Package 'BFI'

July 18, 2023

Type Package

Description

(Logistic) families.

Title Bayesian Federated Inference

Version 0.5.2
Date 2023-07-16
Author Hassan Pazira [aut, cre], Marianne Jonker [aut], Anthony Coolen [aut]
Maintainer Hassan Pazira hassan.pazira@radboudumc.nl
Description Bayesian Federated Inference method combines data from different (medical) centers without sharing them. In this version of the package, the user can fit models specifying Gaussian and Binomial (Logistic) families.
Encoding UTF-8
Suggests knitr, rmarkdown
VignetteBuilder knitr
R topics documented:
BFI-package . bfi . inv.prior.cov . MAP.estimation . Nurses . summary.bfi . trauma
BFI-package Bayesian Federated Inference

Bayesian Federated Inference method combines data from different (medical) centers without sharing them. In this version of the package, the user can fit models specifying Gaussian and Binomial

2 bfi

Details

Package: BFI
Type: Package
Version: 0.5.2
Date: 2023-07-16
License: GPL (>=2)

Author(s)

Hassan Pazira

Maintainer: Hassan Pazira <hassan.pazira@radboudumc.nl>

References

Jonker M.A., Pazira H. and Coolen A.C.C. (2023). *Bayesian Federated Inference for Statistical Models, Statistics in Medicine*, Vol. 0(0), 0-0. https://doi.org/10.48550/arXiv.2302.07677

bfi

Bayesian Federated Inference

Description

bfi function is used (in central server) to estimate the parameters in the GLM and Survival models by BFI method using the aggregated results form the local centers.

Usage

```
bfi(theta_hats = NULL, A_hats, Lambda,
    L = NULL, stratified = FALSE, nuisance = 1L)
```

Arguments

theta_hats a list of L vectors of the maximum a posteriori (MAP) estimates of L centers.

See 'Details'.

A_hats a list of L curvature matrices for L centers. See 'Details'.

Lambda a list of L+1 matrices. Each matrix used as the prior of the inverse variance-

covariance matrix of Gaussian distribution. The first L matrices are for L local centers and the last one is associated with the combined data. See 'Details'.

L number of locations/centers.

stratified logical flag for performing the stratified analysis. If stratified=TRUE, the pa-

rameters selected in the nuisance argument can be different across centers. De-

fault is stratified=FALSE. See 'Details'.

nuisance a vector of one or two elements. It is useable if stratified=TRUE. For the

binomial family the length of the vector should be one which referes to 'intercept', and for gaussian this vector can have maximum two elements which

refere to 'intercept' and/or 'sigma2'. See 'Details'.

bfi 3

Details

bfi function implements

Value

bfi returns a list containing the following components:

the ta_hat the p- or (p+1)-dimensional vector of estimates obtained by the 'BFI' method

if stratified=FALSE. When stratified=TRUE, in this case dimension of this vector is L+p-1 (for binomial family) or 2*L+p-1 (for gaussian family).

See 'Details';

A_hat the curvature matrix obtained by the 'BFI' method if stratified=FALSE. In

this case, it's a $p \times p$ - or $(p+1) \times (p+1)$ -dimensional matrix depending on the family used. If stratified=TRUE, it's a list of L matrices corresponding to

each center. This is not the same as A_hats in 'Arguments'. See 'Details';

sd the p- or (p+1)-dimensional vector of standard deviation of estimates in theta_hat

if stratified=FALSE, i.e., $sqrt(diag(solve(A_hat)))$. If stratified=TRUE, it's a list of L vectors corresponding to each center. These vectors are standard deviation of parameter estimates obtained from the matrices in A_hat, i.e.,

sqrt(diag(solve(A_hat[[j]]))) where j refers to a center.

Author(s)

Hassan Pazira

Maintainer: Hassan Pazira hassan.pazira@radboudumc.nl

References

Jonker M.A., Pazira H. and Coolen A.C.C. (2023). *Bayesian Federated Inference for Statistical Models, Statistics in Medicine*, Vol. 0(0), 0-0. https://doi.org/10.48550/arXiv.2302.07677

See Also

MAP.estimation.

Examples

```
# y ~ Binomial
        # L is the number of locations
L <- 2
## Local center 1:
##-----
set.seed(1123)
           <- 30
n1
           <- 4
                   \mbox{\tt\#}\mbox{\tt p} (number of coefficients) is the same for all L locations.
р
           <- data.frame(matrix(rnorm(n1 * p), n1, p))
X1
#true_beta <- c(1, 2, 0, 0, 0)
           <- 1 + 2 * X1[,1] ## with an intercept b0=1, b1=2, b2=b3=...=bp=0
eta1
mu1
           <- binomial()$linkinv(eta1)</pre>
у1
           <- rbinom(n1, 1, mu1)
lambda
           <- 0.01
```

4 inv.prior.cov

```
# we assume the same inverse covariance matrix for all locations.
         <- inv.prior.cov(X1, lambda, family=binomial)
         <- MAP.estimation(y1, X1, family=binomial, Lambda)
theta_hat1 <- fit1$theta_hat # intercept and coefficient estimates</pre>
A_hat1 <- fit1$A_hat # curvature matrix
##----
## Local center 2:
        <- 50
n2
         <- 4
                  # p is the same for all L locations
         <- data.frame(matrix(rnorm(n2 * p), n2, p))</pre>
eta2
         <- 1 + 2 * X2[,1] ## with an intercept b0=1, b1=2,b2=b3=...=bp=0
mu2
         <- binomial()$linkinv(eta2)</pre>
y2
         <- rbinom(n2, 1, mu2)
fit2
         <- MAP.estimation(y2, X2, family=binomial, Lambda)</pre>
theta_hat2 <- fit2$theta_hat</pre>
        <- fit2$A_hat
A hat2
##-----
## Combined data
##-----
              <-c(y1, y2)
              <- rbind(X1, X2)
           <- MAP.estimation(y, X, family=binomial, Lambda)
theta_hat_comb <- fit_comb$theta_hat # beta estimates of combined data
### Bayesian Federated Inference
###-----
A_hats <- list(A_hat1, A_hat2)
theta_hats <- list(theta_hat1, theta_hat2)</pre>
bfi(theta_hats, A_hats, Lambda)
# theta (intercept and coefficient) estimates by BFI
(theta_hat_bfi <- bfi(theta_hats, A_hats, Lambda)$theta_hat)</pre>
# Curvature matrix estimate by BFI
bfi(theta_hats, A_hats=A_hats, Lambda=Lambda)$A_hat
# it is not needed to have the first argument ('theta_hats') for 'A_hats' and 'sd':
bfi(A_hats=A_hats, Lambda=Lambda)$A_hat
# SD of the BFI estimates
bfi(A_hats=A_hats, Lambda=Lambda)$sd
### Difference between BFI estimates and estimates with combined data
theta_hat_bfi - theta_hat_comb
```

inv.prior.cov

Creates an inverse covariance matrix for a Gaussian prior

Description

inv.prior.cov builds a matrix which can be used as the inverse of a covariance matrix for a Gaussian prior distribution, to be used in the main functions MAP.estimation() and bfi().

inv.prior.cov 5

Usage

Arguments

X design matrix of dimension $n \times p$, where p is the number of covariates (predic-

tors) plus intercept.

lambda a user supplied lambda sequence. Length of the vector lambda depends on the

arguments X, family, and intercept. If lambda chosen by the user is an scalar, the function inv.prior.cov() consider lambda as a vector whose all elements are equal to that scalar value. Default is lambda=1. If the user choose a vector of two elements as an entry value, the inv.prior.cov() function set lambda as a vector whose all elements, except the last one, are equal to the first element of the entry, and the last element is set to the last element of the entry. Used when

independ=TRUE

family a description of the error distribution and link function used to specify the model.

This can be a character string naming a family function or the result of a call to a family function (see family for details). By default the gaussian family (with

identity link function) is used.

intercept logical flag for fitting an intercept. The intercept is fitted if intercept=TRUE

(the default) or set to zero if intercept=FALSE.

independ logical flag for creating the prior covariance matrix with (in)dependent vari-

ables/parameters. If TRUE (the default), the result is a diagonal matrix which means the parameters are independent. If FALSE, the off-diagonal elements of the resulted matrix are generated from the standard normal distribution rnorm(),

and the diagonal elements are the vector lambda.

set_seed if independ=FALSE, this argument (which should be an integer) ensures consis-

tent results. If set_seed=NULL (the default), the results are not consistent.

Details

inv.prior.cov creats a matrix whose dimension depends on the arguments X, family, and intercept. If we assume the parameters are independent (independ=TRUE), the function inv.prior.cov() returns a diagonal matrix with the vector lambda as its diagonal. If independ=FALSE, inv.prior.cov returns a matrix which is equal to z%*%t(z) where z is a matrix such that all elements are generated by standard normal distribution.

Value

inv.prior.cov returns a matrix. The dimension of the matrix depends on the arguments X, family, and intercept.

Author(s)

Hassan Pazira

Maintainer: Hassan Pazira hassan.pazira@radboudumc.nl

6 MAP.estimation

References

Jonker M.A., Pazira H. and Coolen A.C.C. (2023). *Bayesian Federated Inference for Statistical Models, Statistics in Medicine*, Vol. 0(0), 0-0. https://doi.org/10.48550/arXiv.2302.07677

See Also

MAP.estimation.

Examples

```
#-----
# y ~ Binomial
       <- data.frame(matrix(rnorm(50 * 4), 50, 4))
lambda <- 0.05
# We assume the same (inverse) covariance matrix for all
# locations and consider independency of prior parameters
(Lambda <- inv.prior.cov(X, lambda, family=binomial))</pre>
# No intercept
(Lambda <- inv.prior.cov(X, lambda, family="binomial", intercept = F))
# y ~ Gaussian
Χ
         <- data.frame(matrix(rnorm(50 * 3), 50, 3))</pre>
        <- 0.01
lambda
sigma2e <- 0.5
# If we consider dependency for all prior parameters:
(Lambda <- inv.prior.cov(X, family="gaussian", independ = F, set_seed=1123))
# No intercept
(Lambda <- inv.prior.cov(X, family="gaussian", intercept = F, independ = F, set_seed=1123))
```

MAP.estimation

Maximum A Posteriori estimation

Description

MAP.estimation function is used (in local centers) to estimate Maximum A Posterior (MAP) of the parameters for the GLM and Survival models.

Usage

Arguments

У

response vector. When the binomial family is used, this argument can be a vector with entries 0 (failure) or 1 (success). Alternatively, the response can be a matrix where the first column is the number of "successes" and the second column is the number of "failures".

MAP.estimation 7

X design matrix of dimension $n \times p$, where p is the number of covariates (predic-

tors) plus intercept.

family a description of the error distribution and link function used to specify the model.

This can be a character string naming a family function or the result of a call to a family function (see family for details). By default the gaussian family (with

identity link function) is used.

Lambda the matrix used as the prior of the inverse variance-covariance matrix of Gaus-

sian distribution.

intercept logical flag for fitting an intercept. The intercept is fitted if intercept=TRUE

(the default) or set to zero if intercept=FALSE.

initial a vector specifying initial values for the parameters (intercept, coefficients and/or

error variance) to be optimized over. For the gaussian family, it should be a p+1-dimensional vector, and for binomial the length of the vector should be p, where p is the number of covariates plus intercept. Since the 'L-BFGS-B' method is used in the algorithm, these values should always be finite. Default is

a vector of zeros.

control a list of control parameters. See 'Details'.

Details

MAP. estimation function implements

The argument control is a list that can supply any of the following components:

maxit: is the maximum number of iterations. Default is 1e2;

factr: controls the convergence of the 'L-BFGS-B' method. Convergence occurs when the reduction in the objective is within this factor of the machine tolerance. Default is 1e7, that is a tolerance of about 1e-8;

pgtol: helps control the convergence of the 'L-BFGS-B' method. It is a tolerance on the projected gradient in the current search direction. Default is zero, when the check is suppressed;

trace: is a non-negative integer. If positive, tracing information on the progress of the optimization is produced. Higher values may produce more tracing information: for the method 'L-BFGS-B' there are six levels of tracing. To understand exactly what these do see the source code of optim function in the stats package;

REPORT: is the frequency of reports for the 'L-BFGS-B' method if 'control\$trace' is positive. Default is every 10 iterations;

1mm: is an integer giving the number of BFGS updates retained in the 'L-BFGS-B' method. Default is 5.

Value

MAP. estimation returns a list containing the following components:

the ta_hat the p- or (p+1)-dimensional vector corresponding to the maximum a posteriori

(MAP) estimation of the parameters;

A_hat the curvature matrix around the point theta_hat;

sd the p- or (p+1)-dimensional vector of standard deviation of estimates in theta_hat,

i.e., sqrt(diag(solve(A_hat)));

Lambda the matrix used as the prior of the inverse variance-covariance matrix;

formula the formula of the model;

8 MAP.estimation

sample size; n the number of coefficients/regression parameters. In other words, number of prenp dictors plus the intercept if intercept=TRUE, or without intercept if intercept=FALSE; value the value of the 'negative' loglikelihood function corresponding to theta_hat; a description of the error distribution used in the model; family an integer value used to encode the warnings and the errors related to the algoconvergence rithm used to fit the model. The values returned are: **0** algorithm has converged; 1 maximum number of iterations ('maxit') has been reached; 2 Warning from the 'L-BFGS-B' method. See the message after this value; control the list of control parameters used to compute the MAP estimates.

Author(s)

Hassan Pazira

Maintainer: Hassan Pazira hassan.pazira@radboudumc.nl

References

Jonker M.A., Pazira H. and Coolen A.C.C. (2023). *Bayesian Federated Inference for Statistical Models, Statistics in Medicine*, Vol. 0(0), 0-0. https://doi.org/10.48550/arXiv.2302.07677

See Also

bfi and summary.bfi.

Examples

```
#-----
# y ~ Gaussian
#-----
set.seed(11235813)
       <- 30
n
       <- 3
               # number of coefficients (without intercept)
р
       <- data.frame(matrix(rnorm(n * p), n, p))</pre>
Χ
       <-1 + 2 * X[,1]
                           # with an intercept
eta
       <- gaussian()$linkinv(eta)
sigma2 <- 1.5
# the true theta is c(1, 2, 0, 0, sigma2)
       <- rnorm(n, mu, sd=sqrt(sigma2))</pre>
lambda <- 0.01
# inverse of covariance matrix:
Lambda <- inv.prior.cov(X, lambda=c(lambda,sigma2), family=gaussian)</pre>
\# MAP estimates of the parameters of interest (including 'intercept') and curvature matrix
(fit <- MAP.estimation(y, X, family=gaussian, Lambda))</pre>
class(fit)
# MAP estimates without 'intercept'
Lambda <- inv.prior.cov(X, lambda=c(lambda,sigma2), family=gaussian, intercept = F)</pre>
(fit1 <- MAP.estimation(y, X, family=gaussian, Lambda, intercept = F))</pre>
```

Nurses 9

Nurses	Nurses' stress in different hospitals	

Usage

```
data(Nurses)
```

Format

This data set contains three-level simulated data from a hypothetical study on stress in hospitals. The data are from nurses working in wards nested within hospitals. It is a cluster-randomized experiment. In each of 25 hospitals, four wards are selected and randomly assigned to an experimental and a control condition. In the experimental condition, a training program is offered to all nurses to cope with job-related stress. After the program is completed, a sample of about 10 nurses from each ward is given a test that measures job-related stress. Additional variables are: nurse age (years), nurse experience (years), nurse gender (0 = male, 1 = female), type of ward (0 = general care, 1 = special care), and hospital size (0 = small, 1 = medium, 2 = large).

Source

https://multilevel-analysis.sites.uu.nl/datasets/

References

Hox, J., Moerbeek, M., and van de Schoot, R. (2010). *Multilevel Analysis: Techniques and Applications*, Second Edition (2nd ed.). *Routledge*. https://doi.org/10.4324/9780203852279

summary.bfi

Summarizing BFI Fits

Description

Summary method for an object with class 'bfi' created by the MAP.estimation function.

Usage

Arguments

object	fitted bfi object.
curmat	logical; if TRUE, the curvature matrix around the estimated parameters is returned and printed. Default is FALSE.

digits significant digits in printout.

10 summary.bfi

Details

summary.bfi gives information about the MAP estimates of parameters of the model. It can be used for bfi objects built by the MAP.estimation function.

The output of the summary method shows the details of the model, i.e. formula, family and link function used to specify the generalized linear model, followed by information about the estimates, standard deviations and confidence intervals. Information about the log-likelihood and convergence status are also provided.

By default, summary.bfi function does not return the curvature matrix, but the user can use curmat=TRUE to print it.

Value

summary.bfi returns an object of class summary.bfi, a list with the following components:

the component from object. The last element of this vector is the estimate of the dispersion parameter (sigma2). See the MAP.estimation function.
the component from object. See the MAP.estimation function.
the component from object. The last element of this vector is the square root of the estimated dispersion. See the MAP.estimation function.
the component from object. See the MAP.estimation function.
the component from object. See the MAP.estimation function.
the component from object. See the MAP.estimation function.
the component from object. See the MAP.estimation function.
the component from object. See the MAP.estimation function.
the component from object. See the MAP.estimation function.
the component from object. See the MAP.estimation function.
the component from object. See the MAP.estimation function.
the value of the loglikelihood function corresponding to estimates (theta_hat). This is the minus of the value component.
the link function. By default the gaussian family with identity link function and the binomial family with logit link function are used.
the estimated variance of the random error, i.e., sigma2. The dispersion is taken as 1 for the binomial family.
the standard error. se is calculated by dividing sd (standard deviation) by the square root of the sample size.
a 95% confidence interval.

Author(s)

Hassan Pazira

Maintainer: Hassan Pazira hassan.pazira@radboudumc.nl

See Also

MAP.estimation and bfi functions.

trauma 11

Examples

```
# y ~ Gaussian
set.seed(1123581)
        <- 30
        <- 4
        <- data.frame(matrix(rnorm(n * p), n, p))
Χ
        <- 1:2
b
        \leftarrow b[1] + X[, 1] * b[2]
eta
        <- gaussian()$linkinv(eta)
mu
sigma2e <- 0.5
        <- rnorm(n, mu, sd=sqrt(sigma2e))</pre>
lambda <- 0.1
Lambda <- inv.prior.cov(X, lambda=c(lambda,sigma2e), family=gaussian)</pre>
        <- MAP.estimation(y, X, family=gaussian, Lambda)
class(fit)
summary(fit)
sumfit <- summary(fit, curmat = T)</pre>
sumfit logLik
sumfit$dispersion
sumfit$CI
class(sumfit)
```

trauma

Trauma patients from different hospitals

Usage

data(trauma)

Format

This data set consists of data of 371 trauma patients from three hospitals. The binary variable mortality is used as an outcome, and variables age, sex, the Injury Severity Score (ISS, ranging from 1 (low) to 75 (high)) and the Glasgow Coma Scale (GCS, which expresses the level of consciousness, ranging from 3 (low) to 15 (high)) are used as covariates. The data originate from multiple hospitals which can be categorised in three groups as: peripheral hospital without a neurosurgical unit (Status = 1), peripheral hospital with a neuro-surgical unit (Status = 2), and academic medical centre (Status = 3).

References

Jonker M.A., Pazira H. and Coolen A.C.C. (2023). *Bayesian Federated Inference for Statistical Models, Statistics in Medicine*, Vol. 0(0), 0-0. https://doi.org/10.48550/arXiv.2302.07677

Draaisma J.M.Th, de Haan A.F.J., Goris R.J.A. (1989). *Preventable Trauma Deaths in the Netherlands - A prospective Multicentre Study, The journal of Trauma*, Vol. 29(11), 1552-1557.

Index

```
* Bayesian
    bfi, 2
    BFI-package, 1
    inv.prior.cov, 4
    MAP.estimation, 6
    \verb|summary.bfi, 9|
* \ Federated \\
    bfi, 2
    BFI-package, 1
    MAP.estimation, 6
    summary.bfi, 9
* datasets
    Nurses, 9
    trauma, 11
* package
    BFI-package, 1
bfi, 2, 8, 10
BFI-package, 1
family, 5, 7
https://multilevel-analysis.sites.uu.nl/datasets/,
inv.prior.cov, 4
MAP.estimation, 3, 6, 6, 10
Nurses, 9
stats, 7
summary(summary.bfi), 9
summary.bfi, 8, 9
\text{trauma},\, 11
```