], vertex, i);
        }
    }
    return b;
};

// MergeInto : Aggregate * Value *
// Vertex(int) * EdgeIndex(int) ->
// Aggregate
// Base : Vertex(int) -> Aggregate
// FinalizeMerge : Aggregate * Vertex(
// int) * EdgeIndex(int) -> Value
const auto rerooter = [] (const auto &g,
    const auto &base,
                                const auto &
                                merge_into,
                                const auto
                                &
                                finalize_merge
                                ) {

    int n = (int)g.size();
    using Aggregate = decay_t<decltype(
        base(0))>;
    using Value = decay_t<decltype(
        finalize_merge(base(0), 0, 0))>;
    vector<Value> root_dp(n), dp(n);
    vector<vector<Value>> edge_dp(n),
        redge_dp(n);

    vector<int> bfs, parent(n);
    bfs.reserve(n);
    bfs.push_back(0);
    for (int i = 0; i < n; ++i) {
        int u = bfs[i];
        for (auto v : g[u]) {
            if (parent[u] == v)
                continue;
            parent[v] = u;
            bfs.push_back(v);
        }
    }

    for (int i = n - 1; i >= 0; --i) {
        int u = bfs[i];
        int p_edge_index = -1;
        Aggregate aggregate = base(u);
        for (int edge_index = 0; edge_index
            < (int)g[u].size(); ++
            edge_index) {
            int v = g[u][edge_index];
            if (parent[u] == v) {
                p_edge_index = edge_index;
                continue;
            }
            aggregate = merge_into(aggregate,
                dp[v], u, edge_index);
        }
        dp[u] = finalize_merge(aggregate, u
            , p_edge_index);
    }

    for (auto u : bfs) {
        dp[parent[u]] = dp[u];
        edge_dp[u].reserve(g[u].size());
        for (auto v : g[u])
            edge_dp[u].push_back(dp[v]);
        auto dp_exclusive = exclusive(
            edge_dp[u], base(u), merge_into,
            u);
        redge_dp[u].reserve(g[u].size());
        for (int i = 0; i < (int)
            dp_exclusive.size(); ++i)
            redge_dp[u].push_back(
                finalize_merge(dp_exclusive[i
                    ], u, i));
        root_dp[u] = finalize_merge(
            n > 1 ? merge_into(dp_exclusive
                [0], edge_dp[u][0], u, 0) :

```

```

        base(u), u,
        -1);
    for (int i = 0; i < (int)g[u].size()
        (); ++i) {
        dp[g[u][i]] = redge_dp[u][i];
    }
}

return make_tuple(move(root_dp), move
(edge_dp), move(redge_dp));
};
} // namespace reroot

int main() {
    ll n;
    cin >> n;
    vector<vector<ll>> g(n);
    // everything should be 0 based.

    using Aggregate = int;
    using Value = int;

    auto base = [] (int vertex) ->
        Aggregate {
        // task here
    };
    auto merge_into = [] (Aggregate
        vertex_dp, Value neighbor_dp, int
        vertex, int edge_index) ->
        Aggregate {
        // task here
    };
    auto finalize_merge = [] (Aggregate
        vertex_dp, int vertex, int
        edge_index) -> Value {
        // task here
    };
    auto [reroot_result, edge_dp,
        redge_dp] = reroot::rerooter(g,
        base, merge_into, finalize_merge);
}

```

4.9 Centroid_Tree

```

const ll n = 1e5;
vector<ll> sz(n + 5), dead(n + 5);
function<void(ll, ll)> calculate_sz =
    [&](ll u, ll p) {
        sz[u] = 1;
        for (auto v : adj[u]) {
            if (v != p and !dead[v]) {
                calculate_sz(v, u);
                sz[u] += sz[v];
            }
        }
        return;
    };

function<ll(ll, ll, ll)>
    find_centroid = [&](ll u, ll p, ll
    total) -> ll {
        for (auto v : adj[u]) {
            if (v != p and !dead[v] and 2 *
                sz[v] > total)
                return find_centroid(v, u,
                    total);
        }
        return u;
    };

function<void(ll)> decompose = [&] (
    ll u) -> void {
    // if needed change the parameter
    calculate_sz(u, -1);
    ll center = find_centroid(u, -1, sz
        [u]);
    // calculate the ans here
    dead[center] = 1;
    for (auto v : adj[center]) {
        if (!dead[v])
            decompose(v);
    }
};
// call decompose only
decompose(1);

```

4.10 Euler_ckt

```

unordered_map<ll, ll> Start, End, Val;
unordered_map<ll, pair<ll, ll>> Range;
ll start = 0;
void dfs(ll node) {
    visited[node] = true;
    Start[node] = start++;
    for (auto child : adj[node]) {
        if (!visited[child])
            dfs(child);
    }
    End[node] = start - 1;
}
dfs(1);
vector<ll> FlatArray(start + 5);
for (auto i : Start) {
    FlatArray[i.second] = Val[i.first];
    Range[i.first] = {i.second, End[i.
        first]};
}

```

4.11 Min Cost Max Flow

```

#include <bits/stdc++.h>
using namespace std;
const int N = 3e5 + 9;

// Works for both directed, undirected
// and with negative cost too
// doesn't work for negative cycles
// for undirected edges just make the
// directed flag false
// Complexity: O(min(E^2 * V log V, E
// log V * flow))
using T = long long;
const T inf = 1LL << 61;
struct MCMF {
    struct edge {
        int u, v;
        T cap, cost;
        int id;
        edge(int _u, int _v, T _cap, T
            _cost, int _id) {
            u = _u;
            v = _v;
            cap = _cap;
            cost = _cost;
            id = _id;
        }
    };
    int n, s, t, mxid;
    T flow, cost;
    vector<vector<int>> g;
    vector<edge> e;
    vector<T> d, potential, flow_through;
    vector<int> par;
    bool neg;
    MCMF() {}
    MCMF(int _n) { // 0-based indexing
        n = _n + 10;
        g.assign(n, vector<int>());
        neg = false;
        mxid = 0;
    }
    void add_edge(int u, int v, T cap, T
        cost, int id = -1,
        bool directed = true) {
        if (cost < 0)
            neg = true;
        g[u].push_back(e.size());
        e.push_back(edge(u, v, cap, cost,
            id));
        g[v].push_back(e.size());
        e.push_back(edge(v, u, 0, -cost,
            -1));
        mxid = max(mxid, id);
        if (!directed)
            add_edge(v, u, cap, cost, -1,
                true);
    }
    bool dijkstra() {
        par.assign(n, -1);
        d.assign(n, inf);
    }
};

```

```

priority_queue<pair<T, T>, vector<
    pair<T, T>>, greater<pair<T, T
>>> q;
d[s] = 0;
q.push(pair<T, T>(0, s));
while (!q.empty()) {
    int u = q.top().second;
    T nw = q.top().first;
    q.pop();
    if (nw != d[u])
        continue;
    for (int i = 0; i < (int)g[u].
        size(); i++) {
        int id = g[u][i];
        int v = e[id].v;
        T cap = e[id].cap;
        T w = e[id].cost + potential[u]
            - potential[v];
        if (d[u] + w < d[v] && cap > 0)
        {
            d[v] = d[u] + w;
            par[v] = id;
            q.push(pair<T, T>(d[v], v));
        }
    }
}
for (int i = 0; i < n; i++) {
    if (d[i] < inf)
        d[i] += (potential[i] -
            potential[s]);
}
for (int i = 0; i < n; i++) {
    if (d[i] < inf)
        potential[i] = d[i];
}
return d[t] != inf; // for max flow
min cost
// return d[t] <= 0; // for min
cost flow
}
T send_flow(int v, T cur) {
    if (par[v] == -1)
        return cur;
    int id = par[v];
    int u = e[id].u;
    T w = e[id].cost;
    T f = send_flow(u, min(cur, e[id].
        cap));
    cost += f * w;
    e[id].cap -= f;
    e[id ^ 1].cap += f;
    return f;
}
// returns {maxflow, mincost}
pair<T, T> solve(int _s, int _t, T
    goal = inf) {
    s = _s;
    t = _t;
    flow = 0, cost = 0;
    potential.assign(n, 0);
    if (neg) {
        // Run Bellman-Ford to find
        // starting potential on the
        // starting graph
        // If the starting graph (before
        // pushing flow in the residual
        // graph) is a
        // DAG, then this can be
        // calculated in O(V + E) using
        // DP: potential(v) =
        // min({potential[u] + cost[u][v]
        // }) for each u -> v and
        // potential[s] = 0
        d.assign(n, inf);
        d[s] = 0;
        bool relax = true;
        for (int i = 0; i < n && relax; i
            ++){
            relax = false;
            for (int u = 0; u < n; u++) {
                for (int k = 0; k < (int)g[u]
                    .size(); k++) {
                    int id = g[u][k];
                    int v = e[id].v;

```

```

        T cap = e[id].cap, w = e[id]
            ].cost;
        if (d[v] > d[u] + w && cap
            > 0) {
            d[v] = d[u] + w;
            relax = true;
        }
    }
}
for (int i = 0; i < n; i++)
    if (d[i] < inf)
        potential[i] = d[i];
}
while (flow < goal && dijkstra())
    flow += send_flow(t, goal - flow);
flow_through.assign(mxid + 10, 0);
for (int u = 0; u < n; u++) {
    for (auto v : g[u]) {
        if (e[v].id >= 0)
            flow_through[e[v].id] = e[v ^
                1].cap;
    }
}
return make_pair(flow, cost);
};
int main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
    int n;
    cin >> n;
    assert(n <= 10);
    MCMF F(2 * n);
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            int k;
            cin >> k;
            F.add_edge(i, j + n, 1, k, i * 20
                + j);
        }
    }
    int s = 2 * n + 1, t = s + 1;
    for (int i = 0; i < n; i++) {
        F.add_edge(s, i, 1, 0);
        F.add_edge(i + n, t, 1, 0);
    }
    auto ans = F.solve(s, t).second;
    long long w = 0;
    set<int> se;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            int p = i * 20 + j;
            if (F.flow_through[p] > 0) {
                se.insert(j);
                w += F.flow_through[p];
            }
        }
    }
    assert(se.size() == n && w == n);
    cout << ans << '\n';
    return 0;
}

```

4.12 SCC

```

unordered_map<ll, vector<ll>> adj,
    InvAdj;
stack<ll> order;
unordered_map<ll, bool> visited;
unordered_map<ll, vector<ll>> all_scc;
unordered_map<ll, ll> compId;
void dfs_for_start(ll curr) {
    visited[curr] = 1;
    for (auto i : adj[curr])
        if (!visited[i])
            dfs_for_start(i);
    order.push(curr);
}
vector<ll> curr_comp;
void dfs_for_scc(ll curr) {
    visited[curr] = 1;
    for (auto i : InvAdj[curr])

```

```

    if (!visited[i])
        dfs_for_scc(i);
    curr_comp.push_back(curr);
}
inline void scc() {
    ll n, e, u, v;
    cin >> n >> e;
    for (ll i = 0; i < e; i++) {
        cin >> u >> v;
        adj[u].push_back(v);
        InvAdj[v].push_back(u);
    }
    for (ll i = 1; i <= n; i++)
        if (!visited[i])
            dfs_for_start(i);
    visited.clear();
    while (!order.empty()) {
        if (!visited[order.top()]) {
            curr_comp.clear();
            dfs_for_scc(order.top());
            ll sz = all_scc.size() + 1;
            all_scc[sz] = curr_comp;
            for (auto i : curr_comp)
                compId[i] = sz;
        }
        order.pop();
    }
}
// no. of ways and min cost of
// connecting the sccs
const ll MOD = 1e9 + 7, N = 1e5 + 2,
INF = 1e18 + 2;
ll n, m, comp[N];
vector<ll> adj[N], rev[N];
bitset<N> vis;
void DFS1(ll u, stack<ll> &TS) {
    vis[u] = true;
    for (ll v : adj[u])
        if (!vis[v])
            DFS1(v, TS);
    TS.push(u);
}
void DFS2(ll u, const ll scc_no, ll &
    min_cost, ll &ways, vector<ll> &cost
) {
    vis[u] = true;
    comp[u] = scc_no;
    for (ll v : rev[u])
        if (!vis[v]) {
            if (min_cost == cost[v])
                ++ways;
            else if (min_cost > cost[v]) {
                ways = 1;
                min_cost = cost[v];
            }
            DFS2(v, scc_no, min_cost, ways,
                cost);
        }
}
signed main() {
    FIO cin >> n;
    vector<ll> cost(n + 1);
    for (ll i = 1; i <= n; ++i)
        cin >> cost[i];
    cin >> m;
    while (m--) {
        ll u, v;
        cin >> u >> v;
        adj[u].push_back(v);
        rev[v].push_back(u);
    }
    ll tot = 0, ways = 1;
    stack<ll> TS;
    for (ll i = 1; i <= n; ++i)
        if (!vis[i])
            DFS1(i, TS);
    vis.reset();
    ll scc_no = 0;
    while (!TS.empty()) {
        ll u = TS.top();
        TS.pop();
        if (!vis[u]) {
            ll tmp_cst = cost[u], tmp_ways =
                1;

```

```

            DFS2(u, ++scc_no, tmp_cst,
                tmp_ways, cost);
            tot += tmp_cst;
            ways = (ways * tmp_ways) % MOD;
        }
    }
    cout << tot << ' ' << ways;
} // TC: O(V+E)

```

4.13 0-1 BFS

```

vector<ll> d(n, INF);
d[s] = 0;
deque<ll> q;
q.push_front(s);
while (!q.empty()) {
    ll v = q.front();
    q.pop_front();
    for (auto edge : adj[v]) {
        ll u = edge.first;
        ll w = edge.second;
        if (d[v] + w < d[u]) {
            d[u] = d[v] + w;
            if (w == 1)
                q.push_back(u);
            else
                q.push_front(u);
        }
    }
}

```

4.14 Hull

```

// Convex Hull
#pragma GCC target("avx2")
#pragma GCC optimize("O3")
#pragma GCC optimize("unroll-loops")
#include <bits/stdc++.h>
using namespace std;

typedef long long int ll;
typedef long double ld;
typedef pair<ll, ll> pl;
typedef vector<ll> vl;
typedef complex<ll> pt;

#define G(x) ll x; cin >> x;
#define F(i, l, r) for (ll i = l; i < (
    r); ++i)
#define A(a) (a).begin(), (a).end()
#define CRS(a, b) (conj(a) * (b)).Y
#define K first
#define V second
#define X real()
#define Y imag()
#define N 100010

namespace std {
    bool operator<(pt a, pt b) { return a.X
        == b.X ? a.Y < b.Y : a.X < b.X; }
} // namespace std

bool in_hull(pt p, vector<pt> &hu,
    vector<pt> &hd) {
    if (p == *hu.begin() || p == *hd.
        begin())
        return false; // change to true if
            border counts as inside
    if (p < *hu.begin() || *hd.begin() <
        p)
        return false;
    auto u = upper_bound(A(hu), p);
    auto d = lower_bound(hd.rbegin(), hd.
        rend(), p);
    return CRS(*u - p, *(u - 1) - p) > 0
        &&
        CRS(*(d - 1) - p, *d - p) >
            0; // change to >= if
                border counts as "
                    inside"
}

void do_hull(vector<pt> &pts, vector<pt>
    & &hd) {
    for (pt p : pts) {

```

```

    while (h.size() > 1 && CRS(h.back()
        - p, h[h.size() - 2] - p) <=
            0) //
        change
        to <
        0 if
        border
        points
        included

        h.pop_back();
        h.push_back(p);
    }
}

pair<vector<pt>, vector<pt>> get_hull(
    vector<pt> &pts) {
    vector<pt> hu, hd;
    sort(A(pts)), do_hull(pts, hu);
    reverse(A(pts)), do_hull(pts, hd);
    return {hu, hd};
}

vector<pt> full_hull(vector<pt> &pts) {
    auto h = get_hull(pts);
    h.K.pop_back(), h.V.pop_back();
    for (pt p : h.V)
        h.K.push_back(p);
    return h.K;
}

int main() {
    G(n) vector<pt> v;
    F(i, 0, n) { G(x) G(y) v.push_back({x
        , y}); }
    vector<pt> h = full_hull(v);
}

```

4.15 Dynamic Hull

```

// Dynamic Convex Hull
#pragma GCC target("avx2")
#pragma GCC optimize("O3")
#pragma GCC optimize("unroll-loops")
#include <bits/stdc++.h>
using namespace std;

typedef long long int ll;
typedef long double ld;
typedef pair<ll, ll> pl;
typedef vector<ll> vl;
typedef complex<ll> pt;

#define G(x) ll x; cin >> x;
#define F(i, l, r) for (ll i = l; i < (
    r); ++i)
#define A(a) (a).begin(), (a).end()
#define CRS(a, b) (conj(a) * (b)).Y
#define X real()
#define Y imag()
#define N 100010

namespace std {
    bool operator<(pt a, pt b) { return a.X
        == b.X ? a.Y < b.Y : a.X < b.X; }
} // namespace std

// helper function for dyn_in_hull
bool in(pt p, set<pt> &h) {
    if (h.empty() || p < *h.begin() || *h
        .rbegin() < p)
        return false;
    auto i = h.upper_bound(p), j = i--;
    return CRS(*j - p, *i - p) > 0; //
        change to >= if border counts as "
        inside"
}

// returns true if p contained in
// dynamic hull hu / hd
bool in_hull(pt p, set<pt> &hu, set<pt>
    &hd) { return in(p, hu) && in(-p,
    hd); }

// helper function for dyn_add

```

```

void fix_bad(set<pt>::iterator i, set<
    pt> &h, bool l) {
    if (i == --h.begin() || i == h.end())
        return;
    pt p = *i;
    h.erase(p);
    if (!in(p, h))
        h.insert(p);
    else
        fix_bad(l ? --h.lower_bound(p) : h.
            upper_bound(p), h, l);
}

// helper function for dyn_add_to_hull
void add(pt p, set<pt> &h) {
    if (in(p, h))
        return;
    h.insert(p);
    fix_bad(--h.lower_bound(p), h, true);
    fix_bad(h.upper_bound(p), h, false);
}

// adds p to dynamic hull hu / hd
void add_to_hull(pt p, set<pt> &hu, set
    <pt> &hd) { add(p, hu), add(-p, hd);
}

int main() {
    G(n) set<pt> hu, hd;
    F(i, 0, n) { G(x) G(y) add_to_hull({x
        , y}, hu, hd); }
}

```

5 Misc

5.1 Max Pos and Next Greater

```

const ll MXX = 1e5 + 5;
ll mxtree[4 * MXX], arr[MXX];
void mxtree(ll idx, ll left, ll right)
{
    if (left == right)
        mxtree[idx] = left;
    else {
        ll mid = (left + right) / 2;
        mxtree(idx * 2, left, mid);
        mxtree(idx * 2 + 1, mid + 1, right
            );
        ll left = mxtree[idx * 2];
        ll right = mxtree[idx * 2 + 1];
        if (arr[left] < arr[right])
            mxtree[idx] = right;
        else
            mxtree[idx] = left;
    }
}

ll mxPos(ll idx, ll tleft, ll tright,
    ll qlf, ll qright) {
    if (qlf > qright)
        return -1;
    if (qlf == tleft and qright ==
        tright)
        return mxtree[idx];
    ll tmid = (tleft + tright) / 2;
    ll left = mxPos(idx * 2, tleft, tmid,
        qlf, min(qright, tmid));
    ll right = mxPos(idx * 2 + 1, tmid +
        1, tright, max(qlf, tmid + 1),
        qright);
    ll ans;
    if (left == -1)
        ans = right;
    else if (right == -1)
        ans = left;
    else if (arr[left] < arr[right])
        ans = right;
    else
        ans = left;
    return ans;
}

ll main() {
    ll t = 1, n, q, a, b;
    cin >> t;
}

```



```

while (t--) {
    cin >> n >> q;
    for (ll i = 0; i < n; i++)
        cin >> arr[i];
    stack<ll> stk;
    ll nge[n];
    stk.push(0);
    for (ll i = 1; i < n; i++) {
        while (stk.size() and arr[stk.top()] < arr[i]) {
            nge[stk.top()] = i;
            stk.pop();
        }
        stk.push(i);
    }
    while (stk.size()) {
        nge[stk.top()] = n;
        stk.pop();
    }
    ll ans[n];
    ans[n - 1] = 0;
    for (ll i = n - 2; i >= 0; i--) {
        ll tmp = nge[i];
        if (tmp == n)
            ans[i] = 0;
        else
            ans[i] = ans[tmp] + 1;
    }
    maxtree(1, 0, n - 1);
    for (ll i = 0; i < q; i++) {
        cin >> a >> b;
        if (a > b)
            swap(a, b);
        cout << ans[mxPos(1, 0, n - 1, a - 1, b - 1)] << "\n";
    }
}

```

5.2 Knight Move

```

ll X[8]={2,1,-1,-2,-2,-1,1,2};
ll Y[8]={1,2,2,1,-1,-2,-2,-1};

```

5.3 MatrixExpo

```

typedef long long LL;
LL arr[60][60], res[60][60], tmp[60][60], m;

void matMul(LL a[][60], LL b[][60], LL mod) {
    for (ll i = 0; i < m; i++)
        for (ll j = 0; j < m; j++) {
            tmp[i][j] = 0;
            for (ll k = 0; k < m; k++) {
                tmp[i][j] += (a[i][k] * b[k][j]) % mod;
                tmp[i][j] %= mod;
            }
        }
}

void power(LL n, LL mod) {
    for (ll i = 0; i < m; i++)
        for (ll j = 0; j < m; j++)
            if (i == j)
                res[i][j] = 1;
            else
                res[i][j] = 0;

    while (n) {
        if (n & 1) {
            matMul(res, arr, mod);
            for (ll i = 0; i < m; i++)
                for (ll j = 0; j < m; j++)
                    res[i][j] = tmp[i][j];
            n--;
        } else {
            matMul(arr, arr, mod);
            for (ll i = 0; i < m; i++)
                for (ll j = 0; j < m; j++)
                    arr[i][j] = tmp[i][j];
            n /= 2;
        }
    }
}

```

```

    }
}

```

6 Number Theory

6.1 Leap_year

```

bool isLeap(ll n) {
    if (n % 100 == 0)
        return (n % 400 == 0);
    else
        return (n % 4 == 0);
}

// leap year between l and r
ll calNum(ll y) { return (y / 4) - (y / 100) + (y / 400); }
ll leapNum(ll l, ll r) { return calNum(r) - calNum(--l); }

```

6.2 Print_calender

```

ll dayNumber(ll day, ll month, ll year) {
    ll t[] = {0, 3, 2, 5, 0, 3, 5, 1, 4, 6, 2, 4};
    year -= month < 3;
    return (year + year / 4 - year / 100 + year / 400 + t[month - 1] + day) % 7;
}

string getMonthName(ll monthNumber) {
    string months[] = {"January", "February", "March", "April", "May", "June", "July", "August", "September", "October", "November", "December"};
    return months[monthNumber];
}

ll numberOfDays(ll monthNumber, ll year) {
    if (monthNumber == 1 && isLeapYear(year))
        return 29;
    ll monthDays[] = {31, 28, 31, 30, 31, 30, 31, 31, 30, 31, 30, 31};
    return monthDays[monthNumber];
}

void prllCalendar(ll year) {
    printf("Calendar - %d\n\n", year);
    ll days;
    ll current = dayNumber(1, 1, year);
    // i: Iterate through all the months
    // j: Iterate through all the days of the month - i
    for (ll i = 0; i < 12; i++) {
        days = numberOfDays(i, year);
        cout << "    |" << getMonthName(i).c_str() << " |" << endl;
        printf(" Sun Mon Tue Wed Thu Fri Sat\n");
        ll k;
        for (k = 0; k < current; k++)
            printf("    ");
        for (ll j = 1; j <= days; j++) {
            printf("%4d", j);
            if (++k > 6) {
                k = 0;
                cout << endl;
            }
        }
        if (k)
            cout << endl;
        cout << "-----\n";
        current = k;
    }
}

```

6.3 Binary_exponentiation

```

11 binaryExp(11 base, 11 power, 11 MOD
    = mod) {
    11 res = 1;
    while (power) {
        if (power & 1)
            res = (res * base) % MOD;
        base = ((base % MOD) * (base % MOD)
            ) % MOD;
        power /= 2;
    }
    return res;
}
/*
task:  $a^b \mod c$ 
binaryExp(a, binaryExp(b, c, mod - 1),
    mod)
*/

```

6.4 Count_divisor

```

11 maxVal = 1e6 + 1;
vector<11> countDivisor(maxVal, 0);
void countingDivisor() {
    for (11 i = 1; i < maxVal; i++)
        for (11 j = i; j < maxVal; j += i)
            countDivisor[j]++;
}
// TC:  $n \log(n)$ 
// count the number of divisors of all
// numbers in a range.

```

6.5 Check_prime

```

bool prime(11 n) {
    if (n < 2)
        return false;
    if (n <= 3)
        return true;
    if (!(n % 2) || !(n % 3))
        return false;
    for (11 i = 5; i * i <= n; i += 6) {
        if (!(n % i) || !(n % (i + 2)))
            return false;
    }
    return true;
}
// TC:  $\sqrt{n} / 6$ 

```

6.6 SPF

```

// smallest prime factor using sieve
const 11 N = 1e7 + 5;
11 spf[N];
void smallestPrimeFactorUsingSieve() {
    for (11 i = 2; i < N; i++) {
        if (spf[i] == 0) {
            for (11 j = i; j < N; j += i) {
                if (spf[j] == 0)
                    spf[j] = i;
            }
        }
    }
}
// smallest factor of a number
11 factor(11 n) {
    11 a;
    if (n % 2 == 0)
        return 2;
    for (a = 3; a * a <= n; a += 2) {
        if (n % a == 0)
            return a;
    }
    return n;
}
// complete factorization
11 r;
while (n > 1) {
    r = factor(n);
    cout << r << '\n';
    n /= r;
}

```

}

6.7 Sieve

```

const 11 N = 1e7 + 5;
11 prime[N];
void sieveOfEratosthenes() {
    for (11 i = 2; i < N; i++)
        prime[i] = 1;
    for (11 i = 4; i < N; i += 2)
        prime[i] = 0;
    for (11 i = 3; i * i < N; i++) {
        if (prime[i]) {
            for (11 j = i * i; j < N; j += i
                * 2)
                prime[j] = 0;
        }
    }
}

```

6.8 Optimize_sieve

```

vector<11> sieve(const 11 N, const 11 Q
    = 17, const 11 L = 1 << 15) {
    static const 11 rs[] = {1, 7, 11, 13,
        17, 19, 23, 29};
    struct P {
        P(11 p) : p(p) {}
        11 p;
        11 pos[8];
    };
    auto approx_prime_count = [](const 11
        N) -> 11 {
        return N > 60184 ? N / (log(N) -
            1.1) : max(1., N / (log(N) -
            1.1)) + 1;
    };
    const 11 v = sqrt(N), vv = sqrt(v);
    vector<bool> isp(v + 1, true);
    for (11 i = 2; i <= vv; ++i)
        if (isp[i]) {
            for (11 j = i * i; j <= v; j += i
                )
                isp[j] = false;
        }
    const 11 rsize = approx_prime_count(N
        + 30);
    vector<11> primes = {2, 3, 5};
    11 psize = 3;
    primes.resize(rsize);

    vector<P> sprimes;
    size_t pbeg = 0;
    11 prod = 1;
    for (11 p = 7; p <= v; ++p) {
        if (!isp[p])
            continue;
        if (p <= Q)
            prod *= p, ++pbeg, primes[psize
                ++] = p;
        auto pp = P(p);
        for (11 t = 0; t < 8; ++t) {
            11 j = (p <= Q) ? p : p * p;
            while (j % 30 != rs[t])
                j += p << 1;
            pp.pos[t] = j / 30;
        }
        sprimes.push_back(pp);
    }
    vector<unsigned char> pre(prod, 0xFF);
    for (size_t pi = 0; pi < pbeg; ++pi) {
        auto pp = sprimes[pi];
        const 11 p = pp.p;
        for (11 t = 0; t < 8; ++t) {
            const unsigned char m = ~(1 << t);
            for (11 i = pp.pos[t]; i < prod;
                i += p)
                pre[i] &= m;
        }
    }
}

```

```

const ll block_size = (L + prod - 1)
/ prod * prod;
vector<unsigned char> block(
    block_size);
unsigned char *pblock = block.data();
const ll M = (N + 29) / 30;
for (ll beg = 0; beg < M; beg +=
    block_size, pblock -= block_size)
{
    ll end = min(M, beg + block_size);
    for (ll i = beg; i < end; i += prod)
    {
        copy(pre.begin(), pre.end(),
            pblock + i);
    }
    if (beg == 0)
        pblock[0] &= 0xFE;
    for (size_t pi = pbeg; pi < sprimes
        .size(); ++pi) {
        auto &pp = sprimes[pi];
        const ll p = pp.p;
        for (ll t = 0; t < 8; ++t) {
            ll i = pp.pos[t];
            const unsigned char m = ~(1 <<
                t);
            for (; i < end; i += p)
                pblock[i] &= m;
            pp.pos[t] = i;
        }
        for (ll i = beg; i < end; ++i) {
            for (ll m = pblock[i]; m > 0; m
                &= m - 1) {
                primes[psize++] = i * 30 + rs[
                    __builtin_ctz(m)];
            }
        }
    }
    assert(psize <= rsize);
    while (psize > 0 && primes[psize - 1]
        > N)
        --psize;
    primes.resize(psize);
    return primes;
}
// it takes 500ms for generating prime
upto 1e9

```

6.9 nth_prime_number

```

vector<ll> nth_prime;
const ll MX = 86200005;
bitset<MX> visited;
void optimized_prime() {
    nth_prime.push_back(2);
    for (ll i = 3; i < MX; i += 2) {
        if (visited[i])
            continue;
        nth_prime.push_back(i);
        if (1ll * i * i > MX)
            continue;
        for (ll j = i * i; j < MX; j += i +
            i)
            visited[j] = true;
    }
}

```

6.10 nCr

```

// 1:
// more space, less time
const ll MAX = 1e7 + 5;
vector<ll> fact(MAX), ifact(MAX), inv(
    MAX);
void factorial() {
    inv[1] = fact[0] = ifact[0] = 1;
    for (ll i = 2; i < MAX; i++)
        inv[i] = inv[mod % i] * (mod - mod
            / i) % mod;
    for (ll i = 1; i < MAX; i++)
        fact[i] = (fact[i - 1] * i) % mod;
    for (ll i = 1; i < MAX; i++)

```

```

        ifact[i] = ifact[i - 1] * inv[i] %
            mod;
    }
    ll nCr(ll n, ll r) {
        if (r < 0 || r > n)
            return 0;
        return (ll)fact[n] * ifact[r] % mod *
            ifact[n - r] % mod;
    }
    // 2:
    // less space, more time
    const ll MAX = 1e7 + 10;
    vector<ll> fact(MAX), inv(MAX);
    void factorial() {
        fact[0] = 1;
        for (ll i = 1; i < MAX; i++)
            fact[i] = (i * fact[i - 1]) % mod;
    }
    ll binaryExp(ll a, ll n, ll M = mod){};
    // needs to implement
    void inverse() {
        for (ll i = 0; i < MAX; ++i)
            inv[i] = binaryExp(fact[i], mod -
                2);
    }
    ll nCr(ll a, ll b) {
        if (a < b or a < 0 or b < 0)
            return 0;
        ll de = (inv[b] * inv[a - b]) % mod;
        return (fact[a] * de) % mod;
    }
    // 3:
    // nCr mod m where m is not prime
    ll C_mod_p(ll n, ll k, ll p) {
        if (k > n)
            return 0;
        vector<ll> fac(p);
        fac[0] = 1;
        for (int i = 1; i < p; i++)
            fac[i] = fac[i - 1] * i % p;
        ll res = 1;
        while (n || k) {
            ll ni = n % p, ki = k % p;
            if (ki > ni)
                return 0;
            res = res * fac[ni] % p * modInv(
                fac[ki], p) % p * modInv(fac[ni
                    - ki], p) %
                p;
            n /= p;
            k /= p;
        }
        return res;
    }
    // compute nCr mod composite m (non-
    prime)
    ll nCr_mod_m(ll n, ll k, ll m) {
        // Step 1: factorize m
        vector<int> primes;
        int tmp = m;
        for (int i = 2; i * i <= tmp; i++) {
            if (tmp % i == 0) {
                primes.push_back(i);
                while (tmp % i == 0)
                    tmp /= i;
            }
        }
        if (tmp > 1)
            primes.push_back(tmp);
        // Step 2: compute result mod each
        prime
        vector<ll> rem, mod;
        for (int p : primes) {
            rem.push_back(C_mod_p(n, k, p));
            mod.push_back(p);
        }
        // Step 3: Chinese Remainder Theorem
        (combine)
        ll res = 0;
        for (int i = 0; i < (int)mod.size();
            i++) {
            ll Mi = m / mod[i];

```

```

    ll invMi = binaryExp(Mi, mod[i] -
        2, mod[i]); // modular inverse
    res = (res + rem[i] * Mi % m *
        invMi % m) % m;
}
return res;
}

```

6.11 Factorial_mod

```

// n! mod p : Here P is mod value
// For binaryExp we call 1.6 function
ll factmod(ll n, ll p) {
    ll res = 1;
    while (n > 1) {
        res = (res * binaryExp(p - 1, n / p
            , p)) % p;
        for (ll i = 2; i <= n % p; ++i)
            res = (res * i) % p;
        n /= p;
    }
    return (res % p);
}

```

6.12 PHI

```

// the positive integers less than or
// equal to n that are relatively prime
// to n.
ll phi(ll n) {
    ll result = n;
    for (ll i = 2; i * i <= n; i++) {
        if (n % i == 0) {
            while (n % i == 0)
                n /= i;
            result -= result / i;
        }
    }
    if (n > 1)
        result -= result / n;
    return result;
}
// PHI of 1 to N
const int N = 1e6 + 9;
int phi[N];
int phiS[N];
void totient() {
    for (int i = 1; i < N; i++)
        phi[i] = i;
    for (int i = 2; i < N; i++) {
        if (phi[i] == i) {
            for (int j = i; j < N; j += i)
                phi[j] -= phi[j] / i;
        }
    }
    phiS[0] = phi[0];
    for (int i = 1; i < N; i++)
        phiS[i] = phiS[i - 1] + phi[i];
}

```

6.13 Catalan

```

void catalan(ll n) {
    ll res = 1;
    cout << res << " ";
    for (ll i = 1; i < n; i++) {
        res = (res * (4 * i - 2)) / (i + 1);
        cout << res << " ";
    }
}

```

6.14 Extended_GCD

```

// return {x,y} such that ax + by = gcd
// (a,b)
ll extended_euclid(ll a, ll b, ll &x,
    ll &y) {
    if (b == 0) {
        x = 1;
        y = 0;
        return a;
    }
}

```

```

}
ll x1, y1;
ll d = extended_euclid(b, a % b, x1,
    y1);
x = y1;
y = x1 - y1 * (a / b);
return d;
}
ll inverse(ll a, ll m) {
    ll x, y;
    ll g = extended_euclid(a, m, x, y);
    if (g != 1)
        return -1;
    return (x % m + m) % m;
}

```

6.15 Large Mod

```

ll mod(string &num, ll a) {
    ll res = 0;
    for (ll i = 0; i < num.length(); i++)
        res = (res * 10 + num[i] - '0') % a;
    return res;
}

```

6.16 Factorial_Divisor

```

ll factorialDivisors(ll n) {
    ll result = 1;
    for (ll i = 0; i < allPrimes.size();
        i++) {
        ll p = allPrimes[i];
        ll exp = 0;
        while (p <= n) {
            exp = exp + (n / p);
            p = p * allPrimes[i];
        }
        result = result * (exp + 1);
    }
    return result;
}

```

6.17 Number_conversion

```

// 10 - ary to m - ary
char a[16] = {'0', '1', '2', '3', '4', '5', '6', '7', '8', '9', 'A', 'B', 'C', 'D', 'E', 'F'};
string tenToM(ll n, ll m) {
    ll temp = n;
    string result = "";
    while (temp != 0) {
        result = a[temp % m] + result;
        temp /= m;
    }
    return result;
}
// m - ary to 10 - ary
string num = "0123456789ABCDE";
ll mToTen(string n, ll m) {
    ll multi = 1;
    ll result = 0;
    for (ll i = n.size() - 1; i >= 0; i--) {
        result += num.find(n[i]) * multi;
        multi *= m;
    }
    return result;
}

```

6.18 Number_of_1_in_bit_till_N

```

ll cntOnes(ll n) {
    ll cnt = 0;
    for (ll i = 1; i <= n; i <= 1) {
        ll x = (n + 1) / (i << 1);
        cnt += x * i;
        if ((n + 1) % i && n & i)
            cnt += (n + 1) % i;
    }
    return cnt;
}

```

}

6.19 Disarrangement

```

11 disarrange(11 n) {
    if (n == 1)
        return 0;
    if (n == 2)
        return 1;
    return (n - 1) * (disarrange(n - 1) +
        disarrange(n - 2));
}
// D(n) = (n!)/e

```

6.20 Millar_Rabin

```

bool check_composite(11 n, 11 a, 11 d,
    11 s) {
    11 x = binaryExp(a, d, n);
    if (x == 1 || x == n - 1)
        return false;
    for (11 r = 1; r < s; r++) {
        x = (u128)x * x % n;
        if (x == n - 1)
            return false;
    }
    return true;
};
bool MillerRabin(11 n, 11 iter = 5) {
    // returns true if n is probably
    // prime, else returns false.
    if (n < 4)
        return n == 2 || n == 3;
    11 s = 0;
    11 d = n - 1;
    while ((d & 1) == 0) {
        d >>= 1;
        s++;
    }
    for (11 i = 0; i < iter; i++) {
        11 a = 2 + rand() % (n - 3);
        if (check_composite(n, a, d, s))
            return false;
    }
    return true;
}

```

6.21 Modular_operation

```

// Addition :
11 mod_add(11 a, 11 b, 11 MOD = mod) {
    a = a % MOD, b = b % MOD;
    return ((a + b) % MOD) + MOD) % MOD;
}
// Subtraction :
11 mod_sub(11 a, 11 b, 11 MOD = mod) {
    a = a % MOD, b = b % MOD;
    return (((a - b) % MOD) + MOD) % MOD;
}
// Multiplication :
11 mod_mul(11 a, 11 b, 11 MOD = mod) {
    a = a % MOD, b = b % MOD;
    return (((a * b) % MOD) + MOD) % MOD;
}
// Division :

```

```

11 mminvprime(11 a, 11 b) { return
    binaryExp(a, b - 2, b); }
11 mod_div(11 a, 11 b, 11 MOD = mod) {
    a = a % MOD, b = b % MOD;
    return (mod_mul(a, mminvprime(b, MOD)
        , MOD) + MOD) % MOD;
}

```

6.22 MSLCM

```

// For a given number N, maximum sum
// LCM indicates the set of numbers
// whose LCM
// is N and summation is maximum. Let,
// MSLCM(N) denote this maximum sum of
// numbers. Given the value of N you
// will have to find the value:
// summation of
// MSLCM(i) from i to 2n
11 MSLCM(11 n) {
    11 l = 1, r, val, ret = 0;
    while (l <= n) {
        val = n / l, r = n / val;
        ret += val * ((l + r) * (r - l + 1)
            / 2);
        l = r + 1;
    }
    return ret - 1;
}

```

6.23 Find numbers in between [L, R] which are divisible by all Array elements

```

void solve(11 *arr, 11 N, 11 L, 11 R) {
    11 LCM = arr[0];
    for (11 i = 1; i < N; i++) {
        LCM = (LCM * arr[i]) / (__gcd(LCM,
            arr[i]));
    }
    if ((LCM < L && LCM * 2 > R) || LCM >
        R) {
        return;
    }
    11 k = (L / LCM) * LCM;
    if (k < L)
        k = k + LCM;
    for (11 i = k; i <= R; i = i + LCM)
        cout << i << ' ';
}

```

Maximum Value (N)	Number with Most Divisors (n)	Number of Divisors ($\tau(n)$)
10^3	83,160	128
10^6	720,720	240
10^7	9,609,600	640
10^8	98,280,000	672
10^9	735,134,400	1,344
10^{10}	7,242,460,800	2,688
10^{11}	73,346,256,000	5,376
10^{12}	936,966,912,400	10,752

7 Mathematics

7.1 Area Formulas

Rectangle	length \times width
Square	side ²
Triangle	$\frac{1}{2} \times \text{base} \times \text{height}$
Parallelogram	base \times height
Pyramid (no base)	$\frac{1}{2} \times (\text{perimeter of base}) \times (\text{slant height})$
Polygon	$\frac{1}{2} \sum_{i=1}^n (x_i y_{i+1} - x_{i+1} y_i) $ $a + \frac{b}{2} - 1$ (for lattice co-ordinates)

a = interior lattice pts, b = boundary pts.

7.2 Volume Formulas

Cube	side ³
Rectangular Prism	length \times width \times height
Cylinder	$\pi \times \text{radius}^2 \times \text{height}$
Sphere	$\frac{4}{3} \pi \times \text{radius}^3$
Pyramid	$\frac{1}{3} \times (\text{base area}) \times (\text{height})$

7.3 Surface Area Formulas

Cube	$6 \times \text{side}^2$
Rectangular Prism	$2(lw + lh + wh)$ (l = length, w = width, h = height)
Cylinder	$2\pi r(r + h)$
Sphere	$4\pi r^2$
Pyramid	base area + $\frac{1}{2} \times (\text{perimeter}) \times (\text{slant height})$

7.4 Triangles

Semiperimeter	$s = \frac{a+b+c}{2}$
Area	$A = \sqrt{s(s-a)(s-b)(s-c)}$
Circumradius	$R = \frac{abc}{4A}$
Inradius	$r = \frac{A}{s}$
Median	$m_a = \frac{1}{2} \sqrt{2b^2 + 2c^2 - a^2}$
Angle bisector	$s_a = \sqrt{\frac{bc}{1 - (a/(b+c))^2}}$

Side lengths: a, b, c .

7.5 Sum Equations

$$\sum_{i=k}^n c^i = \frac{c^{n+1} - c^k}{c - 1} \quad \sum_{i=1}^n i = \frac{n(n+1)}{2}$$

$$\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6} \quad \sum_{i=1}^n i^3 = \left(\frac{n(n+1)}{2} \right)^2$$

$$\sum_{i=1}^n i^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30} \quad \sum_{i=1}^n (2i-1) = n^2$$

7.6 Trigonometry

Sine law	$\frac{\sin \alpha}{a} = \frac{\sin \beta}{b} = \frac{\sin \gamma}{c} = \frac{1}{2R}$
Cosine law	$a^2 = b^2 + c^2 - 2bc \cos \alpha$
Tangent law	$\frac{a+b}{a-b} = \frac{\tan(\frac{\alpha+\beta}{2})}{\tan(\frac{\alpha-\beta}{2})}$
$\sin(A \pm B)$	$\sin A \cos B \pm \cos A \sin B$
$\cos(A \pm B)$	$\cos A \cos B \mp \sin A \sin B$
$\tan(A \pm B)$	$\frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$
$\sin 2\theta$	$2 \sin \theta \cos \theta$
$\cos 2\theta$	$\cos^2 \theta - \sin^2 \theta$
$\tan 2\theta$	$\frac{2 \tan \theta}{1 - \tan^2 \theta}$
Half-angle	$\sin(\frac{\theta}{2}) = \pm \sqrt{\frac{1 - \cos \theta}{2}}, \cos(\frac{\theta}{2}) = \pm \sqrt{\frac{1 + \cos \theta}{2}}, \tan(\frac{\theta}{2}) = \frac{1 - \cos \theta}{\sin \theta}$
Sum identities	$\sin r + \sin w = 2 \sin(\frac{r+w}{2}) \cos(\frac{r-w}{2})$ $\cos r + \cos w = 2 \cos(\frac{r+w}{2}) \cos(\frac{r-w}{2})$
General	$(V + W) \tan\left(\frac{r-w}{2}\right) = (V - W) \tan\left(\frac{r+w}{2}\right)$
	$a \cos x + b \sin x = r \cos(x - \varphi)$
	$a \sin x - b \cos x = r \sin(x - \varphi)$
	where $r = \sqrt{a^2 + b^2}, \varphi = \text{atan2}(b, a)$

7.7 Logarithmic Basic

$\log_b 1 = 0$	$\log_b b = 0$
$b^{\log_b a} = a$	$x^{\log_b y} = y^{\log_b x}$
$\log_a b = \frac{1}{\log_b a}$	$\log_a x = \frac{\log_b x}{\log_b a}$
$\log_b(AB) = \log_b A + \log_b B$	
$\log_b\left(\frac{A}{B}\right) = \log_b A - \log_b B$	
$\log_a c = \log_a b \times \log_b c$	
$\log_b(A^x) = x \log_b A$	

7.8 Series

Catalan: $C_n = \frac{1}{n+1} \binom{2n}{n}, C_n = \sum_{k=0}^n C_k C_{n-k}$

Arithmetic: $a_n = a + (n-1)d, s_n = \frac{n}{2}(2a + (n-1)d)$

Geometric: $a_n = ar^{n-1}, s_n = \frac{a(1-r^n)}{1-r}$

Derangements: $D_n = n! \sum_{k=0}^n \frac{(-1)^k}{k!}, D_n = \left\lfloor \frac{n!}{e} + \frac{1}{2} \right\rfloor$

Fibonacci: $f_n = \frac{\phi^n - (1-\phi)^n}{\sqrt{5}}, \phi = \frac{1+\sqrt{5}}{2}$

7.9 Pick's Theorem

$A = I - \frac{1}{2}B + 1$ (I = interior points, B = boundary points)

7.10 Stars and Bars

Number of solutions of $x_1 + \dots + x_k = n$:

$\binom{n-1}{k-1}$ when $x_i > 0$; $\binom{n+k-1}{k-1}$ when $x_i \geq 0$.

7.11 Facts

$\left\lfloor \frac{a}{b} \right\rfloor = \left\lfloor \frac{a-1}{b} \right\rfloor + 1$

Sum l to r : $\frac{l+r}{2}(r-l+1)$

$\left\lfloor \frac{\lfloor n/a \rfloor}{b} \right\rfloor = \left\lfloor \frac{n}{ab} \right\rfloor$

7.12 LCM

$$\text{SUM} = \frac{n}{2} \left(\sum_{d|n} \varphi(d) d + 1 \right)$$

$$\text{lcm}(a, n) + \text{lcm}(n - a, n) = \frac{n^2}{\text{gcd}(a, n)}$$